

DE LA RECHERCHE À L'INDUSTRIE



1. The  $N=28$  region.
2. Coexistence at  $Z=16$ .
3. Perspectives & summary.

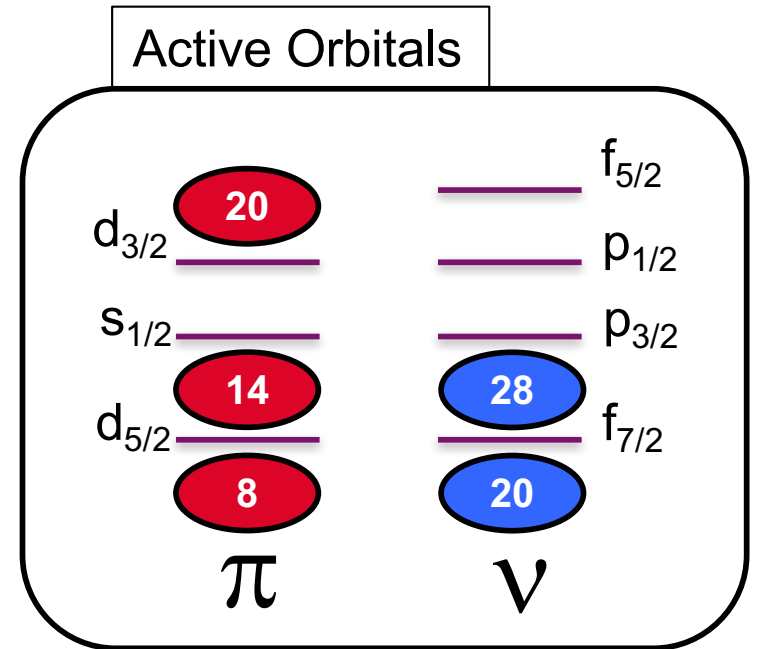
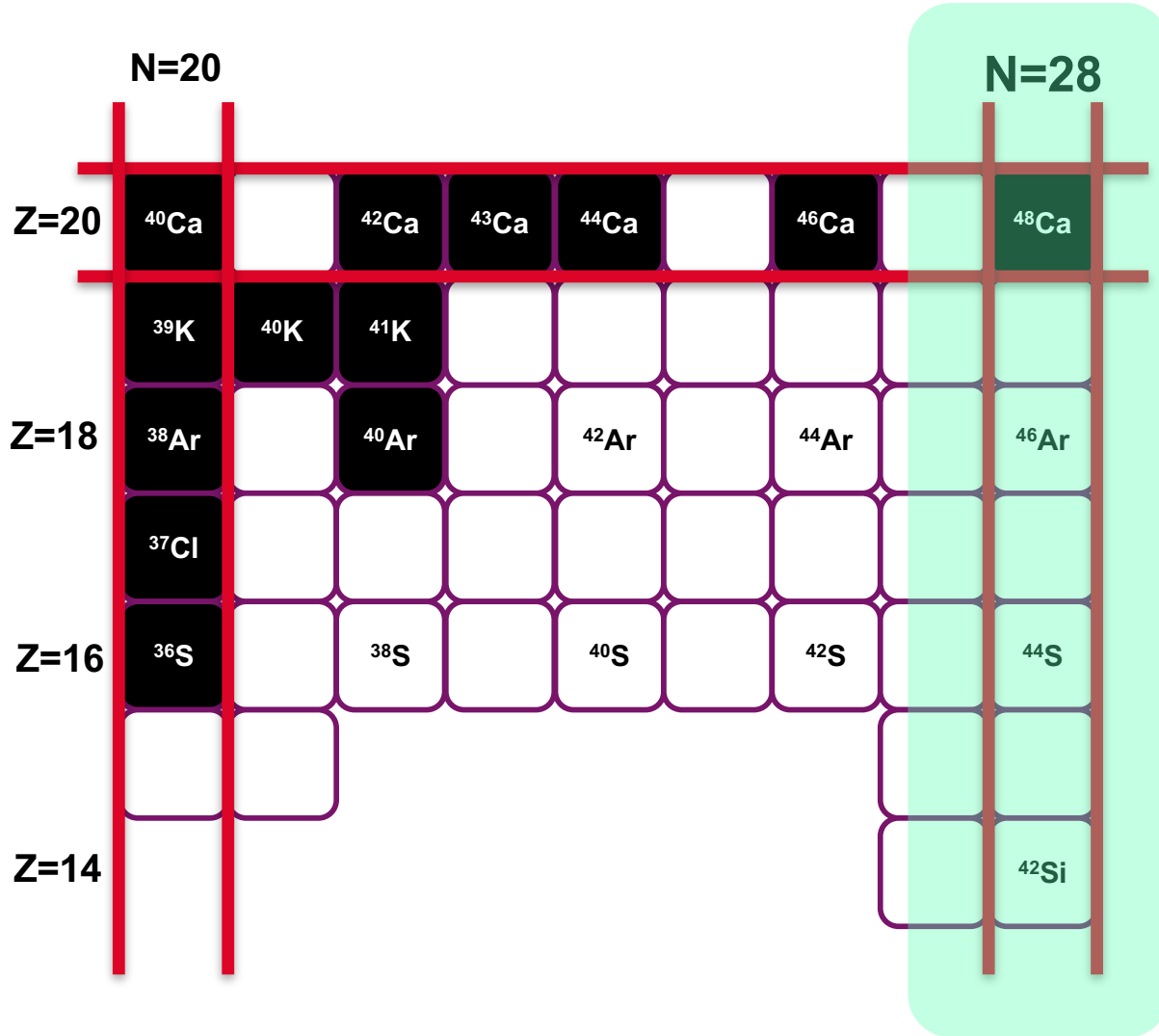
[www.cea.fr](http://www.cea.fr)

# SHAPE TRANSITION & COEXISTENCE AROUND $N=28$

L. GAUDEFROY  
CEA-DAM

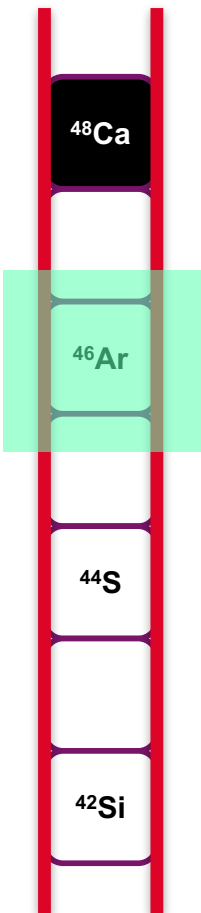
ESNT – October 2017

# THE N=28 REGION



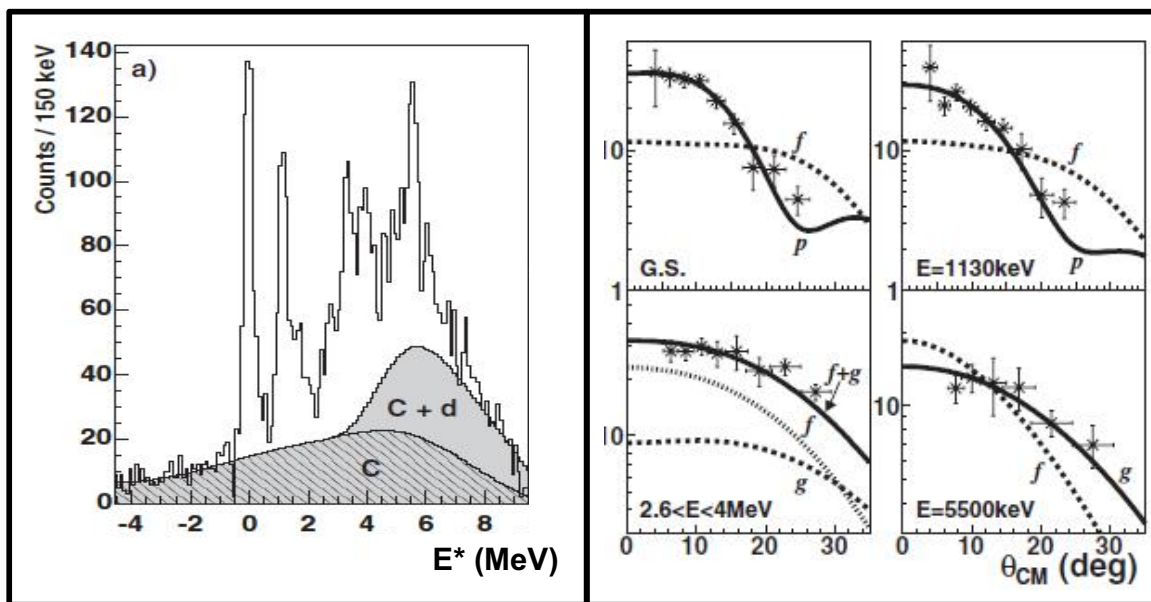
# THE N=28 REGION – NEUTRON SIDE

N=28



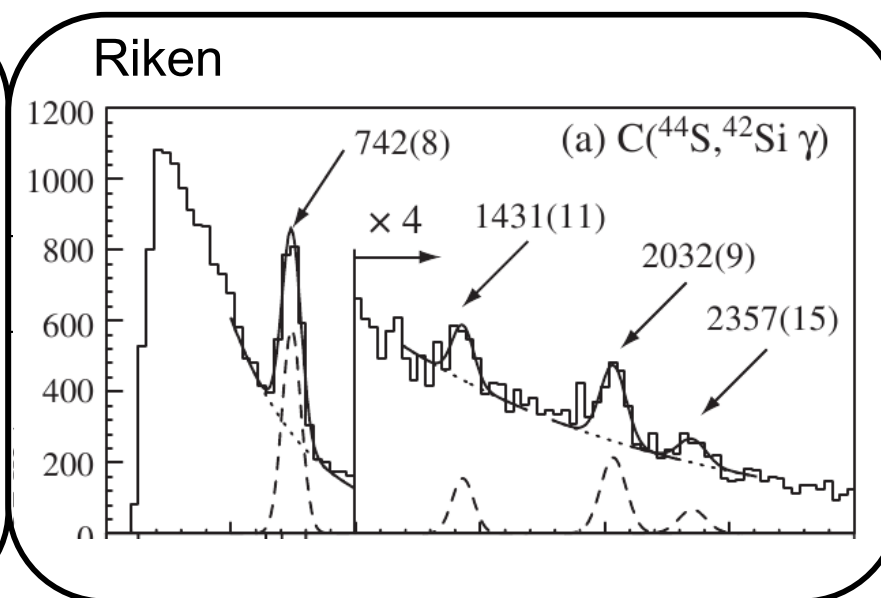
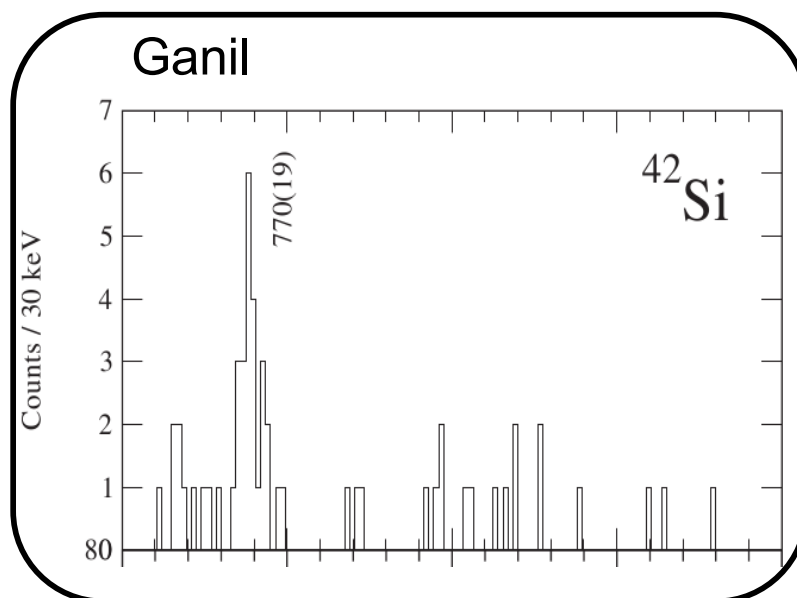
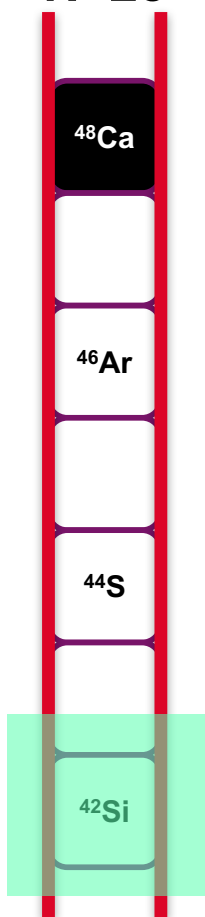
$^{48}\text{Ca}$  :  
Mass measurement  $\rightarrow$  Gap 4,8 MeV

