



Overview of nuclear parton distribution functions from LHC to EIC

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AoF CoE in Quark Matter partner in ERC AdG YoctoLHC

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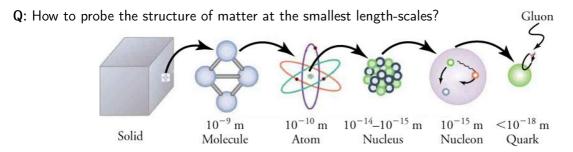




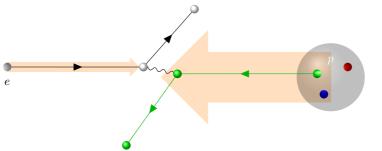
Outlook

- 1. What, how and why? / The age-old questions
- 2. Where are we now? / Recent developments
- 3. What we would like to know better? / More A and towards 3D

Probing the nucleon structure

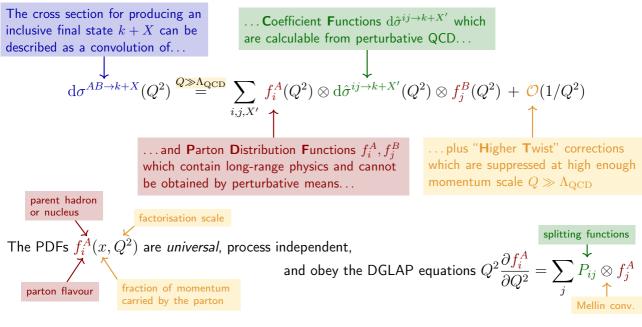


A: Hit it as hard as you can and see what comes out



But what is it that we are probing at sub-nucleon level? → Need help from theory!

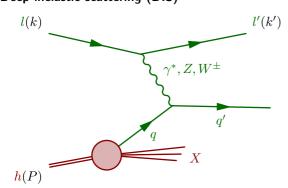
At the heart of it all: Collinear factorisation of QCD



... this is the framework which every PDF analysis and application relies on and tests!

Basic processes – leptonic final states

Deep inelastic scattering (DIS)



For the photon-mediated case:

$$\frac{\mathrm{d}^2 \sigma^{\mathrm{DIS}}}{\mathrm{d}x \mathrm{d}Q^2} = \frac{\mathrm{d}^2 \hat{\sigma}}{\mathrm{d}x \mathrm{d}Q^2} \sum_{i \in \{q,\bar{q}\}} e_i^2 f_i^h(x,Q^2) + \underset{\mathrm{corrections}}{\overset{\mathrm{NLO}}{\mathrm{NLO}}}$$

 $\frac{\mathrm{d}x\mathrm{d}Q^2}{\mathrm{d}x\mathrm{d}Q^2} \frac{\mathrm{d}x\mathrm{d}Q^2}{i\in\{q,\bar{q}\}}$ $Q^2 = -(k-k')^2$ $x = \frac{Q^2}{2P\cdot(k-k')}$ access scale and momentumfraction dependence through external kinematics

Drell-Yan (DY) h'(P') = X $q' = \gamma^*, Z, W^{\pm}$ l'(k')

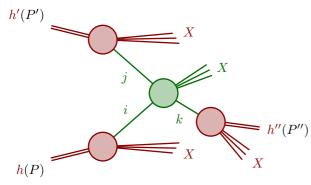
The photon-mediated case:

$$\frac{\mathrm{d}^2 \sigma^{\mathrm{DY}}}{\mathrm{d}y \mathrm{d}M^2} = \frac{4\pi \alpha_{\mathrm{e.m.}}^2}{9M^4} \sum_{i \in \{q,\bar{q}\}} e_i^2 x_1 x_2 f_i^h(x_1, M^2) f_i^{h'}(x_2, M^2) + \sum_{\mathrm{corrections}}^{\mathrm{NLO}} M^2 = (k + k')^2 = x_1 x_2 s$$

$$y = \frac{1}{2} \log \frac{(k_0 + k'_0) + (k_3 + k'_3)}{(k_0 + k'_0) - (k_3 + k'_2)} = \frac{1}{2} \log \frac{x_1}{x_2}$$

Basic processes – hadronic final states

Hadron-production

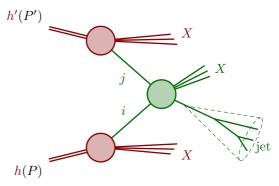


$$\sigma^{h+h'\to h''+X} = \sum_{i,j,k\in\{q,\bar{q},g\}} f_i^h \otimes f_j^{h'} \otimes \hat{\sigma}^{ij\to k+X} \otimes D_k^{h''}$$

Account for the hadronization effects with the parton to hadron fragmentation functions $D_k^{h^{\prime\prime}}$

ightarrow a source of uncertainty for PDF fits

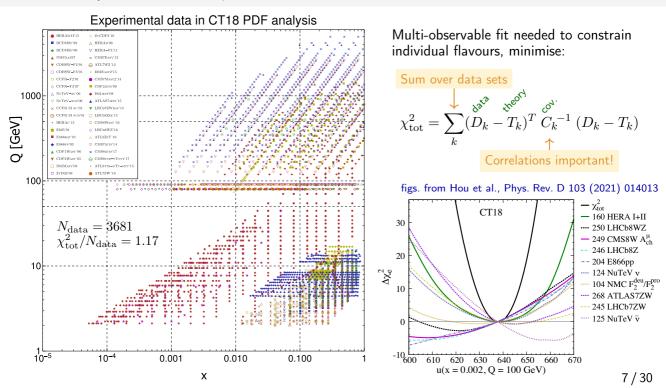
Jet-production



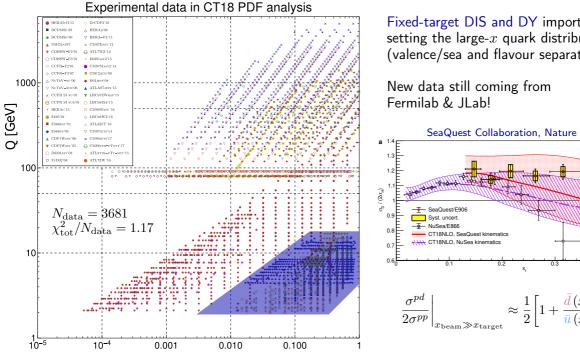
Additional complications:

- need an IR-safe definition of a jet
- non-perturbative corrections

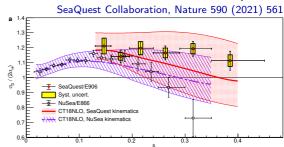
Global analysis – a multi-experiment-multi-observable fit



Global analysis – a multi-experiment-multi-observable fit

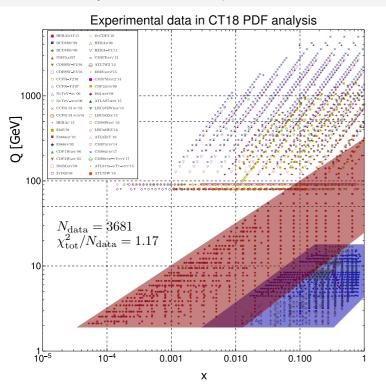


Fixed-target DIS and DY important in setting the large-x quark distributions (valence/sea and flavour separation)

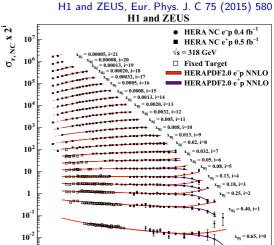


$$\left. \frac{\sigma^{pd}}{2\sigma^{pp}} \right|_{x_{\mathrm{beam}} \gg x_{\mathrm{target}}} \approx \frac{1}{2} \left[1 + \frac{\bar{d}\left(x_{\mathrm{target}}\right)}{\bar{u}\left(x_{\mathrm{target}}\right)} \right]$$

Global analysis – a multi-experiment-multi-observable fit



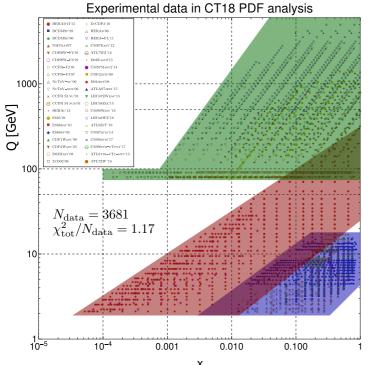
Collider DIS from HERA with large x, Q^2 lever arm \rightarrow gluons through DGLAP



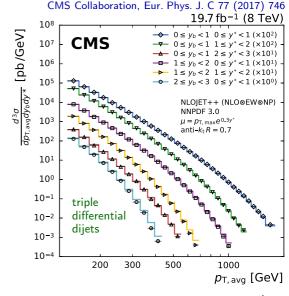
10⁻³

10

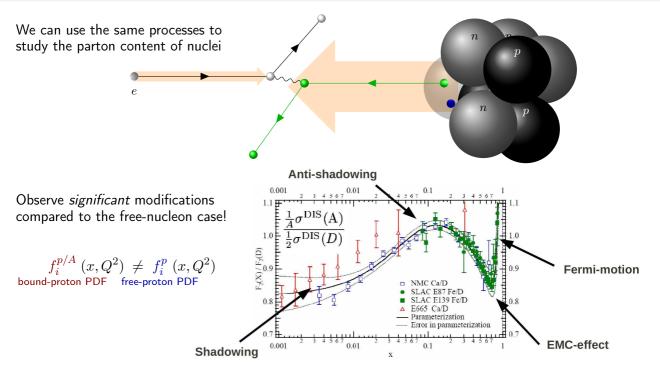
Global analysis – a multi-experiment–multi-observable fit



Hadron colliders give access to new processes $\rightarrow W^{\pm}, Z$, jets, $t\bar{t}$...



Why nuclear PDFs?

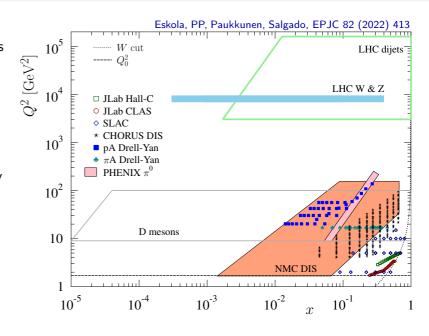


Nuclear PDFs from global analyses

Nuclear PDFs (nPDFs) are fitted with similar global analyses as their free-proton counterparts

- → rely only to the QCD collinear factorisation
- → model-agnostic way to study the nuclear effects

LHC is extending the x,Q^2 reach by orders of magnitude



Recent nPDF global fits

KSASG20

Order in α_s	NLO & NNLO	NLO & NNLO	NLO	NLO	NLO
<i>l</i> A NC DIS	✓	✓	√	✓	✓
uA CC DIS	✓	✓	√	✓	
pA DY	✓		√	✓	✓
$\pi A DY$			√		
RHIC dAu π^0, π^\pm			√		√
$\mid LHCpPb\pi^0,\!\pi^\pm,\!K^\pm \mid$					√
LHC pPb dijets			√	✓	
LHC pPb HQ			√GMVFN	√ FO+PS	√ ME fitting
LHC pPb W,Z		√	√	√	√
LHC pPb γ				✓	
0.117	100000	1.07.05.634	10.10.6.1	1.07.05.634	20.05.634
Q, W cut in DIS	1.3, 0.0 GeV	1.87, 3.5 GeV	1.3, 1.8 GeV	1.87, 3.5 GeV	2.0, 3.5 GeV
$p_{ m T}$ cut in HQ,inc h	N/A	N/A	3.0 GeV	0.0 GeV	3.0 GeV
_ Data points	4353	2410	2077	2188	1496
Free parameters	9	16	24	256	19
Error analysis	Hessian	Hessian	Hessian	Monte Carlo	Hessian
Free-proton PDFs	CT18	own fit	CT18A	\sim NNPDF4.0	∼CTEQ6M
Free-proton corr.	no	no	yes	yes	no
HQ treatment	FONLL	FONLL	S-ACOT	FONLL	S-ACOT
Indep. flavours	3	4	6	6	5
Reference	PRD 104, 034010	arXiv:2112.11904	EPJC 82, 413	arXiv:2201.12363	arXiv:2204.09982
*see also PRD 103 (2021) 114015 & arXiv:2204.13157 10 / 30					

