

Studying nuclear correlations with electron scattering: opportunities in exotic nuclei

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Spectroscopy via knock out reactions-basic idea

Use a probe (ANY probe) to eject the particle we are interested to:



Concept of correlations



[CBuged We H. Dickhoff, Prog. Part. Nucl. Phys **52**, 377 (2004)]

Concept of correlations



Ab-Initio SCGF approaches



The FRPA Method in Two Words

Particle vibration coupling is the main cause driving the distribution of particle strength—on both sides of the Fermi surface...

D(2h1p

= hole

(ph)

(ph)

Oll (pp/hh)

R^{(2p1h}

= particle

CB et al., Phys. Rev. C**63**, 034313 (2001) Phys. Rev. A**76**, 052503 (2007) Phys. Rev. C**79**, 064313 (2009)

•A complete expansion requires <u>all</u> <u>types</u> of particle-vibration coupling

"Extended" Hartree Fock

...these modes are all resummed exactly and to all orders in a *ab-initio* many-body expansion.

•The Self-energy $\Sigma^*(\omega)$ yields both single-particle states and scattering

Self-Consistent Green's Function Approach



Global picture of nuclear dynamics

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- Reciprocal correlations among effective modes
- Guaranties macroscopic conservation laws

Self-Consistent Green's Function Approach



Gorkov and symmetry breaking approaches

V. Somà, CB, T. Duguet, , Phys. Rev. C 89, 024323 (2014)
V. Somà, CB, T. Duguet, Phys. Rev. C 87, 011303R (2013)
V. Somà, T. Duguet, CB, Phys. Rev. C 84, 064317 (2011)

> Ansatz
$$(... \approx E_0^{N+2} - E_0^N \approx E_0^N - E_0^{N-2} \approx ... \approx 2\mu)$$

> Auxiliary many-body state $|\Psi_0
angle \equiv \sum_N^{\mathrm{even}} c_N |\psi_0^N
angle$

Mixes various particle numbers

ightarrow Introduce a "grand-canonical" potential $\ \ \Omega = H \! - \! \mu N$

 $\implies |\Psi_0\rangle$ minimizes $\Omega_0 = \langle \Psi_0 | \Omega | \Psi_0 \rangle$ under the constraint $N = \langle \Psi_0 | N | \Psi_0 \rangle$

This approach leads to the following Feynman diagrams:

 $\Sigma_{ab}^{11\,(1)} = \qquad \stackrel{a}{\overset{o}{b}} - - - \stackrel{c}{\overset{o}{d}} \bigcirc \downarrow \omega'$ $\Sigma_{ab}^{12\,(1)} = \qquad \stackrel{a}{\overset{c}{}} - - - \stackrel{\overline{b}}{\overset{d}{}} \stackrel{\overline{b}}{\overset{d}{}}$ UNIVERSITY OF



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Truncation scheme:	Dyson formulation (closed shells)	Gorkov formulation (semi-magic)
1 st order:	Hartree-Fock	HF-Bogolioubov
2 nd order:	2 nd order	2 nd order (w/ pairing)
 3 rd and all-orders sums, P-V coupling:	ADC(3) FRPA etc	G-ADC(3) work in progress







Ab-initio Nuclear Computation & BcDor code



Ab-initio Nuclear Computation & BcDor code

http://personal.ph.surrey.ac.uk/~cb0023/bcdor/

Computational Many-Body Physics





Download

Documentation

Welcome

From here you can download a public version of my self-consistent Green's function (SCGF) code for nuclear physics. This is a code in J-coupled scheme that allows the calculation of the single particle propagators (a.k.a. one-body Green's functions) and other many-body properties of spherical nuclei. This version allows to:

- Perform Hartree-Fock calculations.
- Calculate the the correlation energy at second order in perturbation theory (MBPT2).
- Solve the Dyson equation for propagators (self consistently) up to second order in the self-energy.
- Solve coupled cluster CCD (doubles only!) equations.

When using this code you are kindly invited to follow the creative commons license agreement, as detailed at the weblinks below. In particular, we kindly ask you to refer to the publications that led the development of this software.