$^{46}\text{Ar}$  :  
(d,p) reaction  $\rightarrow$  Gap reduction by  $\sim 300$  keV.  
L. Gaudefroy et al., PRL **97**, 092501 (2006).



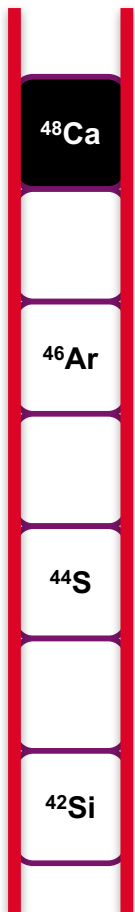
## THE N=28 REGION – NEUTRON SIDE

N=28

 $^{42}\text{Si}$  :In-beam  $\gamma$ -Spectroscopy  $\rightarrow$  Low  $E(2^+_{1}) = 742$  keV.B. Bastin et al., PRL **99**, 022503 (2007).Riken  $\rightarrow R_{4/2}=2,93$  , i.e. well-deformed rotor.S. Takeuchi et al., PRL **109**, 182501 (2012).

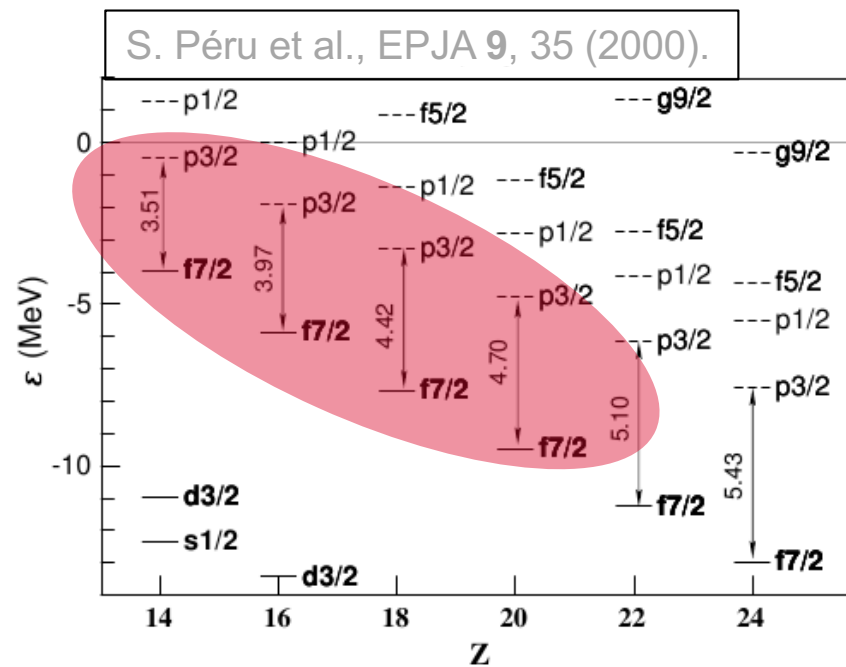
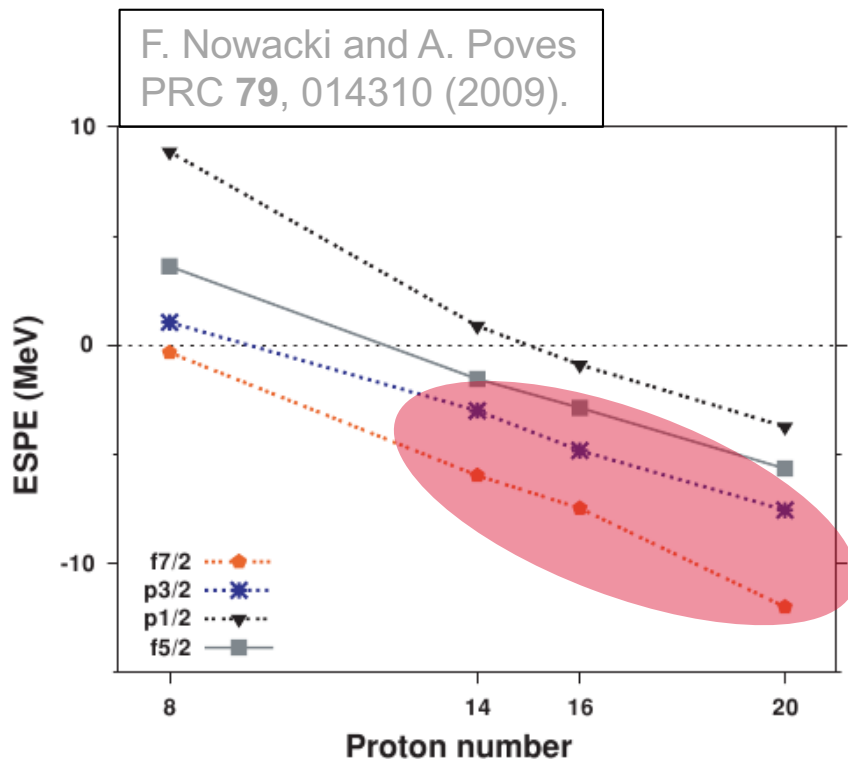
# THE N=28 REGION – NEUTRON SIDE

N=28

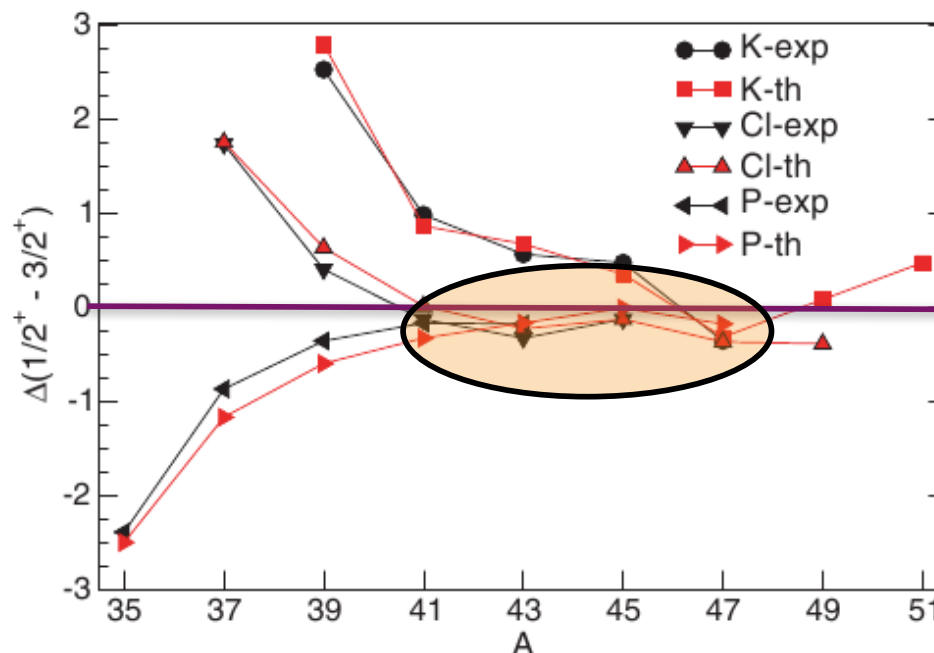
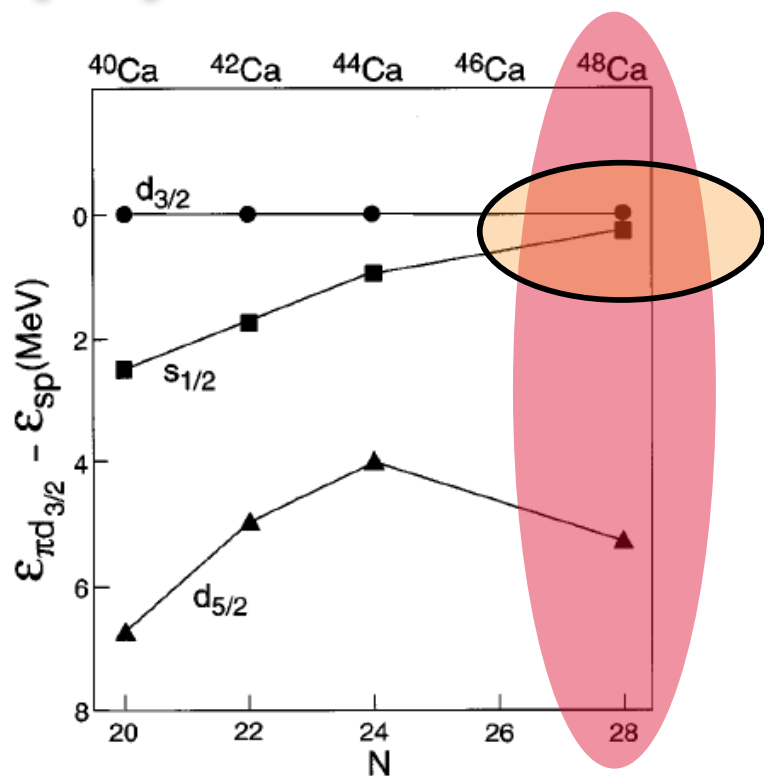
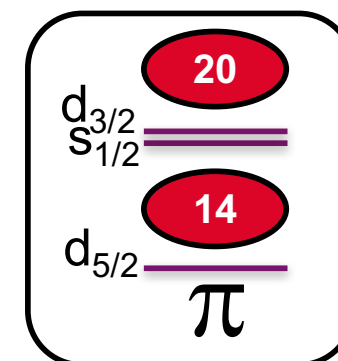
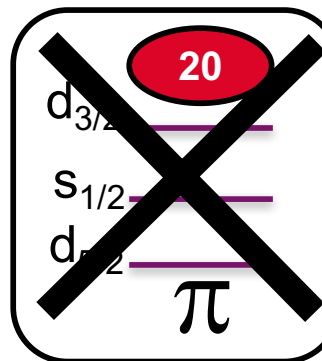
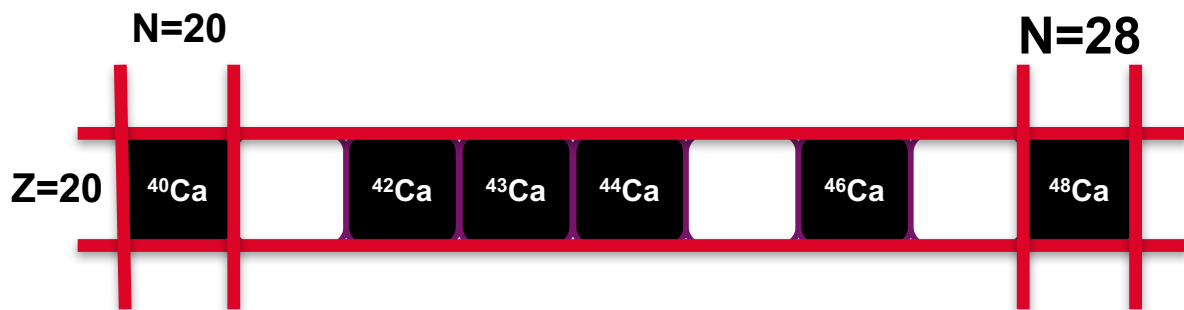


N28 gap reduction from Z=20 down to Z=14:

- ➔ by about 300keV every 2 proton.
- ➔ Well accounted for by SM and MF approaches.