EPPS21

nNNPDF3.0

TUJU21

nCTEQ15HQ*

Example parametrization: EPPS21

■ Define nuclear PDFs in terms of

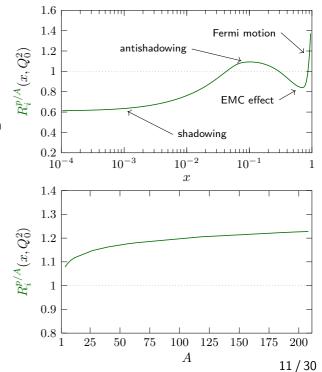
nuclear modification
$$f_{i}^{p/A}\left(x,Q^{2}\right) \ = \ R_{i}^{p/A}\left(x,Q^{2}\right) \, f_{i}^{p}\left(x,Q^{2}\right)$$
 bound-proton PDF free-proton PDF

 $\,\blacksquare\,$ PDFs of the full nucleus are then constructed with

$$f_i^A(x, Q^2) = Z f_i^{p/A}(x, Q^2) + N f_i^{n/A}(x, Q^2),$$

and assuming $f_i^{p/A} \overset{\text{isospin}}{\longleftrightarrow} f_j^{n/A}$

- Parametrize the x and A dependence of $R_i^{p/A}(x,Q_0^2)$ at $Q_0=m_{\rm charm}=1.3~{\rm GeV}$
 - ► Use a phenomenologically motivated piecewise function in *x*
 - ightharpoonup Use a power-law type function in A

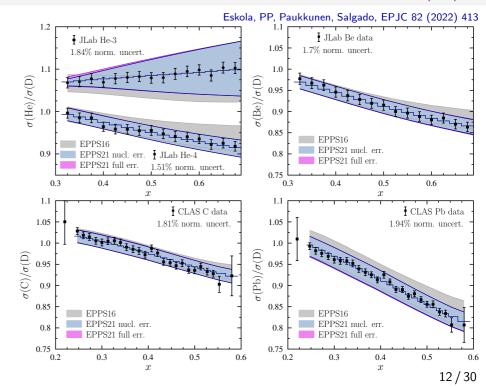


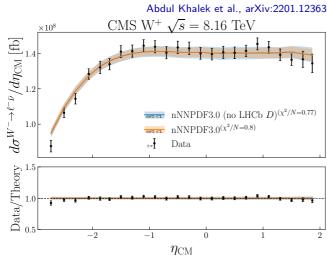
DIS in the "transition region" $W\gtrsim 1.7~{\rm GeV}$ just above the resonance-dominated one

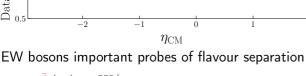
Target-mass corrections important!

N.B. A-dependence not necessarily smooth for light nuclei → need to scale the nuclear modifications for He-3 and Li-6 by factors

$$f_3 = 0.291, \quad f_6 = 0.495$$



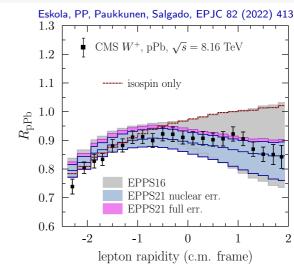




 $\blacksquare ud (c\bar{s}) \to W^+$

 $\blacksquare \bar{u}d (\bar{c}s) \to W^-$

Small-x, high- Q^2 quarks and gluons correlated by DGLAP evolution → sensitivity to gluons



nCTEQ15WZSIH, TUJU21 and nNNPDF3.0 fit to absolute cross sections

EPPS21 uses nuclear-modification ratios to cancel proton-PDF uncertainties

Eskola, PP, Paukkunen, Salgado, EPJC 82 (2022) 271

data from: CMS Collaboration, PLB 800 (2020) 135048 pp baseline: CMS Collaboration, EPJC 76 (2016) 469

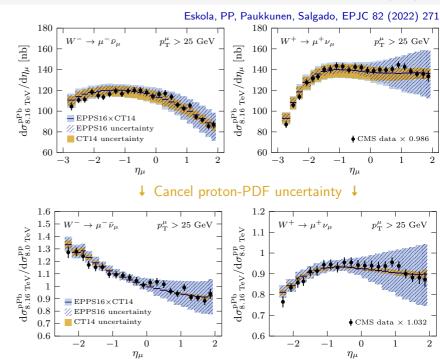
Absolute pPb cross sections sensitive to proton-PDF uncertainties!

Difficult to disentangle nuclear modifications from free-proton d.o.f.s

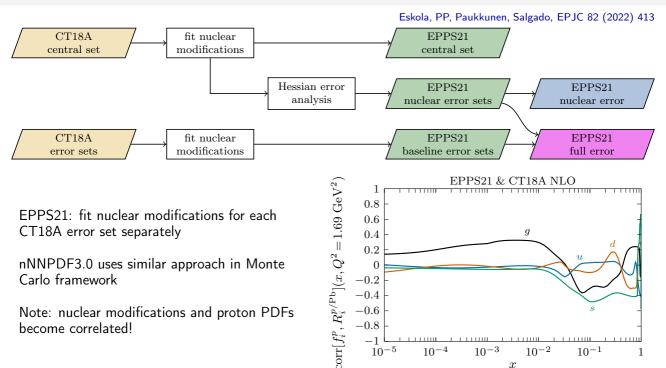
nCTEQ15WZSIH, TUJU21 and nNNPDF3.0 fit to absolute cross sections

Wherever possible, EPPS21 uses nuclear modification ratios to cancel the free-proton-PDF uncertainties

→ can still become relevant with LHC Run 3 statistics Eskola, PP, Paukkunen, Salgado, EPJC 82 (2022) 271

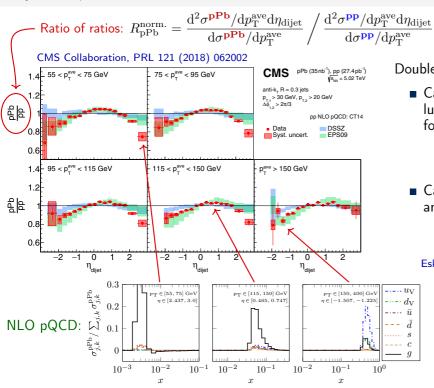


Propagating free-proton PDF uncertainty



15/30

Dijets in pPb at 5.02 TeV



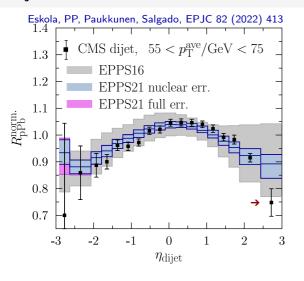
Double ratio convenient for:

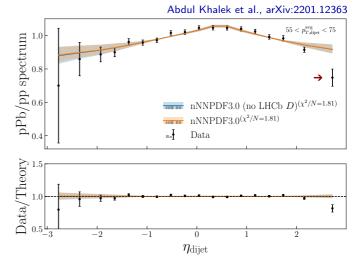
- Cancellation of hadronization and luminosity uncertainties separately for pPb and pp
 - → do not expect strong final-state effects
- Cancellation of free-proton-PDF and scale uncertainties in pPb/pp
 - → direct access to nuclear modifications

Eskola, PP, Paukkunen, EPJC 79 (2019) 511

Good resolution to gluon nuclear modifications for $10^{-3} < x < 0.5$

Dijets in EPPS21 and nNNPDF3.0





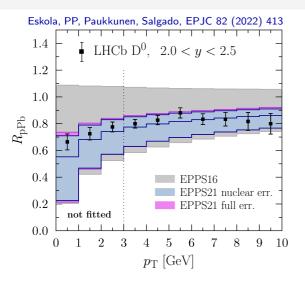
Drastic reduction in the nPDF uncertainties!

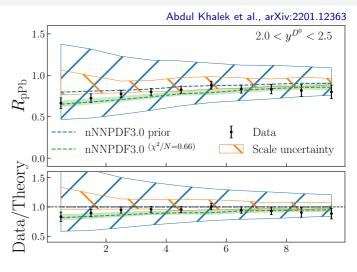
→ Important constraints for the nuclear gluons!

Eskola, PP, Paukkunen, EPJC 79 (2019) 511 Eskola, PP, Paukkunen, Salgado, EPJC 82 (2022) 413 Abdul Khalek et al., arXiv:2201.12363 Both EPPS21 and nNNPDF3.0 find difficulties in reproducing the most forward data points

- → missing data correlations important?
- → NNLO? non-pert. effects?

D⁰s in EPPS21 and nNNPDF3.0





Drastic reduction in the nPDF uncertainties!

→ Important constraints for the nuclear gluons!

Kusina et al., PRL 121 (2018) 052004 Eskola, Helenius, PP, Paukkunen, JHEP 05 (2020) 037 Eskola, PP, Paukkunen, Salgado, EPJC 82 (2022) 413 Abdul Khalek et al., arXiv:2201.12363 nNNPDF3.0 with POWHEG+PYTHIA finds a large scale uncertainty \rightarrow fit only forward data not seen in the S-ACOT- $m_{\rm T}$ GM-VFNS used in EPPS21 Helenius & Paukkunen, JHEP 05 (2018) 196 Eskola, Helenius, PP, Paukkunen, JHEP 05 (2020) 037

Heavy-flavour production mass schemes

FFNS

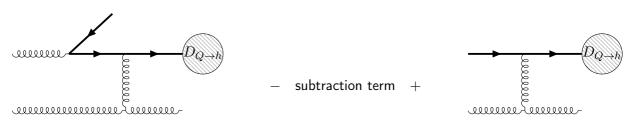
In fixed flavour number scheme, valid at small $p_{\rm T}$, heavy quarks are produced only at the matrix element level

Contains $\log(p_{\mathrm{T}}/m)$ and $\mathcal{O}(m)$ terms

ZM-VFNS

In zero-mass variable flavour number scheme, valid at large $p_{\rm T}$, heavy quarks are treated as massless particles produced also in ISR/FSR

Resums $\log(p_{\mathrm{T}}/m)$ but ignores $\mathcal{O}(m)$ terms



GM-VFNS

A general-mass variable flavour number scheme combines the two by supplementing subtraction terms to prevent double counting of the resummed splittings, valid at all $p_{\rm T}$

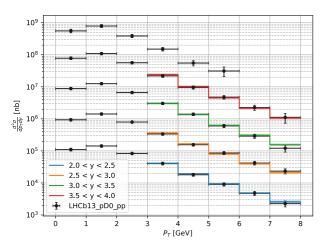
Resums $\log(p_{\rm T}/m)$ and includes $\mathcal{O}(m)$ terms in the FFNS matrix elements

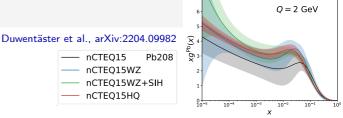
Important: includes also gluon-to-HF fragmentation – large contribution to the cross section!

A data-driven approach - nCTEQ15HQ

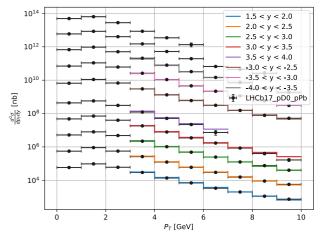
nCTEQ15HQ uses a data-driven approach Lansberg & Shao, EPJC 77 (2017) 1 Kusina et al., PRL 121 (2018) 052004 to fit the D 0 and J/ψ data:

1. Fit the matrix elements to pp data... (assume $2 \rightarrow 2$ kinematics, neglect IS quarks)





2. ... use the fitted matrix elements to fit nuclear PDFs with pPb data



D^0 s at 8.16 TeV – LHCb

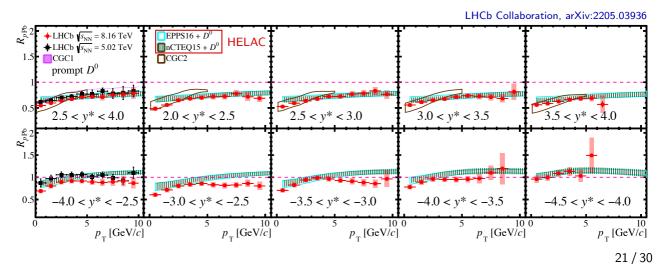
New LHCb measurement at 8.16 TeV (not included in the nPDF analyses yet)

