

# **Stability of V&SHE: fission barrier measurements**

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PRL 113, 262505 and beyond...

# Fission



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Division or splitting into two or more parts.



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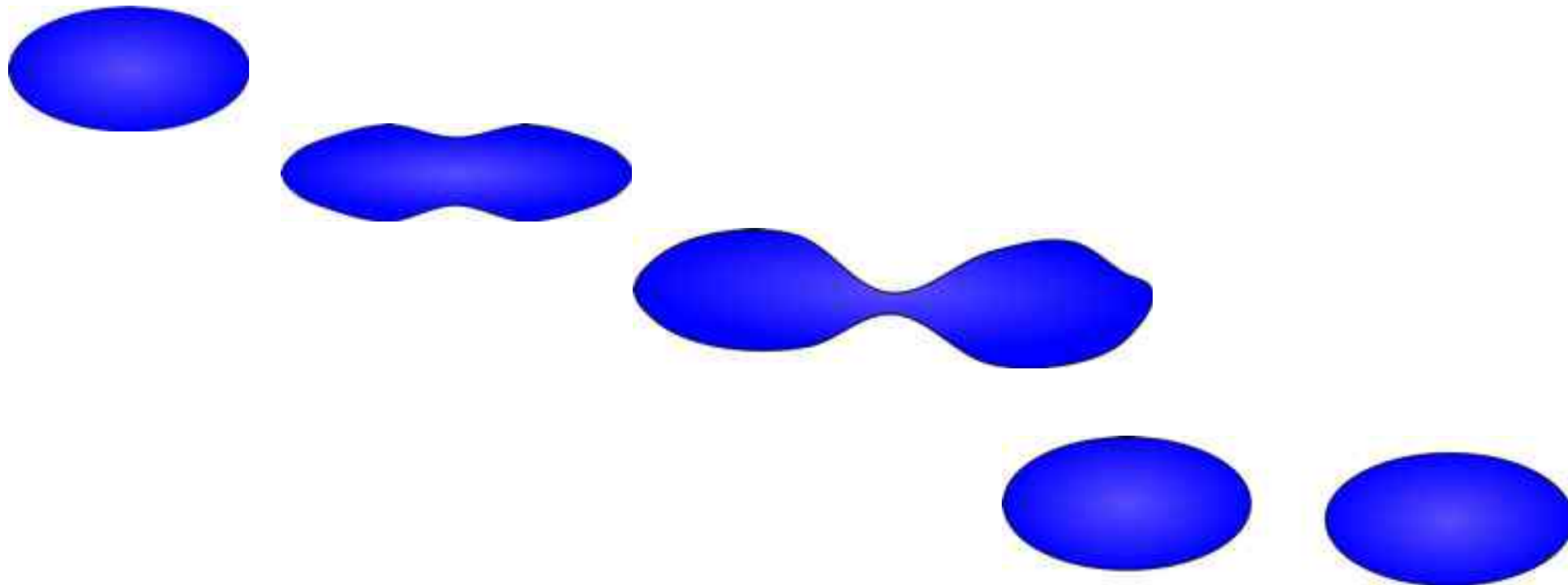
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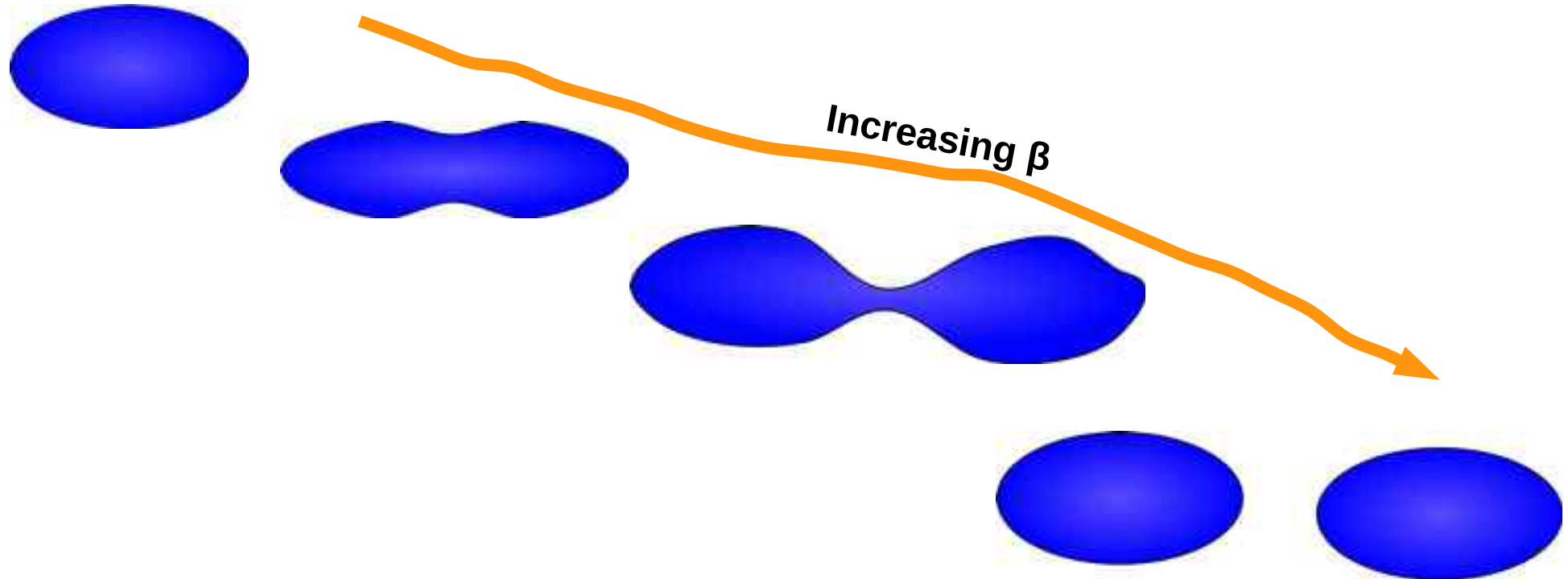
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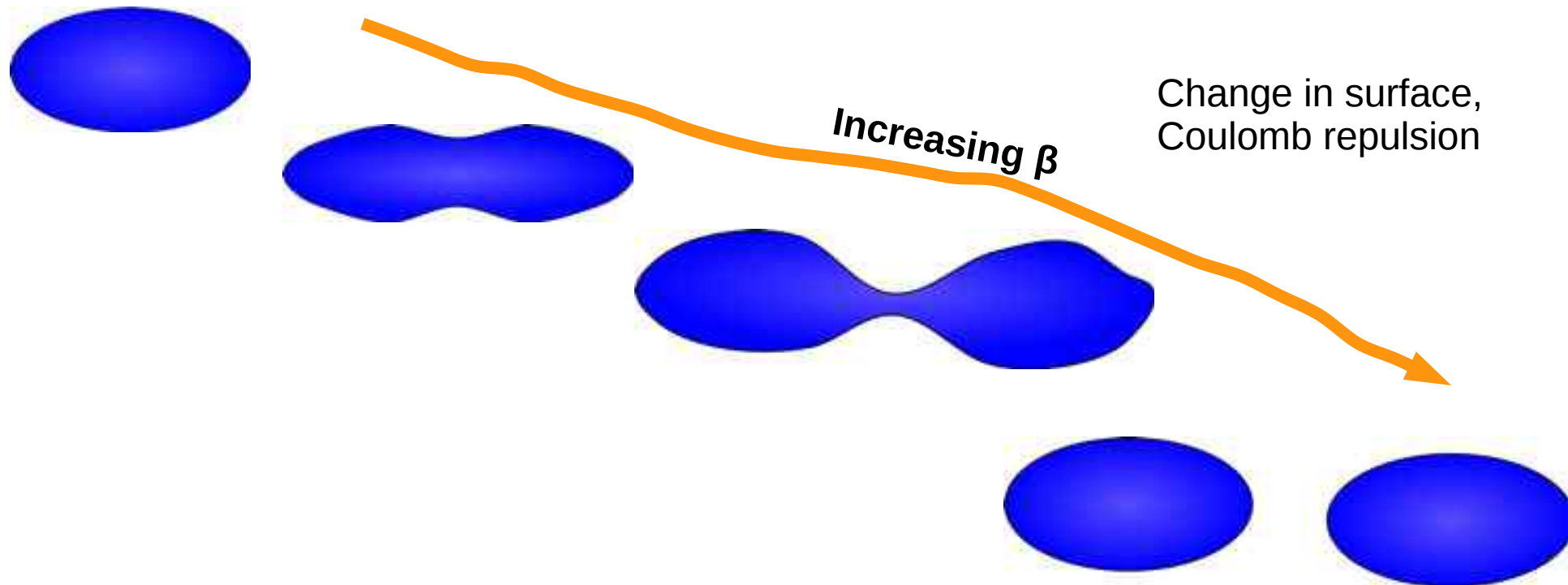