Relevant references (which can also help in using this code) are: Prog. Part. Nucl. Phys. 52, p. 377 (2004), Phys. Rev. A76, 052503 (2007), Phys. Rev. C79, 064313 (2009), Phys. Rev. C89, 024323 (2014)



Reaching medium mass and neutron rich isotopes

Degenerate system (open shells, deformations...)

Hamiltoninan, including three nucleon forces



⁵⁶Ni neutron spectral function



W. Dickhoff, CB, Prog. Part. Nucl. Phys. 53, 377 (2004) CB, M.Hjorth-Jensen, Pys. Rev. C**79**, 064313 (2009)



Medium-mass isotopes from chiral interactions



Modern realistic nuclear forces



Oxygen puzzle...



The oxygen dripline is at ²⁴O, at odds with other neighbor isotope chains.

Phenomenological shell model interaction reflect this in the s.p. energies but no realistic NN interaction alone is capable of reproducing this...

The fujita-Miyazawa 3NF provides repulsion through Pauli screening of other 2NF terms:







Neutron spectral function of Oxygens



Results for the N-O-F chains

A. Cipollone, CB, P. Navrátil, Phys. Rev. Lett. **111**, 062501 (2013) *and* Phys. Rev. C **92**, 014306 (2015)



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Results for the N-O-F chains

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 \rightarrow 3NF crucial for reproducing binding energies and driplines around oxygen

→ cf. microscopic shell model [Otsuka et al, PRL105, 032501 (2010).]

UNIVERSITY OF N3LO (Λ = 500Mev/c) chiral NN interaction evolved to 2N + 3N forces (2.0fm⁻¹) N2LO (Λ = 400Mev/c) chiral 3N interaction evolved (2.0fm⁻¹)

Calcium isotopic chain

Ab-initio calculation of the whole Ca: induced and full 3NF investigated



→ induced and full 3NF investigated

- \rightarrow genuine (N2LO) 3NF needed to reproduce the energy curvature and S_{2n}
- \rightarrow N=20 and Z=20 gaps overestimated!

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→ Full 3NF give a correct trend but over bind!

V. Somà, CB et al. Phys. Rev. C89, 061301R (2014)



V. Somà, CB et al. Phys. Rev. C89, 061301R (2014)

Two-neutron separation energies predicted by chiral NN+3NF forces:



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→ First ab-initio calculation over a contiguous portion of the nuclear chart—open shells are now possible through the Gorkov-GF formalism



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V. Somà, CB et al. Phys. Rev. C89, 061301R (2014)

Two-neutron separation energies predicted by chiral NN+3NF forces:



Lack of deformation due to quenched cross-shell quadrupole excitations

→ First ab-initio calculation over a contiguous portion of the nuclear chart—open shells are now possible through the Gorkov-GF formalism

The sd-pf shell gap

Neutron spectral distributions for ⁴⁸Ca and ⁵⁶Ni:



sd-pf separation is overestimated even with leading order N2LO 3NF

Correct increase of $p_{3/2}$ - $f_{7/2}$ splitting (see Zuker 2003)

		2NF only	2+3NF(ind.)	2+3NF(full)	Experiment
	¹⁶ O:	2.10	2. 41	2.38	2.718±0.210 [19]
CB <i>et al.</i> , arXiv:1211.3315 [nucl-th]	⁴⁴ Ca:	2.48	2.93	2.94	3.520±0.005 [20]

Ni isotopic chain



→ Large J in free space SRG matter (must pay attention to its convergence) → Overall conclusions regarding over binding and S_{2n} remain but details change

IM-SRG results from H. Hergert

Two-neutron separation energies for neutron rich K isotopes

M. Rosenbusch, et al., PRL114, 202501 (2015)



Measurements @ ISOLTRAP

Theory tend to overestimate the gap at N=34, but overall good

→ <u>Error bar in predictions</u> are from extrapolating the manybody expansion to convergence of the model space.