# THE N=28 REGION – PROTON SIDE



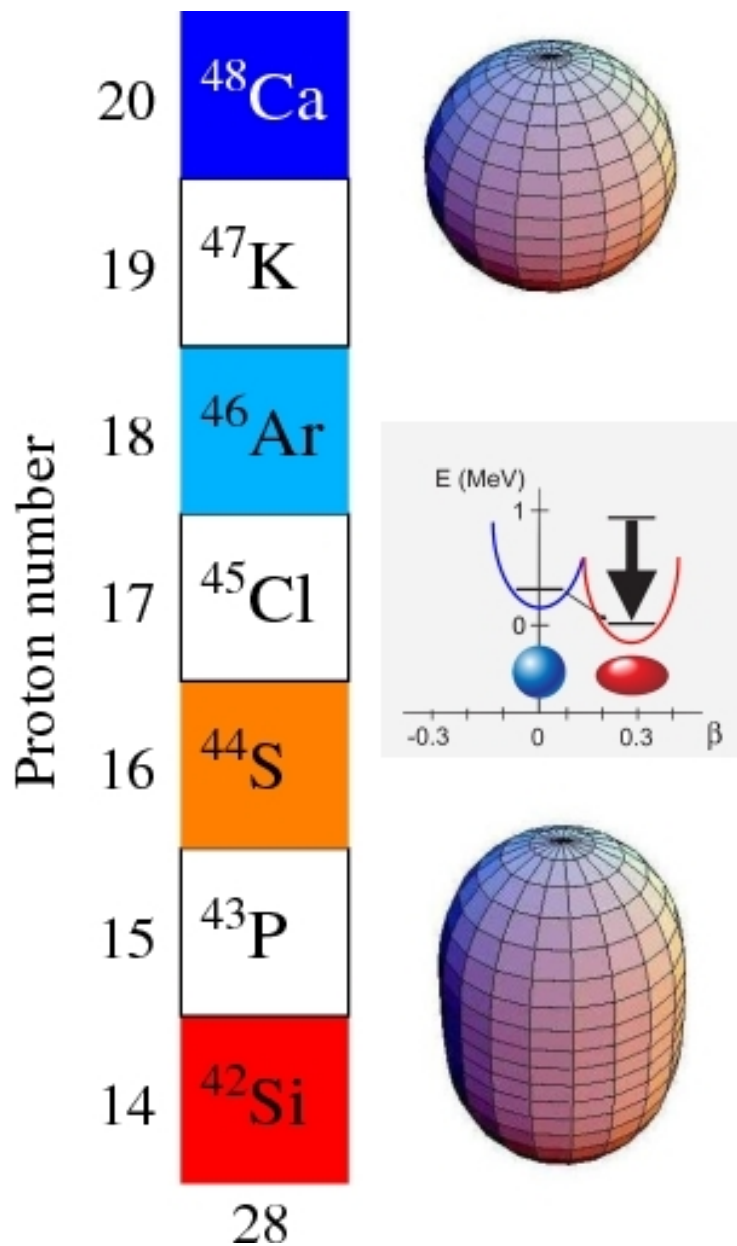
P.D. Cottle and K.W. Kemper  
 PRC 58, 3761 (1998).

P. Doll et al., NPA 263, 210 (1976).

F. Nowacki and A. Poves PRC 79, 014310 (2009).

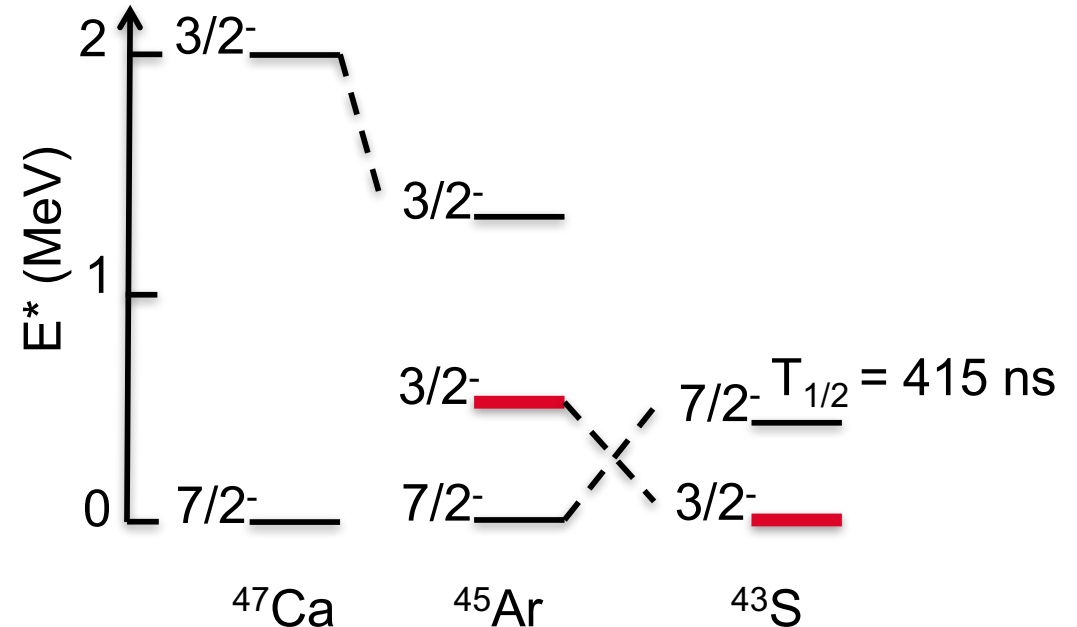
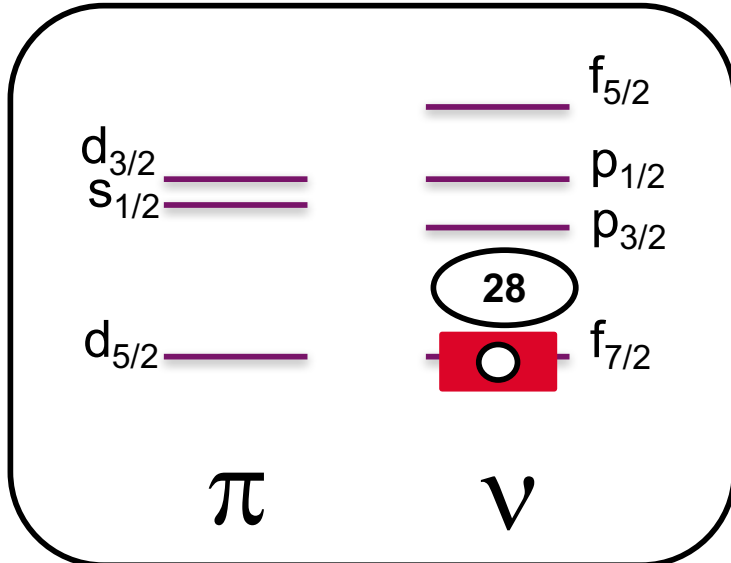
A. Gade et al., PRC 74, 034322 (2006).

## THE N=28 REGION



- Reduction of neutron gap with N/Z.
- Near degeneracy of proton  $s_{1/2} - d_{3/2}$  orbits.
- Both favor quadrupole collectivity mandatory to understand structure evolution.
- Spherical/deformed shape transition : Ca  $\rightarrow$  Si.
- **Transitional nature of sulfur isotopes.**

## Structure of N=27 isotones :



$^{47}\text{Ca}$  : Single particle states.

Evaluated Nuclear Structure Data File.

$^{45}\text{Ar}$  :  $3/2^-_1$  state  $\rightarrow$  Intruder.

Favored by about 2MeV (correlation energy) with respect to  $7/2^-$ .

L. Gaudefroy et al., PRC 78, 034307 (2008).

$^{43}\text{S}$  : Intruder state  $\rightarrow$  GS.

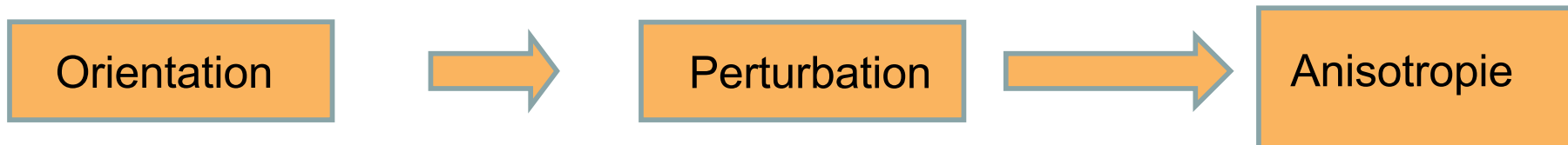
$7/2^-_1 \rightarrow$  Isomer.

} Shape coexistence?

