

SACLAY (S.-et-O.) - L'Église et la Mare - La Ville

# Hyperons, Hypernuclei & Neutron Stars

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**CFisUC, University of Coimbra**



**Production & Study of Neutron-rich Hypernuclei:**

**Physics & Potentialities at FAIR/R<sup>3</sup>B**

**January 19<sup>th</sup>-21<sup>st</sup> 2016, Saclay (France)**

# Outline of the talk

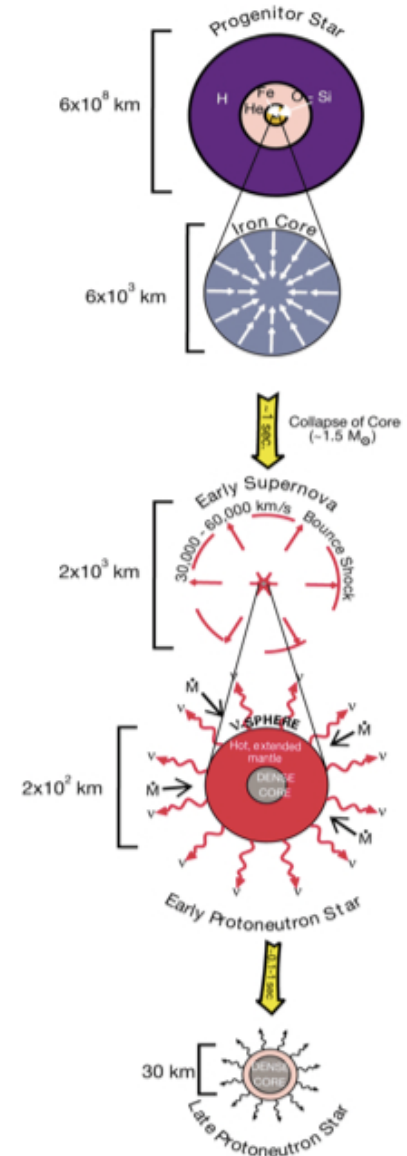
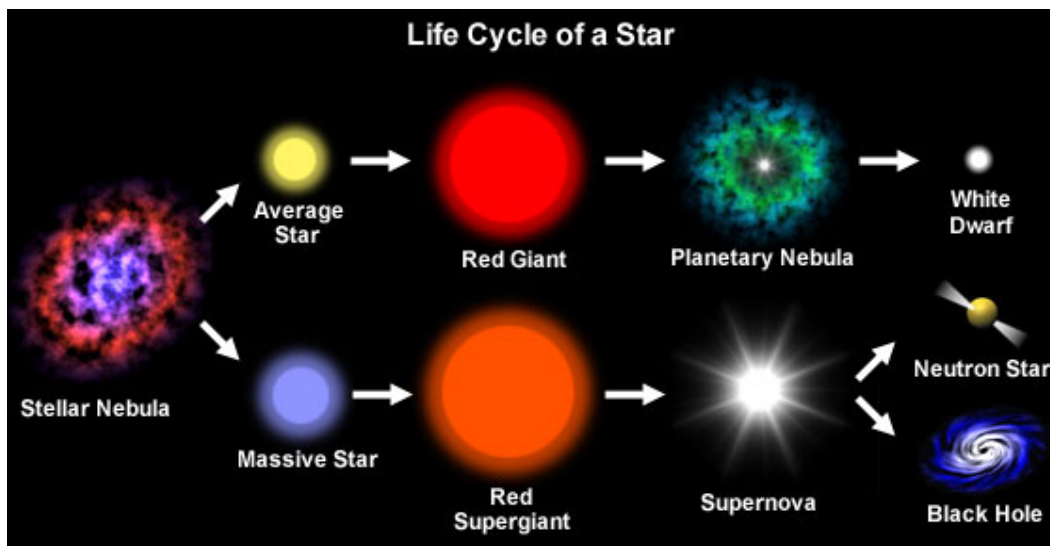
- ❖ Introduction to Neutron Star Phenomenology
- ❖ Role of Hyperons on Neutron Star Properties
- ❖ Lab Constraints of the Hypernuclear EoS

# Neutron stars are different things for different people

- ✧ For **astronomers** are very **little stars** “visible” as radio pulsars or sources of X- and  $\gamma$ -rays.
- ✧ For **particle physicists** are **neutrino sources** (when they born) and probably the only places in the Universe where deconfined quark matter may be abundant.
- ✧ For **cosmologists** are “almost” **black holes**.
- ✧ For **nuclear physicists** & the participants of this workshop are the **biggest neutron-rich hypernuclei** of the Universe ( $A \sim 10^{56}$ - $10^{57}$ ,  $R \sim 10$  km,  $M \sim 1$ - $2 M_{\odot}$ ).

But everybody agrees that ...

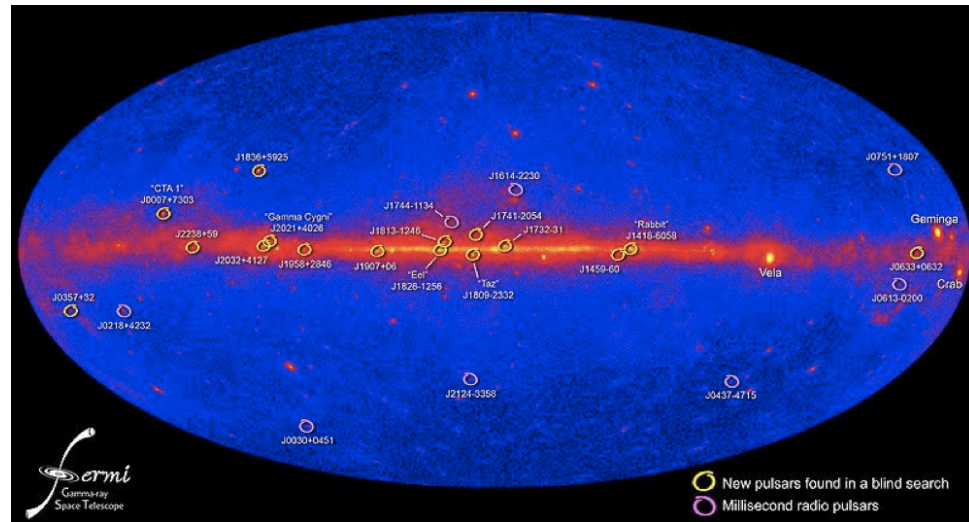
Neutron stars are a type of stellar compact remnant that can result from the gravitational collapse of a massive star ( $8 M_{\odot} < M < 25 M_{\odot}$ ) during a Type II, Ib or Ic supernova event.



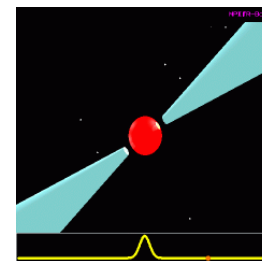
Most NS are observed as pulsars. Nowadays more than 2000 pulsars are known ( $\sim 1900$  Radio PSRs (141 in binary systems),  $\sim 40$  X-ray PSRs &  $\sim 60$   $\gamma$ -ray PSRs)

## Observables

- Period ( $P$ ,  $dP/dt$ )
- Masses
- Luminosity
- Temperature
- Magnetic Field
- Gravitational Waves (future)

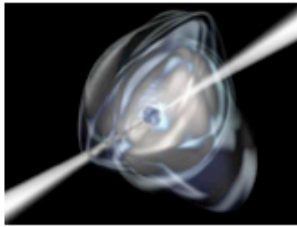


[http://www.phys.ncku.edu.tw/~astrolab/mirrors/apod\\_e/ap090709.html](http://www.phys.ncku.edu.tw/~astrolab/mirrors/apod_e/ap090709.html)

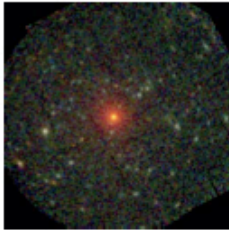


<http://pulsar.ca.astro.it/pulsar/Figs>

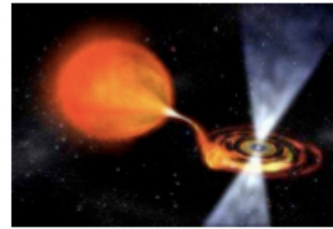
# The 1001 Astrophysical Faces of Neutron Stars



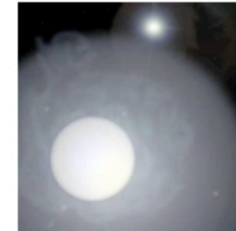
*Anomalous X-ray Pulsars*



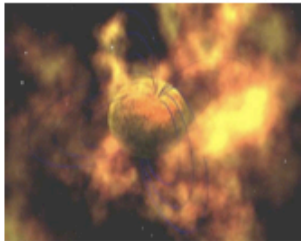
*dim isolated  
neutron stars*



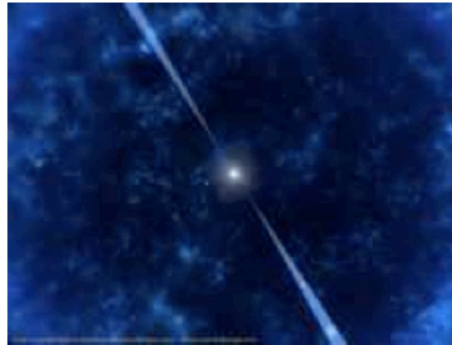
*X-ray binaries*



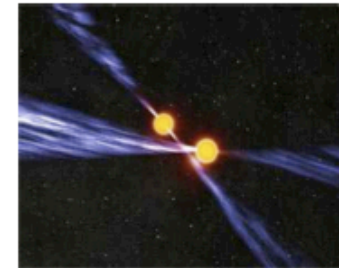
*bursting pulsars*



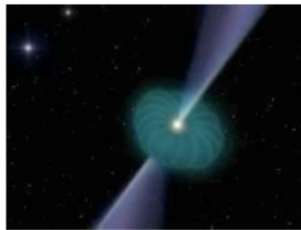
*Soft Gamma Repeaters*



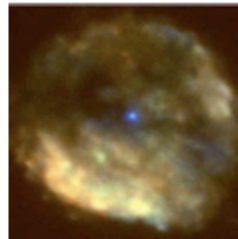
*pulsars*



*binary pulsars*



*Rotating Radio Transients*



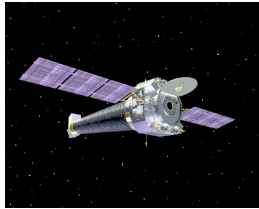
*Compact Central Objects*



*planets around pulsar*

# Observation of Neutron Stars

## X- and $\gamma$ -ray telescopes



Chandra

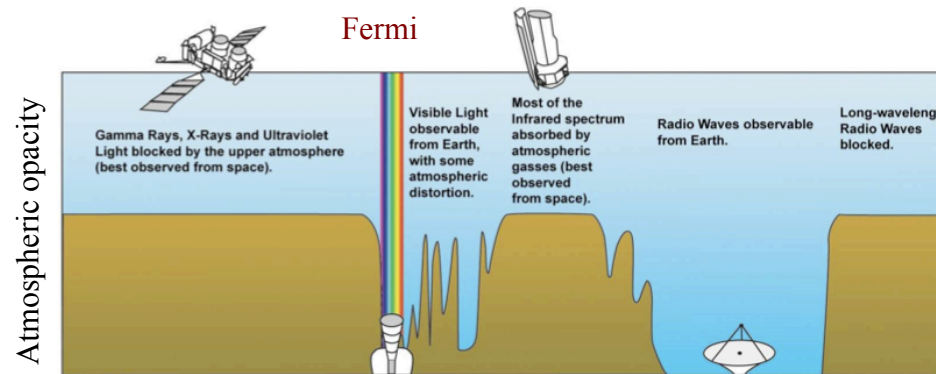


Fermi

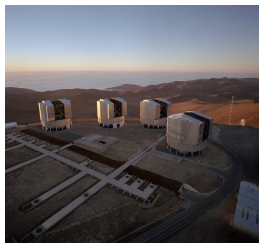
## Space telescopes



HST (Hubble)



## Optical telescopes



VLT (Atacama, Chile)



Arecibo (Puerto Rico):  $d= 305$  m

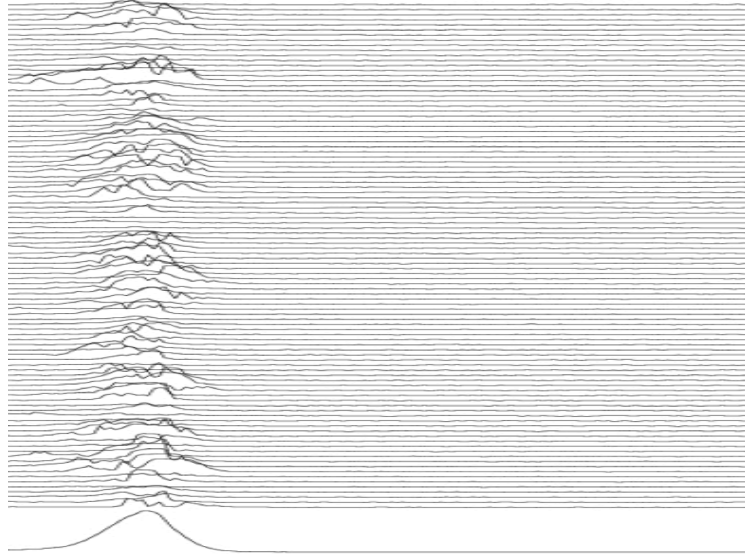


Green Banks (USA):  $d= 100$  m

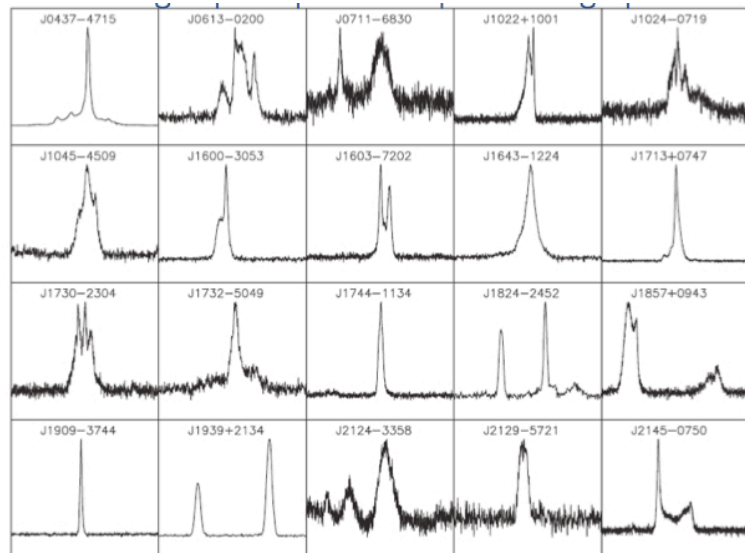


Nançay (France):  $d \sim 94$  m

# The Fingerprint of a Pulsar



Individual pulses are very different. But the average over 100 or more pulses is **extremely stable and specific** of each pulsar



✧ **Top:** 100 single pulses from the pulsar PSR B0950+08 ( $P=0.253$  s) showing the pulse-to-pulse variability in shape and intensity

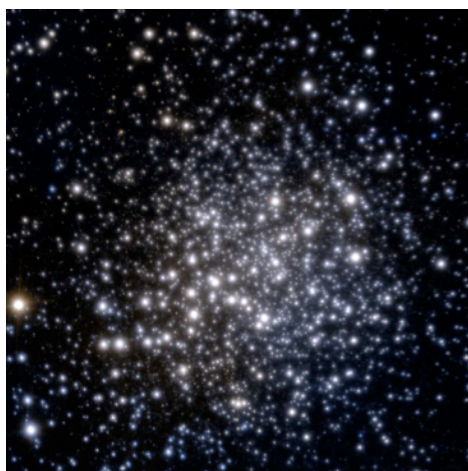
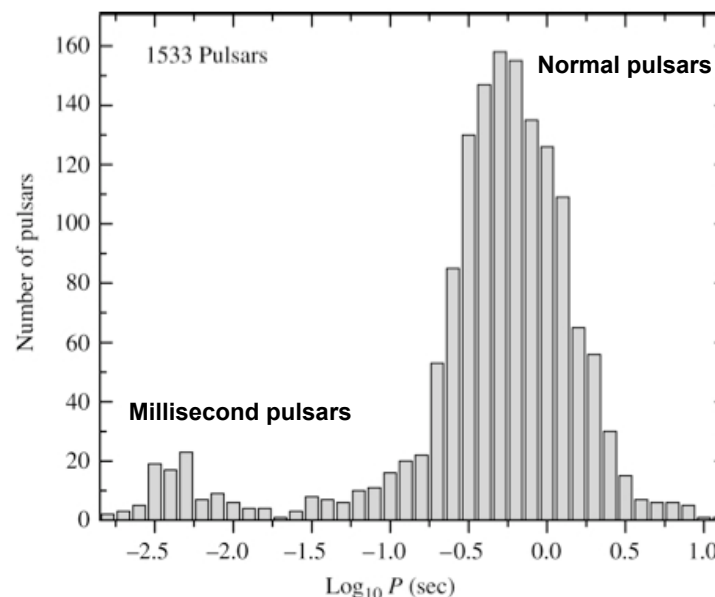
✧ **Bottom:** Average profiles of several pulsars



# Pulsar Rotational Period

The distribution of the rotational period of pulsars shows two clear peaks that indicate the existence of two types of pulsars

- normal pulsars with  $P \sim s$
- millisecond pulsars with  $P \sim ms$



Globular cluster Terzan 5

- First millisecond pulsar discovered in 1982 (Arecibo)
- Nowadays more than 200 millisecond pulsars are known
- PSR J1748-2446ad discovered in 2005 is until now the fastest one with  $P=1.39$  ms (716 Hz)

# Minimum Rotational Period of a Neutron Star

Pulsar **cannot spin arbitrarily fast.**  
The absolute minimum rotational period is obtained when

Centrifugal Force = Gravitational Force



Keplerian Frequency



"... And that, Jimmy, is what we call 'centrifugal force'."

In Newtonian Gravity

$$P_{\min} = 2\pi \sqrt{\frac{R^3}{GM}} \approx 0.55 \left( \frac{M_{\text{sun}}}{M} \right)^{1/2} \left( \frac{R}{10\text{km}} \right)^{3/2} \text{ ms}$$

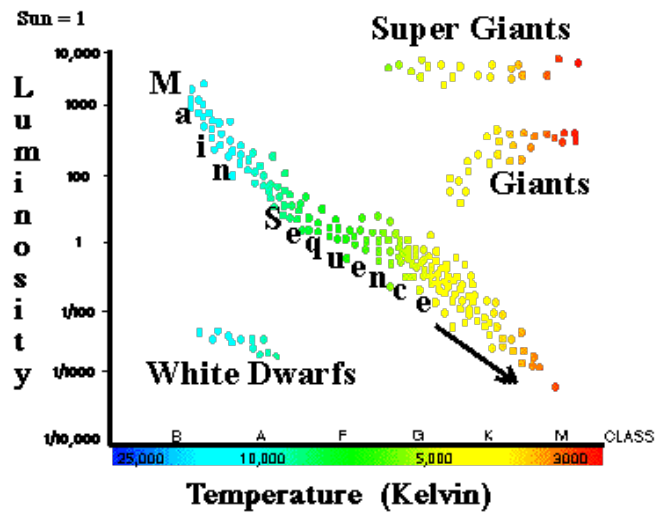
In General Relativity

$$P_{\min} = 0.96 \left( \frac{M_{\text{sun}}}{M} \right)^{1/2} \left( \frac{R}{10\text{km}} \right)^{3/2} \text{ ms}$$

Actual record: PSR J1748-2446ad → **P=1.39595482 ms**

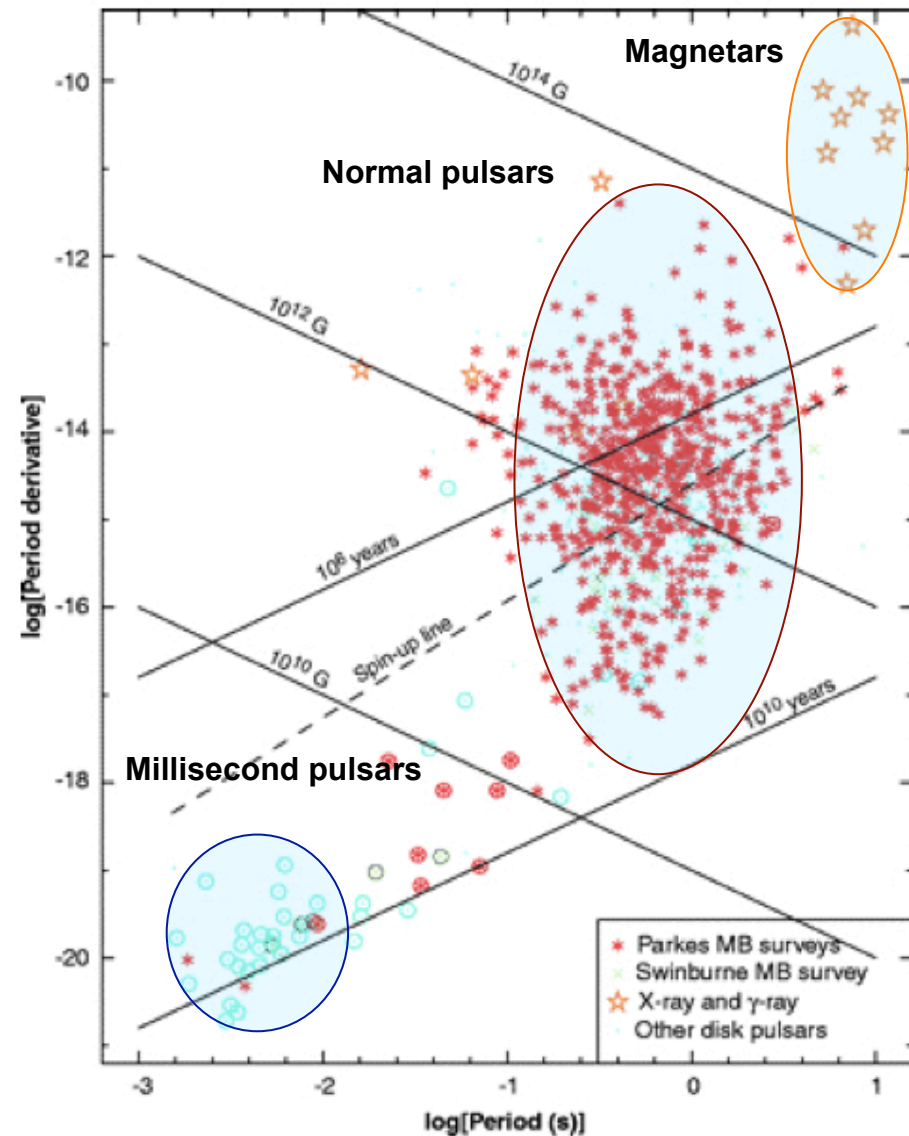
# Pulsar distribution in the P- $\dot{P}$ plane

Pulsar equivalent of the  
Hertzprung-Russell diagram  
for ordinary stars



$$\log \dot{P} = \log \left[ \frac{(2\pi)^2 R^6}{6c^3 I} B_p^2 \sin^2 \alpha \right] - \log P$$

$$\log \dot{P} = \log P - \log(2\tau)$$

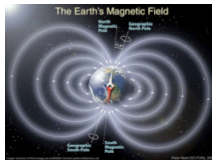


# Magnetic Field of a Pulsar

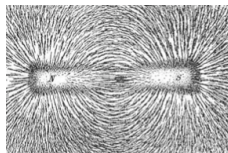
Type of Pulsar	Surface magnetic field
Millisecond	$10^8 - 10^9$ G
Normal	$10^{12}$ G
Magnetar	$10^{14} - 10^{15}$ G

Extremely high compared to ...

