

# Probing nucleon-nucleon correlations via (p,pd) QFS Reactions

**A. O. Macchiavelli**

*Physics Division, Oak Ridge National Laboratory, USA*

**Stefanos Paschalis and Marina Petri**

*Department of Physics, University of York, York, YO10 5DD, UK*



**Experimental and Theoretical Aspects of  
Neutron-Proton Pairing and  
Quartet Correlations in Atomic Nuclei**

**September 4-8th, 2023**



ELSEVIER

Nuclear Physics A649 (1999) 45c

---

---

NUCLEAR  
PHYSICS A

---

---

Why are nuclei described by independent particle motion ?

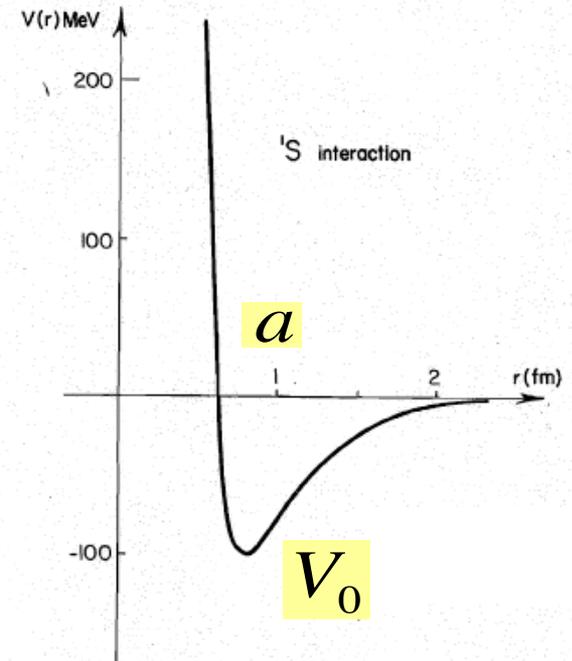
B.R. Mottelson<sup>a\*</sup>

<sup>a\*</sup>The Niels Bohr Institute and NORDITA, Blegdamsvej 17, DK-2100 Copenhagen Ø,  
Denmark

“Quantality Parameter”

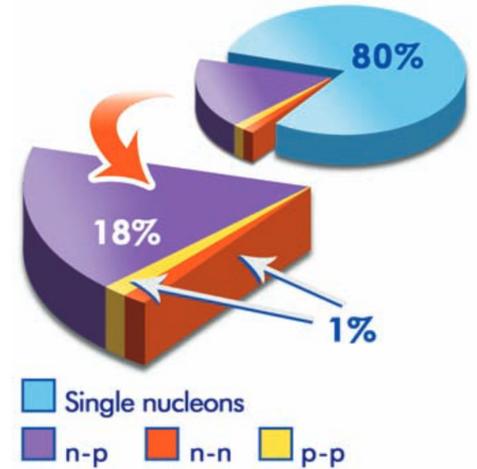
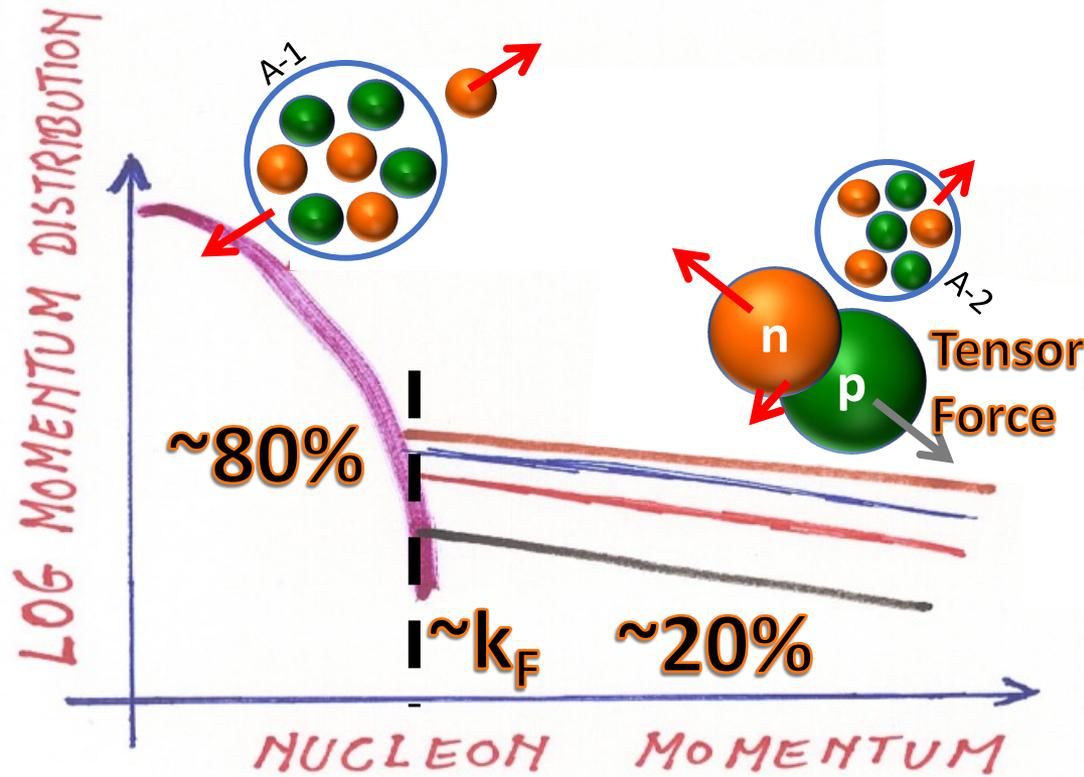
$$\Lambda = \frac{\hbar^2 / Ma^2}{V_0}$$

| Constituents  | M  | $V_0$ [eV]        | a [cm]              | $\Lambda$ | T=0 matter |
|---------------|----|-------------------|---------------------|-----------|------------|
| $^3\text{He}$ | 3  | $9 \cdot 10^{-4}$ | $2.9 \cdot 10^{-8}$ | 0.21      | liquid     |
| $^4\text{He}$ | 4  | $9 \cdot 10^{-4}$ | $2.9 \cdot 10^{-8}$ | 0.16      | liquid     |
| $\text{H}_2$  | 2  | $3 \cdot 10^{-3}$ | $3.3 \cdot 10^{-8}$ | 0.07      | solid      |
| Ne            | 20 | $3 \cdot 10^{-3}$ | $3.1 \cdot 10^{-8}$ | 0.007     | solid      |
| nuclei        | 1  | $1 \cdot 10^8$    | $9 \cdot 10^{-14}$  | 0.4       | liquid     |



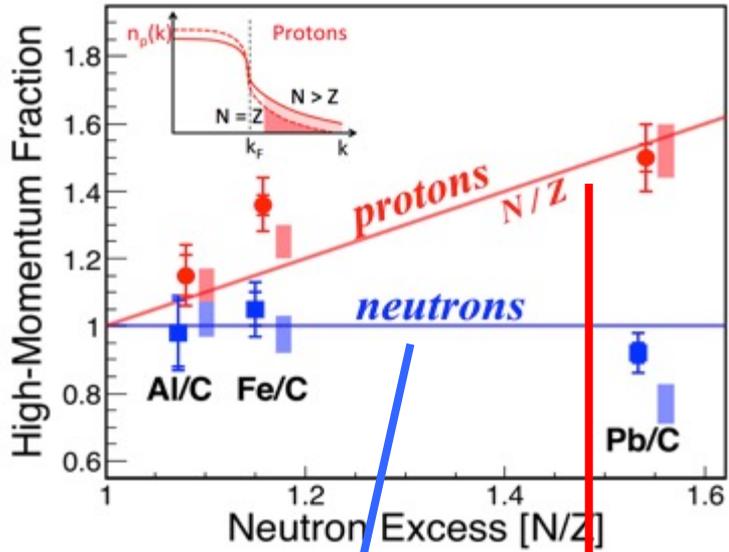
Fermi Liquid  $\rightarrow$  quasiparticles