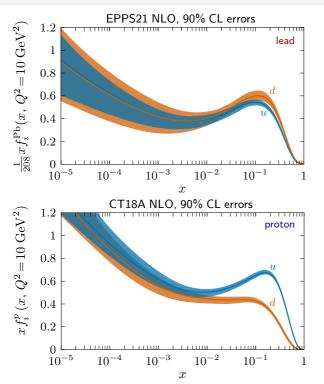
pp reference interpolated from 5 and 13 TeV measurements

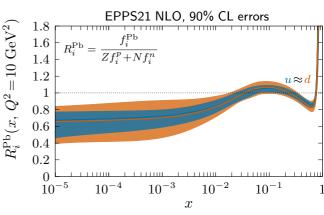
So far compared only against the HELAC matrix-element-fitting results

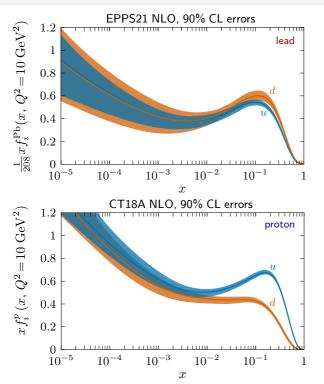
Kusina et al., PRL 121 (2018) 052004

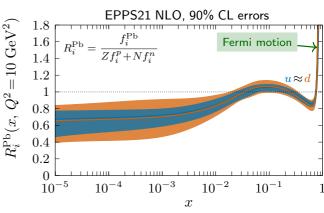
→ to be scrutinised with the direct pQCD calculations

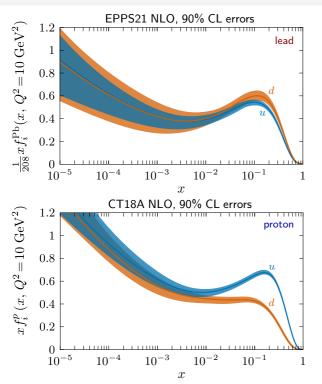


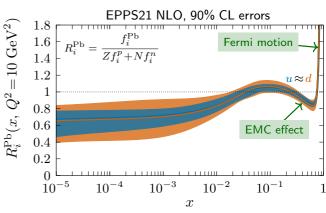


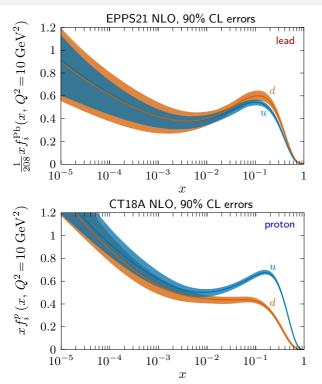


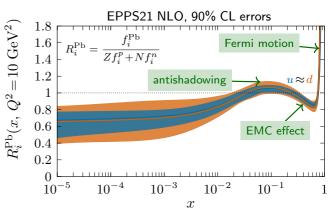


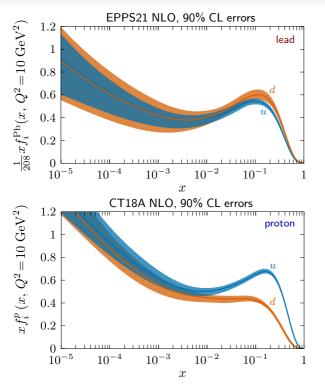


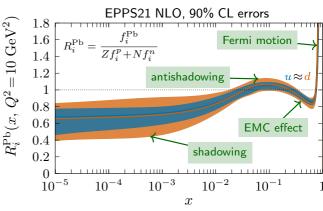




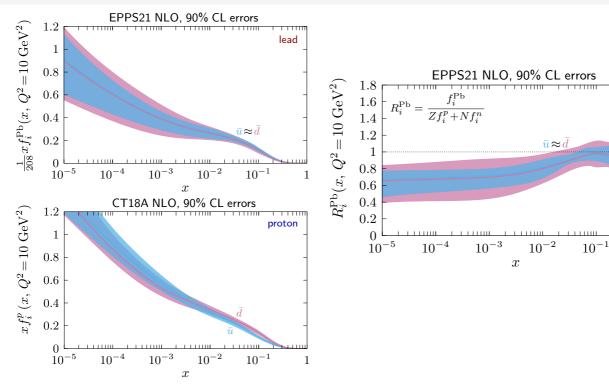


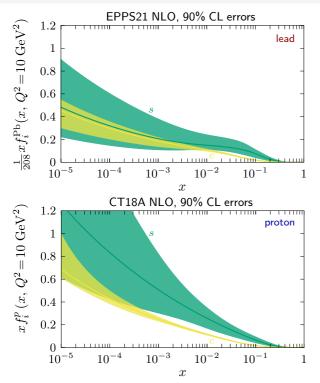


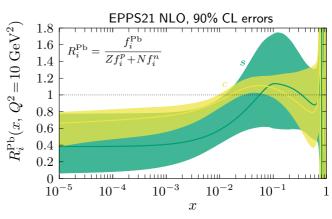




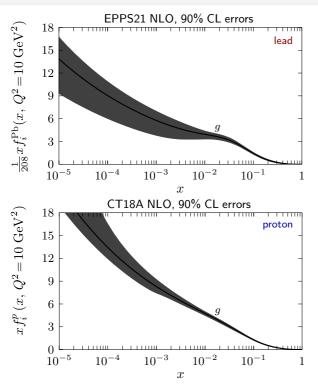
Comparing nuclear and proton PDFs – \bar{u} and \bar{d}

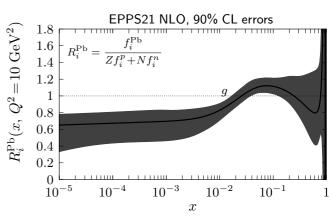




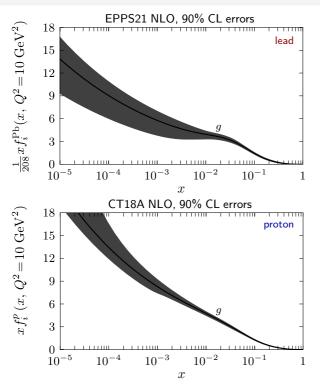


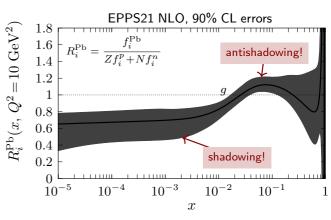
Comparing nuclear and proton PDFs - glue