F. Sarazin et al., PRL 84, 5062 (2000); L. Gaudefroy et al., PRL 109, 202503 (2012).



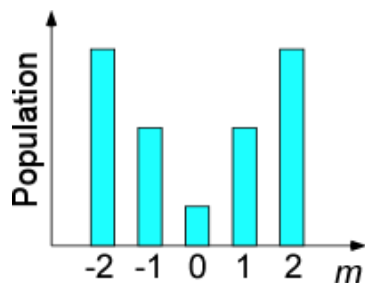
## Principle of the measurement :



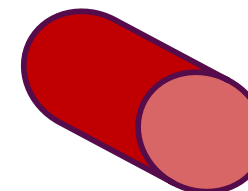
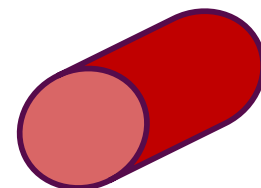
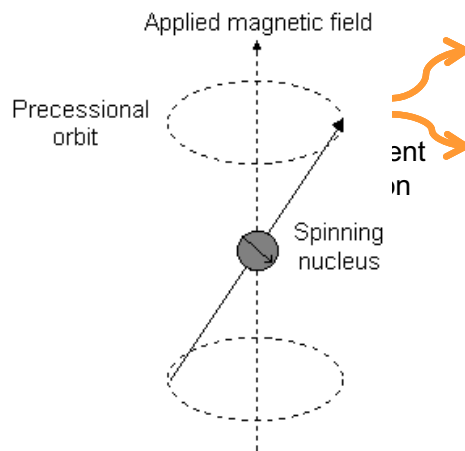
Spin alignment :  
fragm. reaction

Implantation  
appropriate host

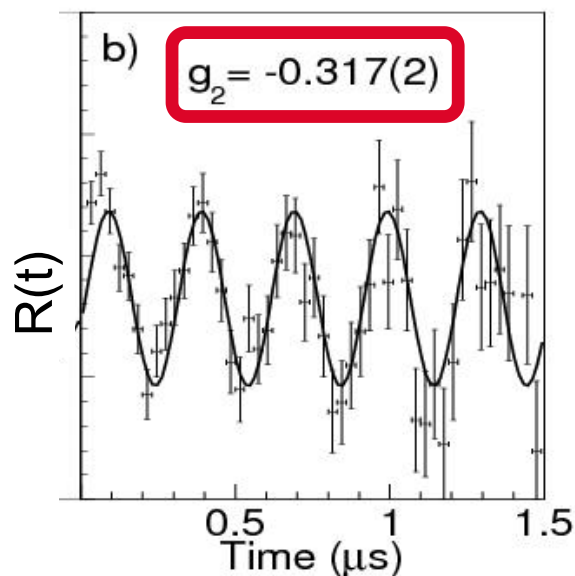
Ge detector for 320 keV  $\gamma$ -ray



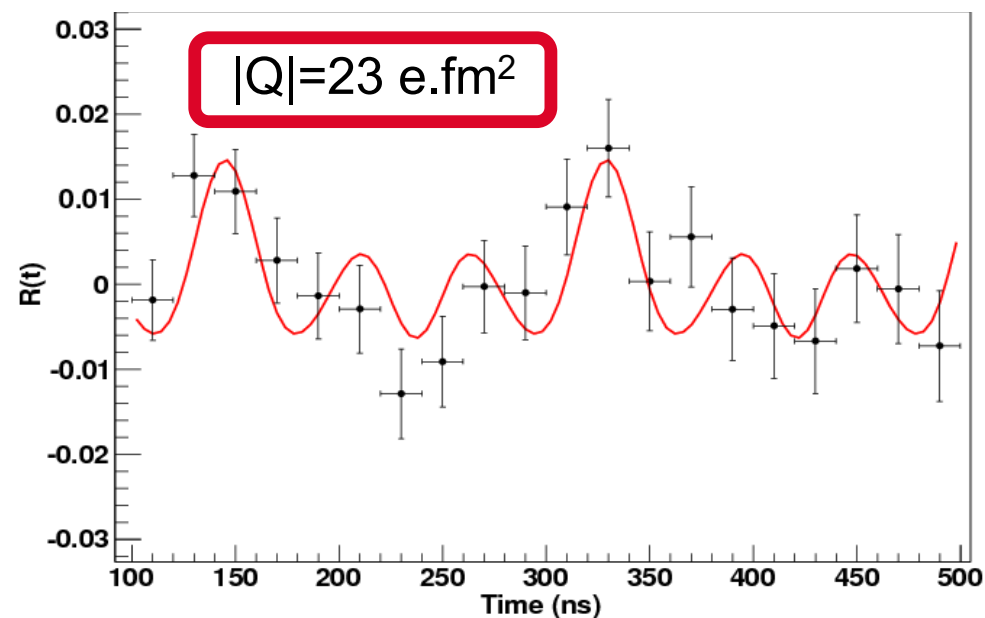
- $\mathbf{B} \perp \mathbf{Z}_{\text{or}} \Rightarrow \omega_L$
- $\mathbf{V}_{zz} \perp \mathbf{Z}_{\text{or}} \Rightarrow \omega_Q$



**→ g-factor @ GANIL & Q-moment @ RIKEN**



L. Gaudefroy et al., PRL 102, 092501 (2009).



R. Chevrier et al., PRL 108, 162501 (2012).

## g-factor @ GANIL:

- Sign & Amplitude :  $J^\pi = 7/2^-$ .
- $T_{1/2} = 415(5) \text{ ns}$ , E2 transition :  $GS = 3/2^-$
- Hindrance factor  $7/2^- \rightarrow 3/2^-$  : 20.

## Q-moment @ RIKEN:

- $Q = 23$ , significantly higher than SP value ( $4 \text{ e.fm}^2$ ).

$$7/2^- \text{---} T_{1/2} = 415 \text{ ns}$$

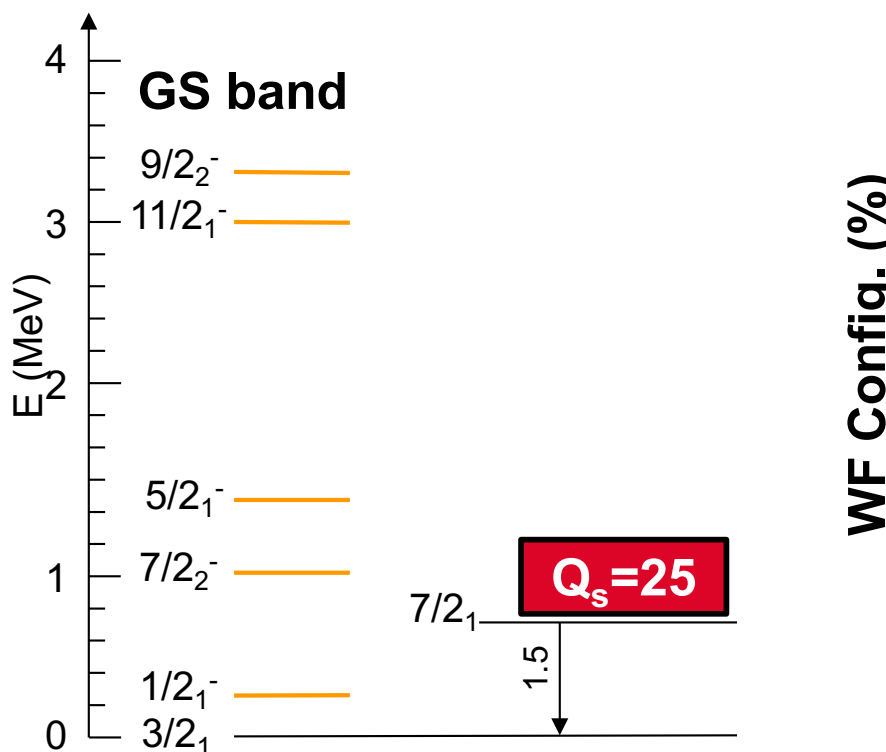
$$3/2^- \text{---}$$

$$^{43}\text{S}$$

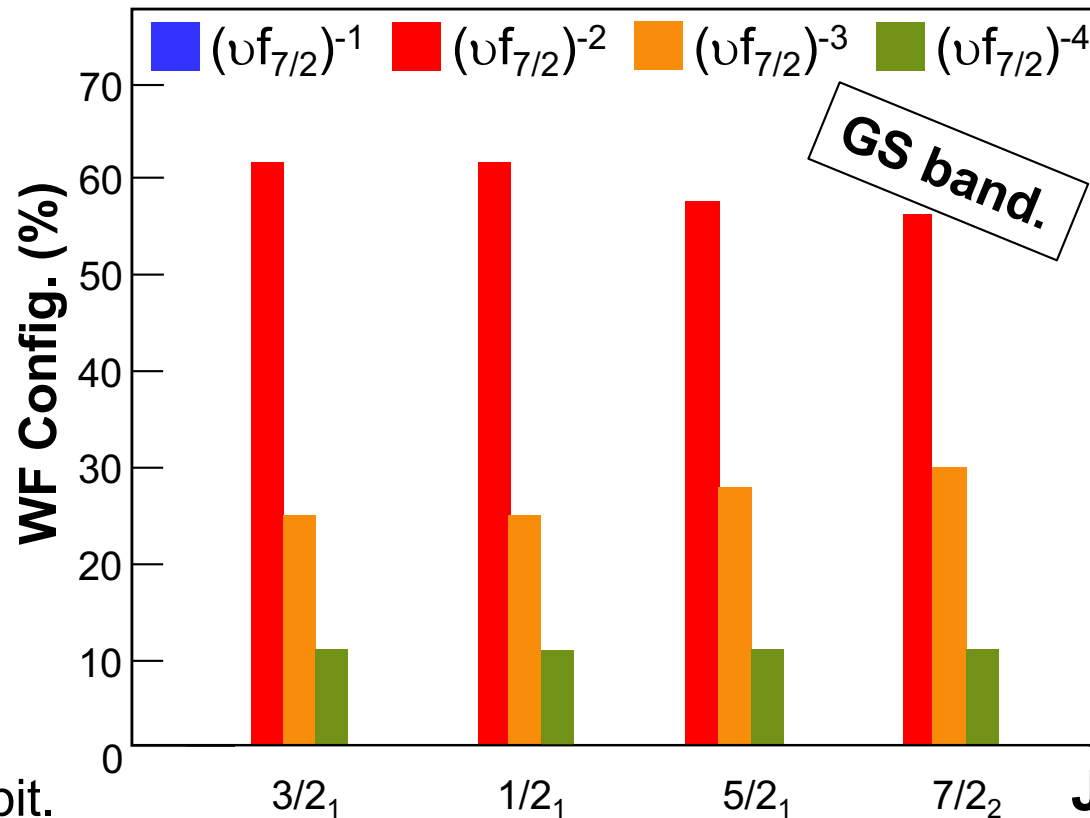
## SM calculations :

ANTOINE : E. Caurier, IReS, Strasbourg 1989-2002.

SDPF-U: F. Nowacki and A. Poves, PRC79, 014310 (2009).



K=1/2 decoupled GS band on p<sub>3/2</sub> orbit.



→ Clear evidence for intrinsic WF.

Shape of the isomer?

- GS axial (prolate – β=0,3) band.
- Isomer not member of the band.
- Q-moment of isomer well reproduced.