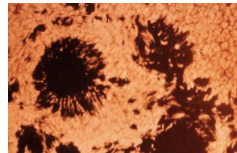
Earth  
0.3 – 0.5 G



Magnet  
 $10^3 - 10^4$  G



Sun spots  
 $10^5$  G



Largest continuous field in lab. (USA)

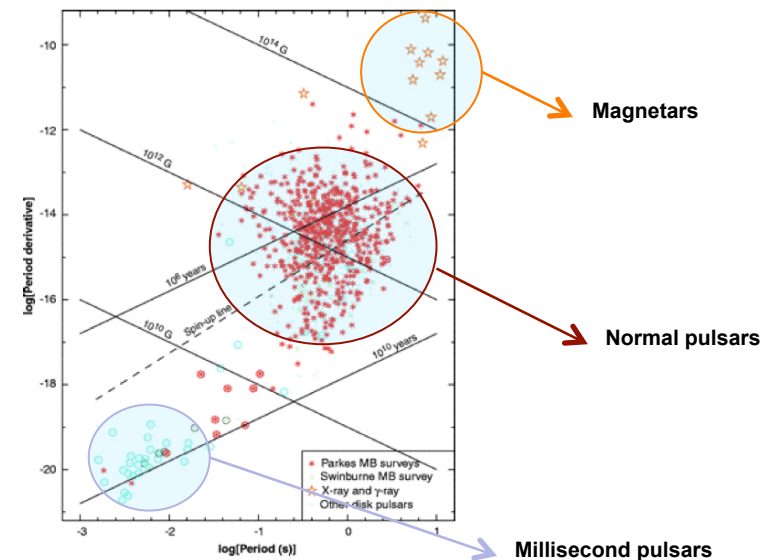
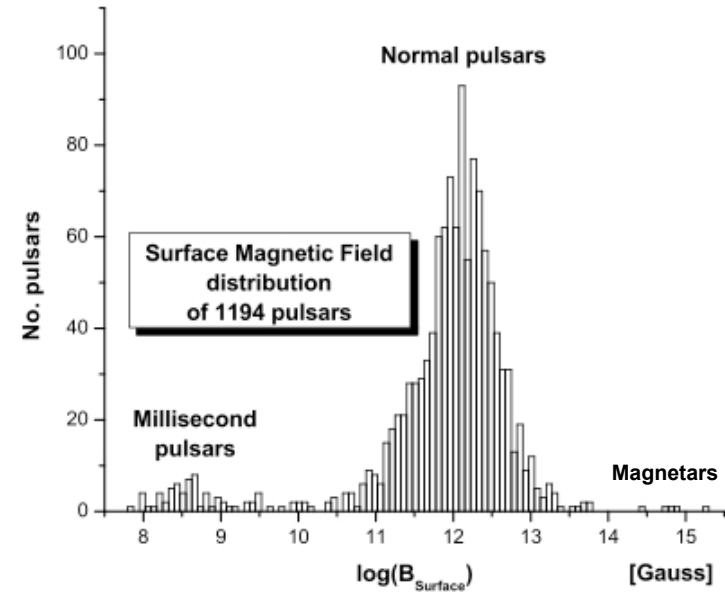


$4.5 \times 10^5$  G

Largest magnetic pulse in lab. (Russia)



$2.8 \times 10^7$  G



## Where the NS magnetic field comes from ?

A satisfactory answer does not exist yet. Several possibilities have been considered:

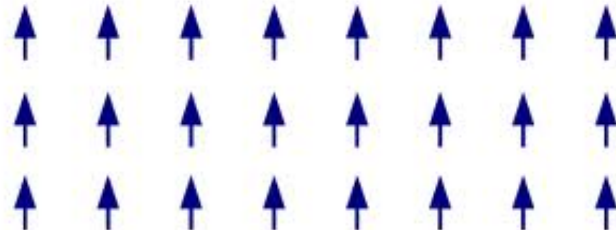
- ✧ **Conservation of the magnetic flux** during the gravitational collapse of the iron core

$$\phi_i = \phi_f \Rightarrow B_f = B_i \left( \frac{R_i}{R_f} \right)^2$$

For a progenitor star with  $B_i \sim 10^2$  G  
&  $R_i \sim 10^6$  km we have  $B_f \sim 10^{12}$  G

- ✧ **Electric currents** flowing in the highly conductive NS interior

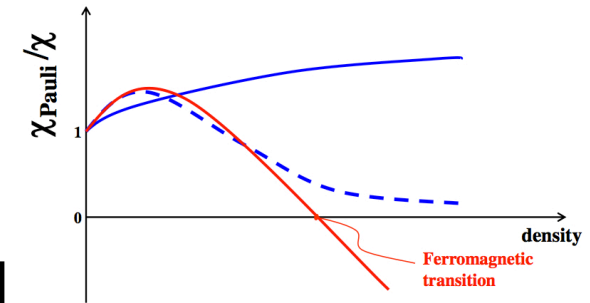
- ✧ **Spontaneous transition to a ferromagnetic state** due to the nuclear interaction



# Ferromagnetic Transition

Considered by many authors with contradictory results:

Year	Autor/Model	Ferromagnetic Transition ?
1969	Brownell, Callaway, Rice (hard sphere gas)	Yes, $k_F > 2.3 \text{ fm}^{-1}$
1969	Clark & Chao	No
1970	Ostgard	Yes, $k_F > 4.1 \text{ fm}^{-1}$
1972	Pandharipande et al., (variational)	No
1975	Backman, Kallaman, Haensel (BHF)	No
1984	Vidaurre (Skyrme)	Yes, $k_F > 1.7-2.0 \text{ fm}^{-1}$
1991	S. Marcos et al., (DBHF)	No
2001	Fantoni et at. (AFDMC)	No
2002/2005	I.V., et al. (BHF)	No
2005/2006	I.V. et al., (Skyrme, Gogny)	Yes, $k_F > 2-3.4 \text{ fm}^{-1}$
2007-2011	F. Sammarruca (DBHF)	No



- ✧ Calculations based on **phenomenological interactions** (e.g., Skyrme, Gogny) predict the transition to occur at  $(1-4)\rho_0$
- ✧ Calculations based on **realistic NN & NNN forces** (e.g., Monte Carlo, BHF, DBHF, LOCV) exclude such a transition

# Neutron Star Structure: General Relativity or Newtonian Gravity ?

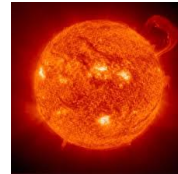
Surface gravitational potential tell us how much compact an object is

$$\frac{2GM}{c^2 R}$$

→ Relativistic effects are very important in Neutron Stars and General Relativity must be used to describe their structure



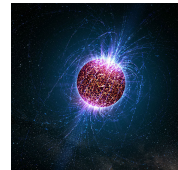
$\sim 10^{-10}$



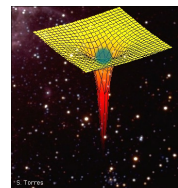
$\sim 10^{-5}$



$\sim 10^{-4} - 10^{-3}$



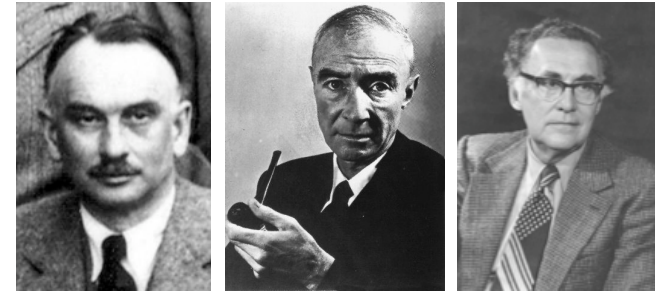
$\sim 0.2 - 0.4$



$1$

# The Tolman-Oppenheimer-Volkoff Equations

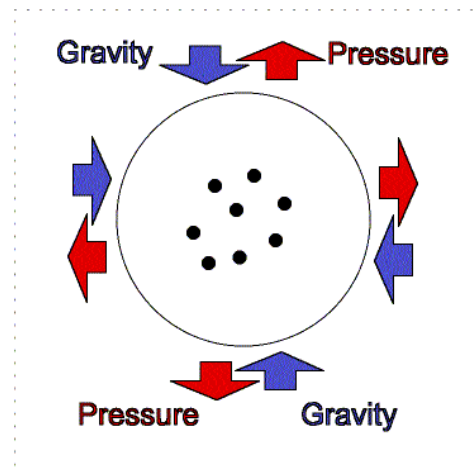
In 1939 Tolman, Oppenheimer & Volkoff obtain the equations that describe the structure of a static star with spherical symmetry in General Relativity (Chandrasekhar & von Neumann obtained them in 1934 but they did not published their work)



Tolman, Phys. Rev. 55, 364 (1939)



Oppenheimer & Volkoff, Phys. Rev. 55, 374 (1939)



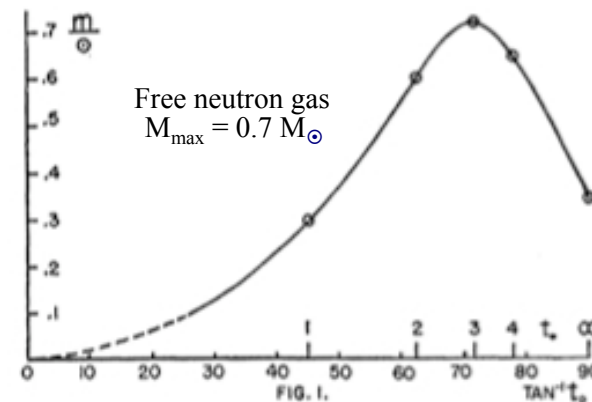
$$\frac{dP}{dr} = -G \frac{m(r)\epsilon(r)}{r^2} \left( 1 + \frac{P(r)}{c^2 \epsilon(r)} \right) \left( 1 + \frac{4\pi r^3 P(r)m(r)}{c^2} \right) \left( 1 - \frac{2Gm(r)}{c^2 r} \right)^{-1}$$

$$\frac{dm}{dr} = 4\pi r^2 \epsilon(r)$$

boundary conditions

$$P(0) = P_o, \quad m(0) = 0$$

$$P(R) = 0, \quad m(R) = M$$

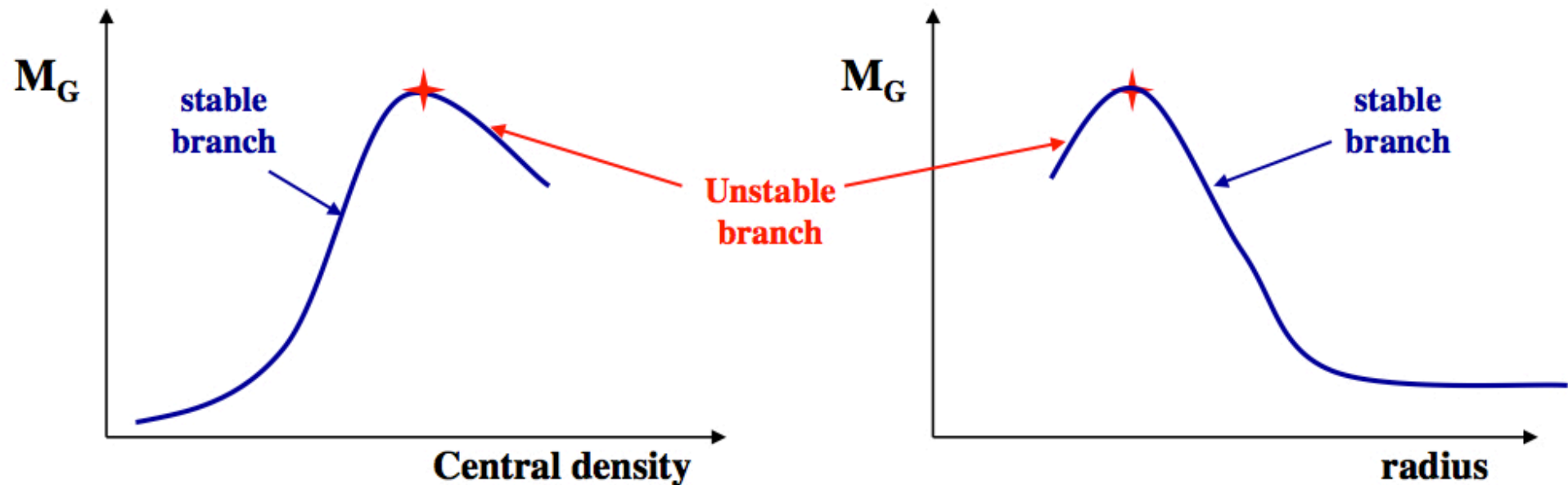




# Stability solutions of the TOV equations

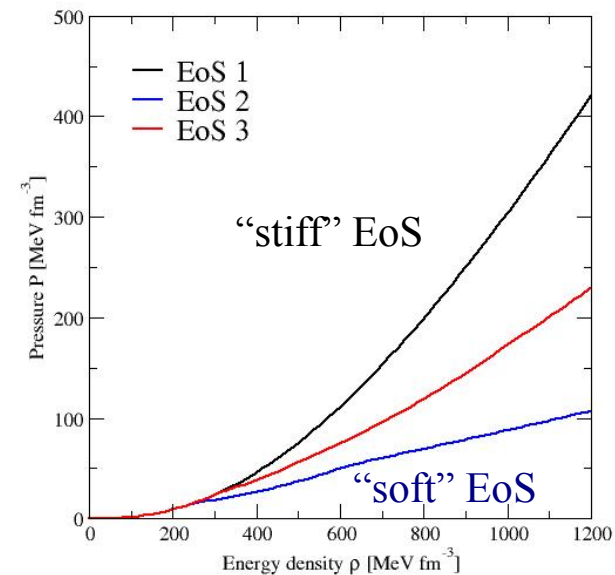
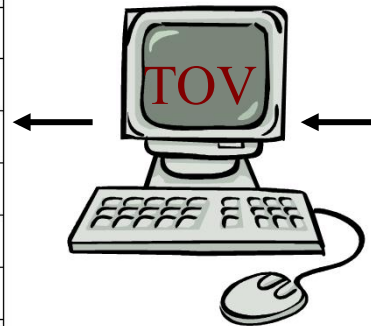
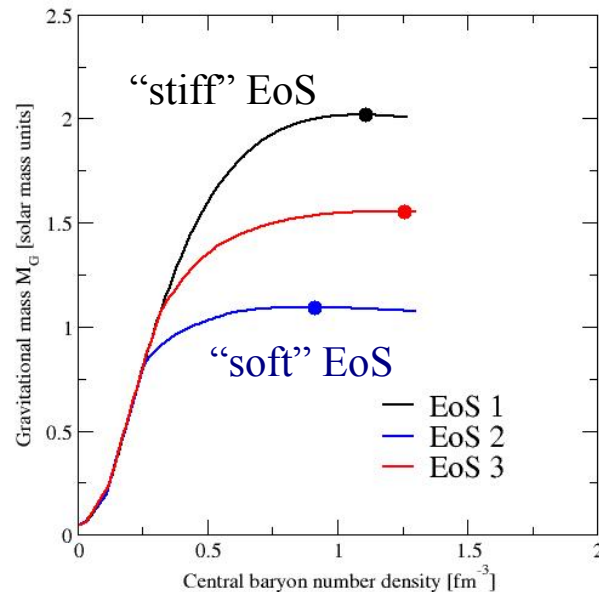
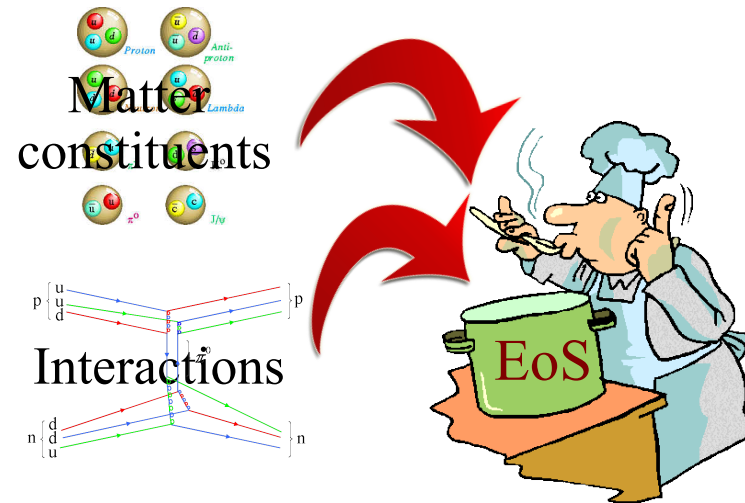
- ✧ The solutions of the TOV eqs. represent **static equilibrium configurations**
- ✧ Stability is required with respect to **small perturbations**

$$\frac{dM_G}{d\rho_c} > 0, \text{ or } \frac{dM_G}{dr} < 0$$



# The role of the Equation of State

The only ingredient needed to solve the TOV equations is the (poorly known) EoS (i.e.,  $p(\epsilon)$ ) of dense matter



## Upper limit of the Maximum Mass

$M_{\max}$  depends mainly on the behaviour of EoS,  $P(\epsilon)$ , at high densities. Any realistic EoS must satisfy two conditions:

$$\blacksquare \text{ Causality: } \frac{dP}{d\rho} \leq c^2 \quad \blacksquare \text{ Stability: } \frac{dP}{d\rho} > 0$$

If the EoS is known up to  $\rho_r$ , these conditions imply:

$$M_{\max} \leq 3M_{\odot} \left( \frac{5 \times 10^{14} \text{ g / cm}^3}{\rho_r} \right)^{1/2}$$

If rotation is taken into account  $M_{\max}$  can increase up to 20%:

$$M_{\max} \leq 3.89M_{\odot} \left( \frac{5 \times 10^{14} \text{ g / cm}^3}{\rho_r} \right)^{1/2}$$

# How to Measure Neutron Star Masses

Use Doppler variations in spin period to measure orbital velocity changes along the line-of-sight

- 5 Keplerian parameters can normally be determined:

$P, a \sin i, \epsilon, T_0$  &  $\omega$

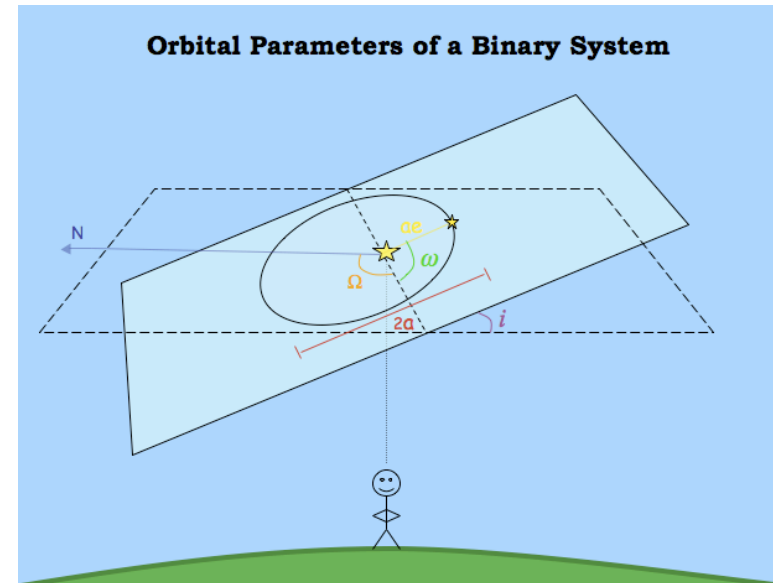
- 3 unknowns:  $M_1, M_2, i$

Kepler's 3<sup>rd</sup> law

$$\frac{G(M_1 + M_2)}{a^3} = \left(\frac{2\pi}{P}\right)^2 \rightarrow$$

$$f(M_1, M_2, i) \equiv \frac{(M_2 \sin i)^3}{(M_1 + M_2)^2} = \frac{Pv^3}{2\pi G}$$

mass function



# In few cases small deviations from Keplerian orbit due to GR effects can be detected

Measure of at least 2 post-Keplerian parameters



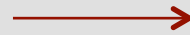
High precision NS mass determination

$$\dot{\omega} = 3T_{\otimes}^{2/3} \left( \frac{P_b}{2\pi} \right)^{-5/3} \frac{1}{1-\varepsilon} (M_p + M_c)^{2/3}$$



Periastron precession

$$\gamma = T_{\otimes}^{2/3} \left( \frac{P_b}{2\pi} \right)^{1/3} \varepsilon \frac{M_c (M_p + 2M_c)}{(M_p + M_c)^{4/3}}$$



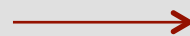
Time dilation and grav. redshift

$$r = T_{\otimes} M_c$$



Shapiro delay “range”

$$s = \sin i = T_{\otimes}^{-1/3} \left( \frac{P_b}{2\pi} \right)^{-2/3} x \frac{(M_p + M_c)^{2/3}}{M_c}$$