# Results from JLab on Short-Range Correlations (SRC)



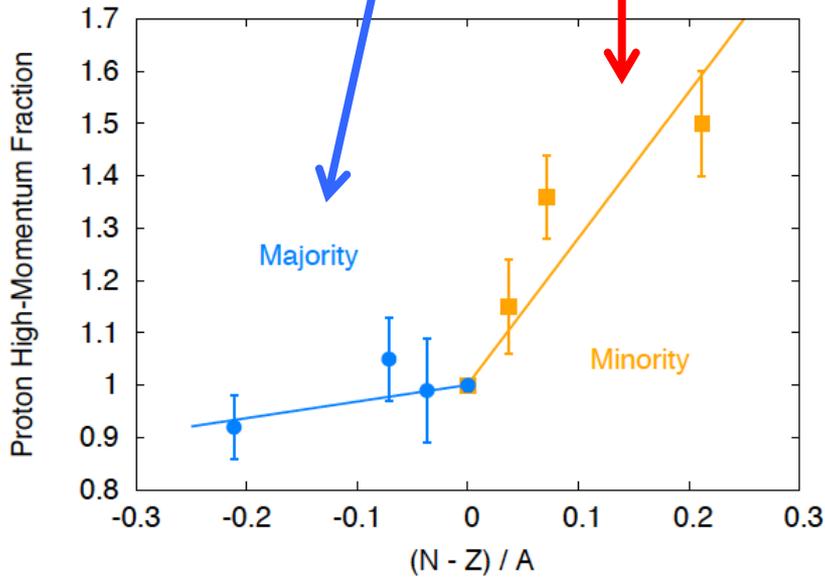
Manifestation of tensor part of the NN interaction which favours the  $S=1, T=0$  (quasi-deuteron) channel

# SRC



$$N > Z : R_{\text{SRC}} = \gamma \left( 1 + SL_{\text{SRC}}^{\text{p}} \frac{N - Z}{A} \right),$$

$$N < Z : R_{\text{SRC}} = \gamma \left( 1 + SL_{\text{SRC}}^{\text{n}} \frac{N - Z}{A} \right).$$

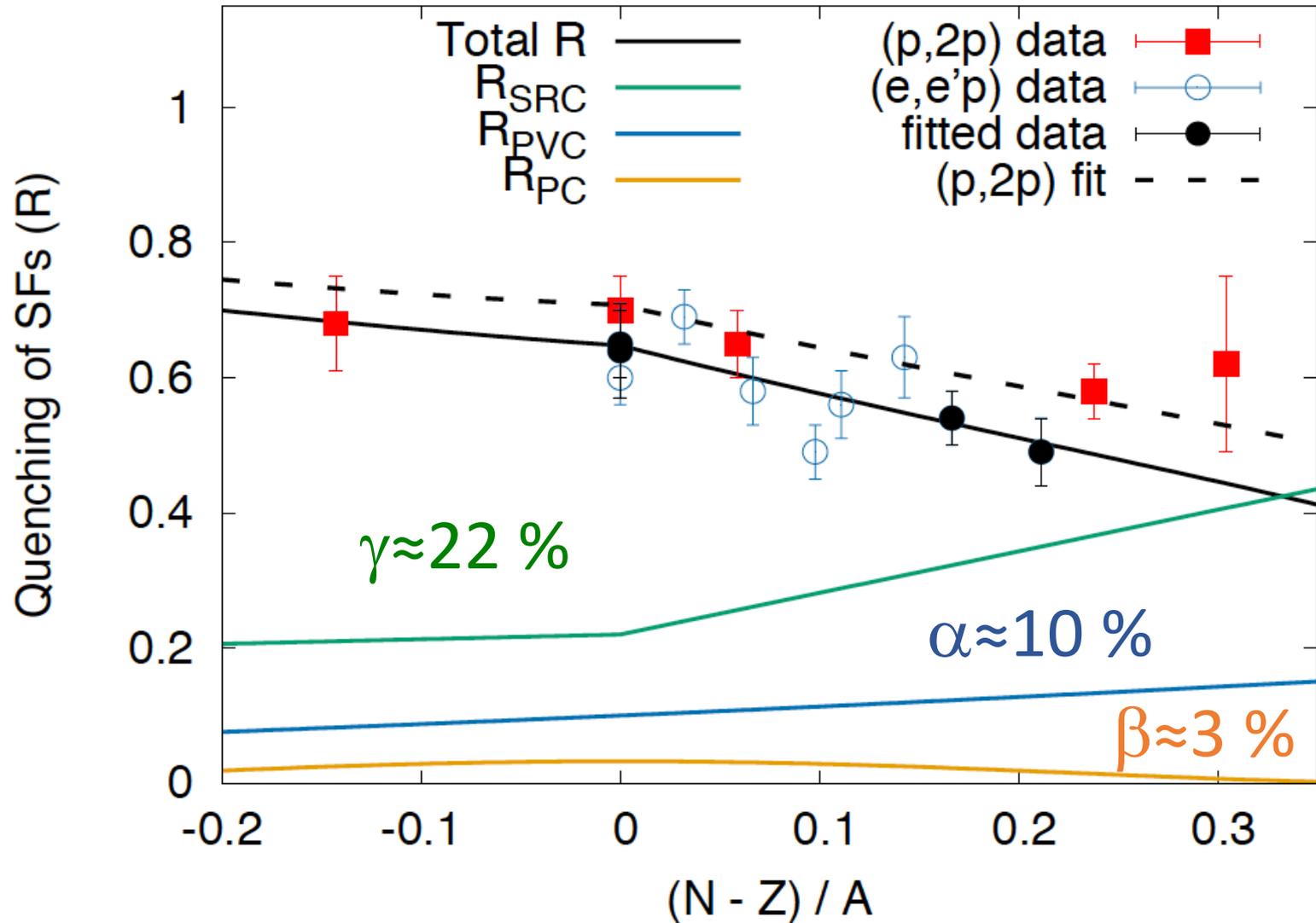


$$SL_{\text{SRC}}^{\text{p}} = 2.8 \pm 0.7$$

$$SL_{\text{SRC}}^{\text{n}} = 0.3 \pm 0.2$$

$$R = 1 - \left( R_{\text{PVC}} + R_{\text{PC}} + R_{\text{SRC}} \right)$$

$\alpha$                        $\beta$                        $\gamma$



## How do the IPM particles get dressed by the SRC?

We follow the seminal discussions of Brueckner,

*“The evidence is that for relative distances less than roughly  $10^{-13}$ cm, nucleon pairs in nuclei are correlated in the same way as they are in the deuteron or in free scattering processes”*

[from K.A. Brueckner, Proceedings of the Rutherford Jubilee Int. Conf. Manchester 1961, Ed. J.B.Birks, London, **1961**]

# Strong Interest in Theory

PHYSICAL REVIEW C **104**, 034311 (2021)

---

## Short-range correlation physics at low renormalization group resolution

A. J. Tropiano <sup>1</sup>, S. K. Bogner,<sup>2</sup> and R. J. Furnstahl <sup>1</sup>

<sup>1</sup>*Department of Physics, The Ohio State University, Columbus, Ohio 43210, USA*

<sup>2</sup>*Facility for Rare Isotope Beams and Department of Physics and Astronomy, Michigan State University, East Lansing, Michigan 48824, USA*