# <sup>43</sup>S SM SHAPE PARAMETERS

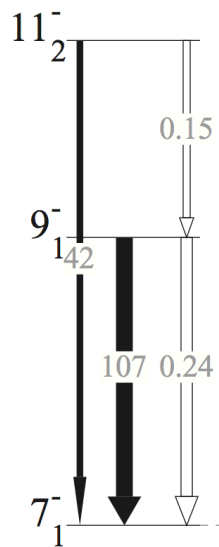
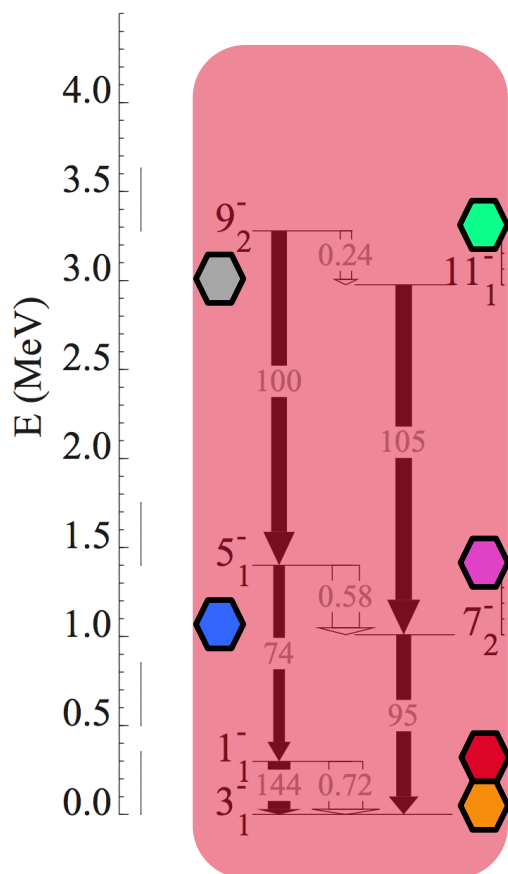
## E2 Rotational Invariants :

K. Kumar, PRL28, 249 (1972).

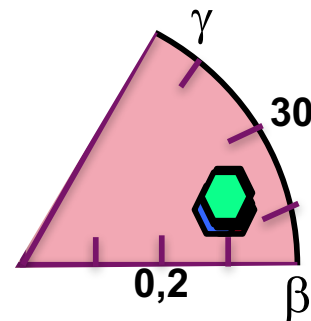
$$Q^2_i = \langle s | P^{(2)} | s \rangle = \frac{1}{\sqrt{5}} \frac{1}{2I_s + 1} \sum_t M_{sr}^2,$$

$$Q^3_i \cos(3\gamma) = \langle s | P^{(3)} | s \rangle = \frac{-1}{2I_s + 1} (-)^{2I_s}$$

$$\times \sum_{rt} \left\{ \begin{matrix} 2 & 2 & 2 \\ I_s & I_r & I_t \end{matrix} \right\} M_{sr} M_{rt} M_{ts},$$



<sup>43</sup>S



- Axial prolate GS Band.

R. Chevrier and L. Gaodefroy, PRC 89, 051301(R) (2014).

# <sup>43</sup>S SM SHAPE PARAMETERS

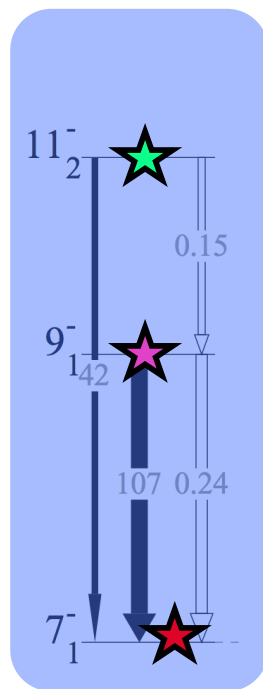
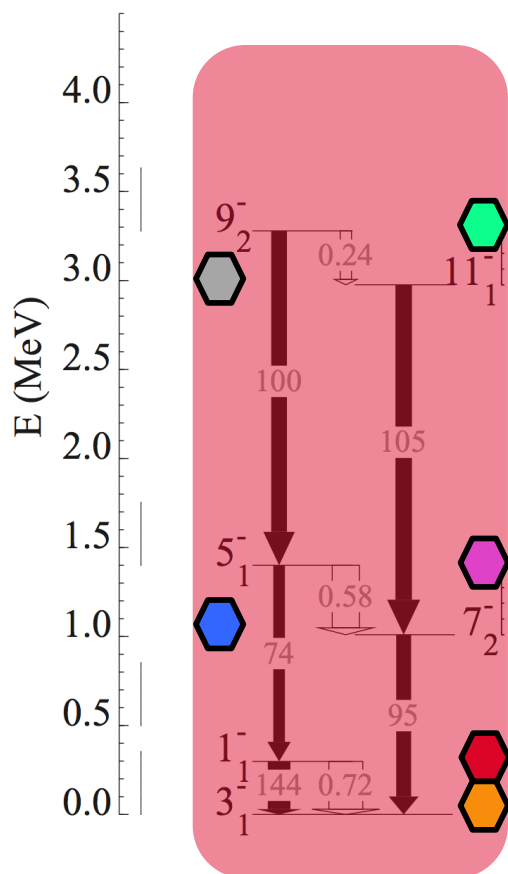
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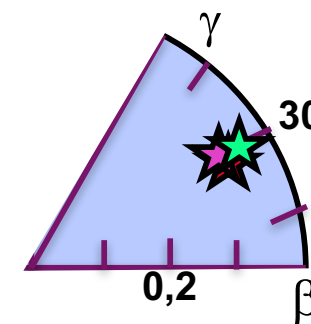
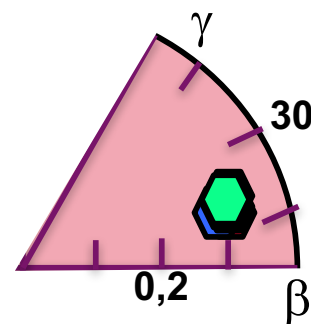
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$$Q^3_i \cos(3\gamma) = \langle s | P^{(3)} | s \rangle = \frac{-1}{2I_s + 1} (-)^{2I_s}$$

$$\times \sum_{rt} \left\{ \begin{matrix} 2 & 2 & 2 \\ I_s & I_r & I_t \end{matrix} \right\} M_{sr} M_{rt} M_{ts},$$



<sup>43</sup>S

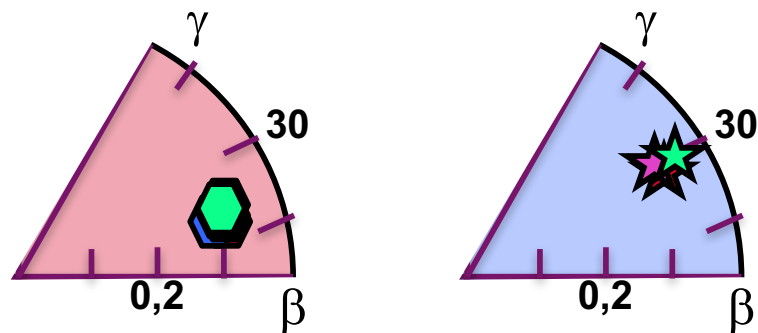


- Axial prolate GS Band.
- Triaxial structure on isomer.

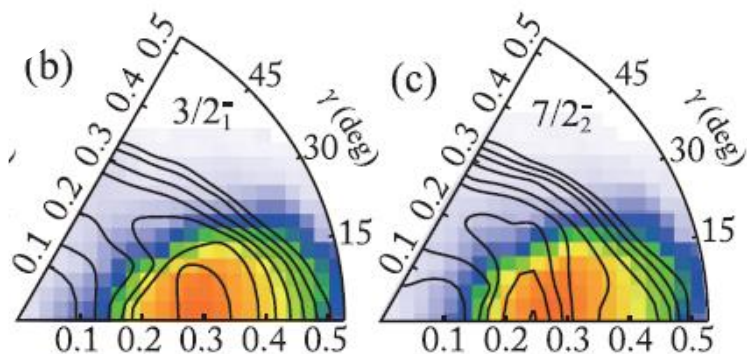
R. Chevrier and L. Gaodefroy, PRC 89, 051301(R) (2014).

## SM approach:

R. Chevrier and L.G., PRC **89**, 051301(R) (2014).

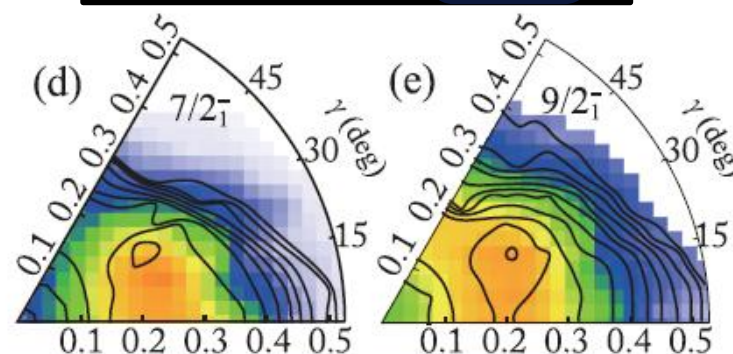
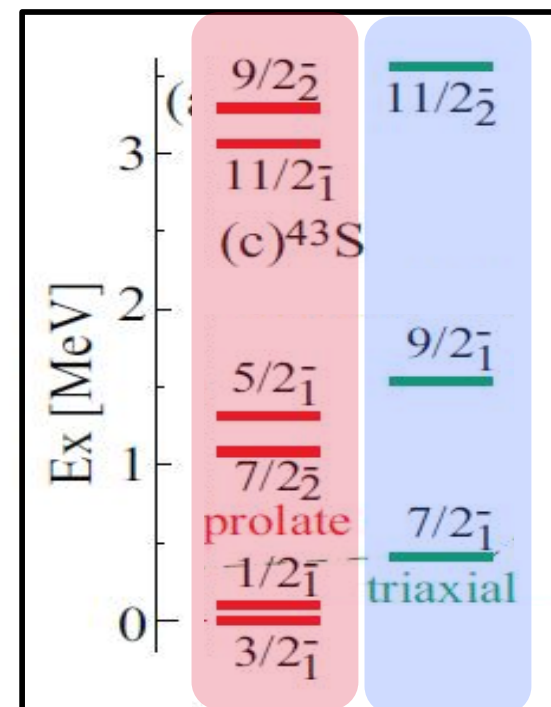


- Axial prolate GS Band.
- Triaxial structure on isomer.



## AMD approach with D1S Gogny:

M. Kimura et al., PRC **87**, 011301(R) (2013).



See also : Y. Utsuno et al., PRL **114**, 032501 (2015).

➔ Same conclusions with BMF approx. to SM.

→ 1993 : Suggestion of N=28 erosion from short  $\beta$ -decay half-life of  $^{44}\text{S}$ .

O. Sorlin et al., PRC **47**, 2941 (1993).

→ 1996 : Deformation in  $^{44}\text{S}$  ( $\beta=0.26$ ) from B(E2).

T. Glasmacher et al., PLB **395**, 163 (1997).

→ 2005 : Observation of  $0^+_2$  state – coexistence?

S. Grévy et al., EPJA **25**, 111 (2005).

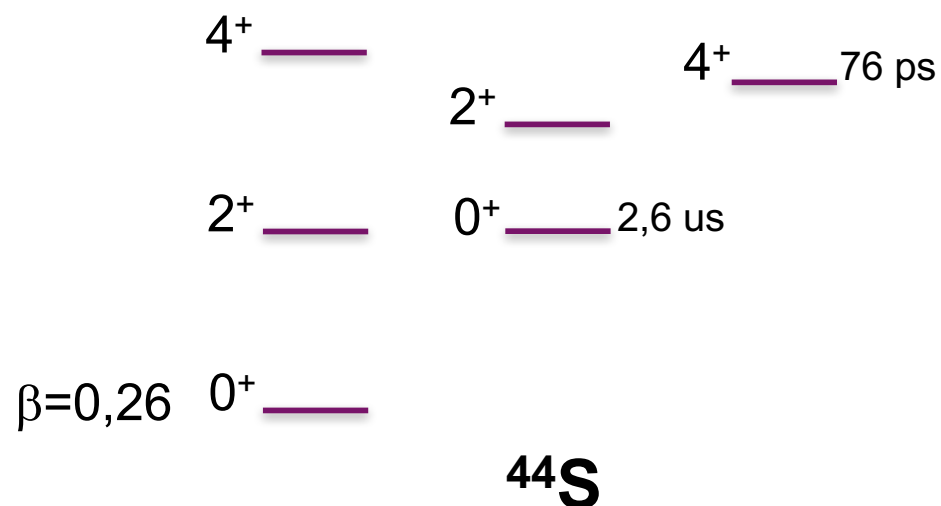
→ 2010 :  $\rho^2(E0 \ 0^+_2 \rightarrow 0^+_1)$  – Sphe./Def. shape coexistence.