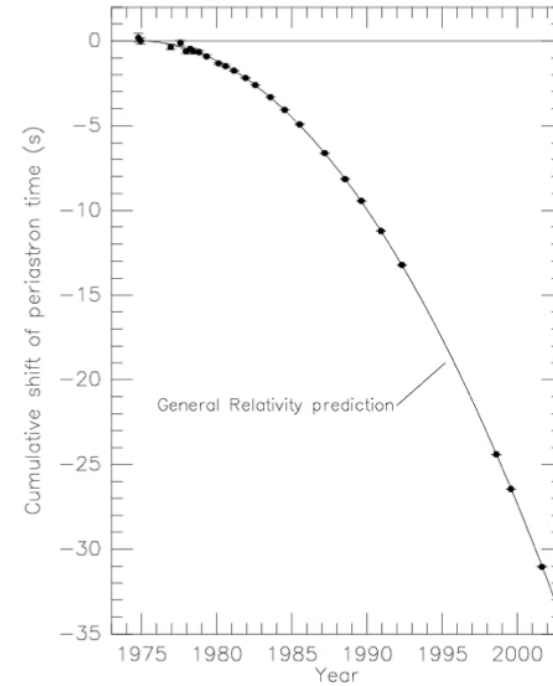
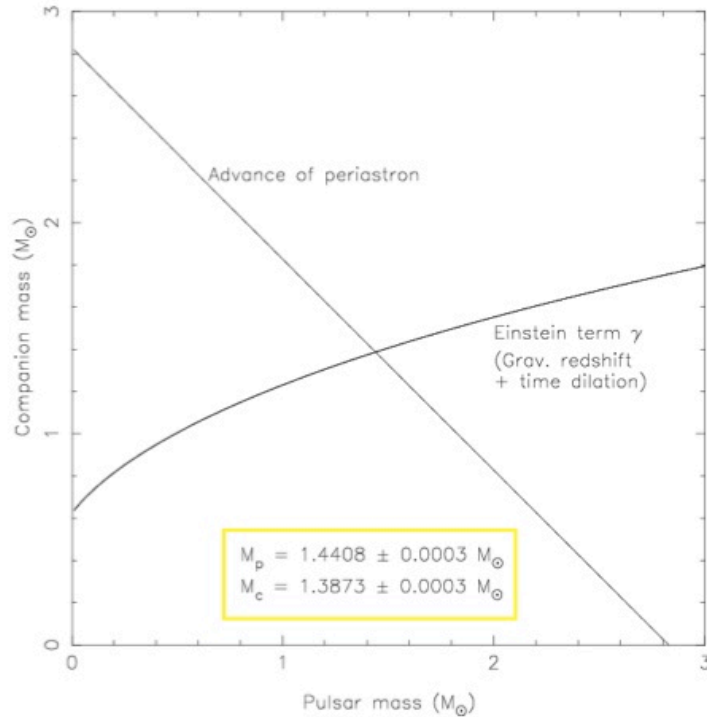
Shapiro delay “shape”

$$\dot{P}_b = -\frac{192\pi}{5} T_{\otimes}^{5/3} \left( \frac{P_b}{2\pi} \right)^{-5/3} f(\varepsilon) \frac{M_p M_c}{(M_p + M_c)^{1/3}}$$



Orbit decay due to GW emission

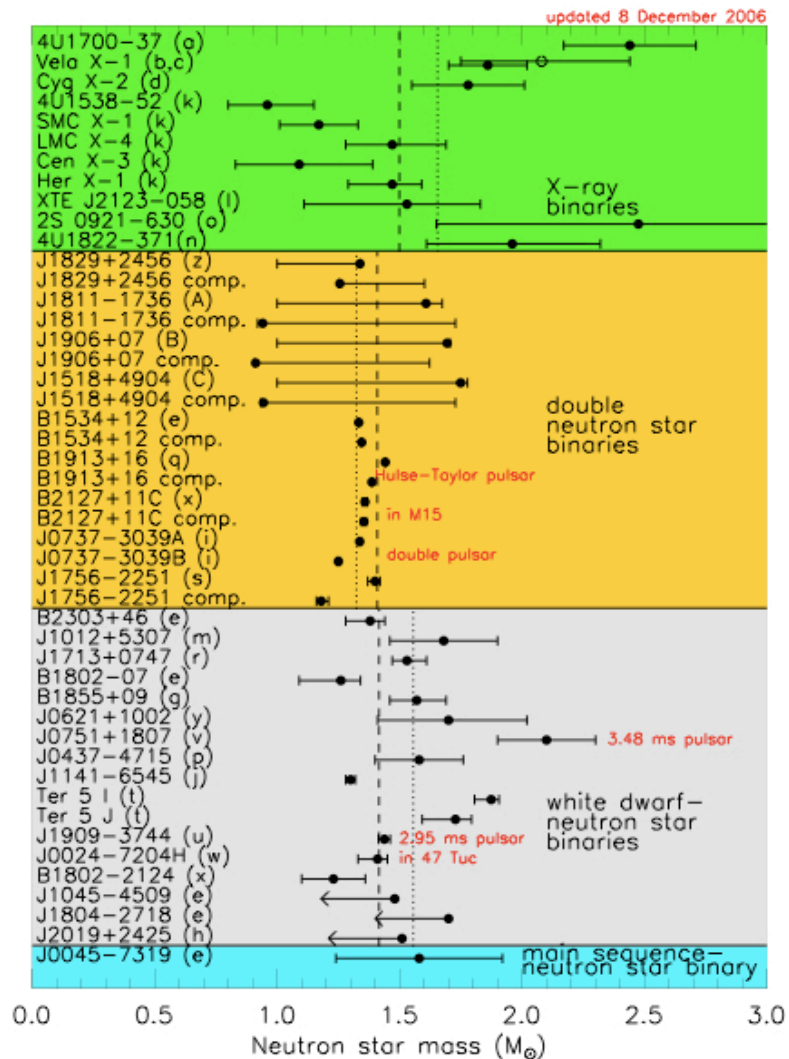
# An example: the mass of the Hulse-Taylor pulsar (PSR J1913+16)



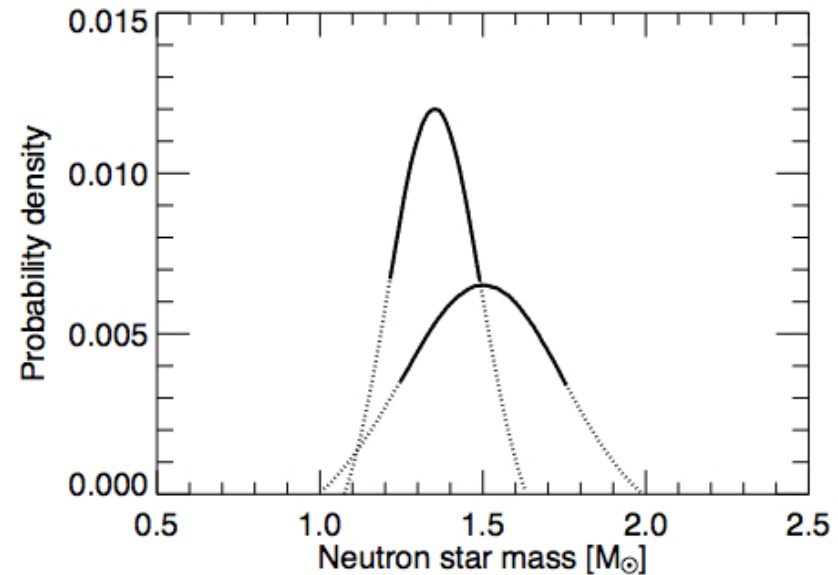
Parameter	Value
Orbital period $P_b$ (d)	0.322997462727(5)
Projected semi-major axis $x$ (s)	2.341774(1)
<u>Eccentricity <math>e</math></u>	<u>0.6171338(4)</u>
Longitude of periastron $\omega$ (deg)	226.57518(4)
Epoch of periastron $T_0$ (MJD)	46443.99588317(3)
Advance of periastron $\dot{\omega}$ (deg yr $^{-1}$ )	4.226607(7)
Gravitational redshift $\gamma$ (ms)	4.294(1)
Orbital period derivative $(\dot{P}_b)^{obs}$ ( $10^{-12}$ )	-2.4211(14)



# Measured Neutron Star Masses (up to ~ 2006-2008)



(Lattimer & Prakash 2007)



up to ~ 2006-2008 any valid  
 EoS should predict

$$M_{\max} [EoS] > 1.4 - 1.5 M_{\odot}$$

N.B. I will comment on more recent measurements later when talking about the “hyperon problem”

# Limits on the Neutron Star Radius

The radius of a neutron star with mass  $M$  cannot be arbitrarily small

General Relativity:  
a Neutron Star is not a  
Black Hole

$$R > \frac{2GM}{c^2}$$

Finite Pressure:  
Neutron Star matter cannot  
be arbitrarily compressed

$$R > \frac{9}{4} \frac{GM}{c^2}$$

Causality:  
speed of sound must  
be smaller than  $c$

$$R > 2.9 \frac{GM}{c^2}$$

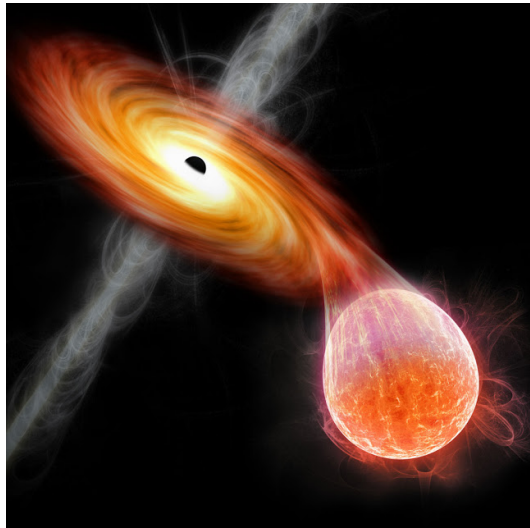


# How to measure Neutron Star Radii

Radii are very difficult to measure because NS:

- ✧ are very small ( $\sim 10$  km)
- ✧ are far from us (e.g., the closest NS, RX J1856.5-3754, is at  $\sim 400$  ly)

A possible way to measure it is to use the thermal emission of low mass X-ray binaries:



NS radius can be obtained from

- ✧ Flux measurement + Stefan-Boltzmann's law
- ✧ Temperature (Black body fit+atmosphere model)
- ✧ Distance estimation (difficult)
- ✧ Gravitational redshift  $z$  (detection of absorption lines)

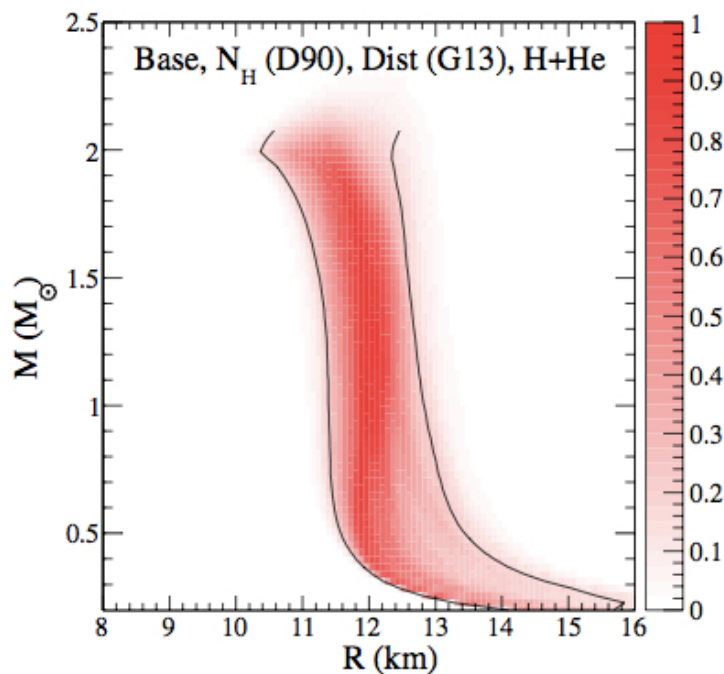
$$R_{\infty} = \sqrt{\frac{FD^2}{\sigma_{SB}T^4}} \rightarrow R_{NS} = \frac{R_{\infty}}{1+z} = R_{\infty} \sqrt{1 - \frac{2GM}{R_{NS}c^2}}$$

# Recent Estimations of Neutron Star Radii

The recent analysis of the thermal spectrum from 5 quiescent LMXB in globular clusters is still controversial



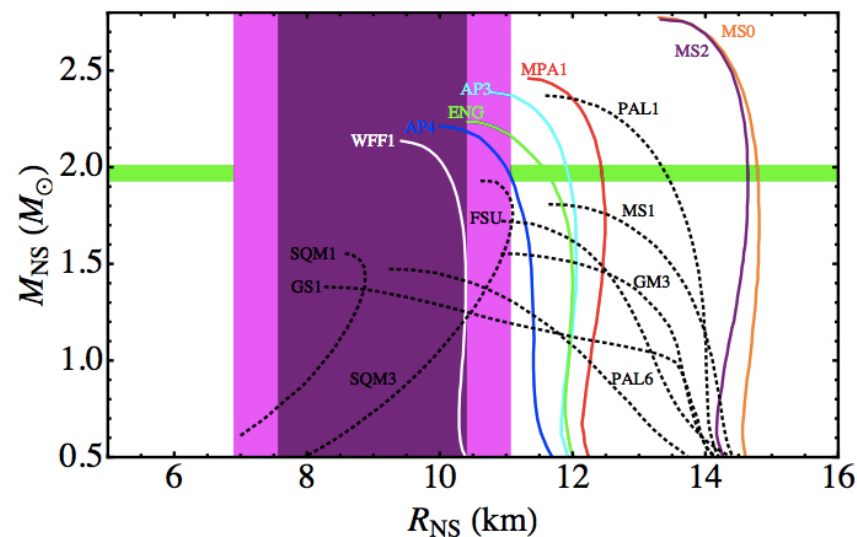
Steiner et al. (2013, 2014)



$$R = 12.0 \pm 1.4 \text{ km}$$



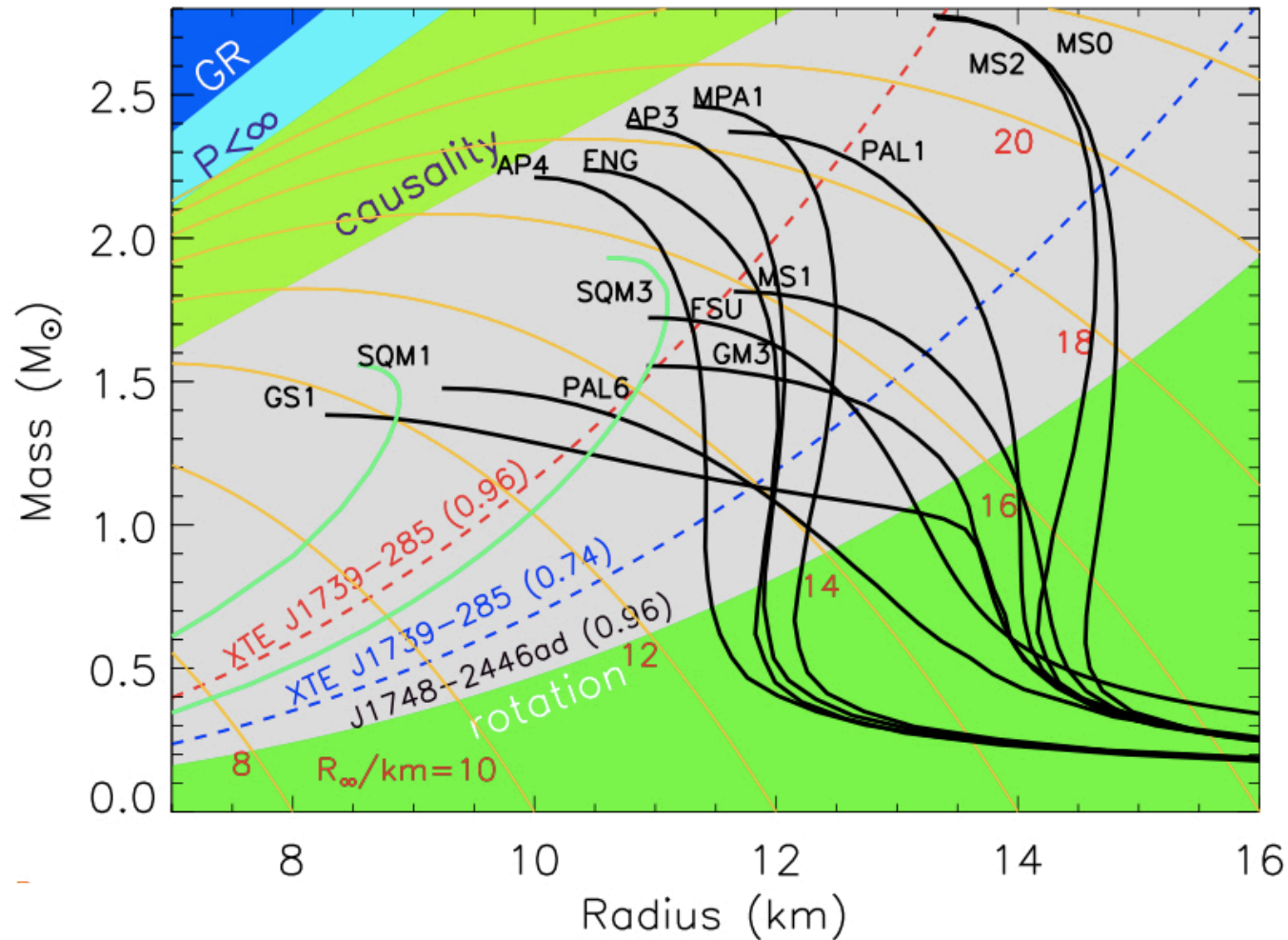
Guillot et al. (2013, 2014)



$$R = 9.1^{+1.3}_{-1.5} \text{ km} \text{ 2013 analysis}$$

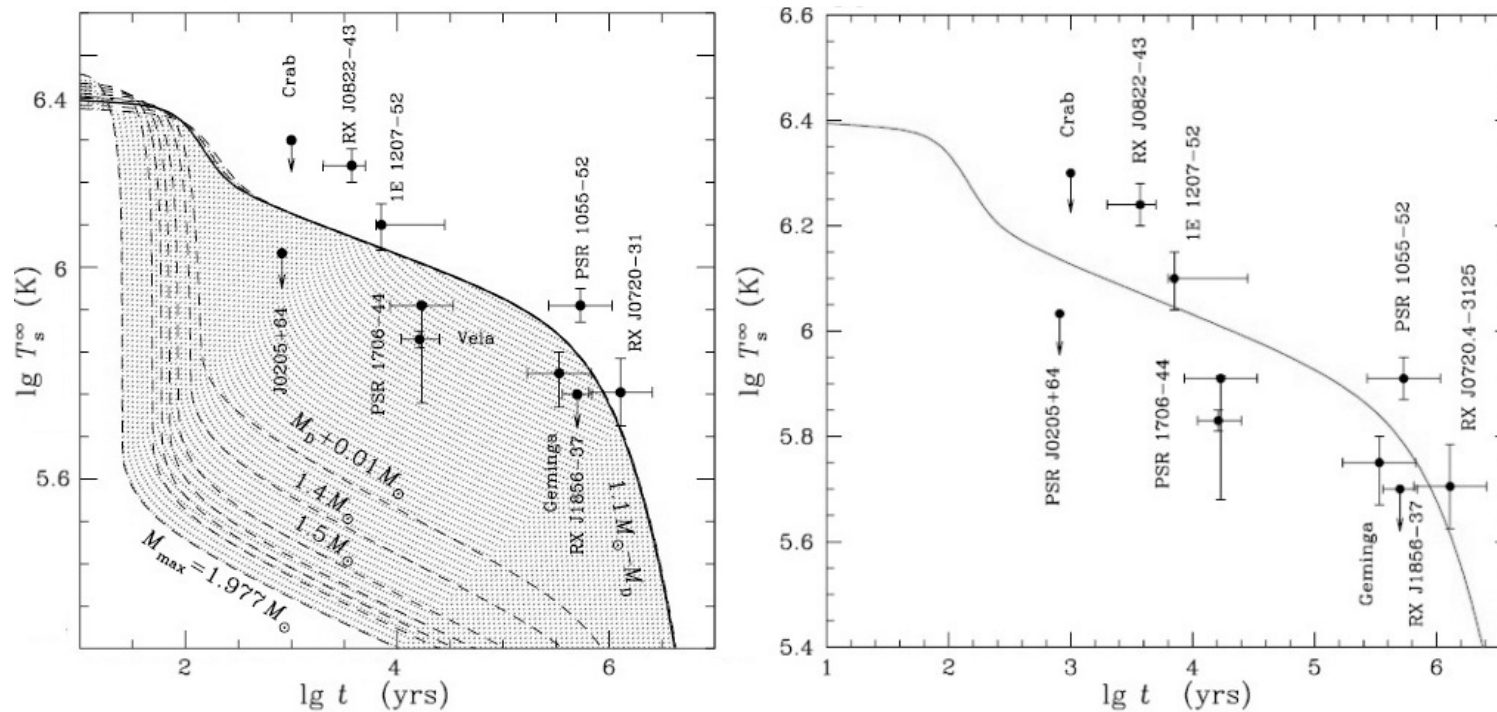
$$R = 9.4 \pm 1.2 \text{ km} \text{ 2014 analysis}$$

# Limits of the Mass & Radius of a Neutron Star



# Thermal Evolution of Neutron Stars

Information, complementary to that from mass & radius, can be also obtained from the measurement of the **temperature (luminosity) of neutron stars**



# Neutron Star Cooling in a Nutshell



## Two cooling regimes

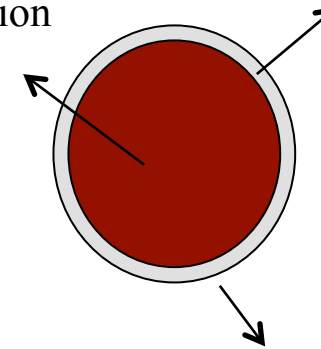
Slow

Low NS mass

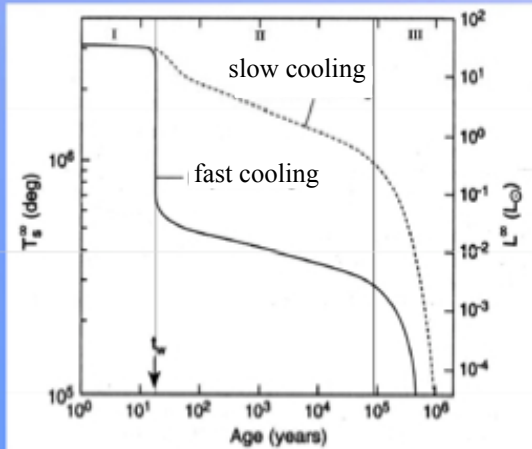
Fast

High NS mass

Core cools by  
neutrino emission



Surface photon emission  
dominates at  $t > 10^6$  yrs



- I. Core relaxation epoch
- II. Neutrino cooling epoch
- III. Photon cooling epoch

$$\frac{dE_{th}}{dt} = C_v \frac{dT}{dt} = -L_\gamma - L_\nu + H$$

- ✓  $C_v$ : specific heat
- ✓  $L_\gamma$ : photon luminosity
- ✓  $L_\nu$ : neutrino luminosity
- ✓  $H$ : “heating”