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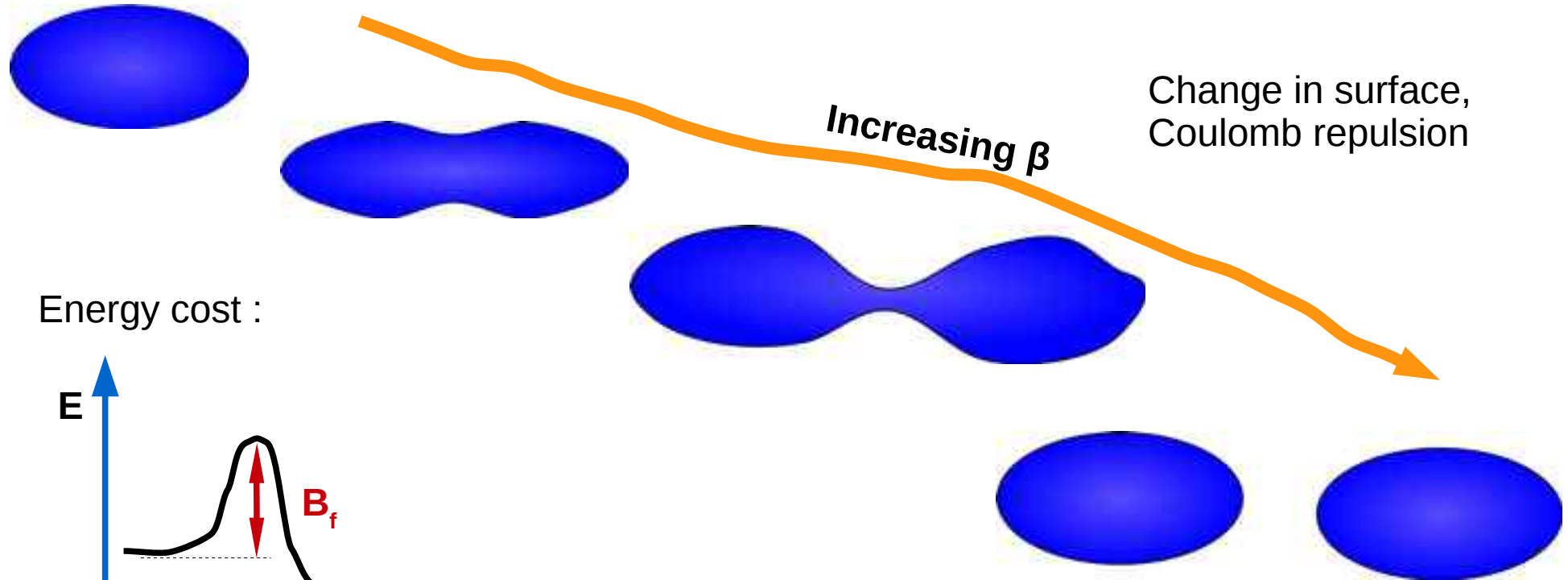
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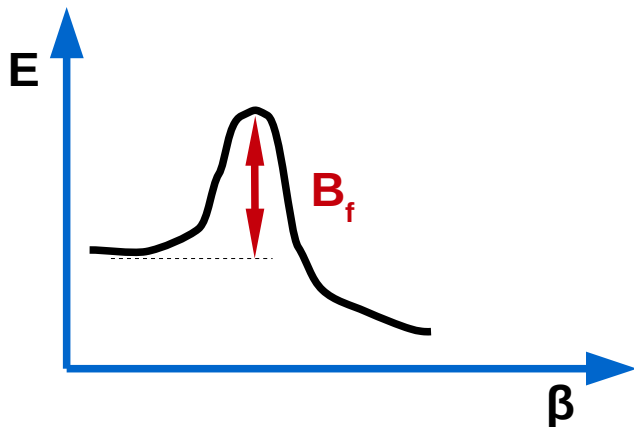
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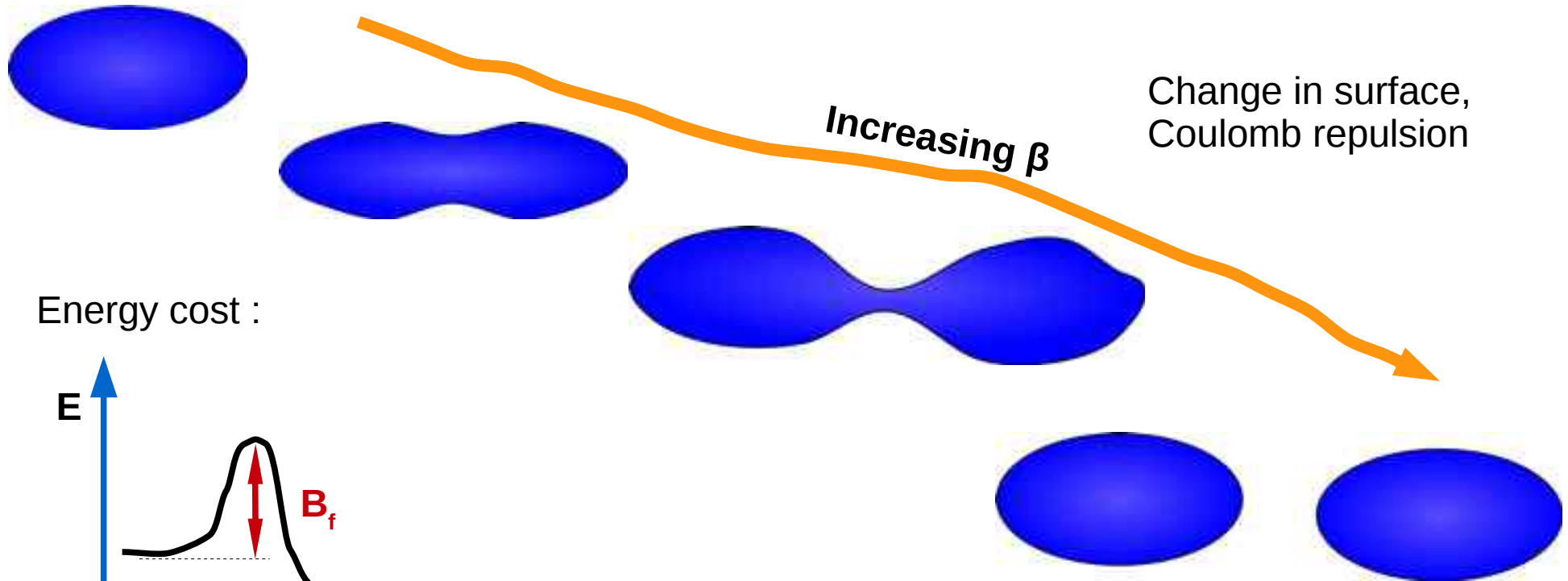
Energy cost :