NNLO-sat : a global fit up to A≈24

A. Ekström et al. Phys. Rev. C91, 051301(R) (2015)



NNLOsat (V2 + W3) -- Grkv 2nd ord.

From SCGF:

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V2-N3LO(500) + W3-NNLO(400MeV/c) w/ SRG at 2.0 fm⁻¹
 A. Cipollone, CB, P. Navrátil, Phys. Rev. Lett. **111**, 062501 (2013)
 V. Somà, CB *et al.* Phys. Rev. C**89**, 061301R (2014)

BE and radii for Oxygens

- New fits of chiral interactions (NNLOsat) highly improve comparison to data

- Deficiencies remain for neutron rich isotopes



FIG. 1. Oxygen binding energies. Results from SCGF and IMSRG calculations performed with EM [20-22] and NNLO_{sat} [26] interactions are displayed along with available experimental data.

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V. Somà, V. Lapuox, CB, et al., in preparation

BE and charge radii in ^ACa



BE and charge radii in ^ACa



Ca neutron spectral distributions @ 2nd order

NN(N3L0500-EM) + 3NFs(NNL0400) at λ_{SRG} =2.0/fm





Spectroscopic Factors



Z/N asymmetry dependence of SFs - Theory

Ab-initio calculations explain (a very weak) the Z/N dependence but the effect is much lower than suggested by direct knockout

Rather the quenchng is high correlated to the gap at the Femi surface.



Single nucleon transfer in the oxygen chain

[F. Flavigny et al, PRL110, 122503 (2013)]

\rightarrow Analysis of ¹⁴O(d,t)¹³O and ¹⁴O(d,³He)¹³N transfer reactions @ SPIRAL

Reaction	<i>E</i> * (MeV)	J^{π}	R ^{HFB} (fm)	<i>r</i> ₀ (fm)	$C^2 S_{exp}$ (WS)	$\frac{C^2 S_{\rm th}}{0p+2\hbar\omega}$	R _s (WS)	$C^2 S_{exp}$ (SCGF)	$C^2 S_{\text{th}}$ (SCGF)	R _s (SCGF)
14 O (<i>d</i> , <i>t</i>) 13 O	0.00	3/2-	2.69	1.40	1.69 (17)(20)	3.15	0.54(5)(6)	1.89(19)(22)	3.17	0.60(6)(7)
14 O (<i>d</i> , 3 He) 13 N	0.00	$1/2^{-}$	3.03	1.23	1.14(16)(15)	1.55	0.73(10)(10)	1.58(22)(2)	1.58	1.00(14)(1)
	3.50	$3/2^{-}$	2.77	1.12	0.94(19)(7)	1.90	0.49(10)(4)	1.00(20)(1)	1.90	0.53(10)(1)
$^{16}O(d, t)$ ^{15}O	0.00	$1/2^{-}$	2.91	1.46	0.91(9)(8)	1.54	0.59(6)(5)	0.96(10)(7)	1.73	0.55(6)(4)
16 O (<i>d</i> , 3 He) 15 N [19,20]	0.00	$1/2^{-}$	2.95	1.46	0.93(9)(9)	1.54	0.60(6)(6)	1.25(12)(5)	1.74	0.72(7)(3)
	6.32	$3/2^{-}$	2.80	1.31	1.83(18)(24)	3.07	0.60(6)(8)	2.24(22)(10)	3.45	0.65(6)(3)
18 O (<i>d</i> , 3 He) 17 N [21]	0.00	$1/2^{-}$	2.91	1.46	0.92(9)(12)	1.58	0.58(6)(10)			





- Overlap functions and strengths from GF

- Rs independent of asymmetry

Quenching of absolute spectroscopic factors





Nucl. Phys. A553 (1993) 297c

NIKHEF:



A common misconception about SRC:

"The quenching is constant over all stable nuclei, so it <u>must be</u> a shortrange effect"

Actually, NO!

All calculations show that SRC have just a small effect at the Fermi surface. And the correlation to the <u>experimental p-h</u> gap is much more important.