# Neutrino Emission

Name	Process	Emissivity (erg cm <sup>-3</sup> s <sup>-1</sup> )	
Modified Urca cycle (neutron branch)	$n + n \rightarrow n + p + e^- + \bar{\nu}_e$	$\sim 2 \times 10^{21} R T_9^8$	Slow
	$n + p + e^- \rightarrow n + n + \nu_e$		
Modified Urca cycle (proton branch)	$p + n \rightarrow p + p + e^- + \bar{\nu}_e$	$\sim 10^{21} R T_9^8$	Slow
	$p + p + e^- \rightarrow p + n + \nu_e$		
Bremsstrahlung	$n + n \rightarrow n + n + \nu + \bar{\nu}$	$\sim 10^{19} R T_9^8$	Slow
	$n + p \rightarrow n + p + \nu + \bar{\nu}$		
	$p + p \rightarrow p + p + \nu + \bar{\nu}$		
Cooper pair formations	$n + n \rightarrow [nn] + \nu + \bar{\nu}$	$\sim 5 \times 10^{21} R T_9^7$	Medium
	$p + p \rightarrow [pp] + \nu + \bar{\nu}$	$\sim 5 \times 10^{19} R T_9^7$	
Direct Urca cycle (nucleons)	$n \rightarrow p + e^- + \bar{\nu}_e$	$\sim 10^{27} R T_9^6$	Fast
	$p + e^- \rightarrow n + \nu_e$		
Direct Urca cycle ( $\Lambda$ hyperons)	$\Lambda \rightarrow p + e^- + \bar{\nu}_e$	$\sim 10^{27} R T_9^6$	Fast
	$p + e^- \rightarrow \Lambda + \nu_e$		
Direct Urca cycle ( $\Sigma^-$ hyperons)	$\Sigma^- \rightarrow n + e^- + \bar{\nu}_e$	$\sim 10^{27} R T_9^6$	Fast
	$n + e^- \rightarrow \Sigma^- + \nu_e$		
$\pi^-$ condensate	$n + \langle \pi^- \rangle \rightarrow n + e^- + \bar{\nu}_e$	$\sim 10^{26} R T_9^6$	Fast
$K^-$ condensate	$n + \langle K^- \rangle \rightarrow n + e^- + \bar{\nu}_e$	$\sim 10^{25} R T_9^6$	Fast

Anything beyond just neutrons & protons results in an **enhancement**  
of the neutrino emission

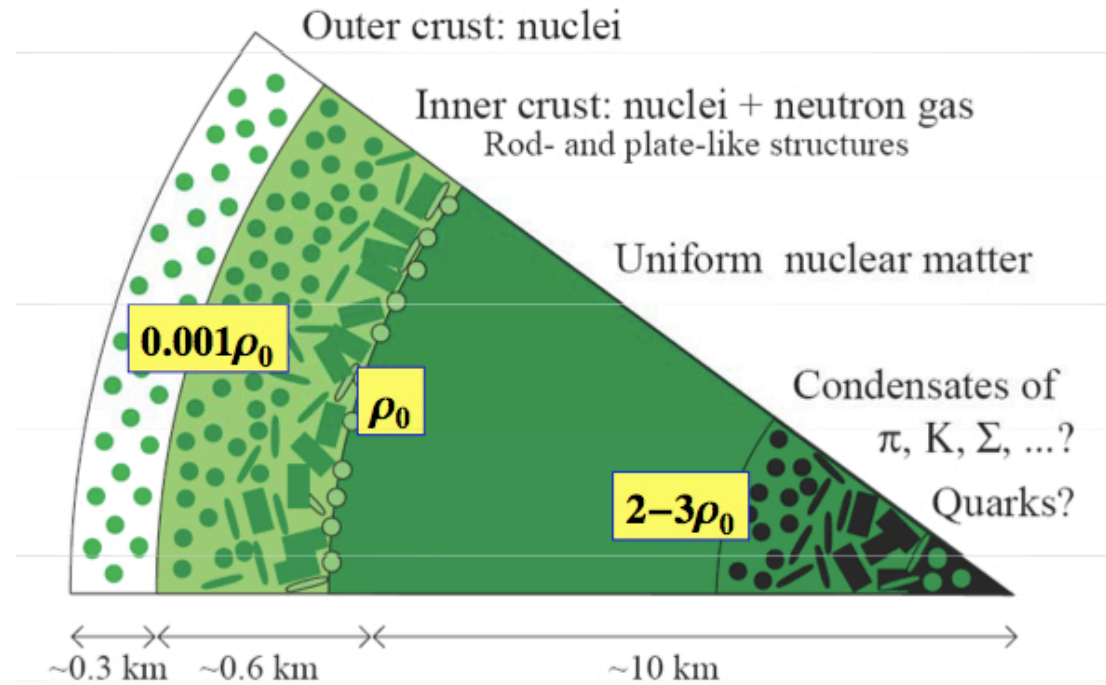
# Anatomy of a Neutron Star

Equilibrium composition  
determined by

- ✓ Charge neutrality

$$\sum_i q_i \rho_i = 0$$

- ✓ Equilibrium with respect to weak interacting processes



$$\begin{array}{l}
 b_1 \rightarrow b_2 + l + \bar{\nu}_l \\
 b_2 + l \rightarrow b_1 + \nu_l
 \end{array}
 \longrightarrow
 \mu_i = b_i \mu_n - q_i (\mu_e - \mu_{\nu_e}), \quad \mu_i = \frac{\partial \varepsilon}{\partial \rho_i}$$

# Hyperons in Neutron Stars

Hyperons in NS considered by many authors since the pioneering work of Ambartsumyan & Saakyan (1960)



## Phenomenological approaches

- ✧ **Relativistic Mean Field Models:** Glendenning 1985; Knorren et al. 1995; Shaffner-Bielich & Mishustin 1996, Bonano & Sedrakian 2012, ...
- ✧ **Non-relativistic potential model:** Balberg & Gal 1997
- ✧ **Quark-meson coupling model:** Pal et al. 1999, ...
- ✧ **Chiral Effective Lagrangians:** Hanauske et al., 2000
- ✧ **Density dependent hadron field models:** Hofmann, Keil & Lenske 2001



## Microscopic approaches

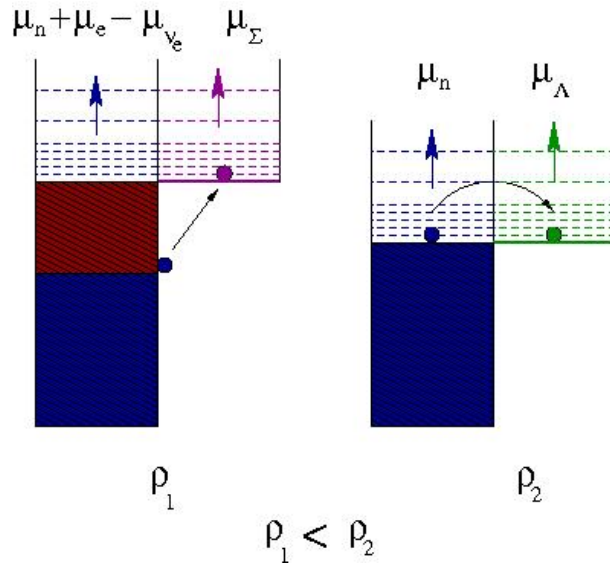
- ✧ **Brueckner-Hartree-Fock theory:** Baldo et al. 2000; I. V. et al. 2000, Schulze et al. 2006, I.V. et al. 2011, Burgio et al. 2011, Schulze & Rijken 2011
- ✧ **DBHF:** Sammarruca (2009), Katayama & Saito (2014)
- ✧  $V_{\text{low } k}$ : Djapo, Schaefer & Wambach, 2010
- ✧ **Quantum Monte Carlo:** Lonardonì et al., (2014)



Sorry if I missed somebody

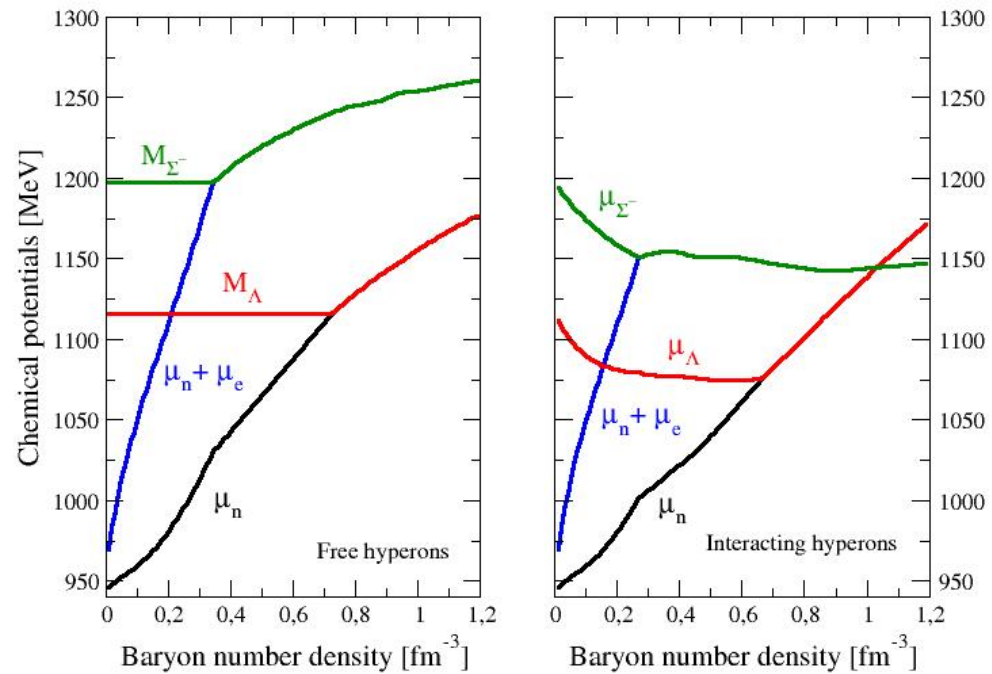
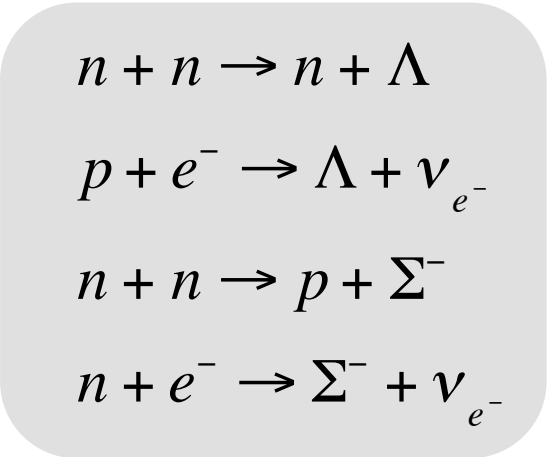


Hyperons are expected to appear in the core of neutron stars at  $\rho \sim (2-3)\rho_0$  when  $\mu_N$  is large enough to make the conversion of N into Y energetically favorable.



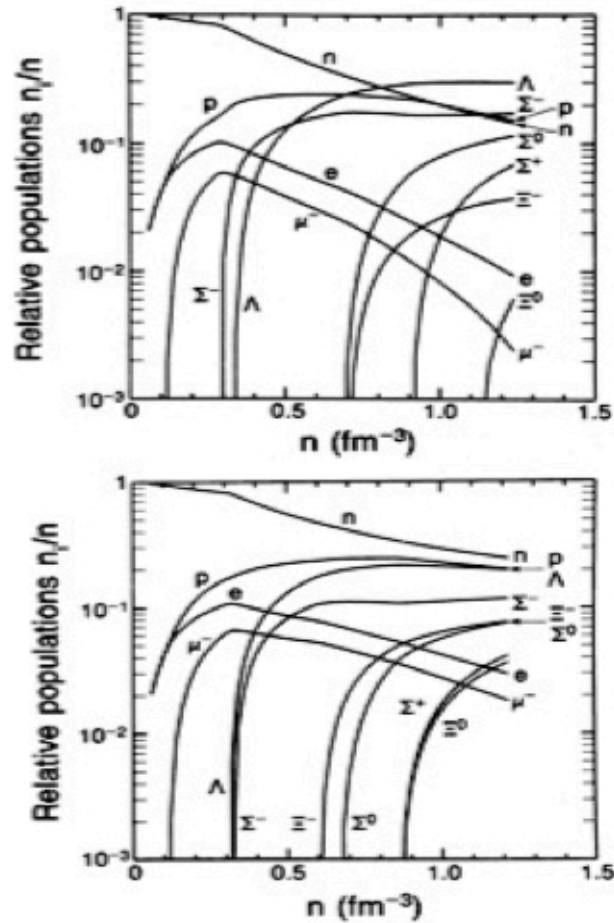
$$\mu_{\Sigma^-} = \mu_n + \mu_{e^-} - \mu_{\nu_{e^-}}$$

$$\mu_{\Lambda} = \mu_n$$

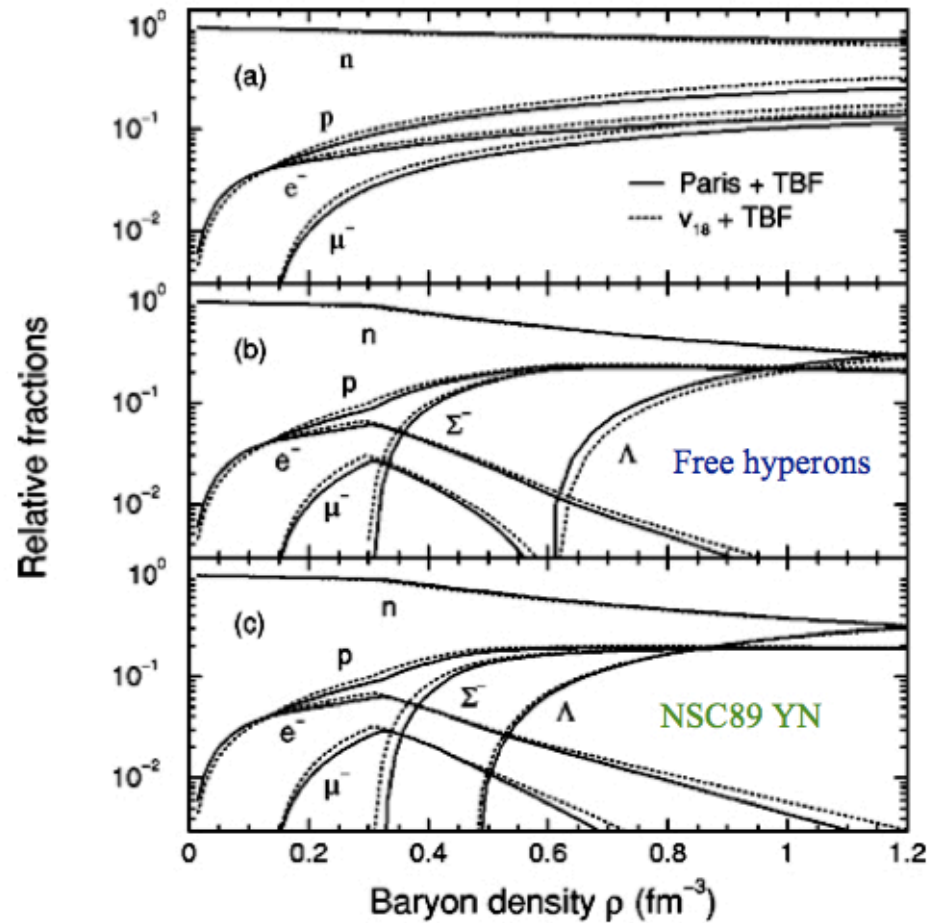


# Neutron Star Matter Composition

## RMFT



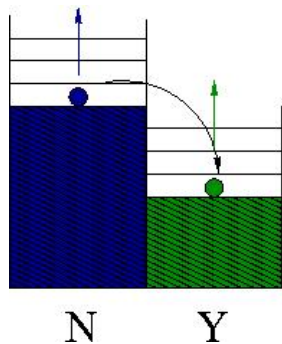
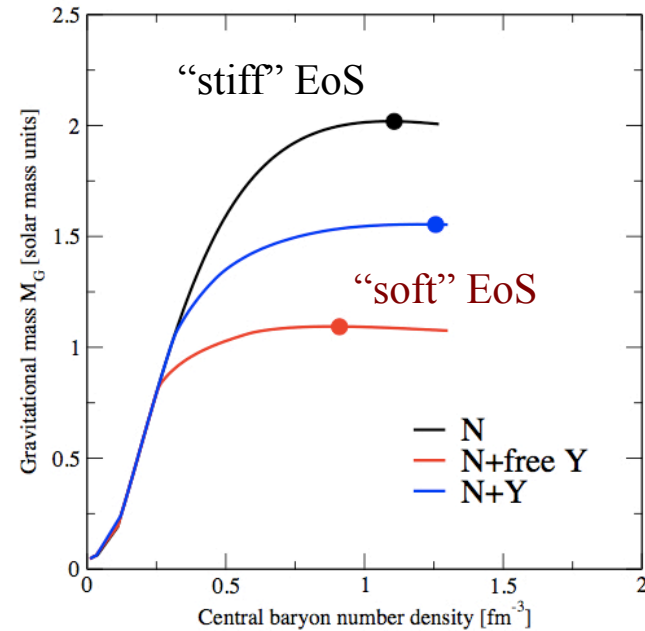
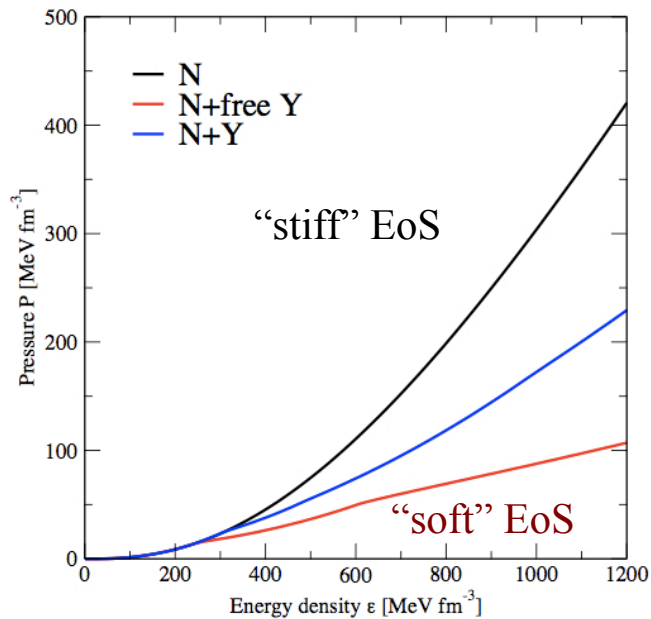
## BHF



N. K. Glendenning, APJ 293, 470 (1985)

M. Baldo et al., PRC 61, 055801 (2000)

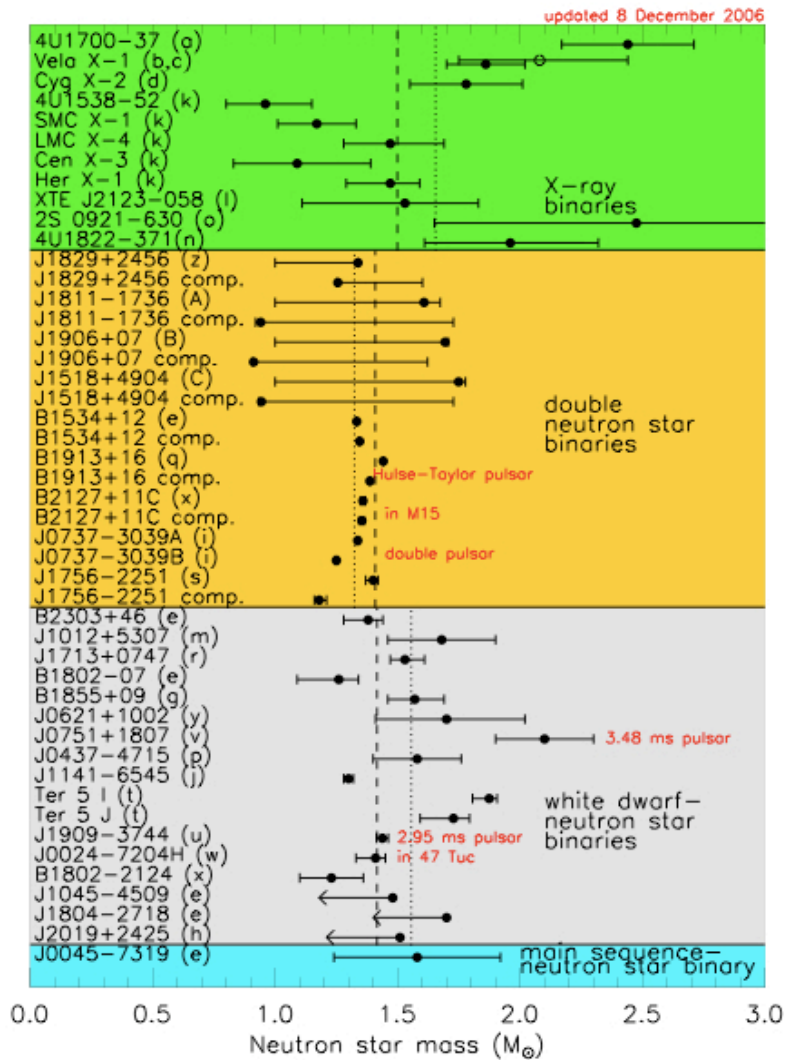
# Effect of Hyperons in the EoS and Mass of Neutron Stars



Relieve of Fermi pressure due to the appearance of hyperons →  
EoS softer → reduction of the mass