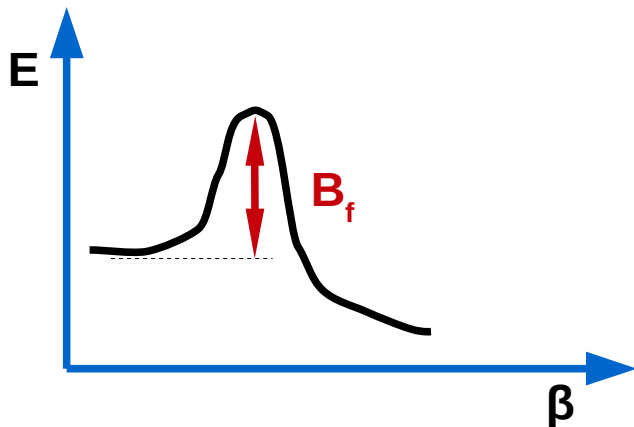
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Energy cost :



$B_f$  can be calculated within the liquid drop model.



# Fission

**But:** The nucleus is a quantum object!

→ Tunneling through the barrier,

→ *Shell effects* are present. (Actually:  $Z$  protons and  $N$  neutrons in Coulomb and nuclear interaction at the quantum scale.)

# Fission

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# Fission

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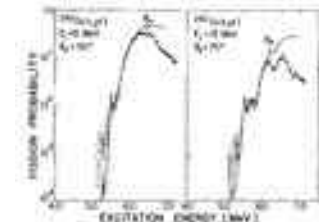
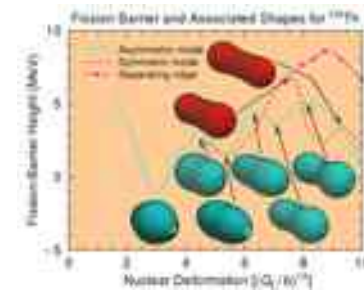
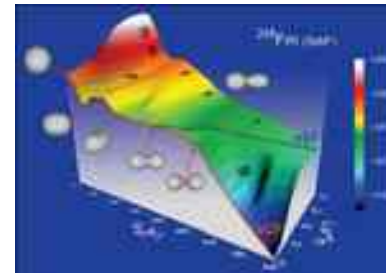
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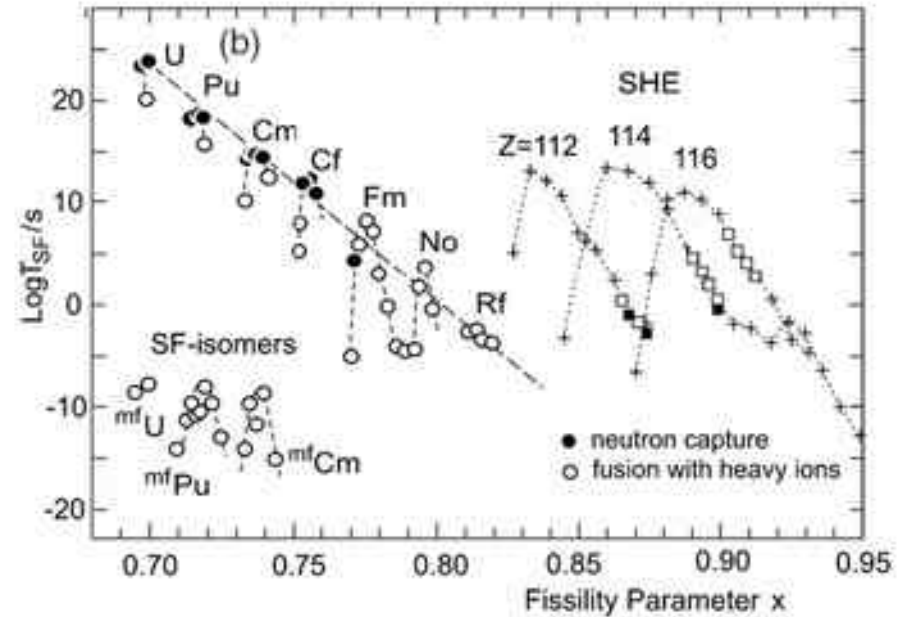
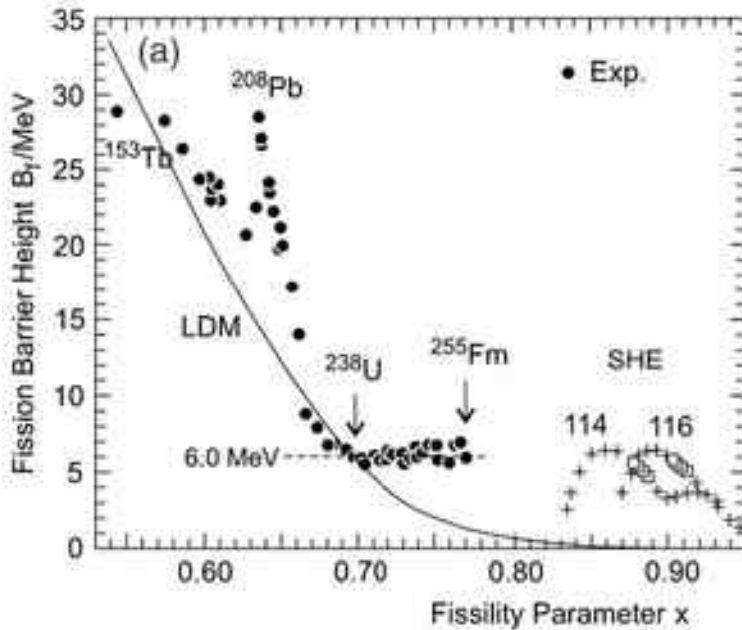
Several frameworks for calculation/determination:

- Microscopic-Macroscopic
- Density functional theory
- Phenomenological determination



# $B_f$ and SHE synthesis

$B_f$  is a key parameter for the stability of SHE



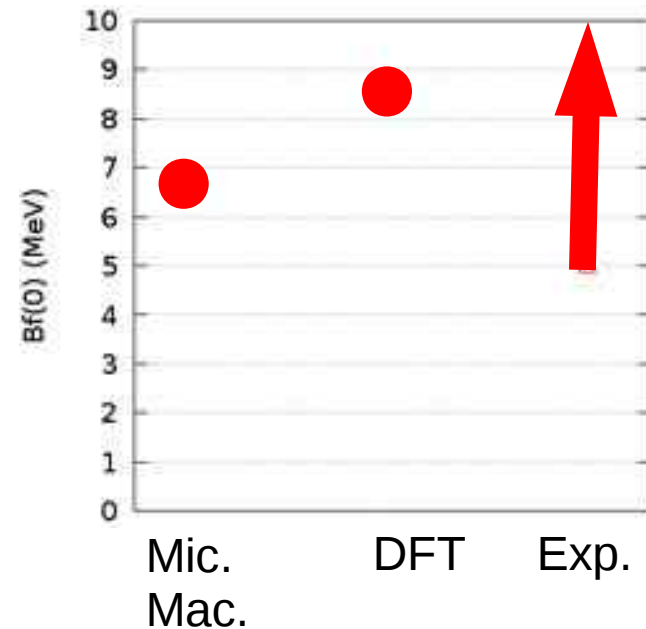
Yuri Oganessian

J. Phys. G: Nucl. Part. Phys. **34** (2007) R165–R242

# Study of $^{254}\text{No}$

Why measure  $B_f$  in  $^{254}\text{No}$  ?