 (Received 18 June 2021; accepted 30 August 2021; published 13 September 2021)

---

PHYSICAL REVIEW C **106**, 024324 (2022)

---

## Quasi-deuteron model at low renormalization group resolution

A. J. Tropiano <sup>1</sup>, S. K. Bogner <sup>2,\*</sup>, R. J. Furnstahl <sup>1</sup> and M. A. Hisham <sup>1,†</sup>

<sup>1</sup>*Department of Physics, The Ohio State University, Columbus, Ohio 43210, USA*

<sup>2</sup>*Facility for Rare Isotope Beams and Department of Physics and Astronomy, Michigan State University, East Lansing, Michigan 48824, USA*

 (Received 25 May 2022; accepted 28 July 2022; published 19 August 2022)

*“The nuclear wave function must include two-body short-range correlations (SRCs) with deuteron-like quantum numbers.”*



Regular Article - Theoretical Physics

## Embedding short-range correlations in relativistic density functionals through quasi-deuterons

S. Burrello<sup>1,a</sup> , S. Typel<sup>1,2,b</sup> 

<sup>1</sup> Technische Universität Darmstadt, Fachbereich Physik, Institut für Kernphysik, Schlossgartenstraße 9, 64289 Darmstadt, Germany

<sup>2</sup> GSI Helmholtzzentrum für Schwerionenforschung GmbH, Theorie, Planckstraße 1, 64291 Darmstadt, Germany

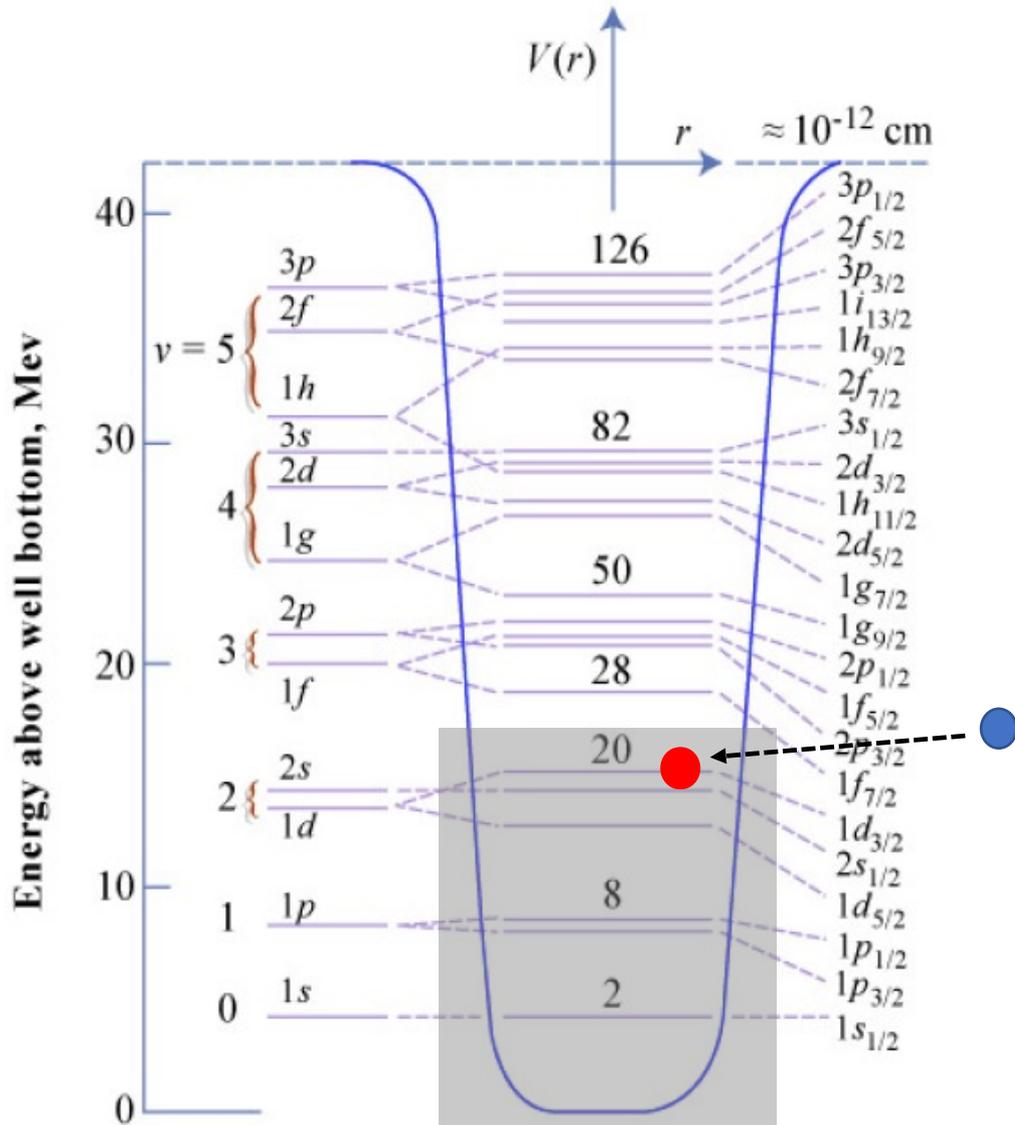
Received: 1 April 2022 / Accepted: 12 June 2022 / Published online: 6 July 2022