C. Force et al., PRL **105**, 102501 (2010).

→ 2017 : High K isomer  $4^+_1$  state : Triple shape coexistence.

J.J. Parker et al., PRL **118**, 052501 (2017).

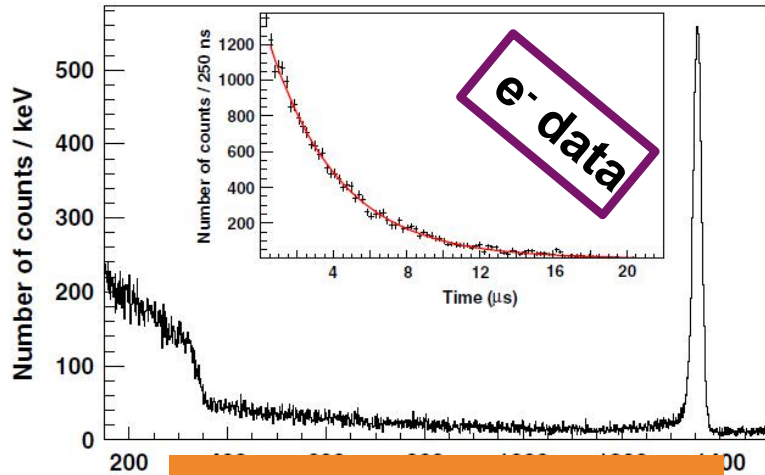
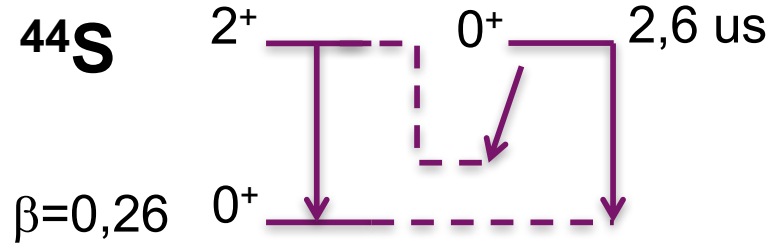
First reported in D. Santiago-Gonzales et al., PRC **83**, 061305 (R) (2011).



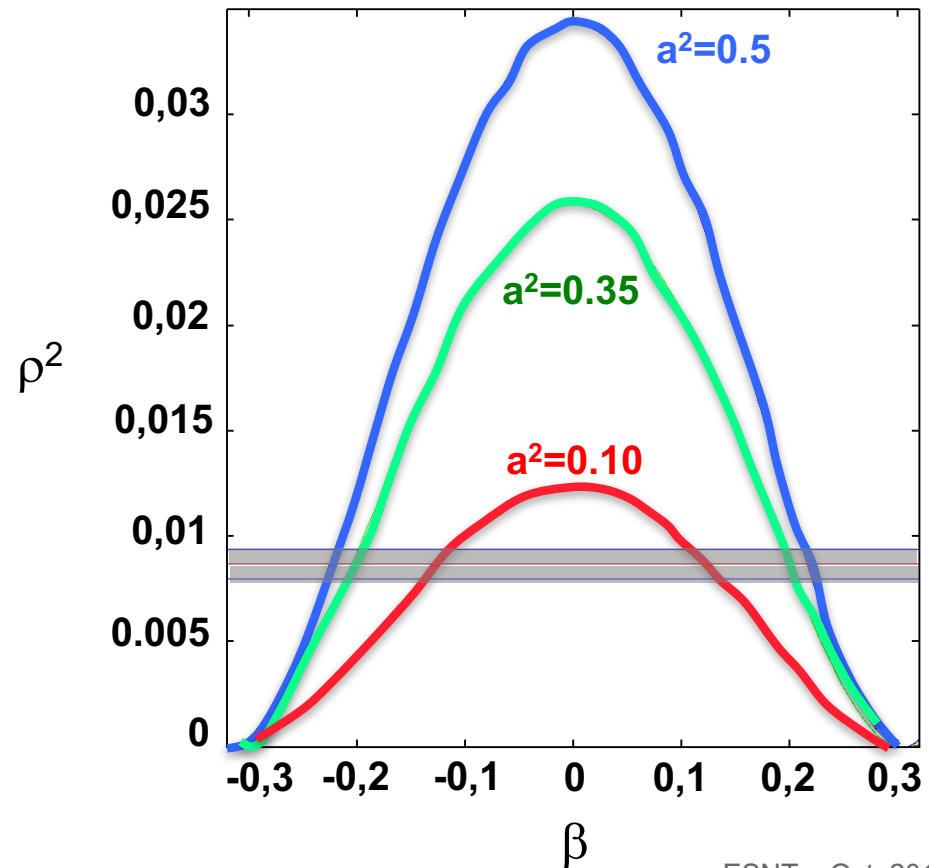
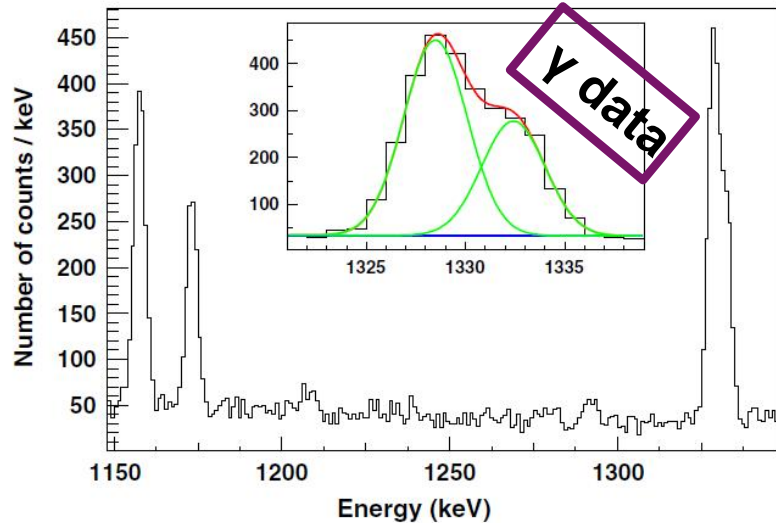
# $\gamma$ AND $e^-$ SPECTROSCOPY

## GANIL

C. Force et al., PRL105, 102501 (2010).



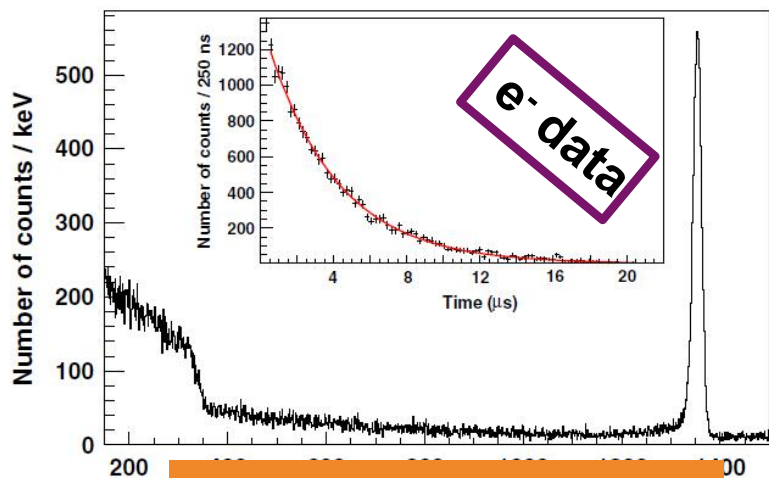
$\rho^2(E_0) = 8,7(7) \cdot 10^{-3}$



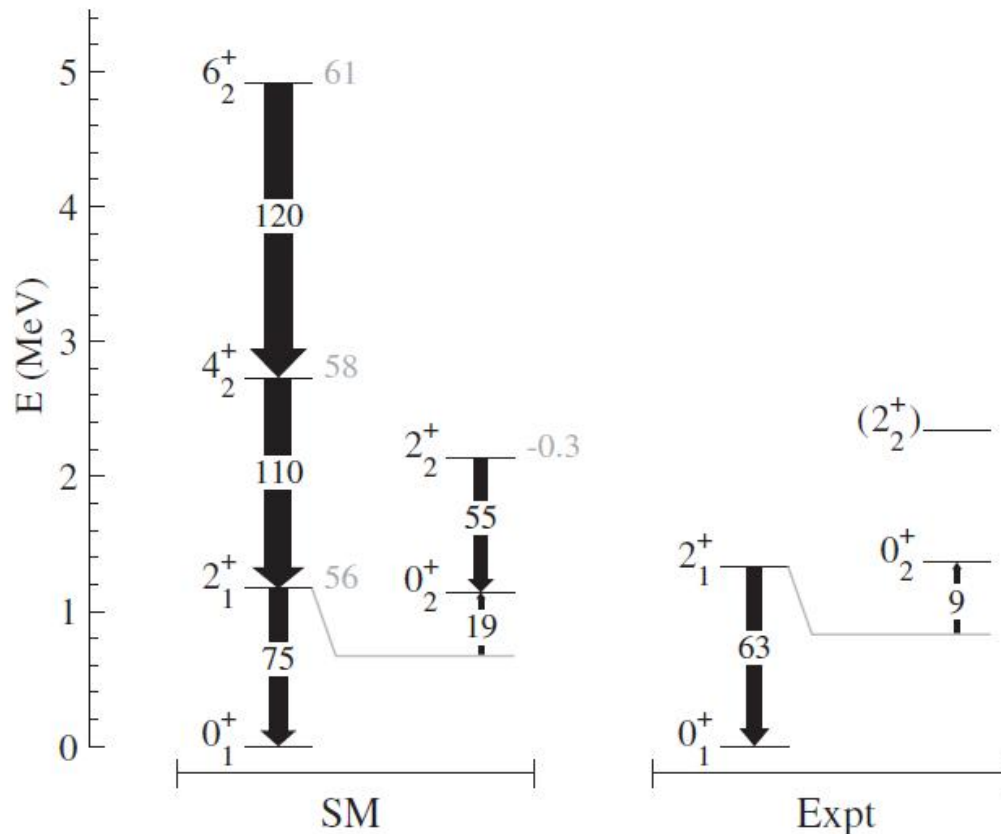
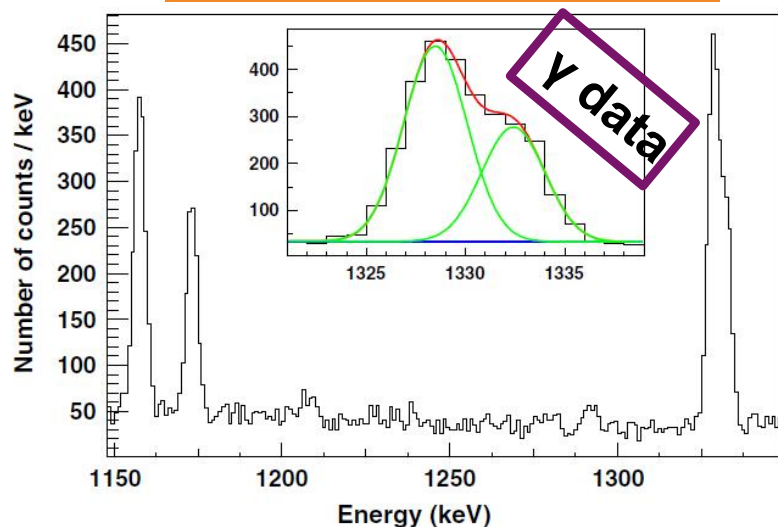