- Production cross section *large* enough  $\rightarrow \sim 1 \mu\text{barns}$
- Several prediction exist:
  - Previously: experimental lower bound limit  
 $B_f > 5 \text{ MeV}$
- Shell effect strength is large ( $B_f^{\text{LD}} = 0.9 \text{ MeV}$ )

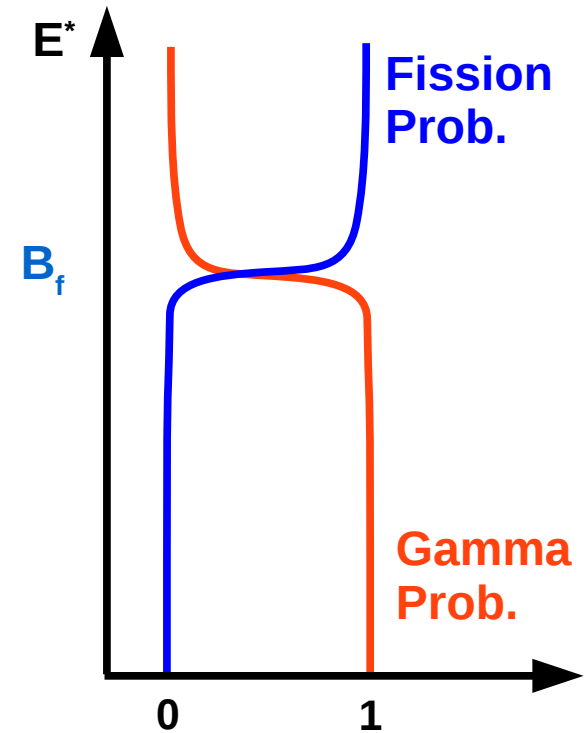




## Method: competition Fission/Gamma

If  $B_f < S_n$  :

$$P_{\text{fission}} \approx \Gamma_{\text{fission}} / (\Gamma_{\text{fission}} + \Gamma_{\gamma}) \approx 1 - P_{\gamma}$$



## Method: Gamma calorimetry

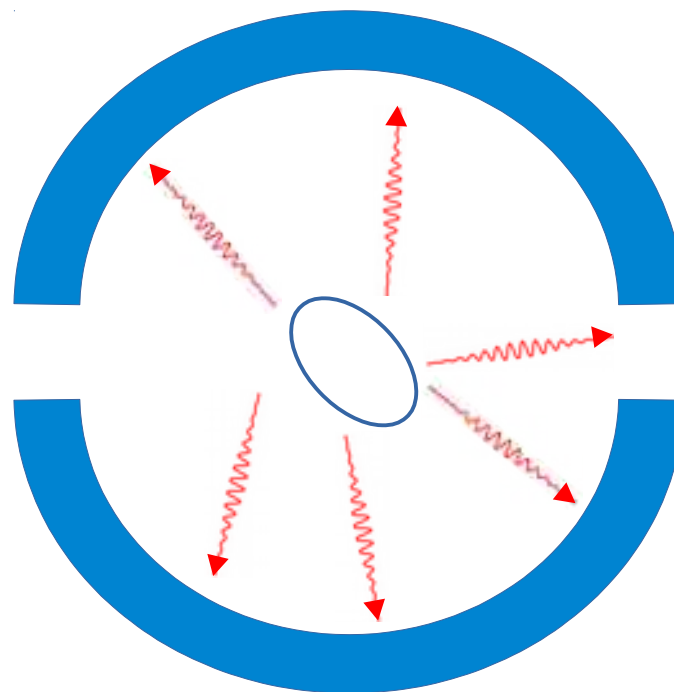
$P_\gamma$  from calorimetric measurements :

- Detecting gamma emitted by the ER, vs.  $E^*$ ,  $I$
- $E^*$  is the sum of the energies of particle evaporated by the nucleus, ending in its ground state.

$$E^* \approx \sum E_\gamma$$

- $I$  is linked to the multiplicity of  $\gamma$  rays emitted

$$I = \sum \delta I_\gamma \approx \langle \delta I_\gamma \rangle \times M_\gamma$$



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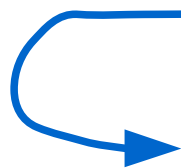
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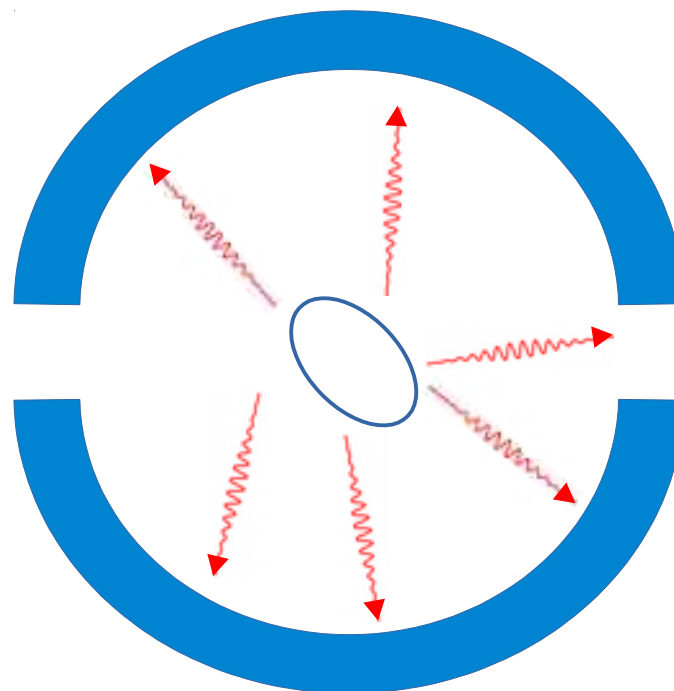
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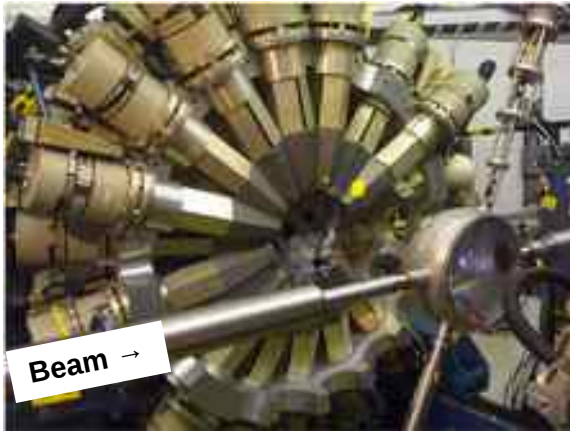
Some knowledge of the level structure needed.