© The Author(s) 2022

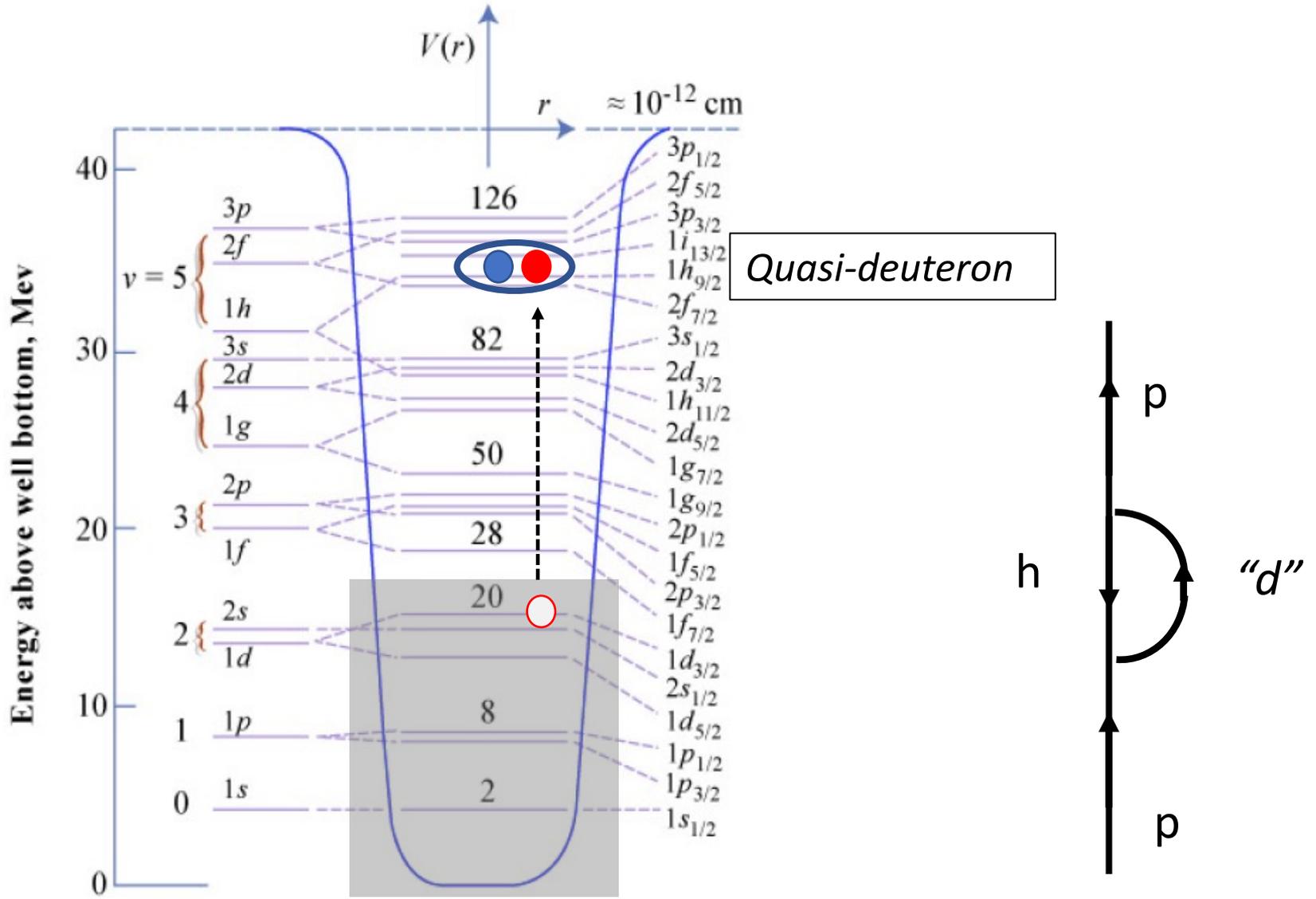
Communicated by Vittorio Somà

*“The formation of clusters at sub-saturation densities, as a result of many-body correlations, constitutes an essential feature for a reliable modelization of the nuclear matter equation of state (EoS).”*

# How do the IPM particles get dressed by the SRC?

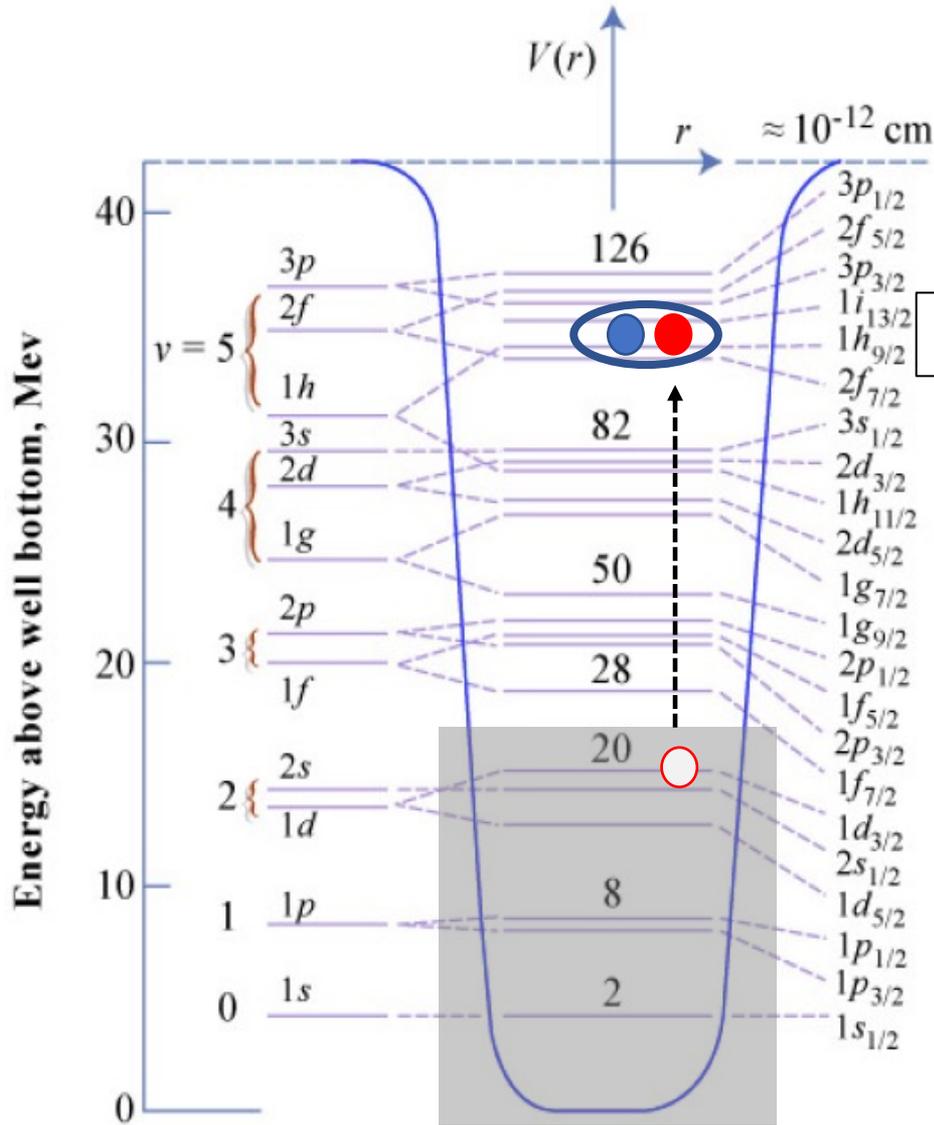


How do the IPM particles get dressed by the SRC?



$|qp\rangle \sim 80\% |p\rangle + 20\% |h\rangle + x |qd\rangle + \dots$

How do the IPM particles get dressed by the SRC?