## GANIL

C. Force et al., PRL105, 102501 (2010).



$$\rho^2(E_0) = 8,7(7) \cdot 10^{-3}$$



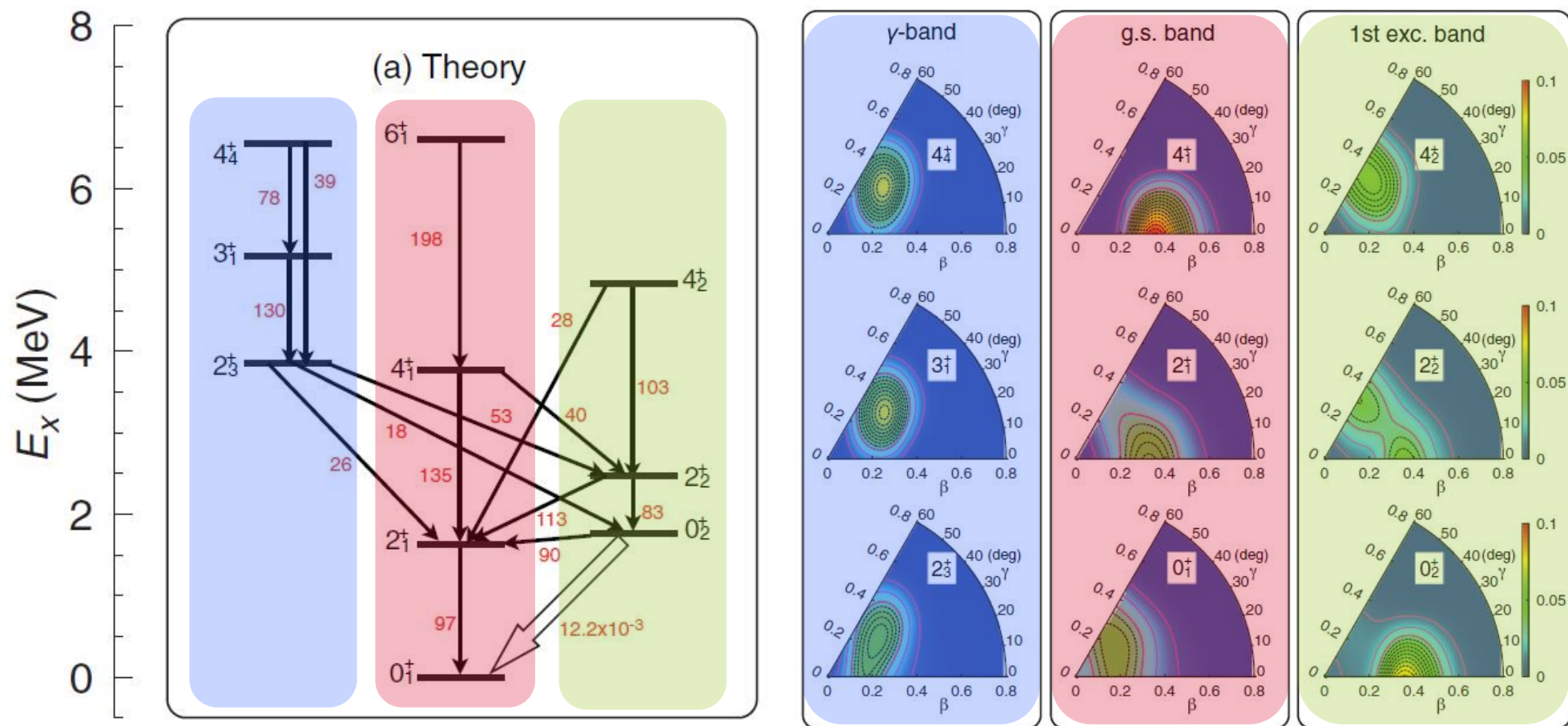
SM calculations:

- GS band; prolate;  $\beta=0,25$ .
- $Q_{SM}(2^+_2)=-0,3 \text{ e.fm}^2$ .

**→ Prolate/Spherical shape coexistence in  $^{44}\text{S}$ .**

- HFB + GCM + AM Projection – D1S Gogny

T. R. Rodriguez and J. L. Egido, PRC **84**, 051307(R) (2011)

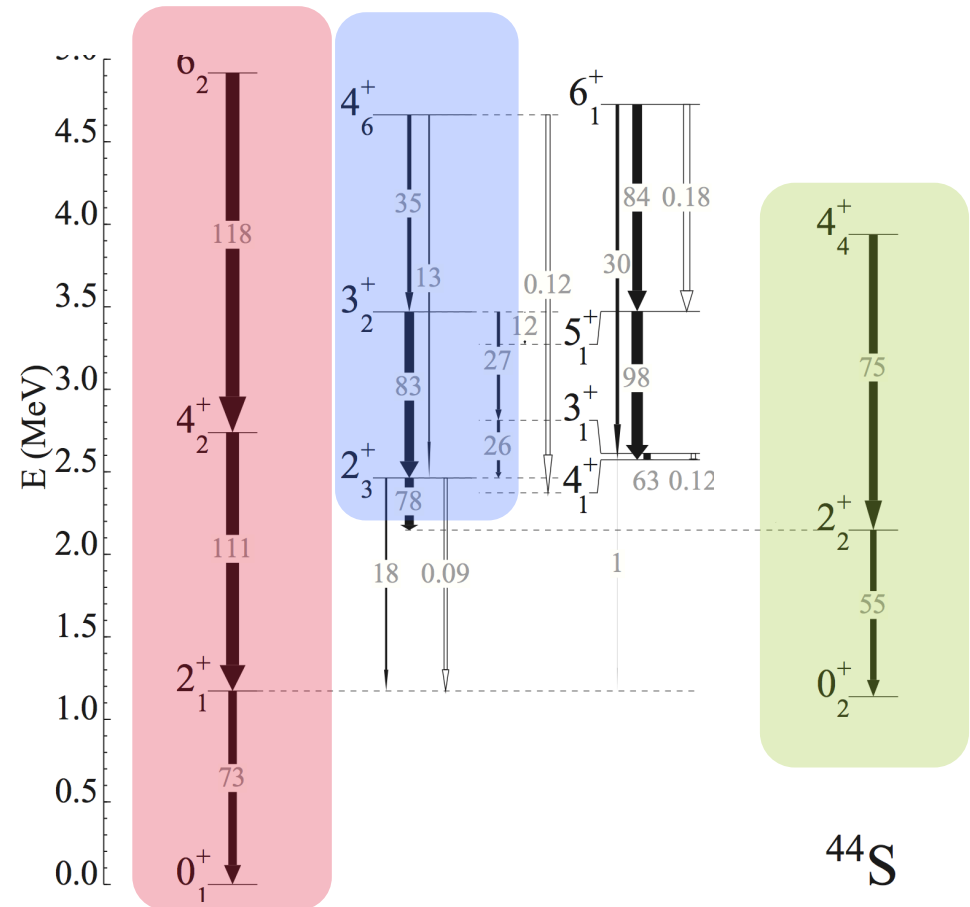
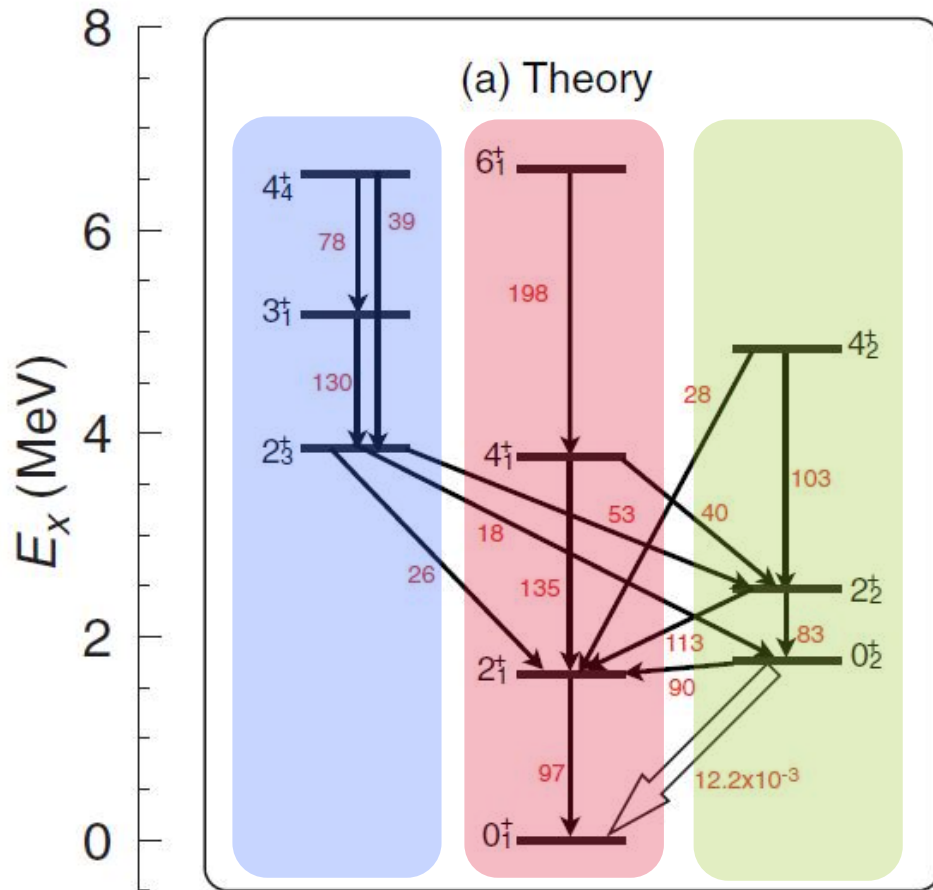


- GS band  $\rightarrow$  toward prolate.

- Excited band  $\rightarrow$  Shape evolution.

$\rightarrow$   $^{44}\text{S}$  : Deformed/Deformed Shape coexistence.