# Experimental setup

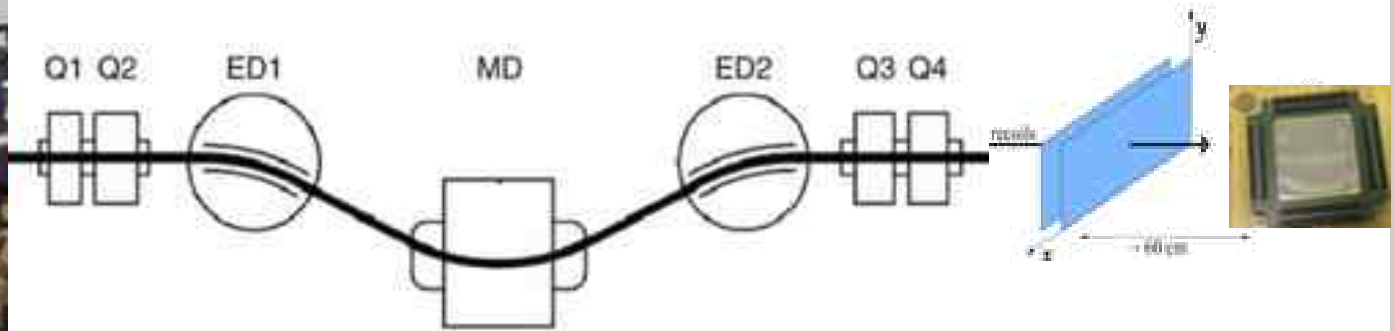


## Gammasphere



- ~ 100 modules (Ge+BGO)
- Detection efficiency:
  - Ge: 10%
  - Ge+BGO: 78%

## Fragment Mass Analyzer



- High selectivity in  $m/Q$
- Poor transmission (7%)

## Focal plane detectors

- Identify the evaporation residues

# Data processing: unfolding

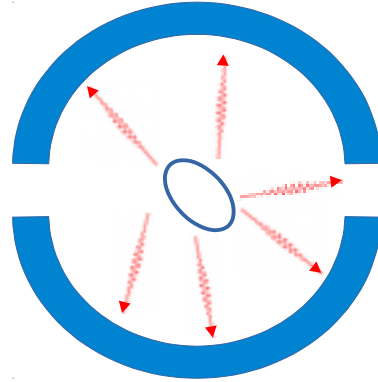
Collecting the total energy and multiplicity of emitted  $\gamma$  rays

## Emitted

- $M$   $\gamma$ -rays
- Total energy  $E_{\text{sum}}$

## Measured

- Number of hits  $k$  (fold)
- Total energy  $H$



# Data processing: unfolding

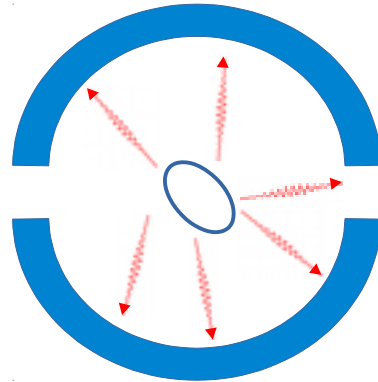
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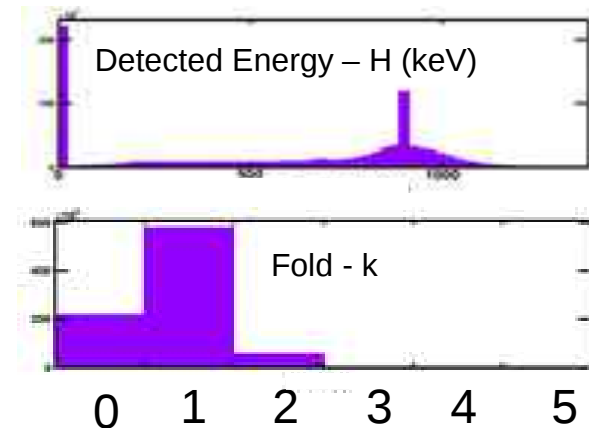
## Measured

- Number of hits  $k$  (fold)
- Total energy  $H$



Calibrate the relation between  $k$  and  $M$ ,  $H$  and  $E$

$^{88}\text{Y}$ :  $E_1 = 1836$  keV  
 $E_2 = 898$  keV



# Data processing: unfolding

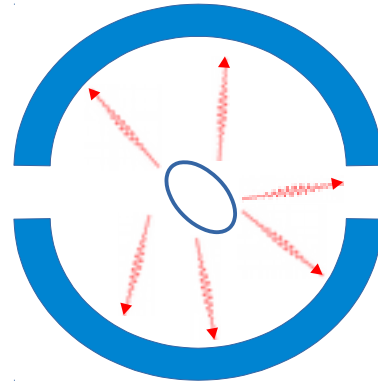
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## Emitted