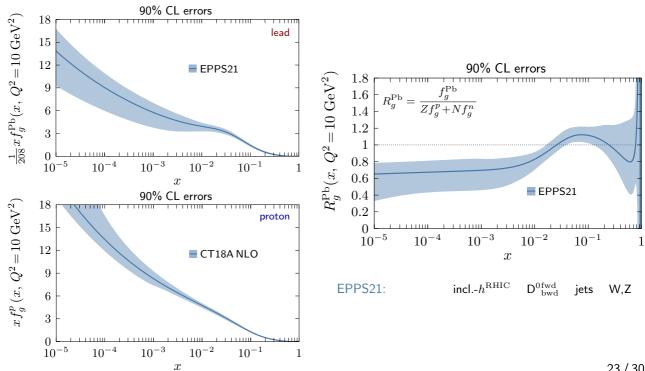


Comparing nuclear and proton PDFs - glue

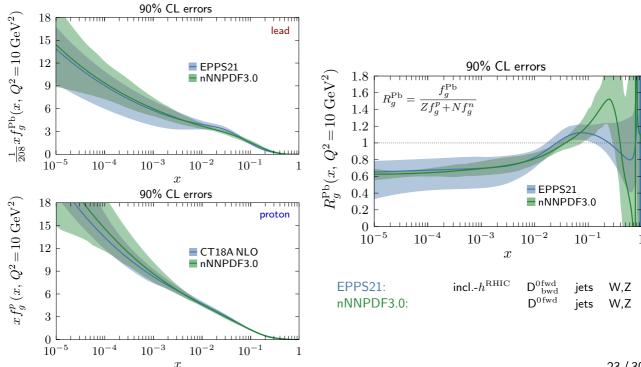




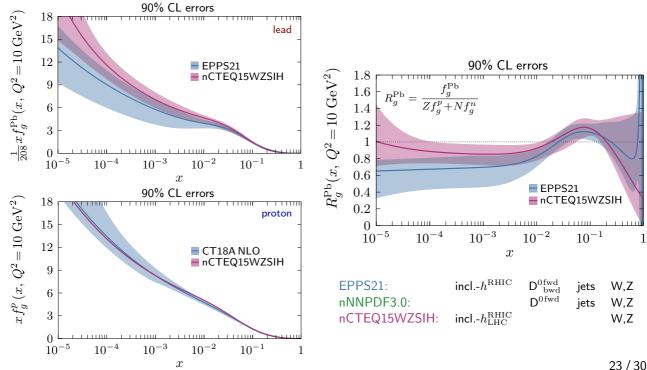
nPDF comparison – glue



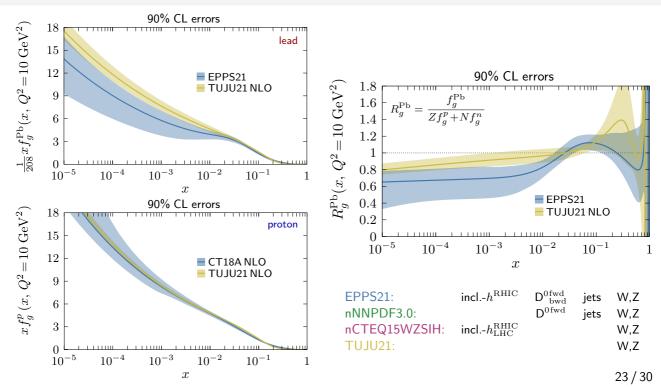
nPDF comparison – glue



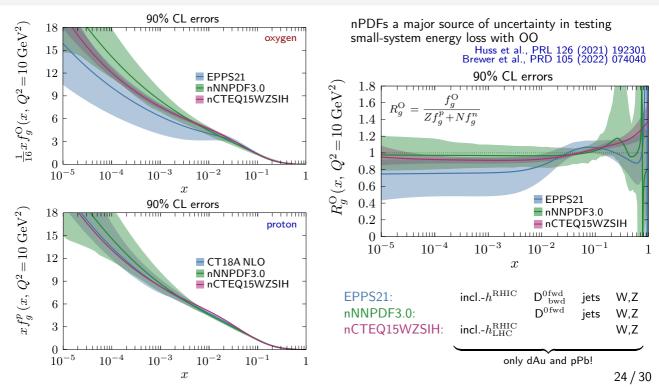
nPDF comparison – glue



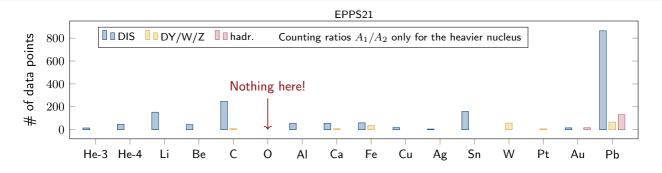
nPDF comparison – glue



nPDF comparison - glue in oxygen



Data availability w.r.t. A



- $\sim 50\%$ of the data points are for Pb!
- \odot Good coverage of DIS measurements for different A (but only fixed target!)
- $\stackrel{ ext{ }}{ ext{ }}$ DY data more scarce, but OK A coverage
- (3) Hadronic observables available only for heavy nuclei!

Light-ion runs at LHC could:

- Complement other light-nuclei DY data with W and Z production (strangeness!)
- Give first direct constraints (e.g. dijets, D-mesons) on light-nuclei small-x gluon distributions!

Dijet production in pO at 9.9 TeV

Similar setup as in CMS 5.02 TeV pPb measurement

Total integrated pO cross section of $81~\mu b$

- Compare with $\sim 330~\mu b$ in pPb at 5.02 TeV
- Sufficient to give reasonable statistics even at relatively low luminosities

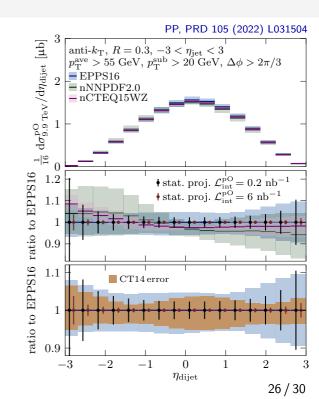
16000 events at 0.2 nb^{-1} 486000 events at 6 nb^{-1}

Problem: absolute cross sections very sensitive to the used free-proton PDFs

■ Difficult to disentangle nuclear modifications from the free-proton d.o.f.s

Problem: We do not expect pp reference at 9.9 TeV

■ Could we use a mixed energy ratio pO(9.9 TeV)/pp(8.8 TeV)?