[W. Dickhoff, CB, Prog. Part. Nucl. Phys. 52, 377 (2004)]



Quenching of SF in stable nuclei

	NIKHEF: Nucl. Phys. A553 (1993) 297		$S_{p1/2}$	$S_{p3/2}$
	1.0 Mean Field Theory	Short-range correlations oriented methods:		
	-	– VMC [Argonne, '94]	0.90	
¥	^{0.8} – ¹⁶ O ⁴⁸ Ca ₉₀ Zr	– GF(SRC) [St.Louis-Tübingen '95]	0.91	0.89
1)		- FHNC/SOC [Pisa '00]	0.90	
S/(2j+	2 ⁷ Li ¹⁴⁰ Ca ²⁰⁸ Pb ₀.4 ¹² C	Including particle-phonon couplings:		
	-	- GF(FRPA) [St.Louis '01]	0.77	0.72
	0.2 - VALENCE PROTONS	[CB et al., Phys. Rev. C 65 , (02)]		
	$_{0.0}$ $_{10^1}$ $_{10^2}$ $_{10^2}$ target mass $-$	• Experiment:	0.63	0.67 ± 0.07 (estimated uncertainty)

SRC are present and verified experimentally

BUT the are NOT the dominant mechanism for quenching SF!!!



Short-range correlations (SRC) Where can one see these??



High momentum components - where are they?

Momentum distribution:

$$n(k) = \int_{-\infty}^{\varepsilon_F} d\omega \ S^{(h)}(k,\omega)$$

 High k components are found at high missing energies

Short-range repulsion in r-space
 ←→ strong potential at large momenta

- A complication: the nuclear interaction includes also a tensor term (from Yukawa's meson meson exchange):

$$S_{12} = 3(\vec{\sigma}_1 \cdot \hat{r})(\vec{\sigma}_2 \cdot \hat{r}) - 1$$

→ interaction amog 2 dipoles!!!!!!

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Distribution of (All) the Nuclear Strength



Interest in short range correlations:

- a fraction of the total number of nucleons:
 - -~10% in light nuclei (VMC, FHNC, Green's function)
 - 15-20% in heavy systems (CBF, Green's function)
- can explain up to 2/3 of the binding energy [see ex. PRC51, 3040 ('95) for ¹⁶O]
- influence NM saturation properties [see ex. PRL90, 152501 ('03)]

Spectral strength of ¹²C from exp. E97-006



Theory vs. measured strength - I

• About 0.6 protons are found in the correlated region:

TABLE I. Correlated strength, integrated over shaded area of Fig. 2 (quoted in terms of the number of protons in ${}^{12}C$.)

Experiment	0.61 ± 0.06
Greens Function Theory [28]	0.46
CBF Theory [3]	0.64



0.170

0.210

0.250

0.290

0.330

0.370 0.410 0.4500.490 0.530 0.570 0.610

0.650

 π emission

 \rightarrow in good agreement P_m (GeV/C) 1e-10 $\mathbf{E}_{\mathbf{m}}$ with early theoretical \mathbf{P}^2 $\overline{2}M$ predictions! $S(E_m,P_m)$ [MeV⁴ sr⁻¹. 1e-11 1e-12 what about the position of the peak? $1e-13^{\perp}_{0}$ 0.2 0.3 0.4 0.1 E_m (GeV)

SRC

correlations



Theory vs. measured strength - II

•Theory reproduces the total amount of correlated strength and its shape

•The exact position of the correlated peak depends on the particular many-body approach and (NN interaction?) used.



Phys. Rev. C70, 0243909 (2004)



Comparison to Experiment in Parallel Kinematics – ¹²C



unstable isotopes from e⁻ scattering





- → Leading order 3NF are crucial to predict many important features that are observed experimentally (drip lines, saturation, orbit evolution, etc...)
- → Experimental binding is predicted accurately up to the lower sd shell (A≈30) but deteriorates for medium mass isotopes (Ca and above) with roughly 1 MeV/A over binding.
- → New fits of chiral interaction are promising for low-energy observables
- → Spectroscopic factors and strength distributions: SITLL UNKNOWN for most isotopes and of high relevance to understand structure and correlations with neutron excess!