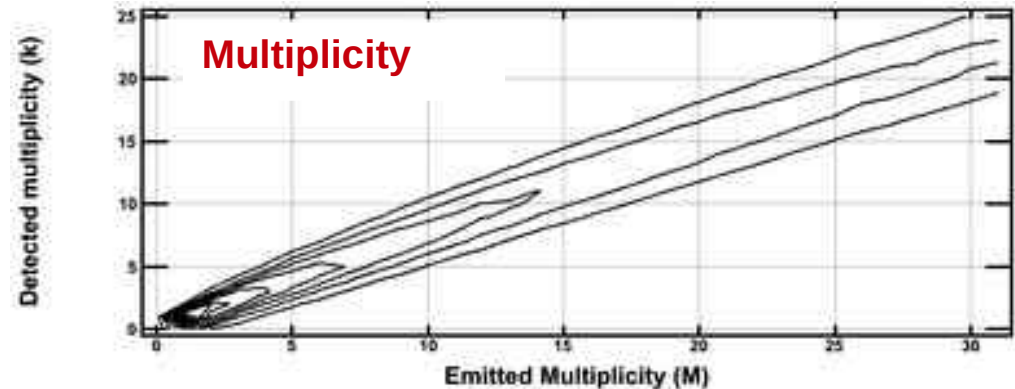
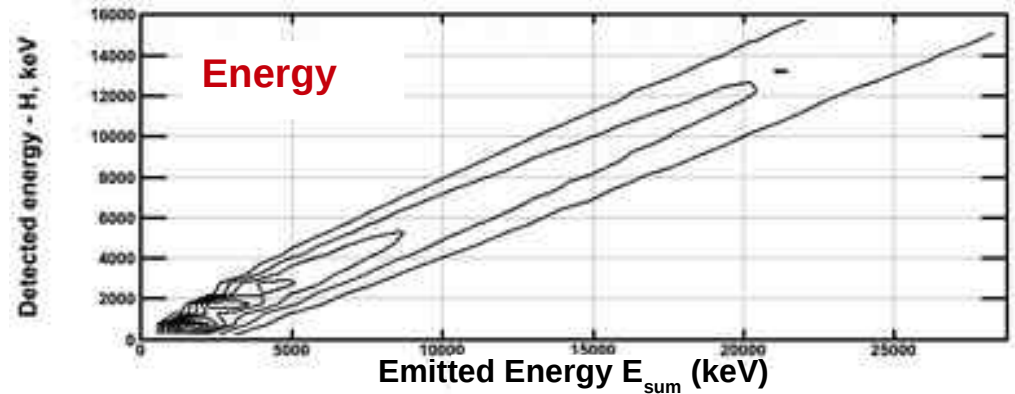
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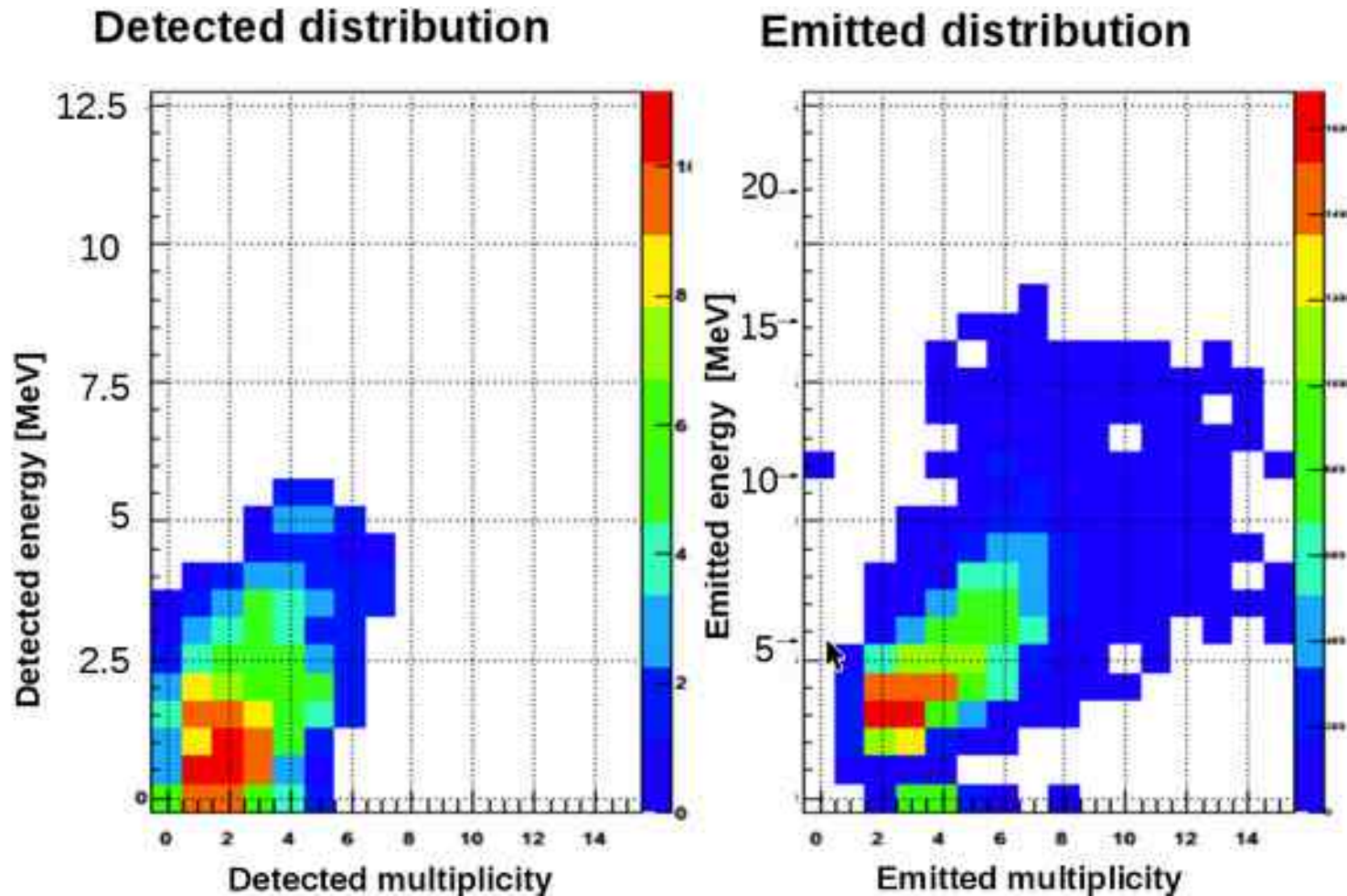


Calorimetric Efficiency:  $H/E = 63\%$   
Detection Efficiency:  $k/M = 70\%$

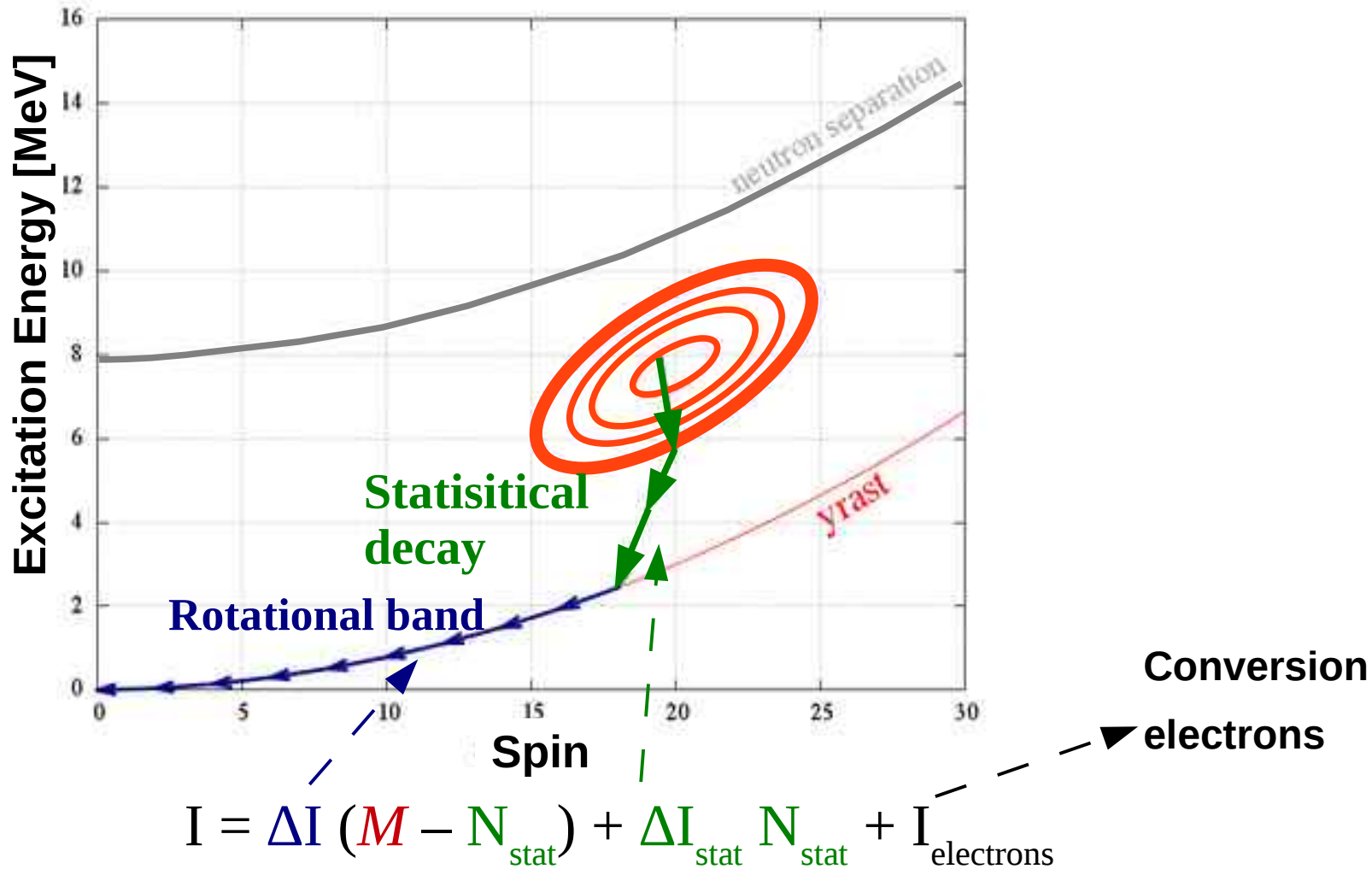
Using a Statistical *unfolding* method



# Reconstructing emitted distribution $M_{\gamma}$ , $E_{\gamma}$



# Reconstructing Entry distribution



# Reconstructing Entry distribution

$$I = \Delta I (M - N_{\text{stat}}) + \Delta I_{\text{stat}} N_{\text{stat}} + I_{\text{electrons}}$$