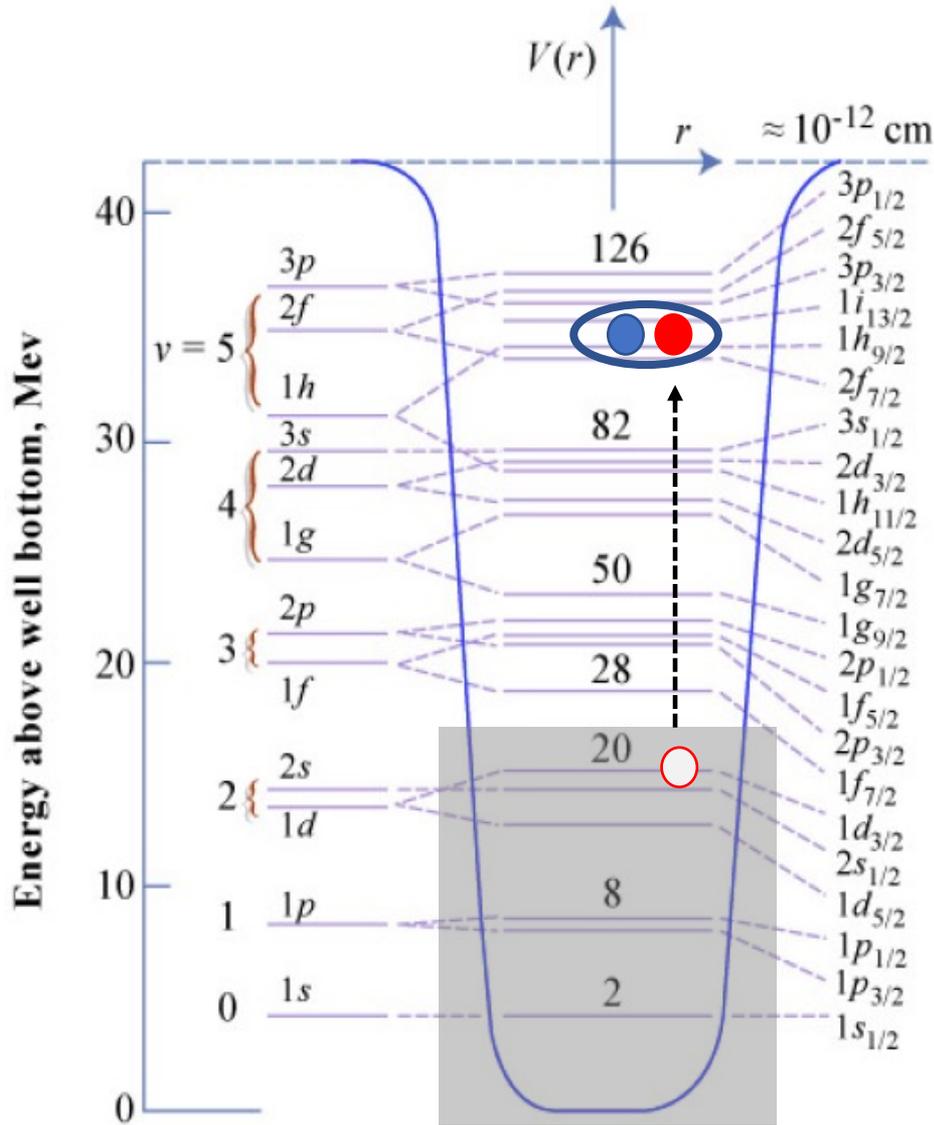


Quasi-deuteron

Maria Patsyuk  
BM@N

$|qp\rangle \sim 80\% |p\rangle + 20\% |h\rangle \times |qd\rangle \text{ ???}$

How do the IPM particles get dressed by the SRC?



Quasi-deuteron

Isao Tanihata - RCNP

(p,pd) reaction studies  
R3B @ GSI

$|qp\rangle \sim 80\% |p\rangle + 20\% |h\rangle + |qd\rangle \text{ ???}$

# Probing nucleon-nucleon correlations in atomic nuclei via (p,pd) QFS Reactions

Experiment G-22-00091 (approved by the GSI PAC)

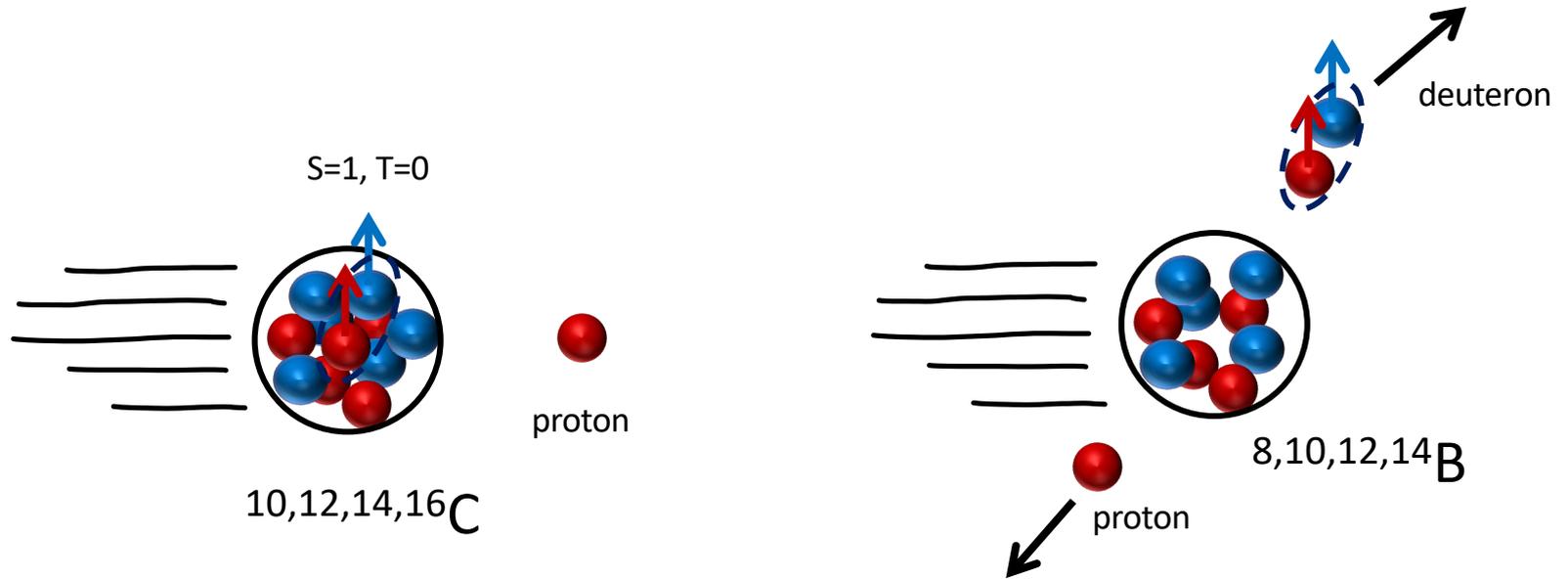
---

M. Petri<sup>1</sup>, S. Paschalis<sup>1</sup>, A. O. Macchiavelli<sup>2</sup>  
for the R<sup>3</sup>B Collaboration

<sup>1</sup> Department of Physics, University of York, UK

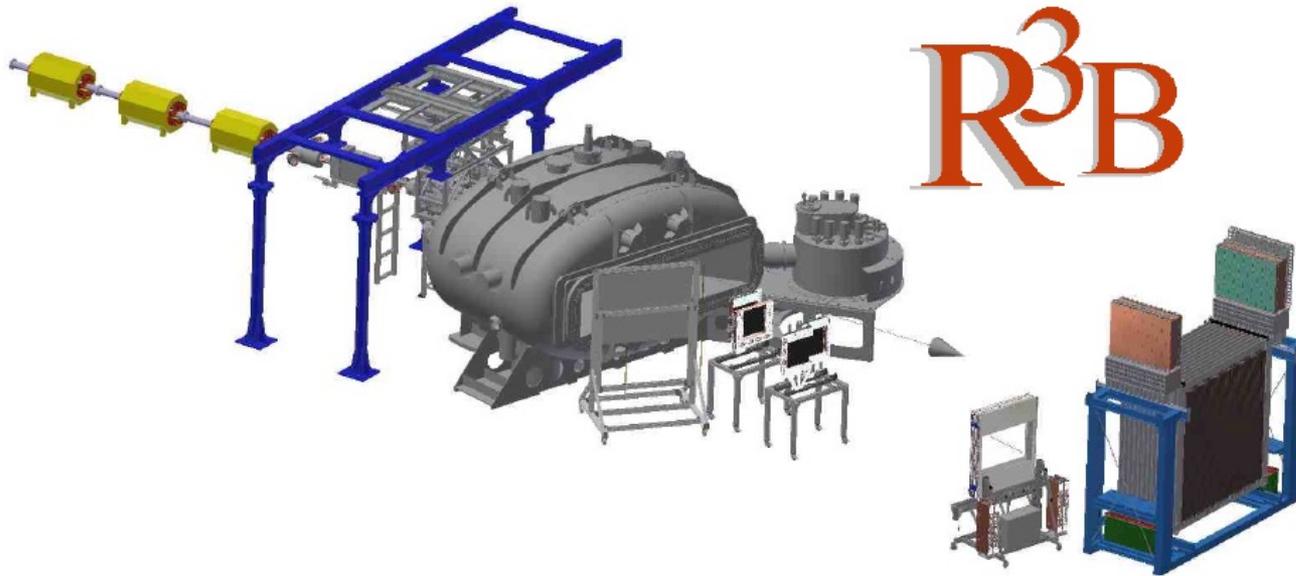
<sup>2</sup> Physics Division, Oak Ridge National Laboratory, USA

# (p,pd) QFS reactions



- Quasi-elastically knocking out deuterons along the C isotopic chain to probe the number of quasi-deuterons in a nucleus and their isospin dependence