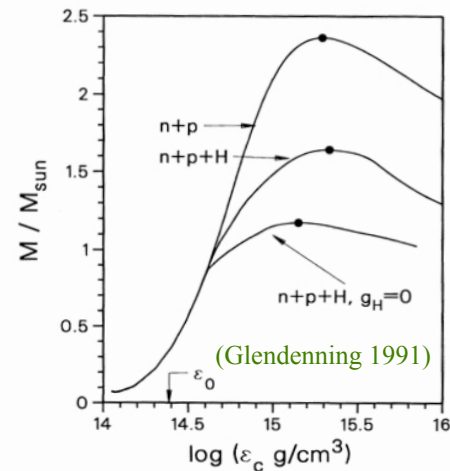
# Hyperons in NS

(up to ~ 2006-2008)

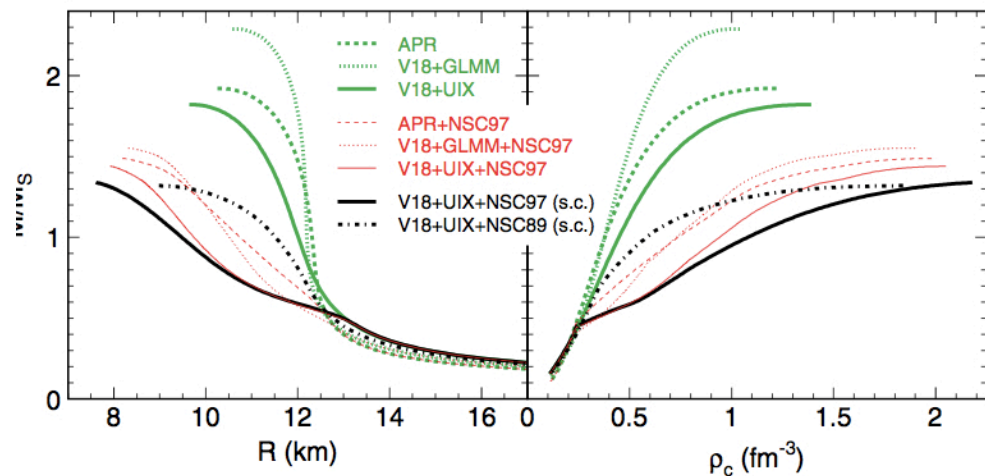


(Lattimer & Prakash 2007)

Phenomenological:  
 $M_{\max}$  compatible with 1.4-1.5  $M_{\odot}$



Microscopic :  $M_{\max} < 1.4-1.5 M_{\odot}$

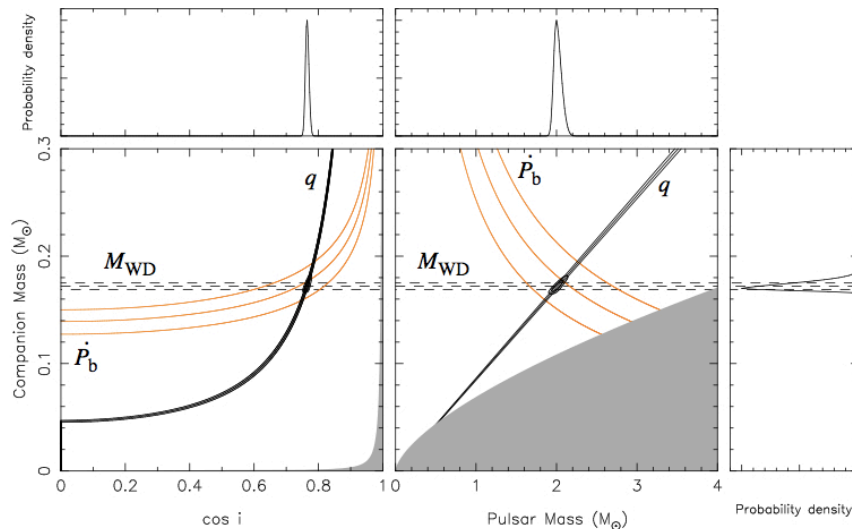
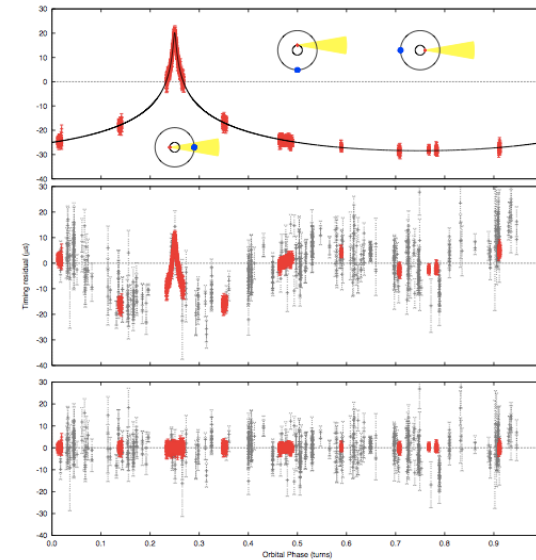


(Schulze, Polls, Ramos & IV 2006)

Recent measurements of high masses  $\longrightarrow$  life of hyperons more difficult

■ PSR J164-2230 (Demorest et al. 2010)

- ✓ binary system ( $P = 8.68d$ ,  $i = 89.17(2)^{\circ}$ )
- ✓ low eccentricity ( $\epsilon = 1.3 \times 10^{-6}$ )
- ✓ companion (WD) mass:  $\sim 0.5M_{\odot}$
- ✓ pulsar mass:  $M = 1.97 \pm 0.04M_{\odot}$



■ PSR J0348+0432 (Antoniadis et al. 2013)

- ✓ binary system ( $P = 2.46h$ ,  $i = 40.2(6)^{\circ}$ )
- ✓ very low eccentricity
- ✓ companion (WD) mass:  $0.172 \pm 0.003M_{\odot}$
- ✓ pulsar mass:  $M = 2.01 \pm 0.04M_{\odot}$

# Formation of Binary Systems

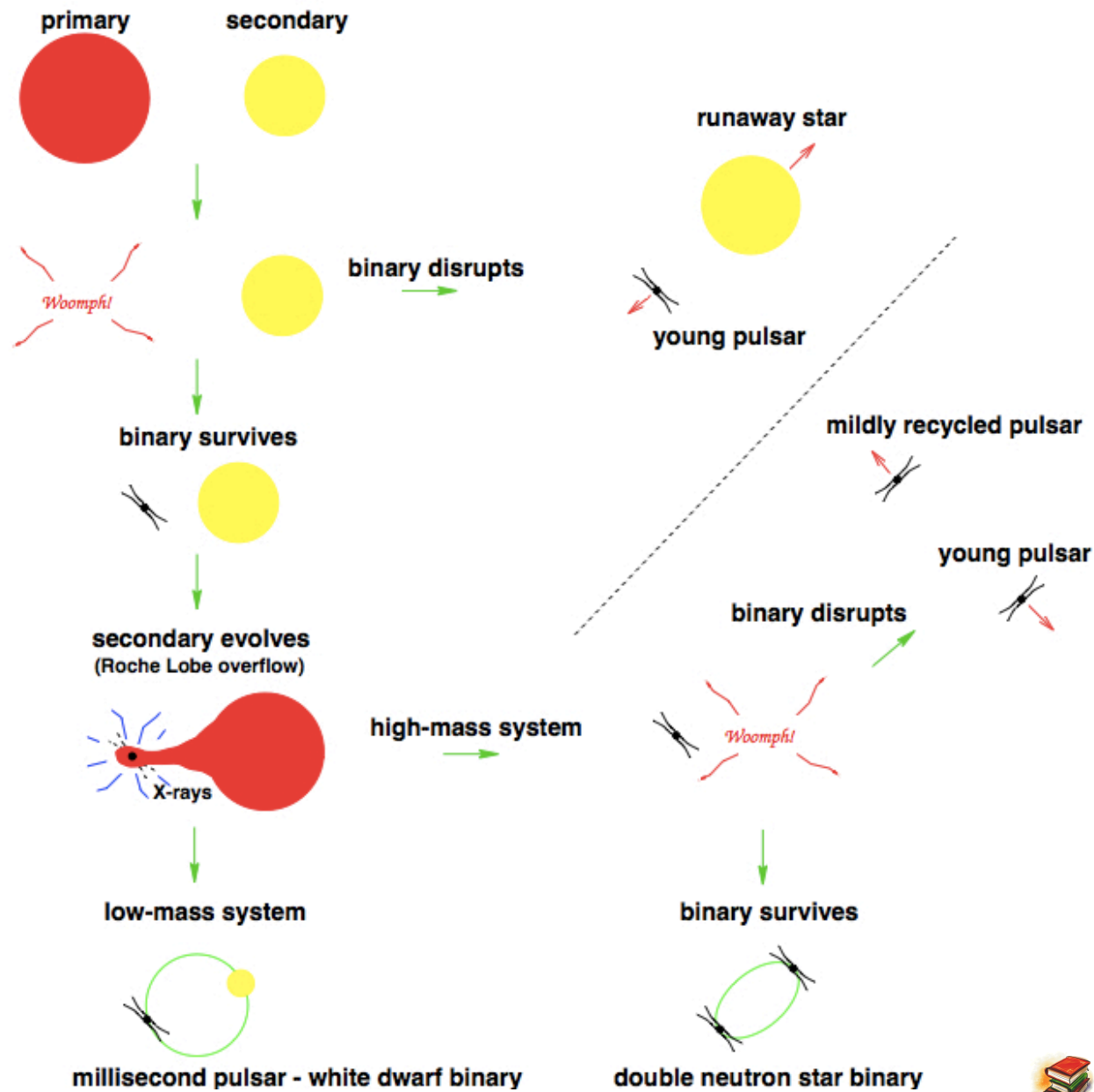
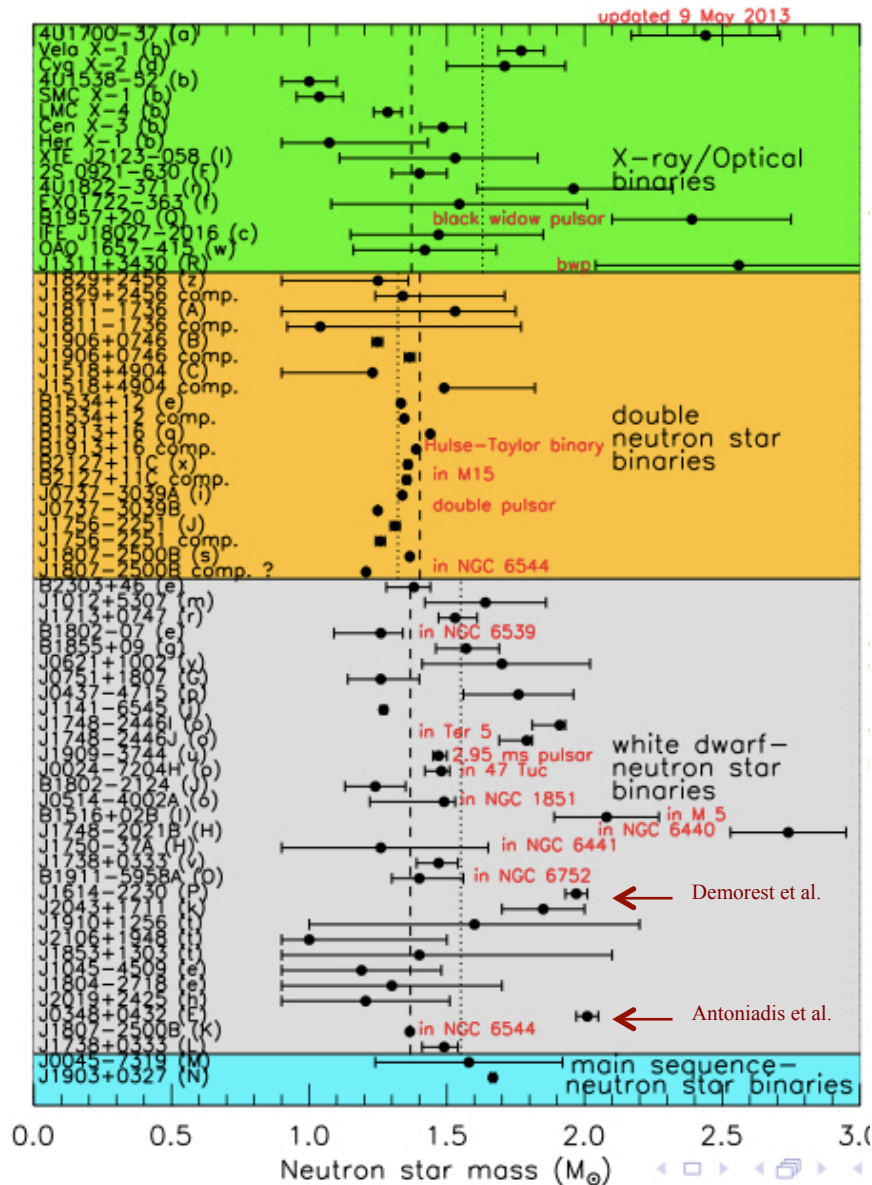


Figure by P.C.C. Freire

# Measured Neutron Star Masses (2016)



Observation of  $\sim 2 M_{\odot}$  neutron stars



Dense matter EoS stiff enough is required such that

$$M_{\max} [EoS] > 2M_{\odot}$$

A natural question arises:

Can hyperons, or strangeness in general, still be present in the interior of neutron stars in view of this constraint?

## The Hyperon Puzzle



“Hyperons → “soft (or too soft) EoS” not compatible (mainly in microscopic approaches) with measured (high) masses. However, the presence of hyperons in the NS interior seems to be unavoidable.”



- ✓ can YN & YY interactions still solve it ?
- ✓ or perhaps hyperonic three-body forces ?
- ✓ what about quark matter ?

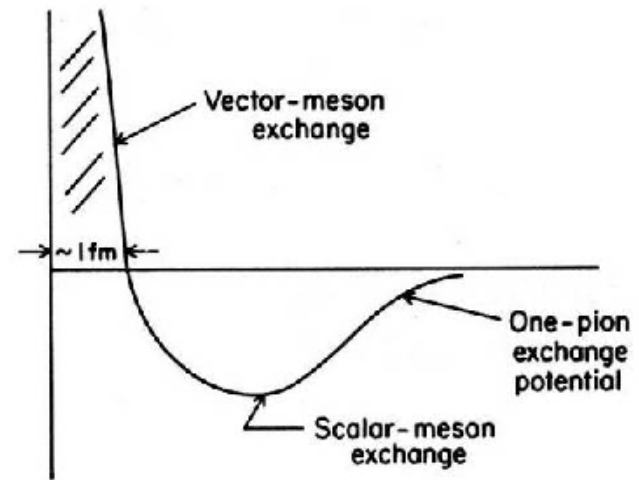


# Solution I: YY vector meson repulsion

(explored in the context of RMF models)

## General Feature:

Exchange of scalar mesons generates attraction (softening), but the exchange of vector mesons generates repulsion (stiffening)



Add vector mesons with hidden strangeness ( $\phi$ ) **coupled to hyperons** yielding a strong repulsive contribution at high densities

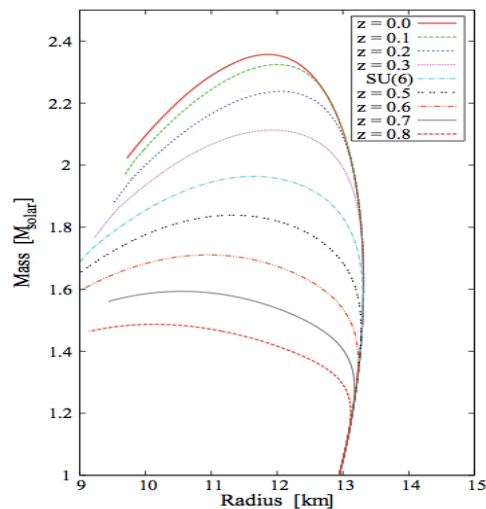


Dexhamer & Schramm (2008), Bednarek et al, (2012), Weissenborn et al., (2012)  
Oertel et al. (2014), Maslov et al. (2015)



## Weissenborn et al. (2012)

- ✓  $\sigma^2, \sigma^3, \sigma^4$  terms
- ✓  $\rho^2, \omega^2, \omega^4$  terms
- ✓ “hidden strangeness” mesons:  $\sigma^*, \phi$   
( $\sigma^{*2}, \phi^2$ )
- ✓  $g_{YV}$  couplings: from SU(6) to SU(3)  
vary  $z=g_8/g_1$  &  $\alpha=F/(F+D)$
- ✓  $g_{YS}$  couplings adjusted by fitting  $U_B^{(N)}$   
( $U_\Lambda^{(N)}=-30, U_\Sigma^{(N)}=+30, U_\Xi^{(N)}=-28$  MeV)

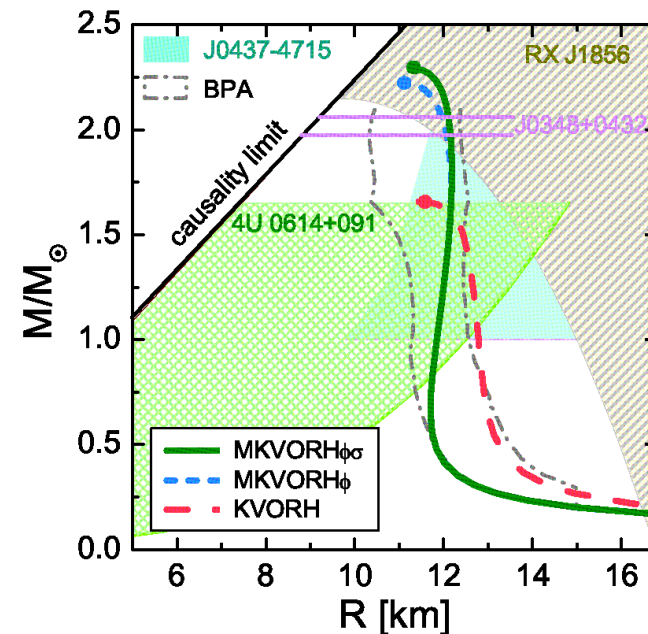


$M_{\max}$  compatible  
with  $2M_\odot$



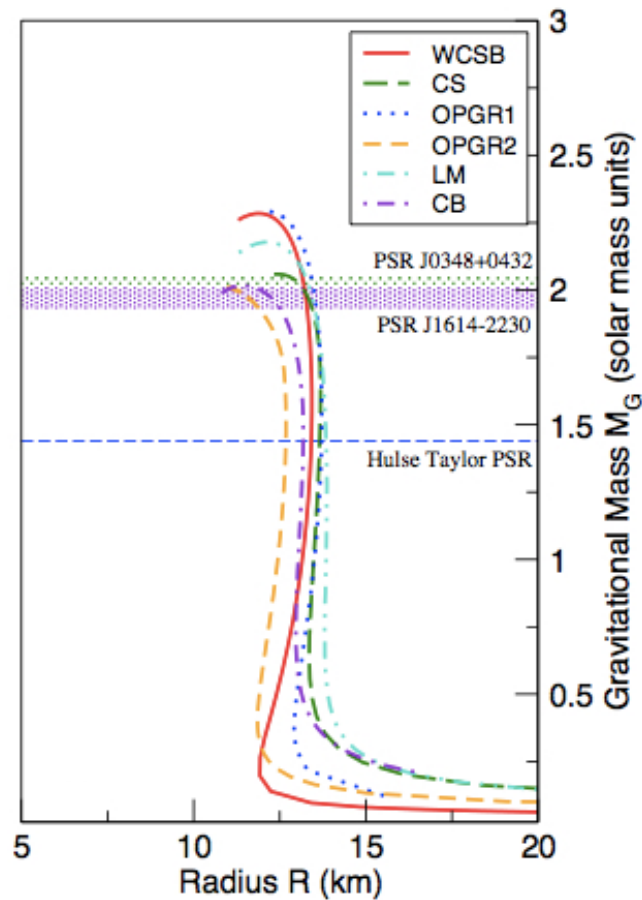
## Maslov et al. (2015)

- ✓ RMF with scaled hadron masses (universal) & coupling constants (not universal)
- ✓ Model flexible enough to satisfy constraints from HIC & astrophysical data
- ✓ Hyperon puzzle partially solved if a reduction of  $\phi$  meson mass is included





Although these and other similar models are able to reconcile the presence of hyperons in the NS interior with the existence of  $2M_{\odot}$  NS, one must be cautious !!



D. Chatterjee & I. V. (2015)

✧ These models contain several **free parameters** which most of the times are **arbitrarily chosen** being the only **justification** our still “scarce” knowledge of the YY interaction.

Hence:

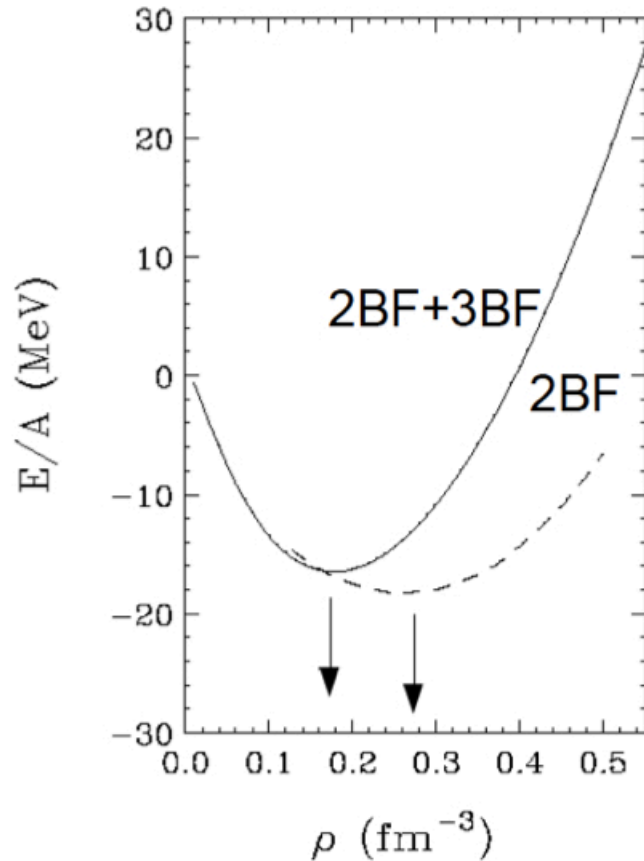
In absence of sufficient experimental data on multi-strange hypernuclei and YY scattering the validity of these models is still questionable.