Dijet $R_{\rm pO}$ in pO at 9.9 TeV

Problem: We do not expect pp reference at 9.9 TeV

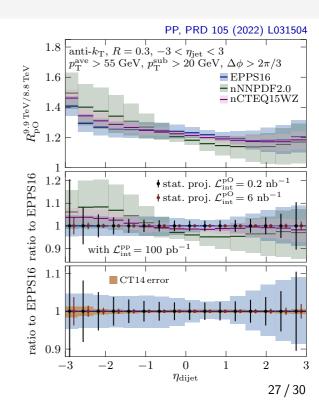
■ Could we use a mixed energy ratio pO(9.9 TeV)/pp(8.8 TeV)? Yes!

Excellent cancellation of free-proton PDFs

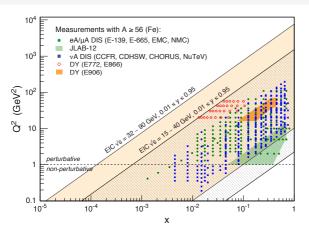
→ Direct access to nuclear modifications

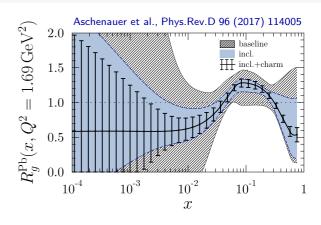
Already few ${\rm nb}^{-1}$ can be expected to be enough to put new constraints on nPDFs (if we have sufficient statistics for the pp reference)

→ Can resolve different nPDF parametrisations!



Gluon constraints from EIC





EIC will significantly widen the kinematic range of DIS constraints for nPDFs

■ Comparing with LHC measurements will put collinear factorization with nuclei to a stringent test

With the $F_{
m L}$ extraction cabability, EIC provides a clean probe to study small-x gluons

lacktriangle Good constraining power to well down to 10^{-2} in a high-energy scenario

Charm-tagged cross-section measurement can vastly reduce high-x gluon uncertainty

Beyond collinear (n)PDFs

Diehl, Eur. Phys. J. A 52 (2016) 149 The "simple" collinear parton correlation function $\Delta = 0$ factorization can be $H(k, P, \Delta)$ extended to include transverse-momentum f(k, P) parton correlation function $f(x, \mathbf{z}) \xrightarrow{\xi = 0} H(x, \mathbf{k}, \xi, \mathbf{b}) \xrightarrow{H(x, \mathbf{k}, \xi, \mathbf{b})} H(x, \mathbf{k}, \xi, \mathbf{b}) \xrightarrow{FT} H(x, \xi, \Delta^2) \text{ GPD}$ $f(x, \mathbf{z}) \xrightarrow{FT} f(x, \mathbf{k}) \xrightarrow{f(x, \mathbf{b})} \text{impact parameter distribution} \xrightarrow{\xi = 0} \sum_{k=0}^{n} A_{nk}(\Delta^2) (2\xi)^k \text{ GFFs}$ and impact-parameter dependence of the parton distributions

... each of these have their own region of applicability in terms of experimental observables, outside of which the factorization is not quaranted to work!

Impact-parameter dependent nPDFs EPS09s and EKS98s

Generalize the nPDFs by defining

nuclear modification spatially dependent nuclear modification
$$R_i^{p/A}\left(x,Q^2\right) = \frac{1}{A}\int\!\mathrm{d}^2\mathbf{s}\ T_A\left(\mathbf{s}\right)\ r_i^A\left(x,Q^2,\mathbf{s}\right)$$
 nuclear thickness function

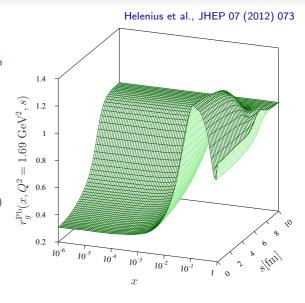
such that

$$\begin{split} \mathrm{d}N^{AB\to k+X}(\mathbf{b}) \\ &= \sum_{i,j,X'} \sum_{N_A,N_B} \int \mathrm{d}^2\mathbf{s}_1 T_A(\mathbf{s}_1) r_i^A(x,Q^2,\mathbf{s}_1) f_i^{N_A}(x,Q^2) \otimes \\ &\int \mathrm{d}^2\mathbf{s}_2 T_B(\mathbf{s}_2) r_i^B(x,Q^2,\mathbf{s}_2) f_i^{N_B}(x,Q^2) \otimes \mathrm{d}\hat{\sigma}^{ij\to k+X'} \delta(\mathbf{s}_2-\mathbf{s}_1-\mathbf{b}) \end{split}$$

reduces to the min. bias cross section when integrated over the impact parameter \boldsymbol{b}

To my knowledge not proven to coincide with the GPD definition of impact-parameter distribution!

See Wu, JHEP 07 (2021) 002 for factorization derivation with similar objects in soft-collinear effective theory





data from: CMS Collaboration, JHEP 05 (2021) 182 pp baseline: CMS Collaboration, EPJC 75 (2015) 147

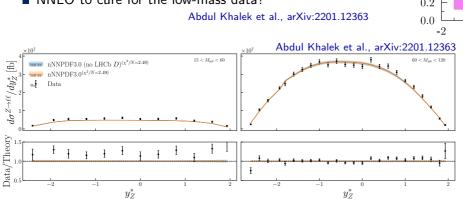
New Run 2 data from CMS

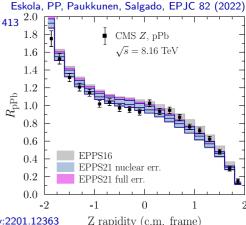
CMS Collaboration, JHEP 05 (2021) 182

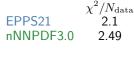
- nNNPDF3.0 include both low-mass and on-peak data
- \blacksquare $R_{\rm pPb}$ studied in EPPS21 \rightarrow not included in the final fit

Both EPPS21 and nNNPDF3.0 observe some tension between the data and fit

- abrupt change in the shape at midrapidity
- NNLO to cure for the low-mass data?