# (p,pd) QFS reactions

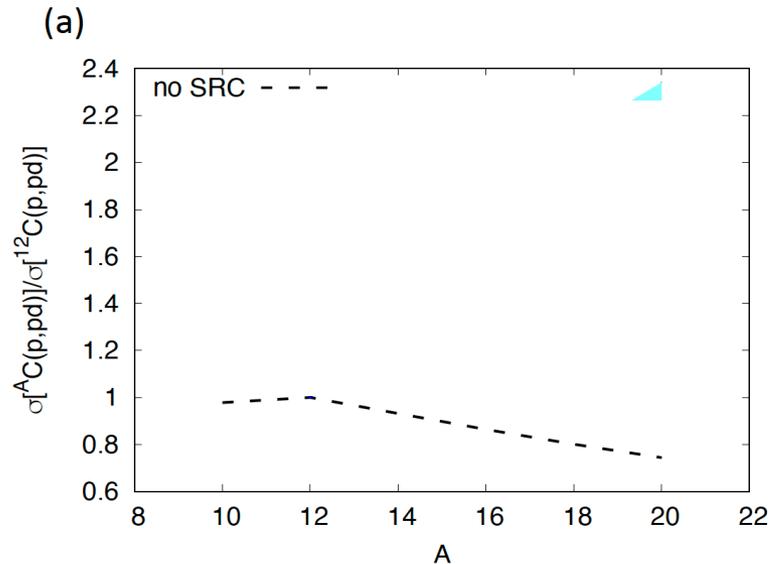


- Kinematically complete measurements (at R<sup>3</sup>B using high purity beams from FRS at high energy (justifying the Quasi-elastic assumption))

# (p,pd) QFS reactions

In a non-interacting system, the  ${}^A\text{C}(p,pd)$  cross section should scale with the number of  $1^+ T=0$  n-p pairs that can be formed in the given  ${}^A\text{C}$  system. The number of  $T=0$  n-p pairs in a system of  $A$  nucleons with isospin  $T$  is given as  $A^2/8 + A/4 - T(T+1)/2$ , which naturally decreases in more asymmetric systems. Specifically for the C isotopes, we estimate that about 50% of these pairs have the  $1^+$  spin/parity assignment that corresponds to the deuteron ground state.

Furthermore, we estimate a 50% overlap between the  $1^+$ ,  $T=0$  shell-model  $p^2_{3/2,1/2}$  n-p pairs and the detected  ${}^3\text{S}_1$  deuteron. Scaling the number of deuterons to the one in  ${}^{12}\text{C}$ , we should expect an  $A$  dependency of the cross section



## SRC and quasi-deuterons

Due to short range correlations single particle excitations of  $\Delta E \sim 50$  MeV will occur with the probability discussed above.

$$\Delta p \sim \frac{\hbar}{\Delta x}$$

This corresponds to changes in the principal oscillator quantum number

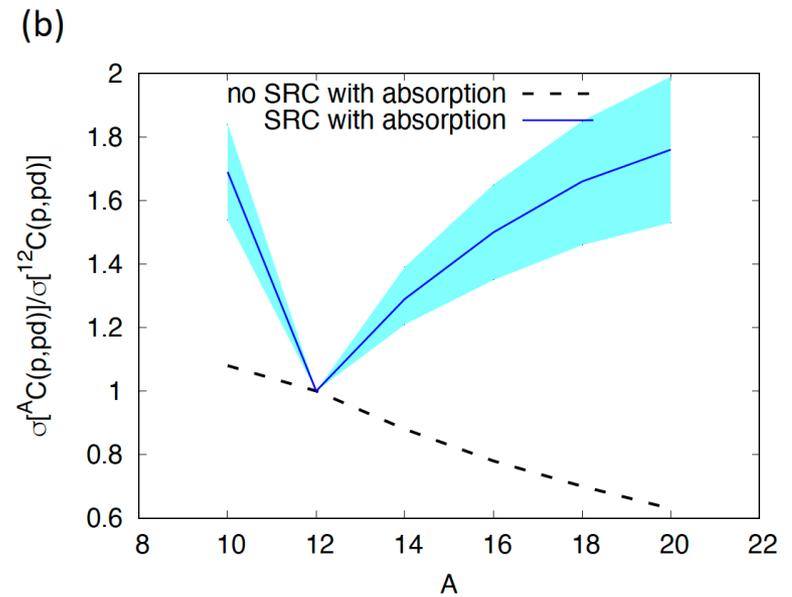
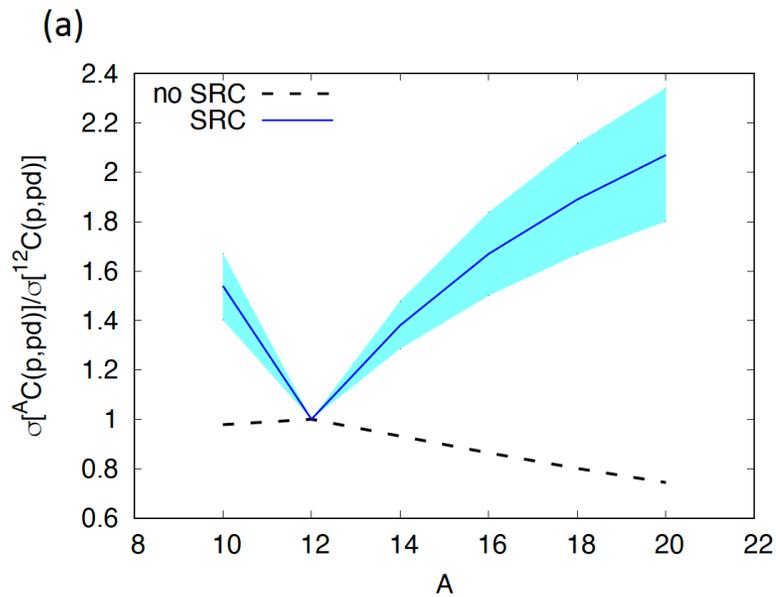
$$\Delta N \sim \Delta E / \hbar \omega_0$$

$$|qp\rangle \sim 80\% |p\rangle + 20\% |h\rangle \times |qd\rangle \quad \text{????}$$

$$|qd\rangle \approx \frac{\sum_j (2j+1) |j^2\rangle^{1+}}{\sum_j (2j+1)}$$

*project the  ${}^3S_1$  amplitude that becomes smaller the larger the  $j$*

# (p,pd) QFS reactions



# Cross-sections estimate

ISSN 1063-7788. Physics of Atomic Nuclei. 2017, Vol. 80, No. 6, pp. 1061–1072. © Pleiades Publishing, Ltd., 2017.  
Original Russian Text © A.A. Terekhin, V.P. Ladygin, Yu.V. Gurchin, A.Yu. Isupov, A.K. Kurilkin, P.K. Kurilkin, N.B. Ladygina, S.M. Piyadin, S.G. Reznikov, A.N. Khrenov,  
2017, published in Yadernaya Fizika, 2017, Vol. 80, No. 6, pp. 594–604.