# Solution II: can Hyperonic TBF solve this puzzle ?

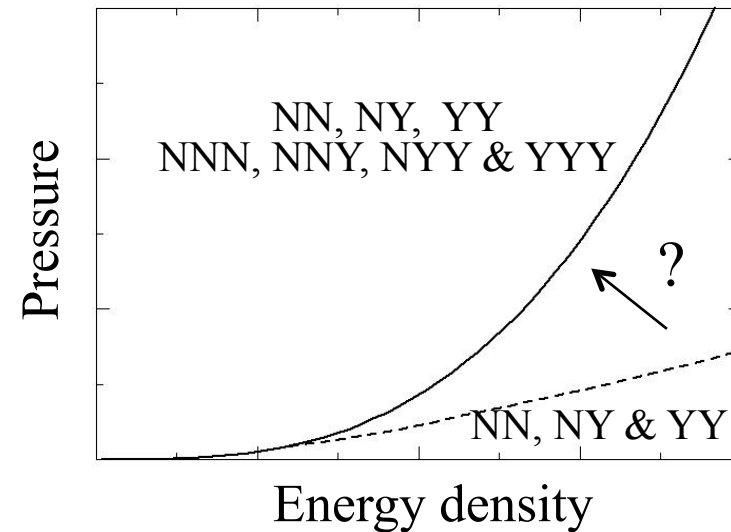
Natural solution based on: **Importance of NNN force in Nuclear Physics**

(Considered by several authors: Chalk, Gal, Usmani, Bodmer, Takatsuka, Loiseau, Nogami, Bahaduri, IV)

## NNN Force

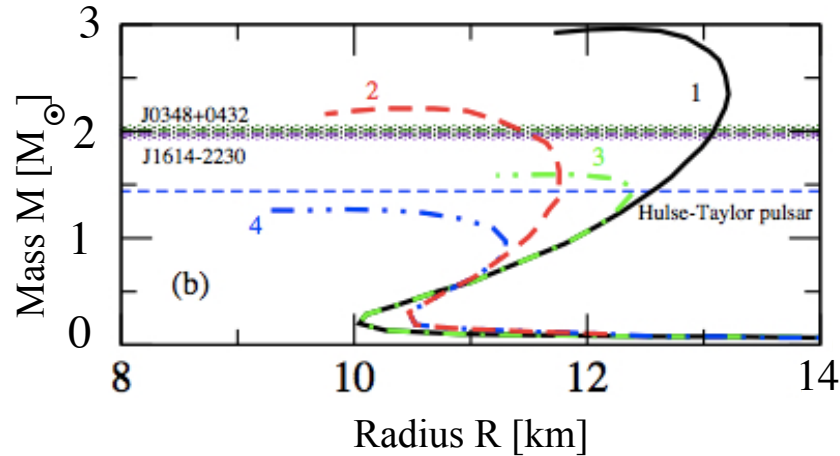


## NNY, NYN & YYY Forces



Can hyperonic TBF provide enough repulsion at high densities to reach  $2M_{\odot}$ ?

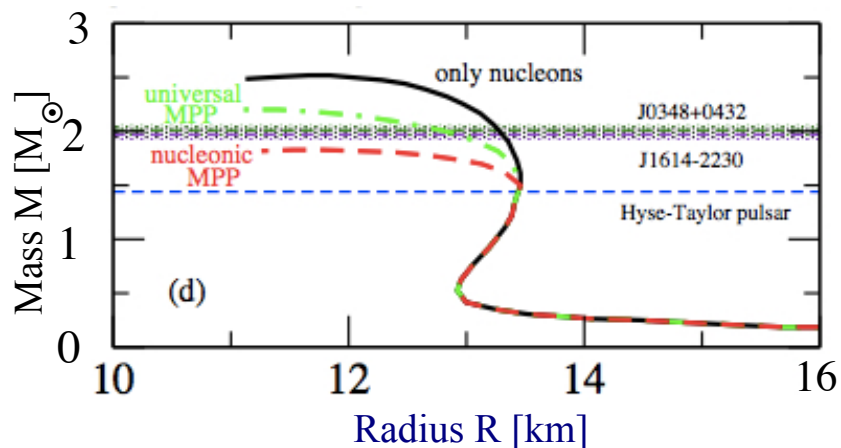
## The results are contradictory



I. V. et al. (2011)

BHF with NN+YN+phenomenological  
YTBF. Different strength of YTBF  
including the case of universal TBF

$$1.27 < M_{\max} < 1.6 M_{\odot}$$

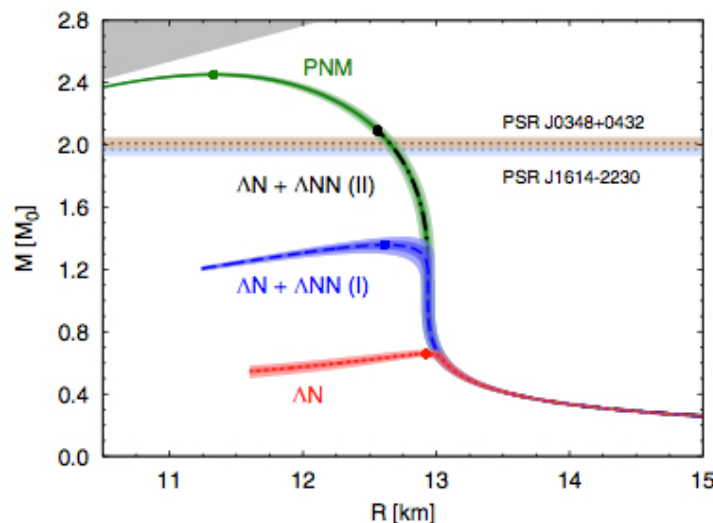
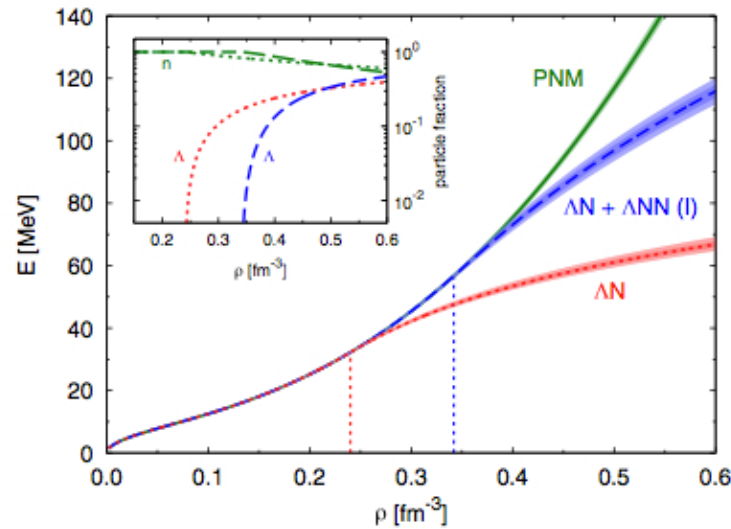


Yamamoto et al. (2015)

BHF with NN+YN+universal  
repulsive TBF (multipomeron  
exchange mechanism)

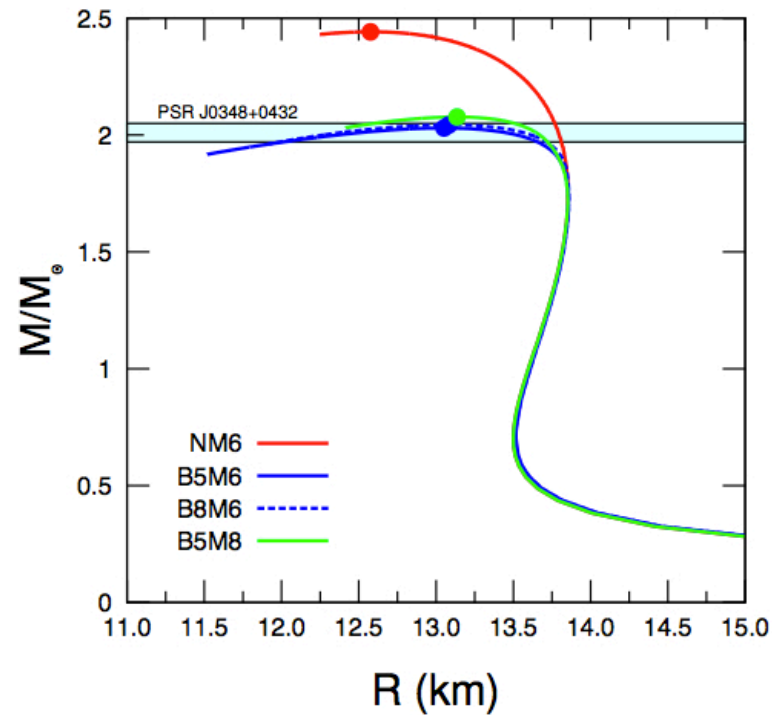
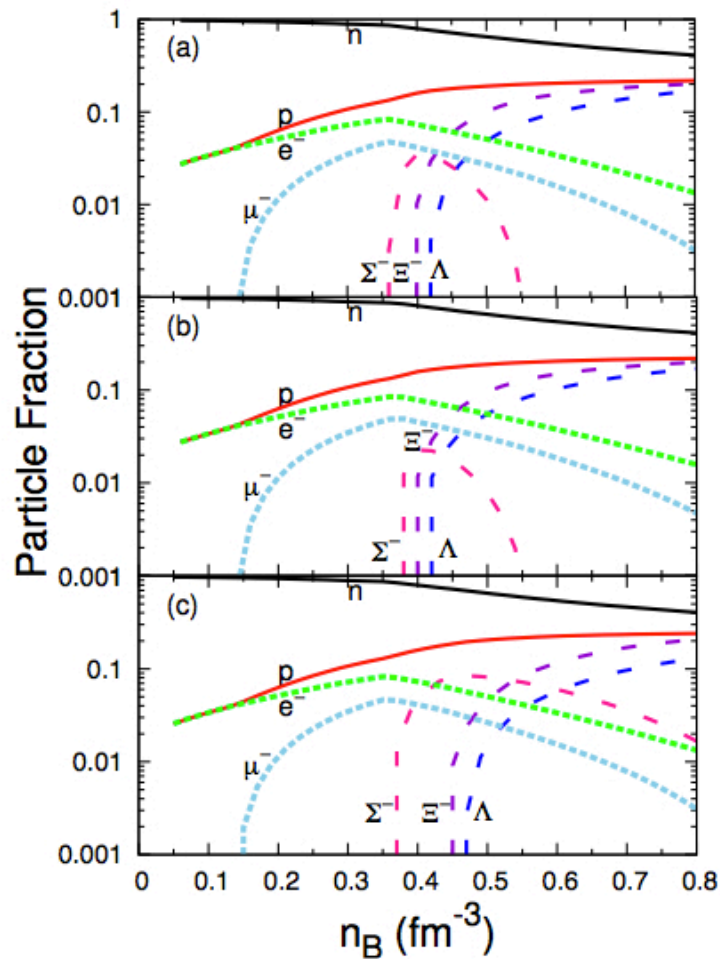
$$M_{\max} > 2 M_{\odot}$$

It should be mentioned also the recent **Quantum Monte Carlo** calculation by **Lonardonì et al. (2015)**



- ❖ First **Quantum Monte Carlo** calculation on **neutron+ $\Lambda$**  matter
- ❖ Strong dependence of  $\Lambda$  onset on  **$\Delta_{nn}$**  force
- ❖ Some of the parametrizations of the  **$\Delta_{nn}$**  force give maximum masses compatible with  $2M_{\odot}$  but the onset of  $\Lambda$  is above the maximum density considered ( $\sim 0.56 \text{ fm}^{-3}$ ). So in fact, **no  $\Lambda$ s** are present in NS interior

and the recent DBHF calculation of hyperonic matter by Katayama & Saito (2014)



- DBHF includes some TBF effects in a natural way
- $M_{\text{max}}$  compatible with  $2M_\odot$
- But the construction of YN is a bit obscure in this work

# Take Away Message



- ✧ It is still an open question whether hyperonic TBFs can, by themselves, solve completely the hyperon puzzle or not.
- ✧ It seems, however, that even if they are not the full solution, most probably they can contribute to it in an important way.



## Solution III: Quark Matter Core

### General Feature:

Some authors have suggested an early phase transition to deconfined quark matter as solution to the hyperon puzzle. Massive neutron stars could actually be hybrid stars with a stiff quark matter core.

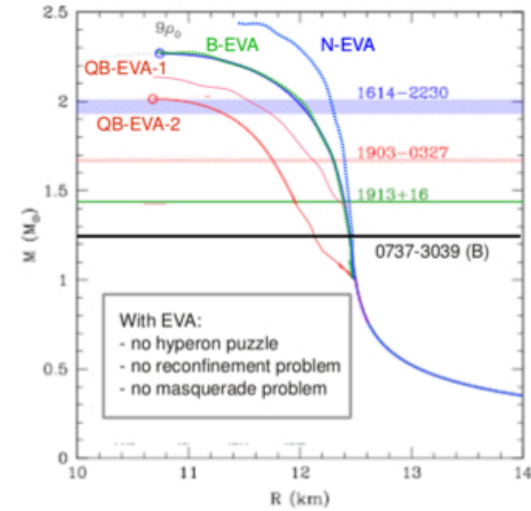
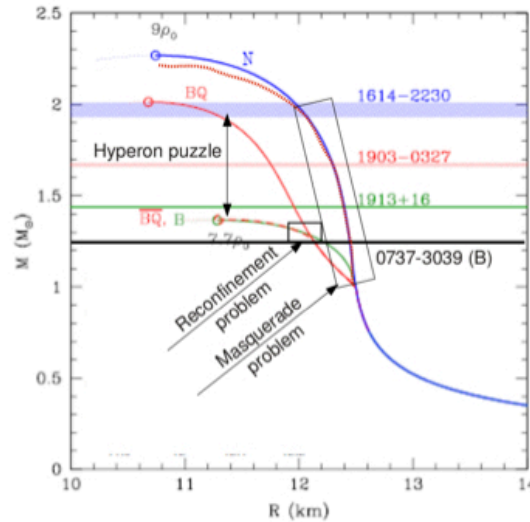
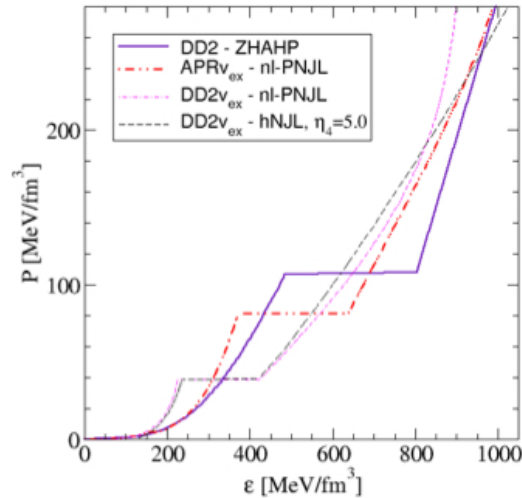
To yield  $M_{\max} > 2M_{\odot}$  Quark Matter should have:

- significant overall quark repulsion  $\longrightarrow$  stiff EoS
- strong attraction in a channel  $\longrightarrow$  strong color superconductivity



Ozel et al., (2010), Weissenborn et al., (2011), Klaehn et al., (2011), Bonano & Sedrakian (2012), Lastowiecki et al., (2012), Zdunik & Haensel (2012)

## A recent work by D. Blaschke & D. Alvarez-Castillo (2015)



Compositeness of baryons (by excluded volume and/or quark Pauli blocking) on the hadronic side + **confinement** and **stiffening effects** on the quark matter:



Earlier phase transition to QM with sufficient **stiffening at high densities** to solve: hyperon puzzle, masquerade problem & reconfinement puzzle

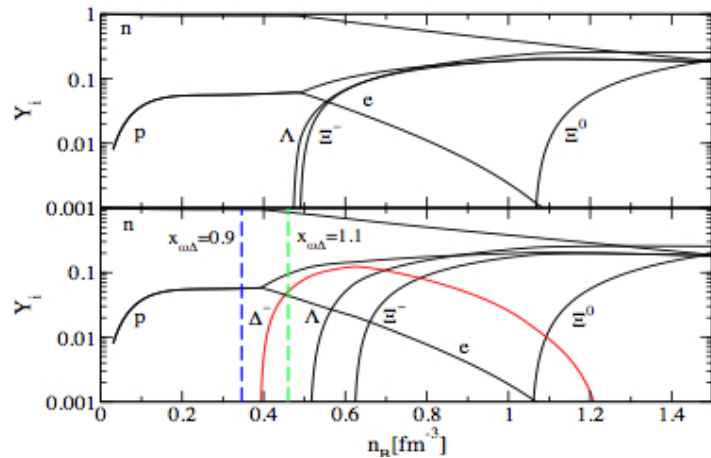
But also in this case we must pay attention



Currently theoretical descriptions of quark matter at high density rely on phenomenological models which are constrained using the few available experimental information on high density baryonic matter from heavy-ion collisions.

# Is there also a $\Delta$ isobar puzzle ?

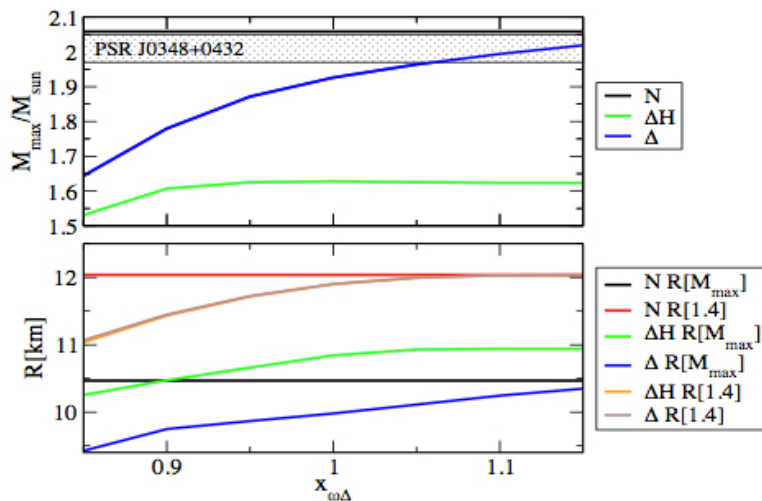
The recent work by Drago et al. (2014) calculation have studied the role of the  $\Delta$  isobar in neutron star matter



❖ Constraints from L indicate an early appearance of  $\Delta$  isobars in neutron stars matter at  $\sim 2-3 \rho_0$  (same range as hyperons)

❖ Appearance of  $\Delta$  isobars modify the composition & structure of hadronic stars

❖  $M_{\max}$  is dramatically affected by the presence of  $\Delta$  isobars



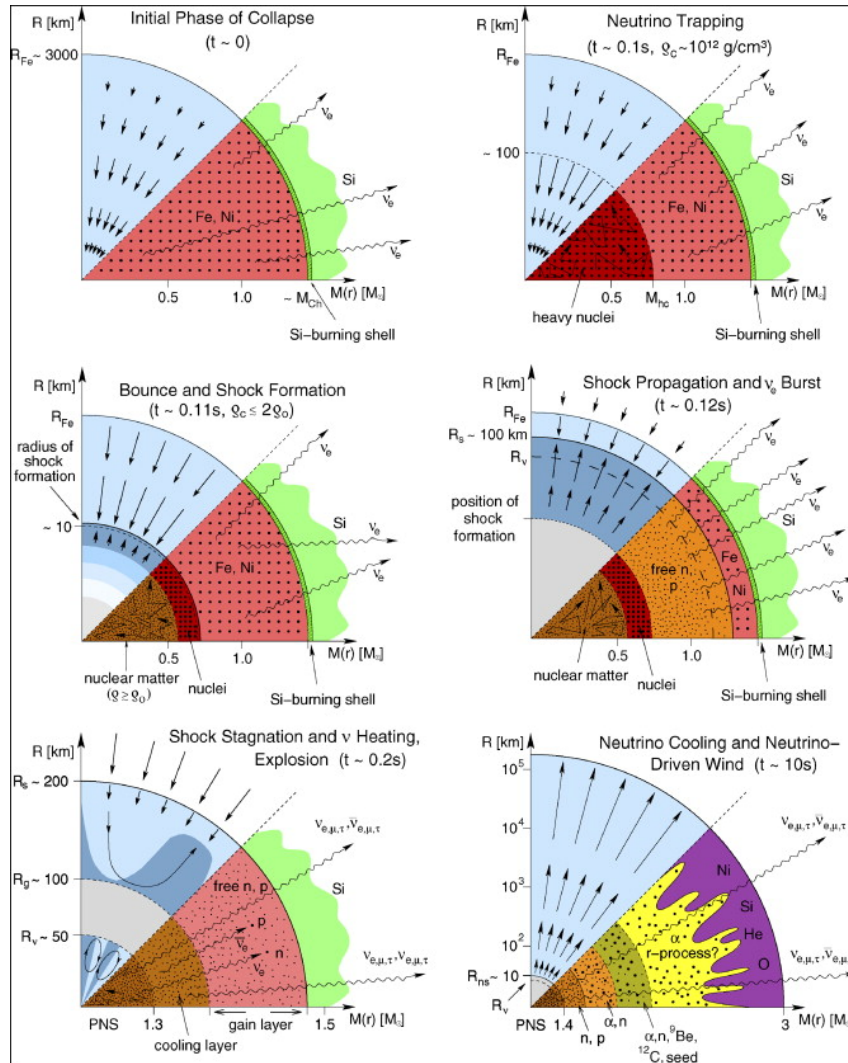
If  $\Delta$  potential is close to that indicated by  $\pi^-$ , e-nucleus or photoabsorption nuclear reactions then EoS is too soft  $\rightarrow$   $\Delta$  puzzle similar to the hyperon one



# Hyperon Stars at Birth

*David Lloyd Glover*

# Proto-Neutron Stars



New effects on PNS matter:

- Thermal effects

$$T \approx 30 - 40 \text{ MeV}$$

$$S / A \approx 1 - 2$$

- Neutrino trapping

$$\mu_\nu \neq 0$$

$$Y_e = \frac{\rho_e + \rho_{\nu_e}}{\rho_B} \approx 0.4$$

$$Y_\mu = \frac{\rho_\mu + \rho_{\nu_\mu}}{\rho_B} \approx 0$$

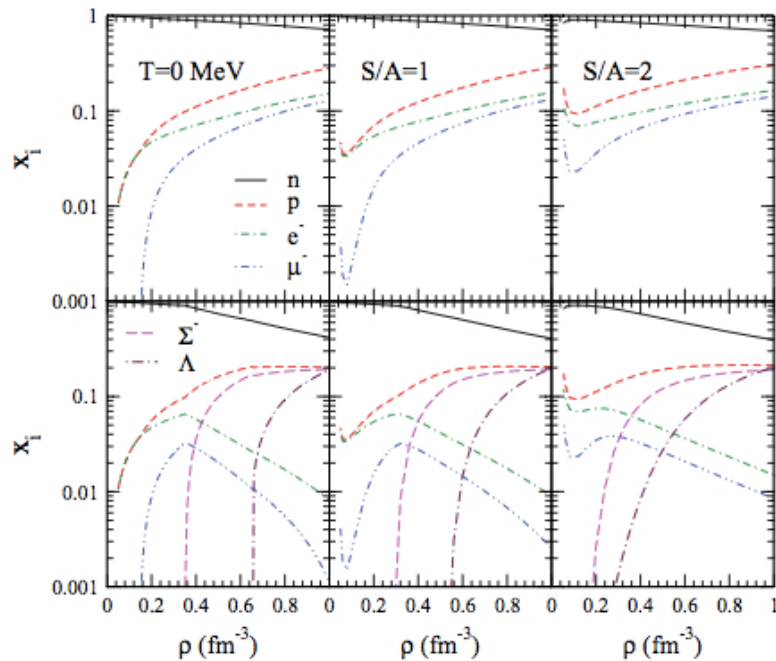
(Janka, Langanke, Marek, Martinez-Pinedo & Muller 2006)

# Proto-Neutron Stars: Composition

- Neutrino free

$$\mu_\nu = 0$$

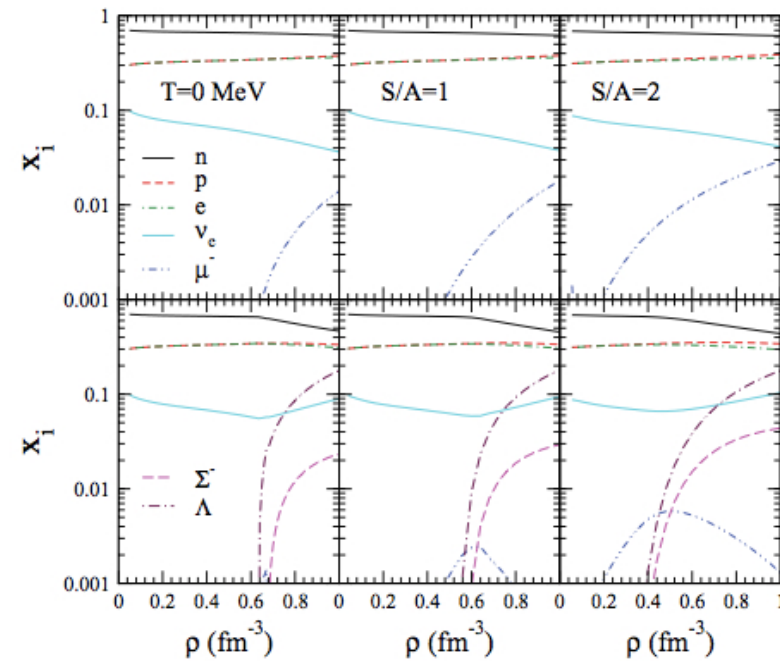
(Burgio & Schulze 2011)



- Neutrino trapped

$$\mu_\nu \neq 0$$

(Burgio & Schulze 2011)



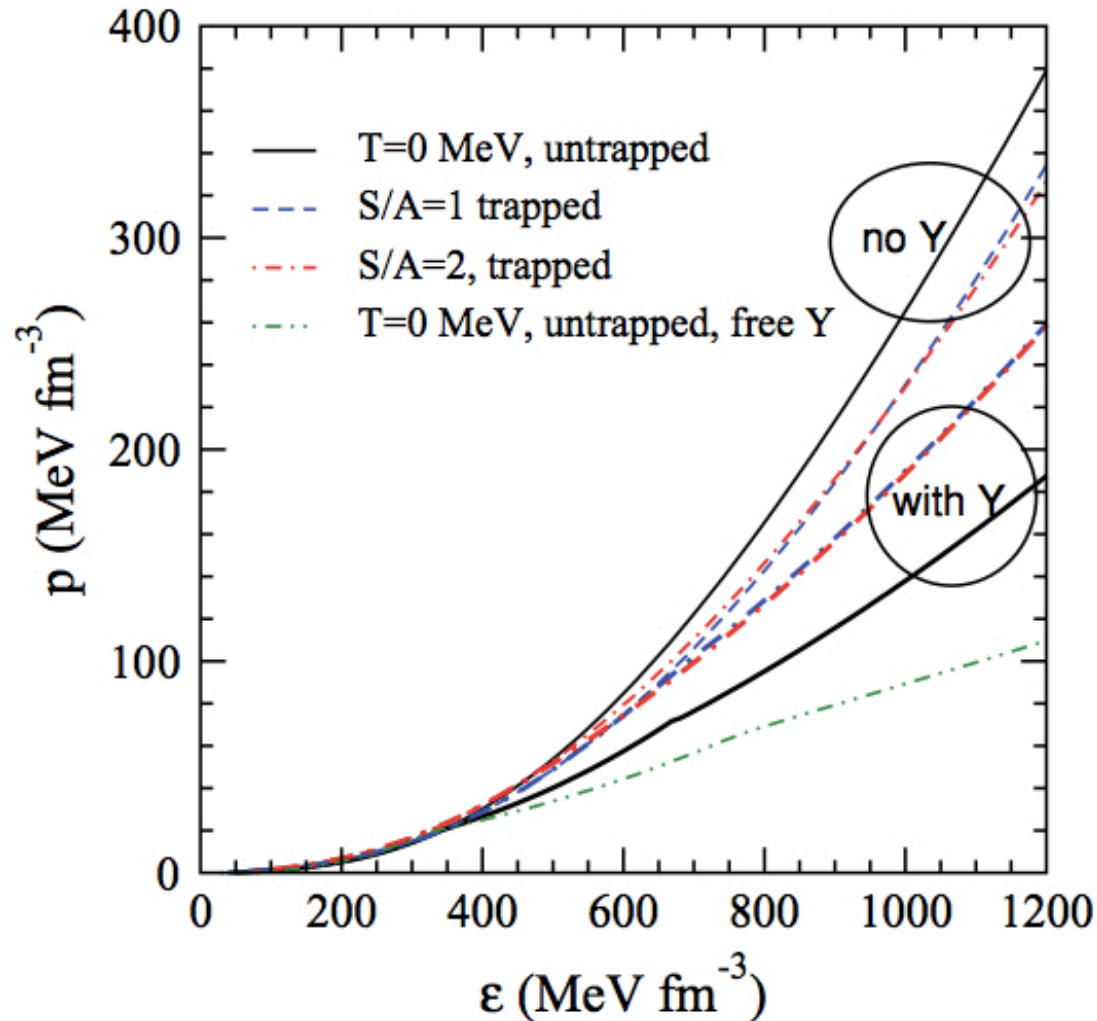
Neutrino trapped



- ✓ Large proton fraction
- ✓ Small number of muons
- ✓ Onset of  $\Sigma^-(\Lambda)$  shifted to higher (lower) density
- ✓ Hyperon fraction lower in  $\nu$ -trapped matter

# Proto-Neutron Stars: EoS

(Burgio & Schulze 2011)



## ■ Nucleonic matter

- ◇  $\nu$ -trapping + temperature  
→ softer EoS

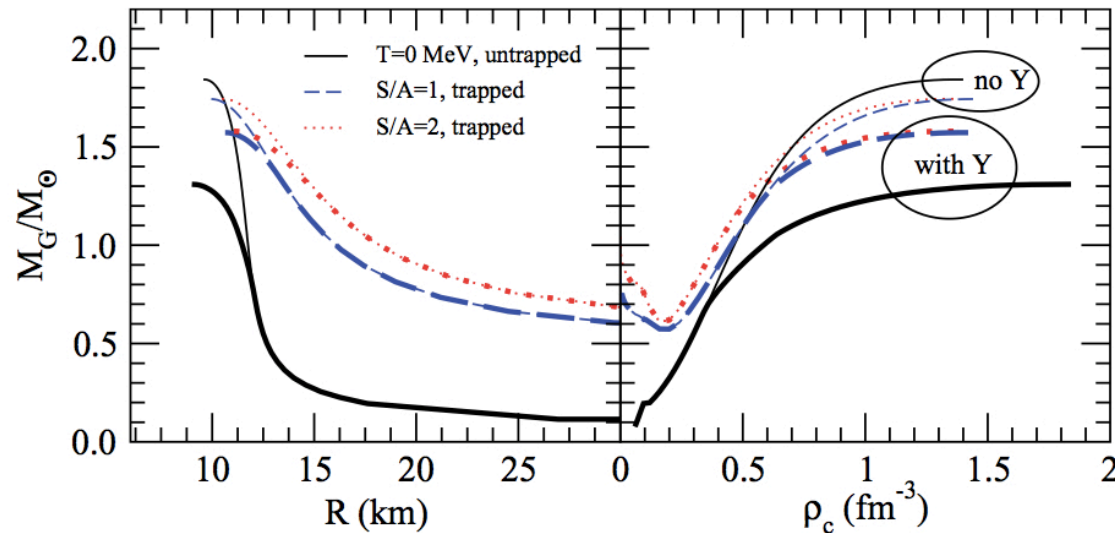
## ■ Hyperonic matter

- ◇  $\nu$ -trapping + temperature  
→ stiffer EoS
- ◇ More hyperon softening  
in  $\nu$ -untrapped matter  
(larger hyperon fraction)



# Proto-Neutron Stars: Structure

(Burgio & Schulze 2011)



## Hyperonic matter

$\nu$ -trapping + T:  
increase of  $M_{\text{max}}$

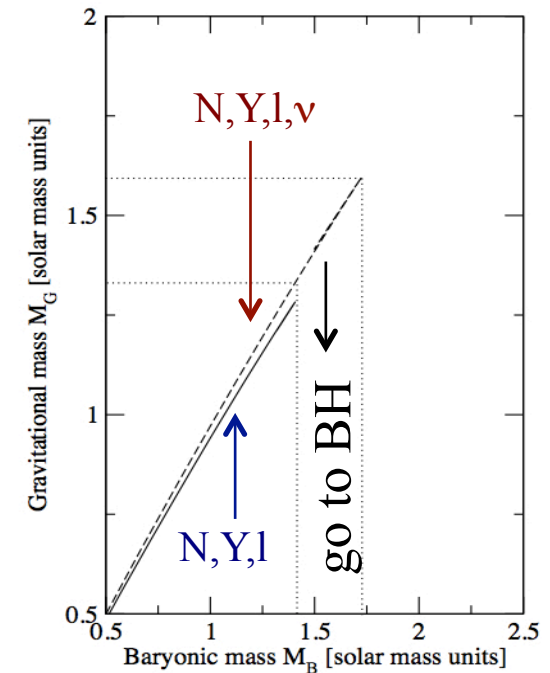


delayed formation  
of a low mass BH

## Nucleonic matter

$\nu$ -trapping + T:  
reduction of  $M_{\text{max}}$

(IV et al. 2003)





# Hyperons & Neutron Star Cooling

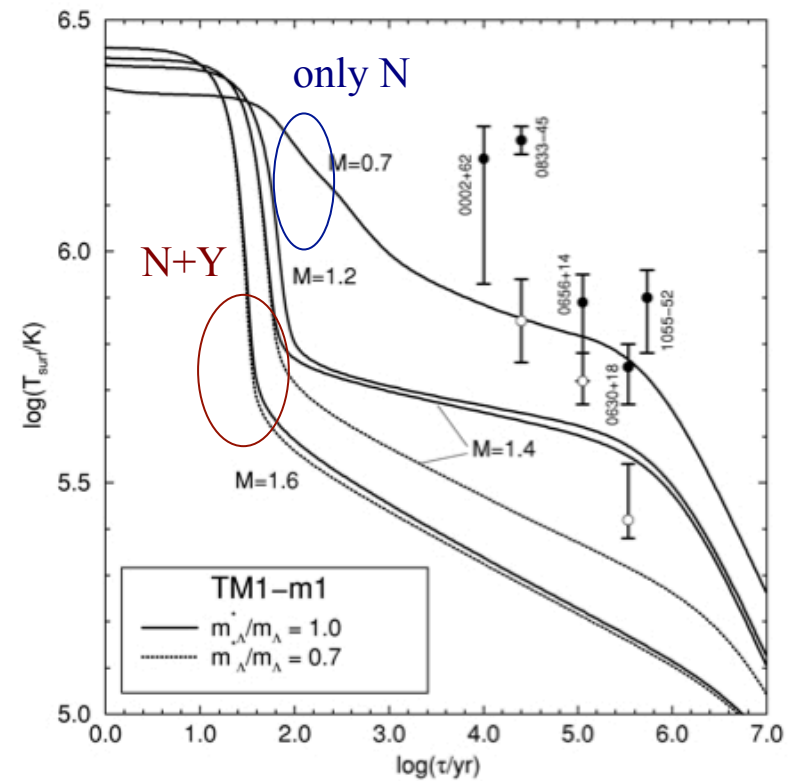
Hyperonic DURCA processes possible  
 as soon as hyperons appear  
 (nucleonic DURCA requires  $x_p > 11-15\%$ )

➔ Additional  
 Fast Cooling  
 Processes

Process	R
$\Lambda \rightarrow p + l + \bar{\nu}_l$	0.0394
$\Sigma^- \rightarrow n + l + \bar{\nu}_l$	0.0125
$\Sigma^- \rightarrow \Lambda + l + \bar{\nu}_l$	0.2055
$\Sigma^- \rightarrow \Sigma^0 + l + \bar{\nu}_l$	0.6052
$\Xi^- \rightarrow \Lambda + l + \bar{\nu}_l$	0.0175
$\Xi^- \rightarrow \Sigma^0 + l + \bar{\nu}_l$	0.0282
$\Xi^0 \rightarrow \Sigma^+ + l + \bar{\nu}_l$	0.0564
$\Xi^- \rightarrow \Xi^0 + l + \bar{\nu}_l$	0.2218

+ partner reactions generating neutrinos,  
 Hyperonic MURCA, ...

(Schaab, Shaffner-Bielich & Balberg 1998)

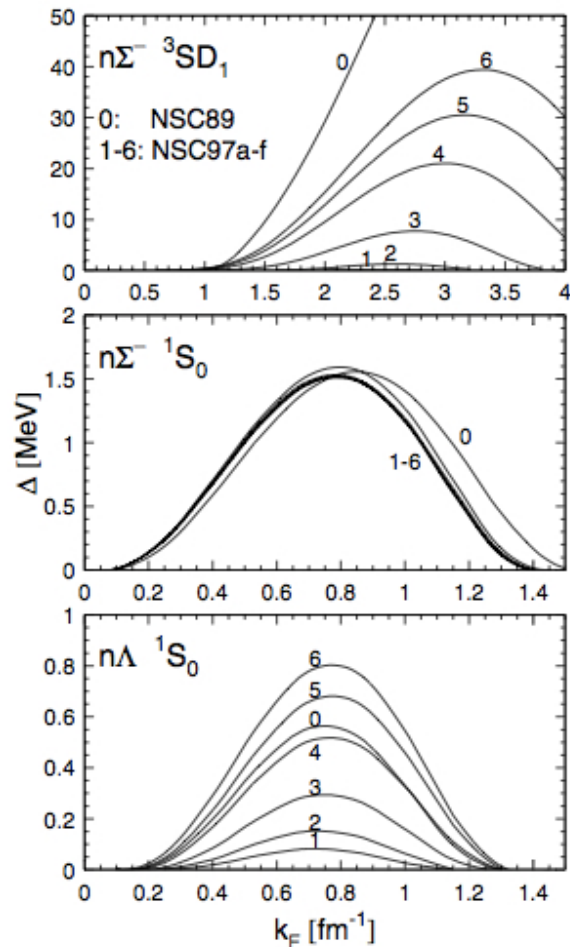


R: relative emissivity w.r.t. nucleonic DURCA

Pairing Gap  $\longrightarrow$  suppression of  $C_v$  &  $\epsilon$  by

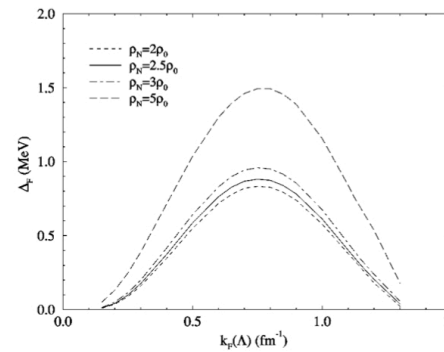
$$\sim e^{(-\Delta/k_B T)}$$

■  $^1S_0$ ,  $^3SD_1$   $\Sigma N$  &  $^1S_0$   $\Lambda N$  gap

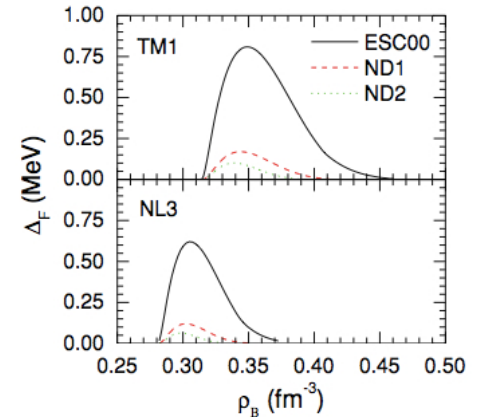


(Zhou, Schulze, Pan & Draayer 2005)

■  $^1S_0$   $\Lambda\Lambda$  gap

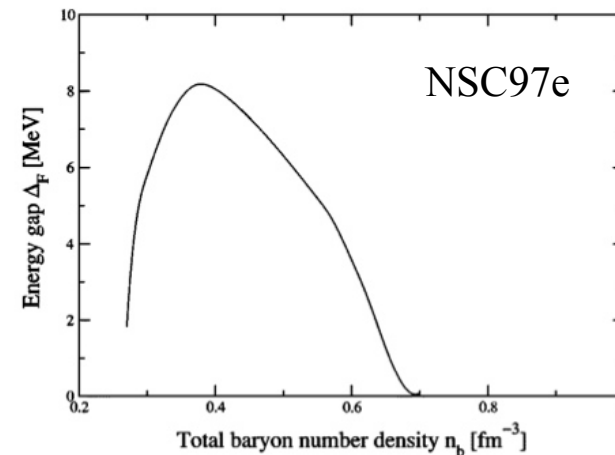


(Balberg & Barnea 1998)



(Wang & Shen 2010)

■  $^1S_0$   $\Sigma\Sigma$  gap



(IV & Tolós 2004)

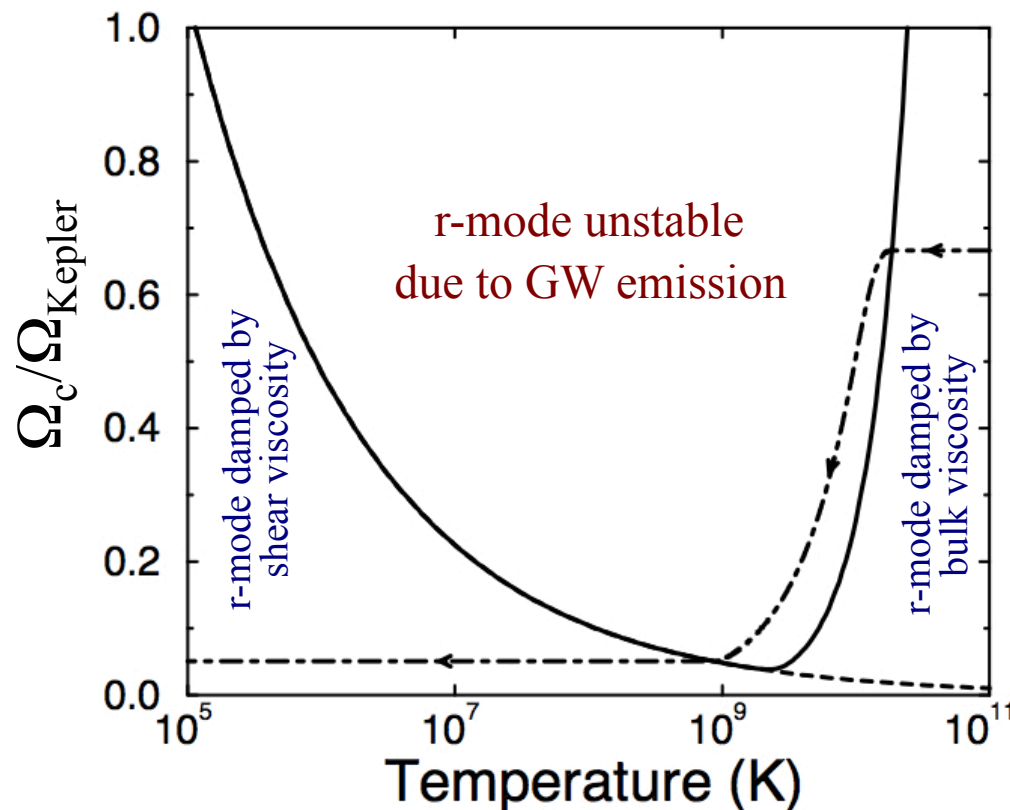
The background of the slide is a reproduction of the famous Japanese woodblock print 'The Great Wave off Kanagawa' by Katsushika Hokusai. It depicts a massive, curling blue wave with white foam, threatening three small boats on the sea. In the distance, the snow-capped Mount Fuji is visible under a pale, hazy sky. The overall color palette is muted, with soft blues, greys, and a pale yellowish-green background.

# **Hyperons & the R-mode instability of Neutron Stars**

# The r-mode Instability

$\Omega_{\text{Kepler}}$  : Absolute Upper Limit  
of Rot. Freq.