PHENIX pion production small-system scan

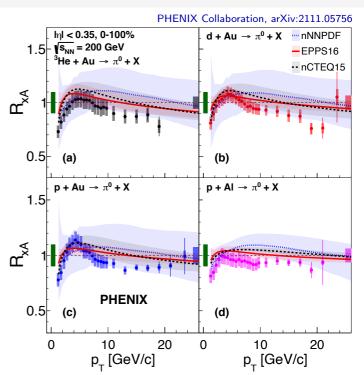
New mid-rapidity π^0 data from PHENIX PHENIX Collaboration, arXiv:2111.05756

- improved precision
- higher p_T → larger x

Contrary to nPDF expectations, measured "Cronin peak" size follows the ordering ${}^{3}{\rm He} + {\rm Au} < d + {\rm Au} < p + {\rm Au}$

- higher-twist (multiple-scattering)?
- flow-like component?

At high $p_{\rm T}$ the nPDF predictions overshoot the data, but mind the large normalisation uncertainties



UPCs in collinear factorisation

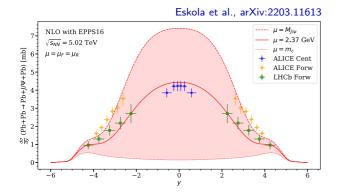
First phenomenological implementation of the exclusive J/ψ photoproduction NLO corrections

Ivanov et al., EPJC 34 (2004) 297 Jones et al., J. Phys. G 43 (2016) 035002

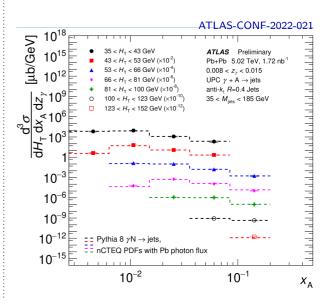
in ultrapheripheral Pb+Pb

Large scale uncertainty

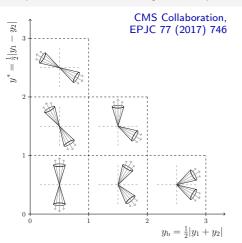
- → perturbative convergence?
- → cancel with nuclear ratios?



ATLAS inclusive dijet photoproduction measurement now fully unfolded



Triple-differential dijets in pPb?

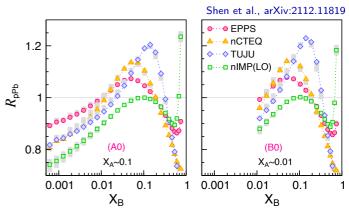


Triple-differential measurement fixes partonic kinematics at LO

→ powerful test of factorisation and PDFs

Measured in pp at 8 TeV CMS Collaboration, EPJC 77 (2017) 746

Should be feasible in pPb with Run 2/3 statistics?



Various observable choices possible, e.g. X_A, X_B, y^*

Ellis & Soper, PRL 74 (1995) 5182

Proton strangeness from νA DIS vs. LHC EW data

 $K_s = \frac{\int_0^1 \mathrm{d} x x [s(x,Q^2) + \bar{s}(x,Q^2)]}{\int_0^1 \mathrm{d} x x [\bar{u}(x,Q^2) + \bar{d}(x,Q^2)]}$

table and fig. from Feng et al., "The Forward Physics Facility at the High-Luminosity LHC", arXiv:2203.05090

		Proton PDF sets					Nuclear PDF sets			
Data set		Ref.	ABMP16	CT18	MSHT20	NNPDF4.0	EPPS21	nCTEQ15	nNNPDF3.0	TUJU21
CHORUS $\sigma^{\nu,\bar{\nu}}_{CC}$	Pb	[1238]	×	Х	✓	✓	✓	×	✓	✓
CHORUS	Pb	[1239]	✓	Х	×	×	X	×	×	×
NOMAD $\mathcal{R}_{\mu\mu}$	Fe	[1195]	✓	Х	×	(✔)	X	×	×	×
CCFR xF_3^p	Fe	[1240]	X	1	×	×	X	×	×	×
CCFR F_2^p	Fe	[1241]	×	1	×	×	X	X	×	×
CDSHW F_2^p, xF_3^p	Fe	[1242]	×	1	×	×	X	X	×	✓
NuTeV $\sigma^{\nu,\bar{\nu}}_{CC}$	Fe	[1196]	✓	✓	✓	✓	X	×	✓	×
NuTeV F_2, F_3	Fe	[1194]	X	X	✓	×	X	×	×	×

Proton-PDF fits traditionally include neutrino-*nucleus* DIS for improved strange-quark constraints → suppressed strangeness

Complementary data from ATLAS EW-boson production confronts this view with preference for unsuppressed strange ATLAS Collaboration, PRL 109 (2012) 012001

Simultaneous fit feasible w/ NNLO c-quark mass corrections
Faura et al., EPJC 80 (2020) 1168

 $K_s = 0.5$ $K_s = 1$ ATLAS-epWZ16 ABMP16 HIH CT18 CT18A MSHT20 NNPDF4.0 (global) ■ NNPDF4.0 (no ν DIS) 0.2 0.4 0.6 0.8 1.0 1.2 $K_{\rm s}(Q=1.6~{\rm GeV})$

O c-quark mass corrections

Faura et al., EPJC 80 (2020) 1168

Bailey et al., EPJC 81 (2021) 341

Ball et al., arXiv:2109.02653

Ball et al., arXiv:2109.02653

Nuclear effects can impact the proton-PDF fits!

NNPDF4.0:

- Different large-x sea-quark behaviour depending on whether the uncertainties from nNNPDF2.0 nuclear PDFs were included or not
- Nuclear data found to constrain the proton PDFs even with nuclear uncertainties included

Ball et al., EPJC 79 (2019) 282 Ball et al., arXiv:2109.02653

MSHT20: take nuclear corrections from DSSZ + additional 3-param. fit Bailey et al., EPJC 81 (2021) 341

CT18: does not report on any use of nuclear corrections