## NUCLEI Experiment

### Differential Cross Section for Elastic Deuteron–Proton Scattering at the Energy of 700 MeV per Nucleon

A. A. Terekhin\*, V. P. Ladygin, Yu. V. Gurchin, A. Yu. Isupov, A. K. Kurilkin,  
P. K. Kurilkin, N. B. Ladygina, S. M. Piyadin, S. G. Reznikov, and A. N. Khrenov

Joint Institute for Nuclear Research, ul. Joliot-Curie 6, Dubna, Moscow oblast, 141980 Russia

Received May 22, 2017

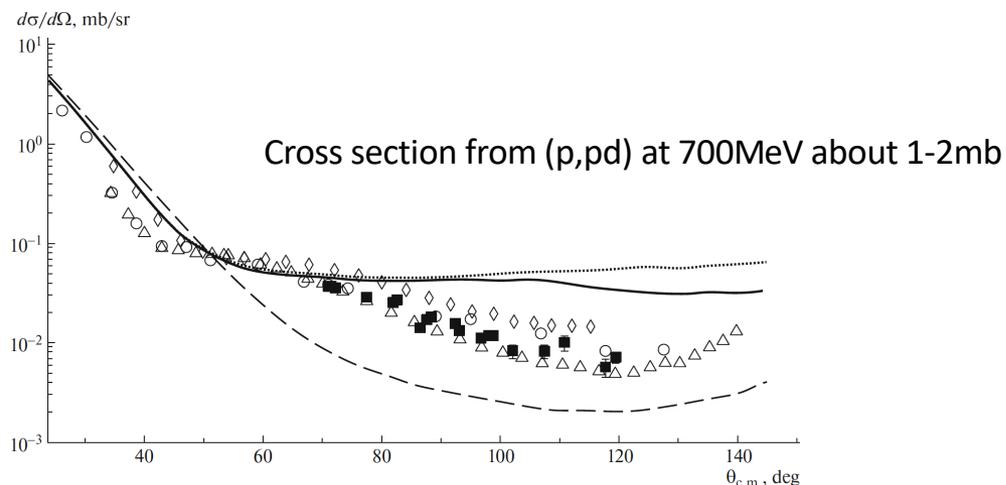


Fig. 8. Differential cross section for elastic deuteron–proton scattering at the energy of 700 MeV per nucleon: (closed boxes) results of measurements at the nucleotron; (open diamonds, circles, and triangles) experimental data at the energies of, respectively, 641.3, 792.7 [34], and 800 MeV/nucleon [35]; and (dotted, dashed, and solid curves) results of, respectively, ONE + SS, ONE + SS + DS, and ONE + SS + DS +  $\Delta$  calculations performed within the relativistic multiple-scattering model [30–32, 44] at the energy of 700 MeV per nucleon.

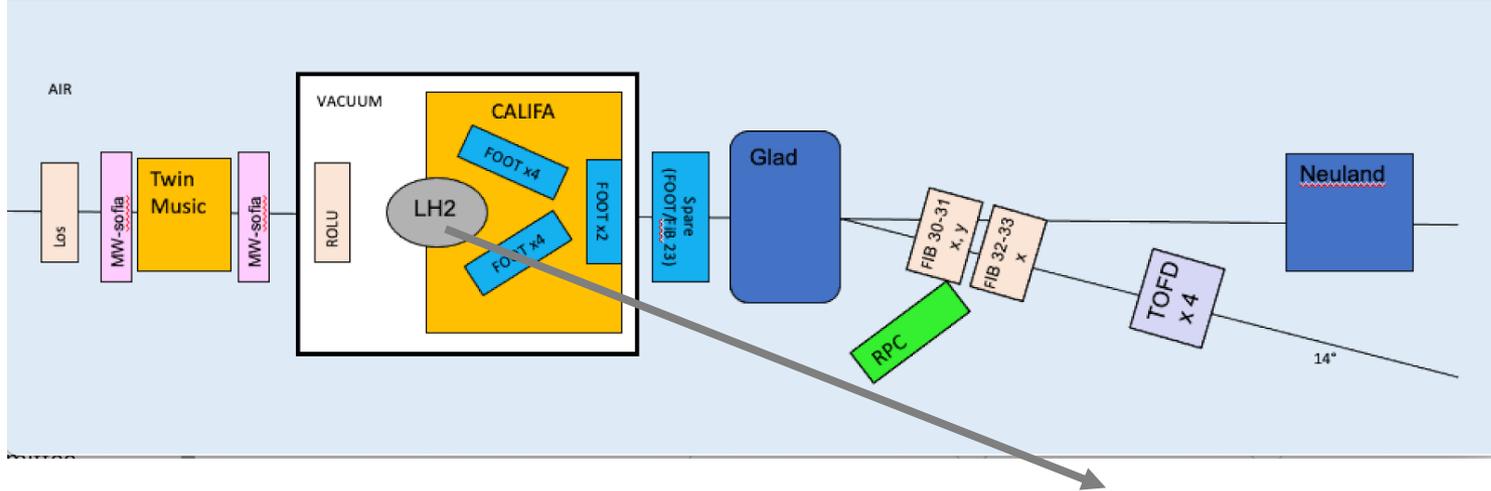
Table 3. Differential cross section for elastic deuteron–proton scattering at the energy of 700 MeV per nucleon

| $\theta_{c.m.}, \text{deg}$ | $d\sigma/d\Omega, \mu\text{b/sr}$ | $\Delta\sigma_{\text{stat}}, \mu\text{b/sr}$ | $\Delta\sigma_{\text{syst}}, \mu\text{b/sr}$ |
|-----------------------------|-----------------------------------|--|--|
| 71.2                        | 36.33                             | 1.20   | 5.07   |
| 71.6                        | 35.91                             | 1.28   | 5.14   |
| 72.3                        | 35.01                             | 1.79   | 7.05   |
| 77.5                        | 28.36                             | 1.12   | 4.93   |
| 82.1                        | 25.12                             | 1.16   | 4.12   |
| 82.8                        | 26.38                             | 1.85   | 6.29   |
| 86.7                        | 13.78                             | 0.91   | 2.11   |
| 87.7                        | 16.61                             | 1.13   | 2.70   |
| 88.4                        | 17.29                             | 1.16   | 4.21   |
| 92.6                        | 15.06                             | 0.79   | 2.61   |
| 93.3                        | 12.98                             | 0.76   | 2.08   |
| 96.8                        | 10.98                             | 0.61   | 1.72   |
| 98.2                        | 11.43                             | 0.67   | 1.92   |
| 98.9                        | 11.62                             | 0.64   | 2.03   |
| 102.0                       | 8.15                              | 1.26   | 2.13   |
| 107.6                       | 7.98                              | 1.21   | 2.33   |
| 110.8                       | 9.77                              | 1.58   | 2.86   |
| 117.8                       | 5.56                              | 1.16   | 1.56   |
| 119.5                       | 7.12                              | 0.83   | 1.47   |

Consistent with experiment S296

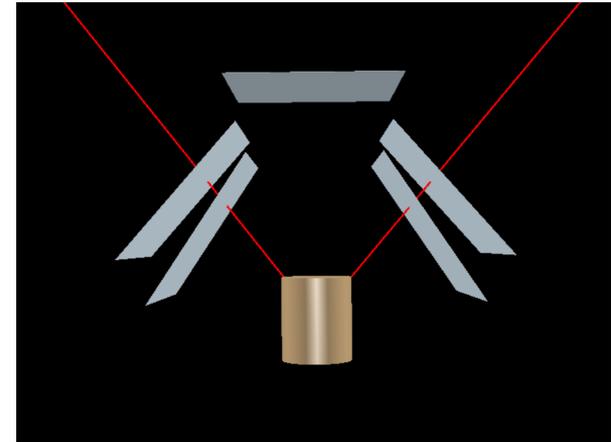
S. Panin *et al.* who estimated 1-2 mb for  $^{12}\text{C}(p,pd)$  at 400MeV/u in the same kinematic region of large momentum transfer

# Setup



The R<sup>3</sup>B setup Protons and deuterons emitted from the (p,pd) reactions of interest will be detected using the FOOT Si tracking detectors and the CALIFA calorimeter.