Instabilities prevent NS  
to reach  $\Omega_{\text{Kepler}}$



r-mode Instability : toroidal mode  
of oscillation

- ✓ restoring force: Coriolis
- ✓ emission of GW in hot & rapidly rotating NS (CFS mechanism)
  - GW makes the mode unstable
  - Viscosity stabilizes the mode

$$A \propto A_0 e^{-i\omega(\Omega)t - t/\tau(\Omega, T)}$$

$$\frac{1}{\tau(\Omega, T)} = -\frac{1}{\tau_{\text{GW}}(\Omega)} + \frac{1}{\tau_{\text{Viscosity}}(\Omega, T)}$$

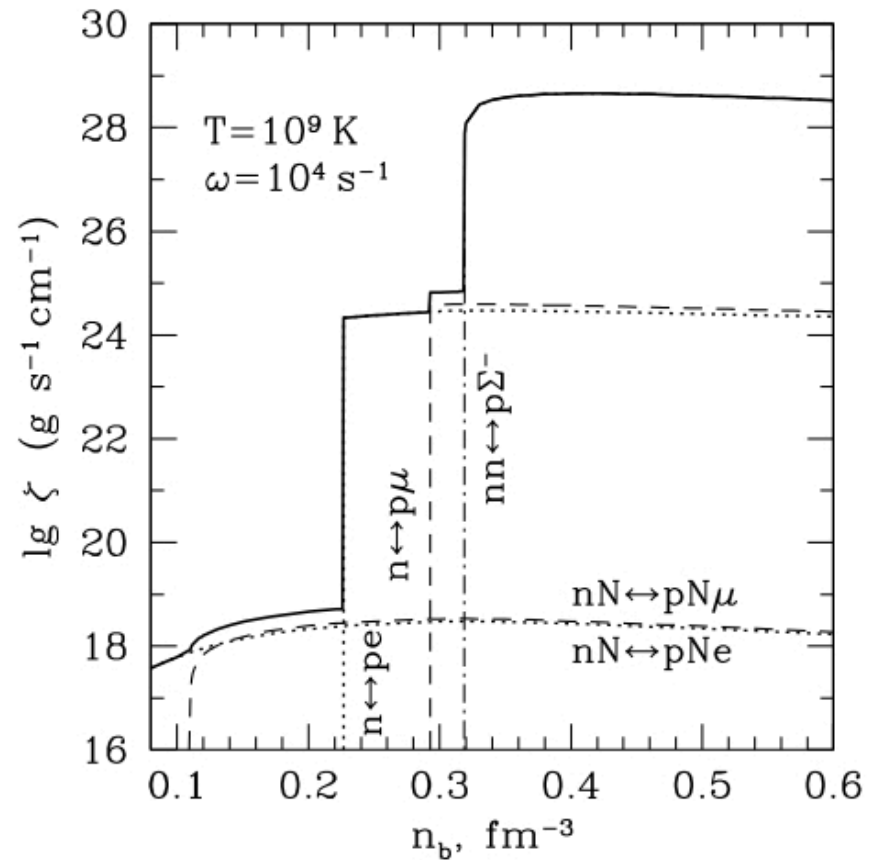
# Hyperon Bulk Viscosity $\xi_Y$

(Lindblom et al. 2002, Haensel et al 2002, van Dalen et al. 2002, Chatterjee et al. 2008, Gusakov et al. 2008, Shina et al. 2009, Jha et al. 2010,...)

## Sources of $\xi_Y$ :

non-leptonic weak reactions	$N + N \leftrightarrow N + Y$ $N + Y \leftrightarrow Y + Y$
Direct & Modified URCA	$Y \rightarrow B + l + \bar{\nu}_l$ $B' + Y \rightarrow B' + B + l + \bar{\nu}_l$
strong reactions	$N + Y \leftrightarrow N + Y$ $N + \Xi \leftrightarrow Y + Y$ $Y + Y \leftrightarrow Y + Y$

(Haensel, Levenfish & Yakovlev 2002)



Reaction Rates &  $\xi_Y$  reduced by  
Hyperon Superfluidity

# Critical Angular Velocity of Neutron Stars

- r-mode amplitude:  $A \propto A_o e^{-i\omega(\Omega)t - t/\tau(\Omega)}$

$$\frac{1}{\tau(\Omega, T)} = -\frac{1}{\tau_{GW}(\Omega)} + \frac{1}{\tau_{\xi}(\Omega, T)} + \frac{1}{\tau_{\eta}(T)}$$

→  $\frac{1}{\tau(\Omega_c, T)} = 0$  r-mode instability region

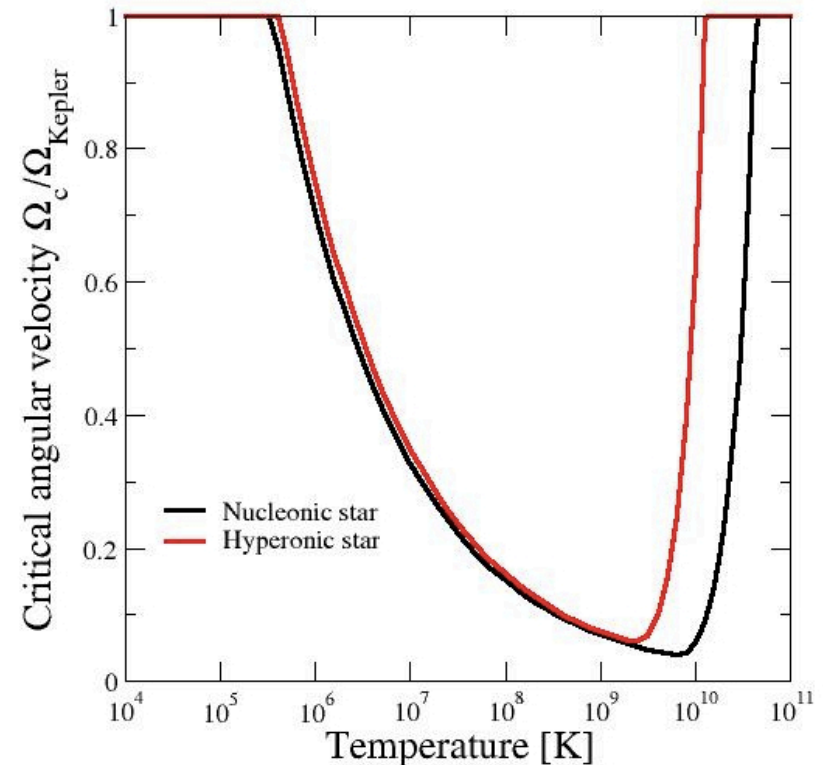
$$\Omega < \Omega_c \quad \text{stable}$$

$$\Omega > \Omega_c \quad \text{unstable}$$



As expected:  
smaller r-mode instability region  
due to hyperons

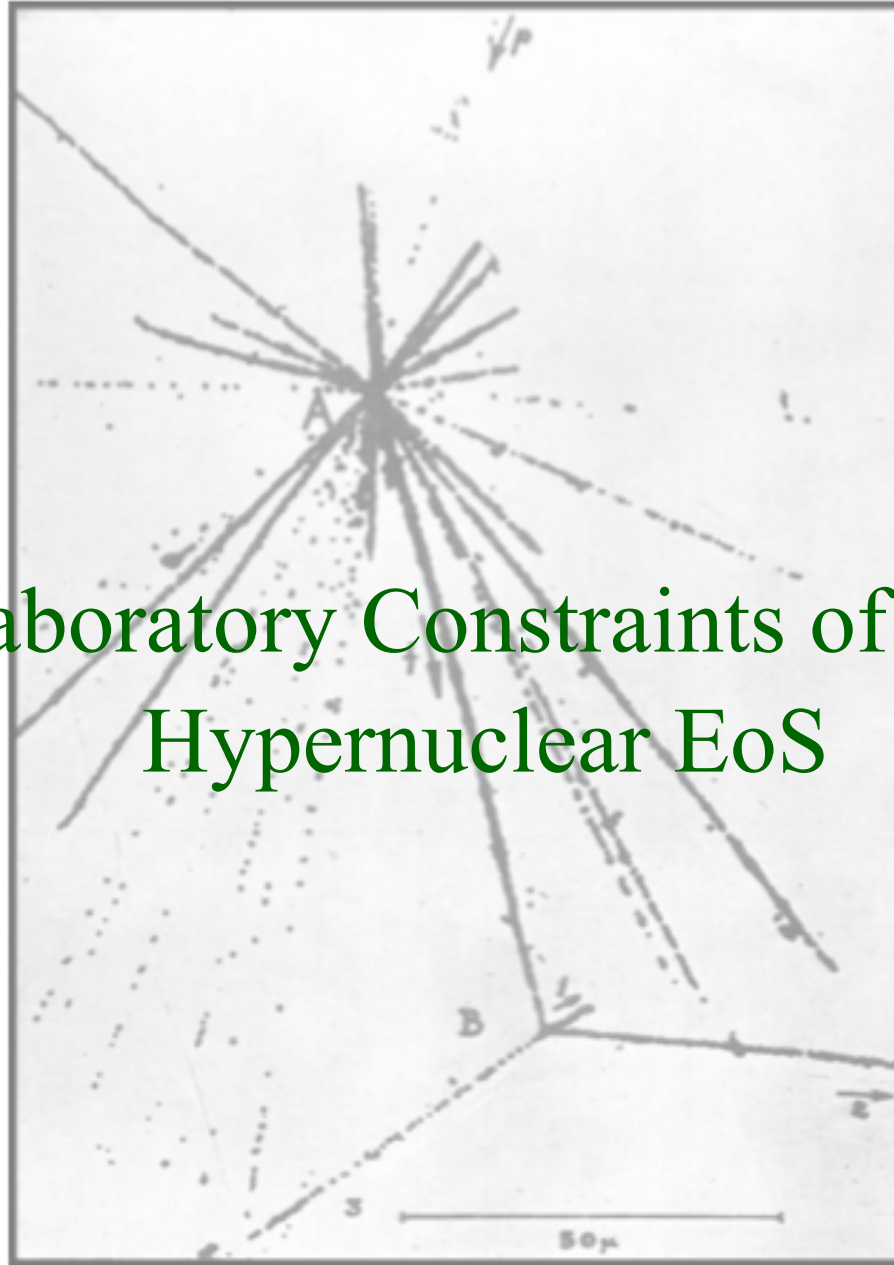
(I.V. & C. Albertus in preparation)



BHF: NN (Av18)+NY (NSC89)  
( $M=1.27M_{\odot}$ )

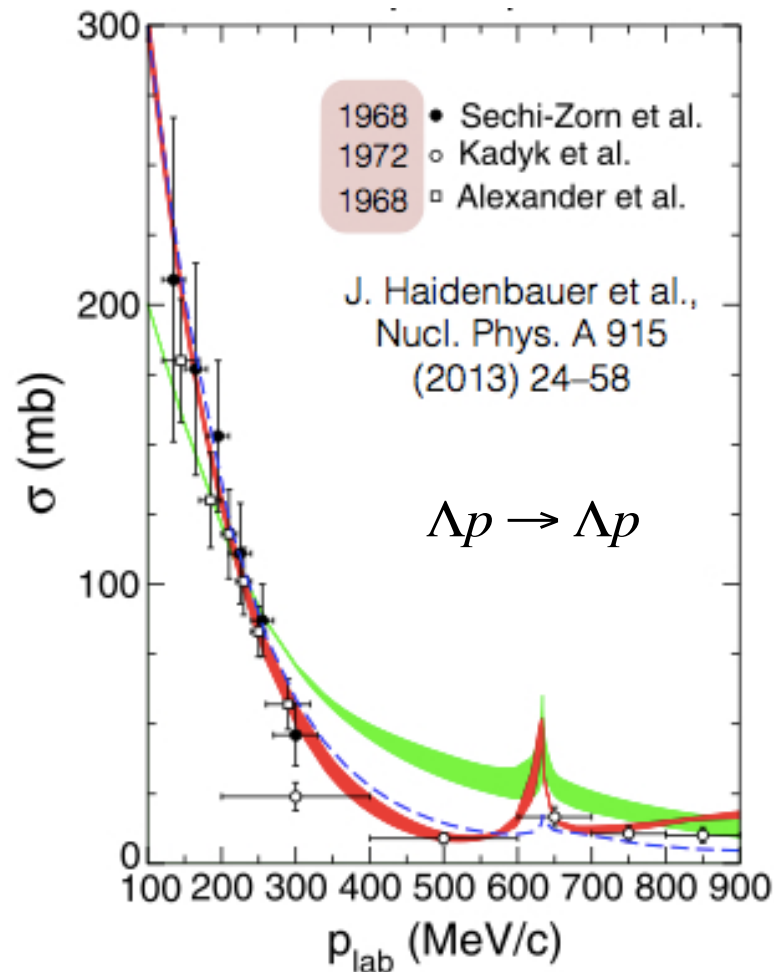


# Laboratory Constraints of the Hypernuclear EoS



# What do we know to include hyperons in the EoS ?

Unfortunately, much less than in the pure nucleonic sector to put stringent constraints on the YN & YY interactions

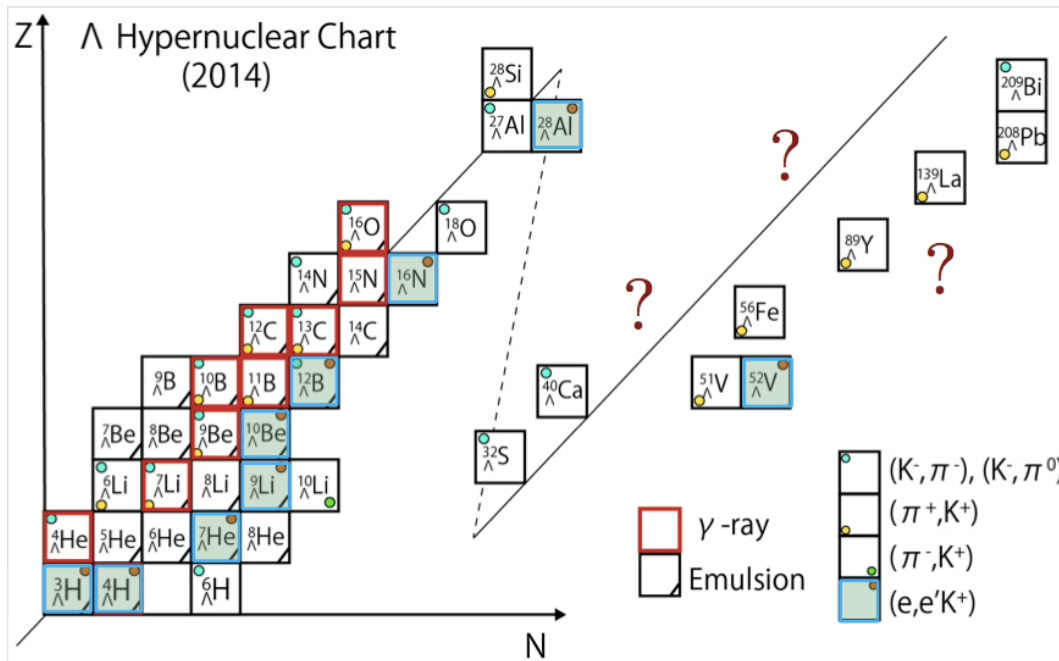


- Very few YN scattering data due to short lifetime of hyperons & low intensity beam fluxes
  - ~35 data points, all from the 1960s
  - 10 new data points, from KEK-PS E251 collaboration (2000)
- No YY scattering data exists

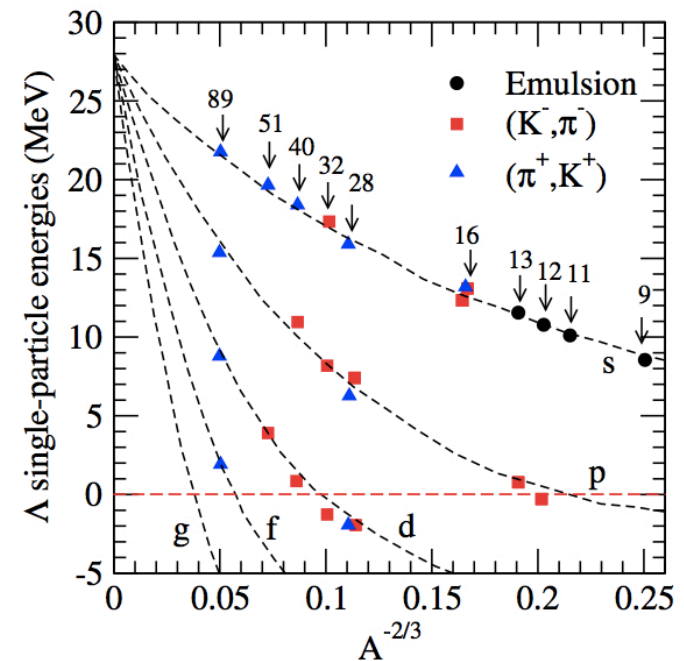
(cf. > 4000 NN data for  $E_{\text{lab}} < 350$  MeV)

➤ Alternative information can be obtained from hypernuclei

- 41 single  $\Lambda$ -hypernuclei  $\rightarrow$   $\Lambda N$  attractive ( $U_{\Lambda}(\rho_0) \sim -30$  MeV)
- 3 double- $\Lambda$  hypernuclei  $\rightarrow$  weak  $\Lambda\Lambda$  attraction ( $\Delta B_{\Lambda\Lambda} \sim 1$  MeV)
- Very few  $\Xi$ -hypernuclei  $\rightarrow$   $\Xi N$  attractive ( $U_{\Xi}(\rho_0) \sim -14$  MeV)
- Ambiguous evidence of  $\Sigma$ -hypernuclei  $\rightarrow$   $\Sigma N$  repulsive ( $U_{\Sigma}(\rho_0) > +15$  MeV) ?



S. N. Nakamura, Hypernuclear Workshop, Jlab 2014, updated from:  
O. Hashimoto and H. Tamura, Prog. Part. Nucl. Phys. 57, 564 (2006)

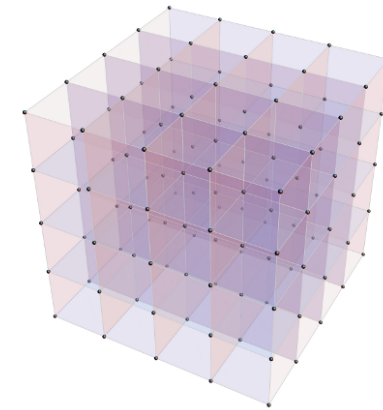


D. Chatterjee & I. V. (2015)

## But there are some problems

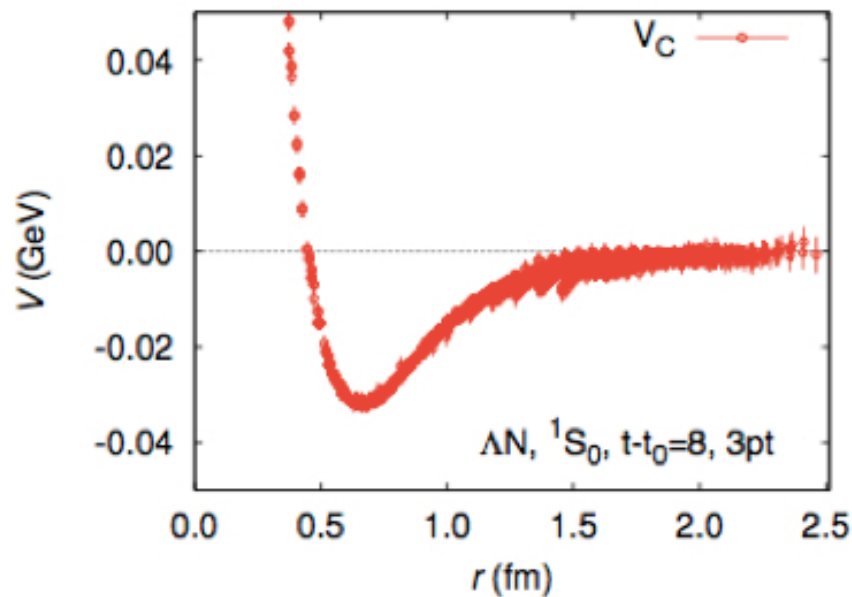
- ✧ Limited amount of scattering data not enough to fully constrain the bare YN & YY interactions → **Strategy:** start from a **NN model & impose  $SU(3)_f$  constraints** to build YN & YY (e.g., Juelich & Nijmegen models)
- ✧ Bare YN & YY is not easy to derive from hypernuclei. Hyperons in nuclei are not free but **in-medium**. Hypernuclei provide **effective hyperon-nucleus interactions**
- ✧ Amount of experimental data on hypernuclei is not enough to constrain the uncertainties of phenomenological models. Parameters are most of the times **arbitrarily chosen**
- ✧ Ab-initio hypernuclear structure calculations with bare YN & YY interactions exists but are less accurate than phenomenological ones due to the **difficulties to solve the very complicated nuclear many-body problem**

# Lattice QCD

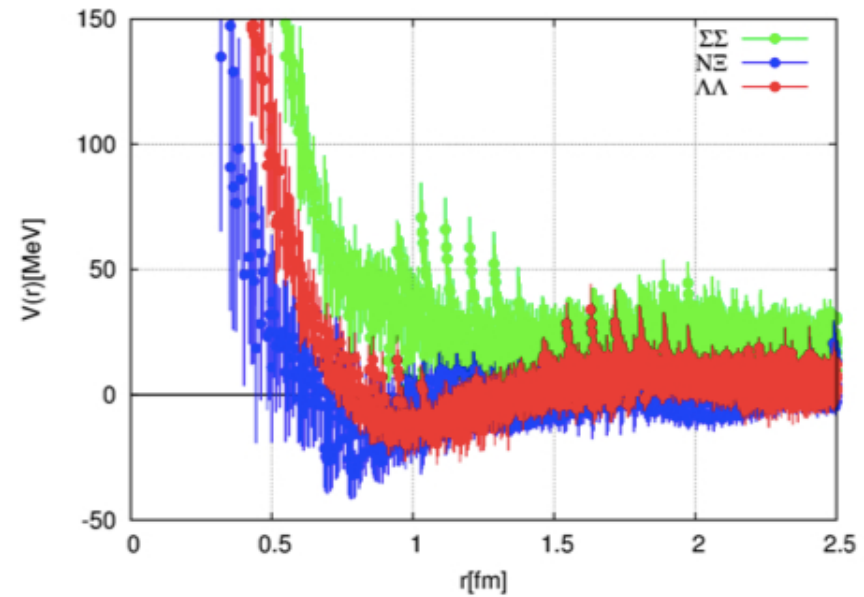


Lattice QCD calculations can provide the much required YN, YY & hyperonic TBFs.

$\Lambda N$  ( $I=0$ )  $^1S_0$  ( $m_\pi=570$  MeV)



$\Lambda\Lambda$ ,  $N\Xi$  &  $\Sigma\Sigma$  ( $I=0$ )  $^1S_0$  ( $m_\pi=145$  MeV)



# Shopping List



We need:

- ✧ More & updated hypernuclear data (FAIR, JLAB, J-PARC)
- ✧ Measurements of multi-strange hypernuclei (FAIR)
- ✧ Study of light hypernuclei (role of hyperonic TBFs)
- ✧ More YN and (hopefully) YY scattering data
- ✧ Lattice QCD calculations
- ✧ Analysis of hyperon-hyperon correlations in HIC
- ✧ Astronomical data sensitive to the strangeness content of NS

- You for your time & attention
- The organizers for their invitation