**Statistical decay**

$$N_{\text{stat}} \sim 3$$

$$\Delta I_{\text{stat}} \sim 0.5 \hbar/\gamma$$

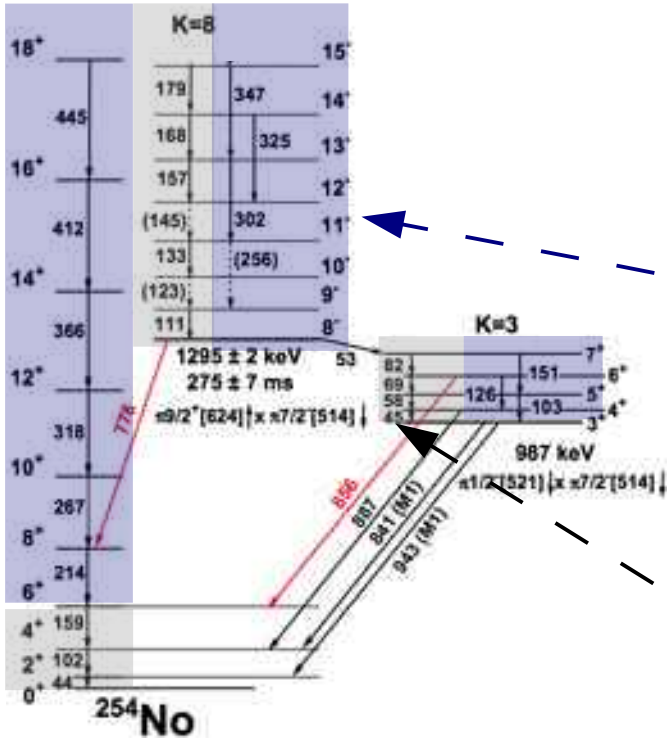
**Rotational bands**

$$\Delta I = 2 \hbar/\gamma$$

**Conversion electrons**

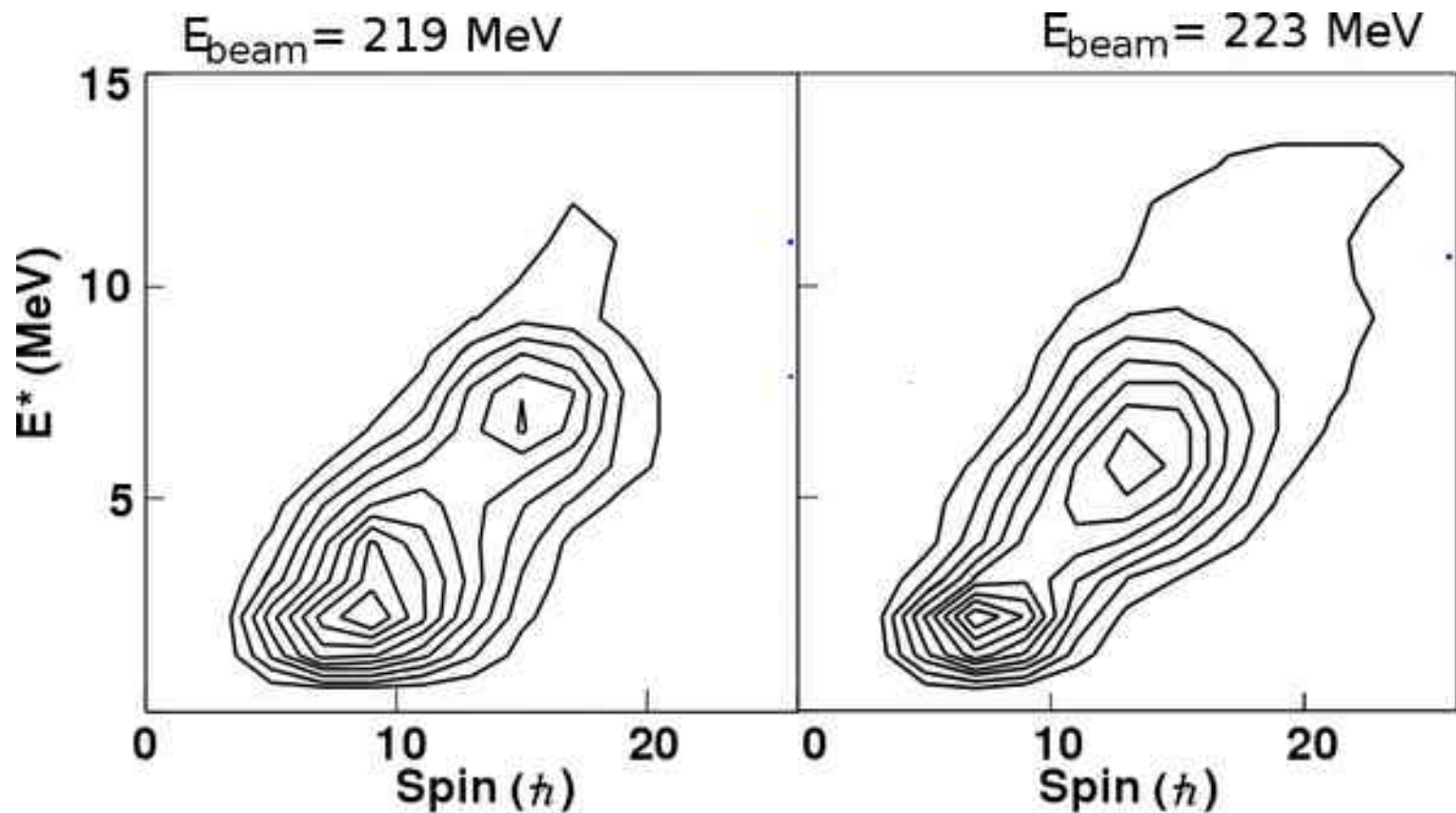
$$I_{\text{electrons}} \sim 8 \hbar$$

$$E_{\text{electrons}} = 900 \text{ keV}$$

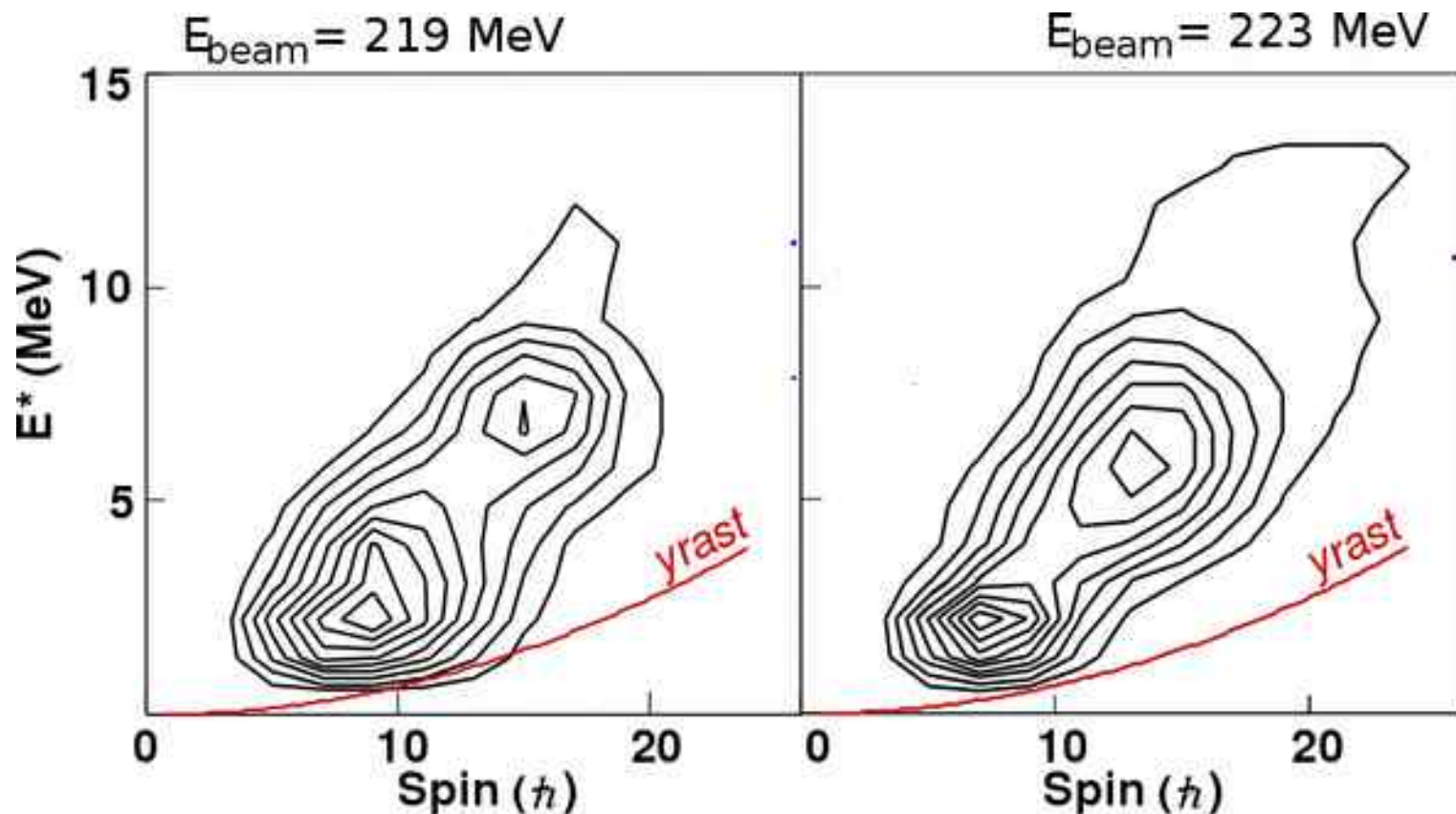