T. R. Rodriguez and J. L. Egido, PRC **84**, 051307(R) (2011)

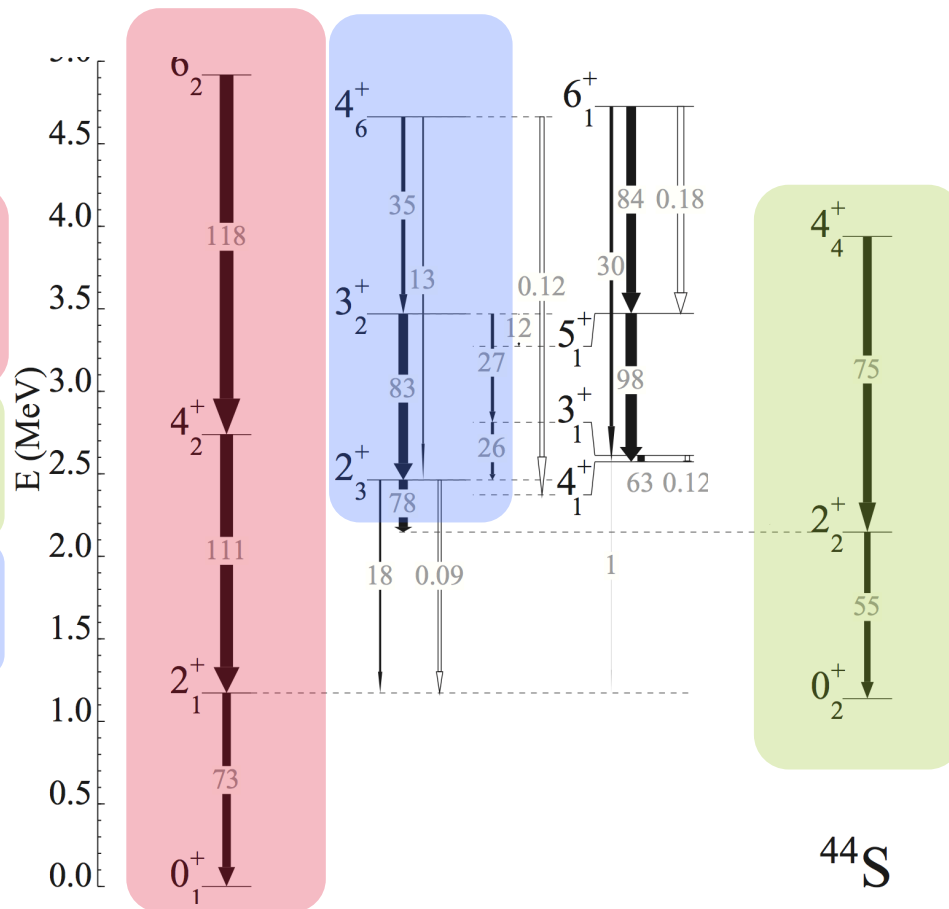


R. Chevrier and L. Gaodefroy, PRC **89**, 051301(R) (2014).

➔ Also good agreement on shape parameters.

Shape parameters from E2 invariants.

$J^\pi$	$Q_i$ ( $e\text{ fm}^2$ )	$\beta$	$\gamma$ (deg)	$\sigma(\gamma)$ (deg)
$0_1^+$	70	0.31	28	8
$2_1^+$	72	0.32	24	8
$4_2^+$	67	0.30	16	7
$6_2^+$	62	0.28	12	7
$0_2^+$	68	0.30	20	6
$2_2^+$	66	0.29	30	8
$4_4^+$	65	0.29	31	8
$2_3^+$	64	0.29	34	7
$3_2^+$	65	0.29	29	8
$4_6^+$	60	0.27	34	10
$3_1^+$	65	0.29	26	4
$4_1^+$	65	0.30	26	5
$5_1^+$	63	0.28	26	4
$6_1^+$	61	0.27	28	3

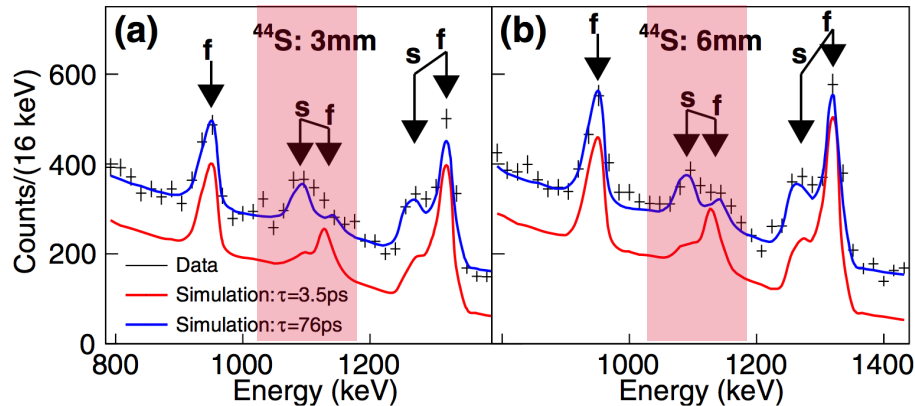


R. Chevrier and L. Gaodefroy, PRC **89**, 051301(R) (2014).

# $^{44}\text{S}$ : $K=4$ EXCITED BAND

## MSU – Recoil-distance method

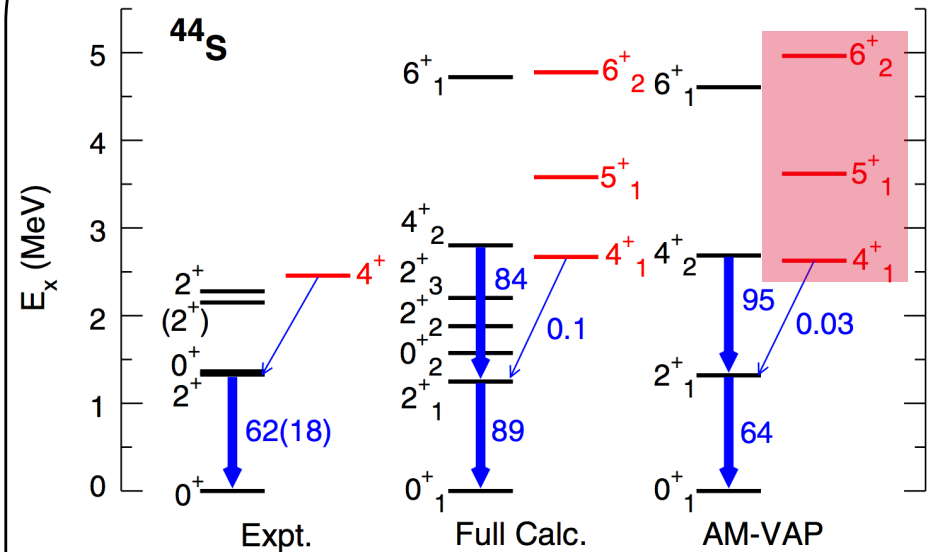
J.J. Parker et al., PRL **118**, 052501 (2017).



✓  $4^+ \rightarrow 2^+$  transition : 76ps.

## BMF-SM

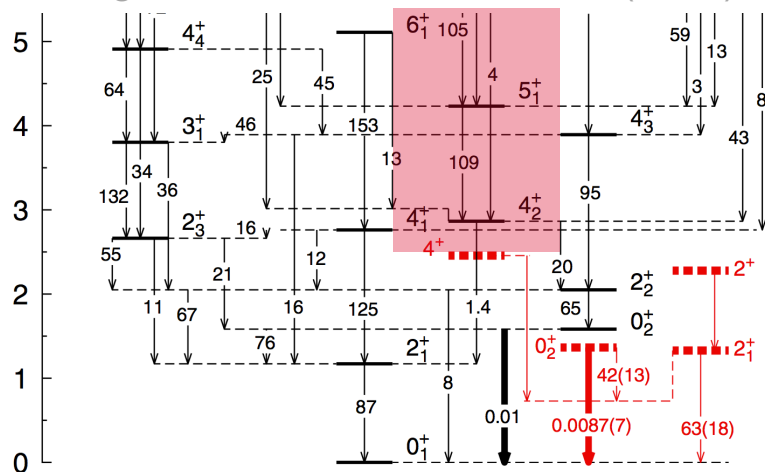
Y. Utsuno et al., PRL **114**, 032501 (2015).



$I^\pi_\sigma$	$ K $						$\beta$	$\gamma$
	0	1	2	3	4	5		
$0^+_1$	1.00						0.24	33
$2^+_1$	0.98	0.00	0.01				0.26	23
$4^+_2$	0.92	0.08	0.00	0.00	0.00		0.28	14
$6^+_1$	0.76	0.23	0.01	0.00	0.00	0.00	0.28	13
$4^+_1$	0.00	0.00	0.00	0.07	0.93		0.23	28
$5^+_1$	0.00	0.00	0.01	0.08	0.85	0.07	0.23	24
$6^+_2$	0.00	0.01	0.01	0.14	0.80	0.04	0.23	26

## BMF – Collective + SP

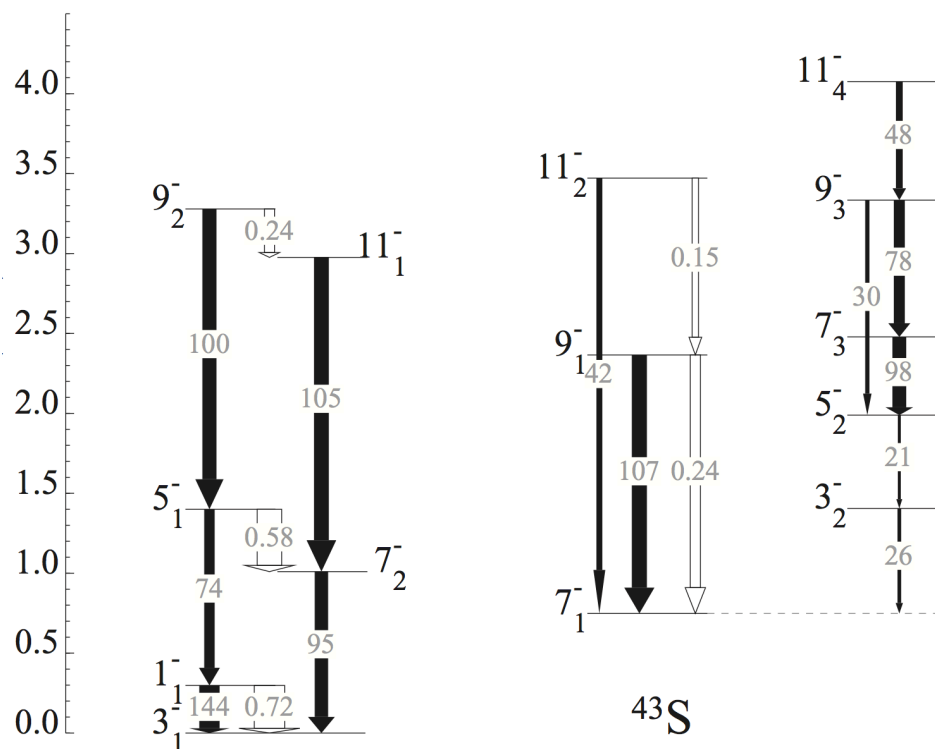
J.L. Egido et al., PRL **116**, 052502 (2016).



Low lying high K isomer.

## SHAPE COEXISTENCE AT N=28

- N=28 → Shape transition from Ca to Si/Mg.
- Complex coexistence features at Z=16.
- Large impact of triaxial degree of freedom.
- Convergence of all theoretical descriptions (BMF, AMD, SM).



- $^{42}\text{S}$  (d,p) good probe for GS rotational band.

B. Elbek et al., Adv. Nucl. Phys. 3, 259 (1969).

- Spectroscopy of  $^{43}\text{S}$  of interest.
- $3/2^-$  intruder GS also predicted in  $^{41}\text{Si}$ .
- Oblate/prolate shape coexistence predicted in  $^{42}\text{Si}$ .

F. Nowacki and A. Poves, PRC79, 014310 (2009).