- FOOT covers 20-60 degrees
- In the angular range considered here, we estimate an integrated cross section of about 1mb for the (p,pd) QFS reactions. Geometric and detection efficiencies of the detectors for measuring (p,pd) at these angles: 20%.
- 5cm LH2 target

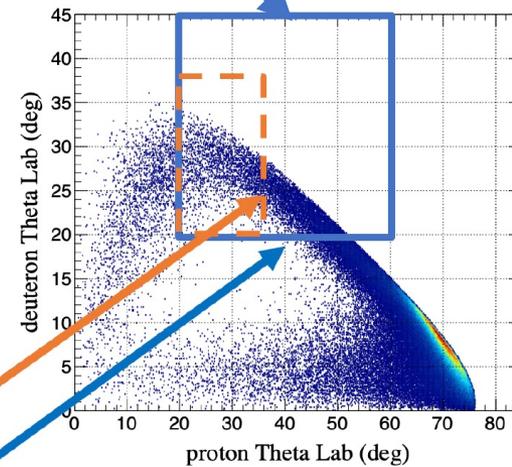
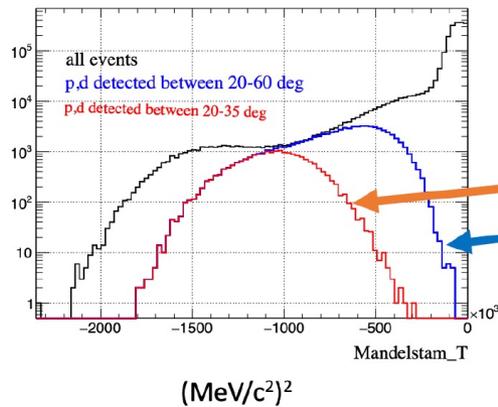


5cm LH2 target (R3BRoot simulations from A. Revel)

Kinematics of the  ${}^A\text{C}(p, pd)$  reaction at 480 MeV/u.

Angular coverage of the Si tracker and CALIFA (20-60 degrees), which includes the majority of the high-momentum transfer events

Kinematics for (p,pd) at 480 MeV/nucleon



High momentum transfer

# Rate estimates

- Assuming a 1 mb cross section, and  $5 \times 10^4$  pps for each incoming isotope of interest

|   | $^{10}\text{C}$ | $^{12}\text{C}$ | $^{14}\text{C}$ | $^{16}\text{C}$ |
|---|-----------------|-----------------|-----------------|-----------------|
| Primary target (mg/cm <sup>2</sup> )          | 16076           | 16076           | 16076           | 16076           |
| <b>Particles/5x10<sup>10</sup> beam/spill</b> | 2.29E+05        | 5.45E+06        | 7.60E+06        | 1.13E+06        |
| Total rate                                    | 2.34E+05        | 5.45E+06        | 7.65E+06        | 1.13E+06        |
| Purity  | 9.79E+01        | 9.97E+01        | 9.95E+01        | 9.96E+01        |
| Spill length (s)                              | 1               | 1               | 1               | 1               |
| <b>Final rate (pps)</b>                       | <b>5.73E+04</b> | <b>1.36E+06</b> | <b>1.90E+06</b> | <b>2.81E+05</b> |

24 h per target will reach a **statistical uncertainty better than 5%** in the cross-section measurements,

# Rate estimates

- Assuming a 1 mb cross section, and  $5 \times 10^4$  pps for each incoming isotope of interest

**STAY TUNED!**

|   | $^{10}\text{C}$ |                 |                 |                 |
|---|-----------------|-----------------|-----------------|-----------------|
| Primary target (mg/cm <sup>2</sup> )          | 16076           | 1               |                 |                 |
| <b>Particles/5x10<sup>10</sup> beam/spill</b> | 2.29E+05        | 5.45E+06        | 7.60E+06        | 1.13E+06        |
| Total rate                                    | 2.34E+05        | 5.45E+06        | 7.65E+06        | 1.13E+06        |
| Purity  | 9.79E+01        | 9.97E+01        | 9.95E+01        | 9.96E+01        |
| Spill length (s)                              | 1               | 1               | 1               | 1               |
| <b>Final rate (pps)</b>                       | <b>5.73E+04</b> | <b>1.36E+06</b> | <b>1.90E+06</b> | <b>2.81E+05</b> |

24 h per target will reach a **statistical uncertainty better than 5%** in the cross-section measurements,

# A somewhat related question

## Science

### Formation of $\alpha$ clusters in dilute neutron-rich matter

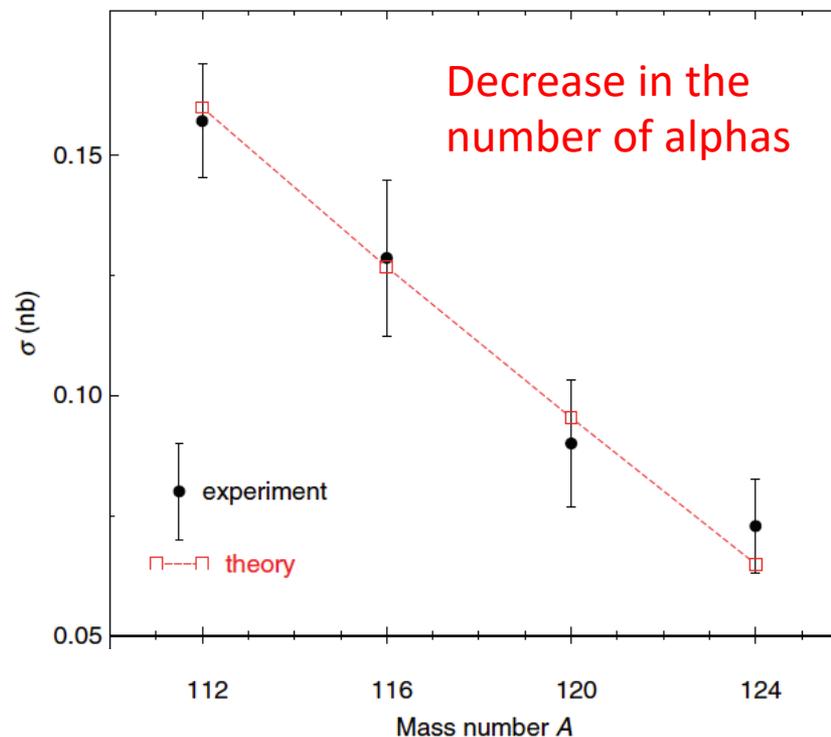
Junki Tanaka, Zaihong Yang, Stefan Typel, Satoshi Adachi, Shiwei Bai, Patrik van Beek, Didier Beaumel, Yuki Fujikawa, Jiaxing Han, Sebastian Heil, Siwei Huang, Azusa Inoue, Ying Jiang, Marco Knösel, Nobuyuki Kobayashi, Yuki Kubota, Wei Liu, Jianling Lou, Yukie Maeda, Yohei Matsuda, Kenjiro Miki, Shoken Nakamura, Kazuyuki Ogata, Valerii Panin, Heiko Scheit, Fabia Schindler, Philipp Schrock, Dmytro Symochko, Atsushi Tamii, Tomohiro Uesaka, Vadim Wagner, Kazuki Yoshida, Juzo Zenihiro and Thomas Aumann

*Science* **371** (6526), 260-264.  
DOI: 10.1126/science.abe4688

Do SRCs have anything to say?



Piet's Shell Model Analysis  
provides a much needed  
reference !



# Acknowledgments

\* This work is based on the research supported in by the Director, Office of Science, Office of Nuclear Physics, of the U.S. Department of Energy under Contract No. DE-AC05-00OR22725.

# Acknowledgments

\* This work is based on the research supported in by the Director, Office of Science, Office of Nuclear Physics, of the U.S. Department of Energy under Contract No. DE-AC05-00OR22725.

**Merci !**