M. Leino et al., Eur. Phys. J. A 6, 63–69 (1999)  
 P. Reiter et al., Phys. Rev. Lett., vol 82 (1999) 509  
 S. K. Tandel et al., Phys. Rev. Lett. 97, 082502 (2006)  
 F.P. Heßberger et al., Eur. Phys. J. A 43, 55–66 (2010)  
 R.M. Clark et al., Physics Letters B 690 (2010) 19–24  
 R.-D. Herzberg et al., Nature 442 (2006) 896

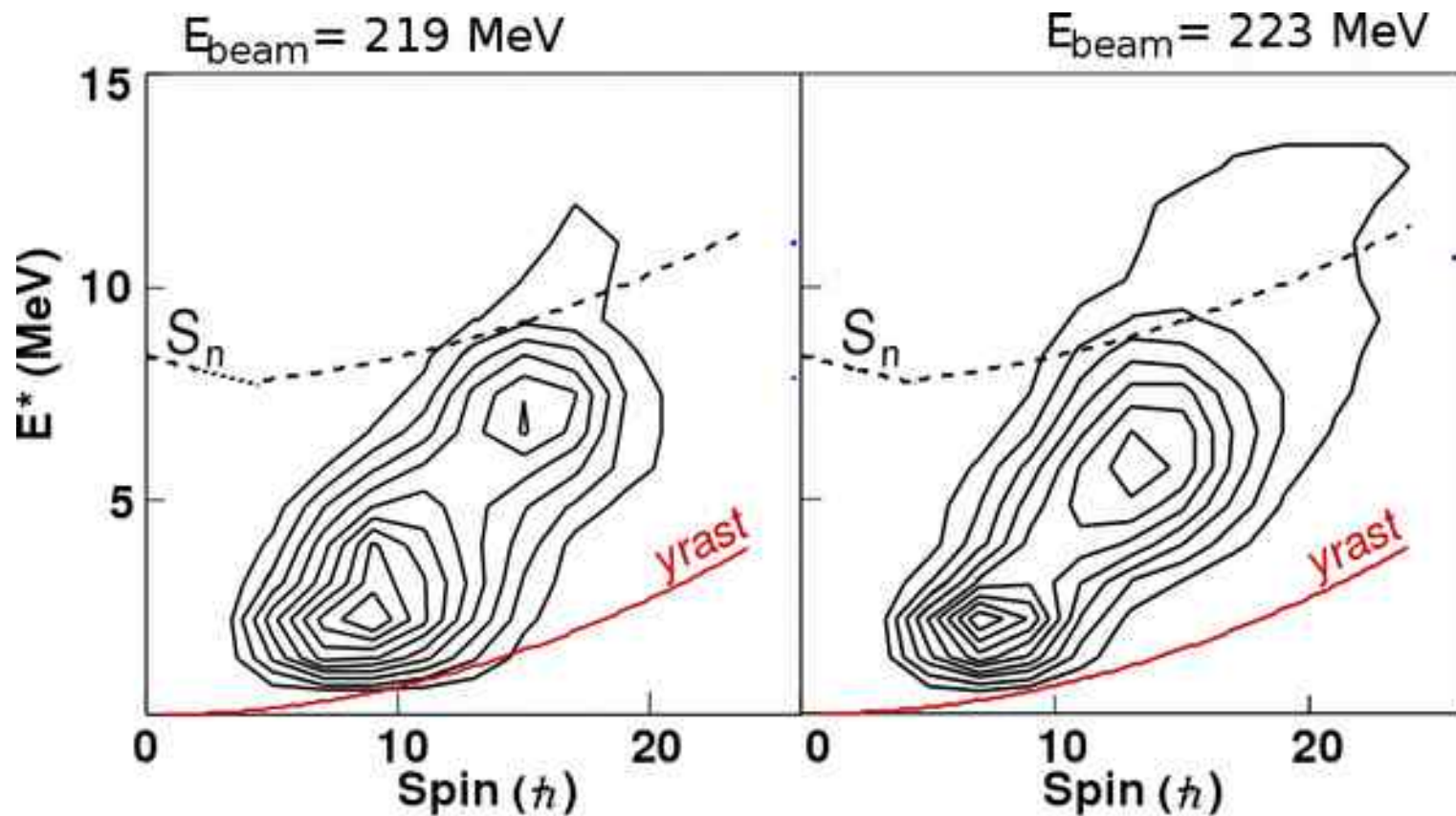
# Entry distribution



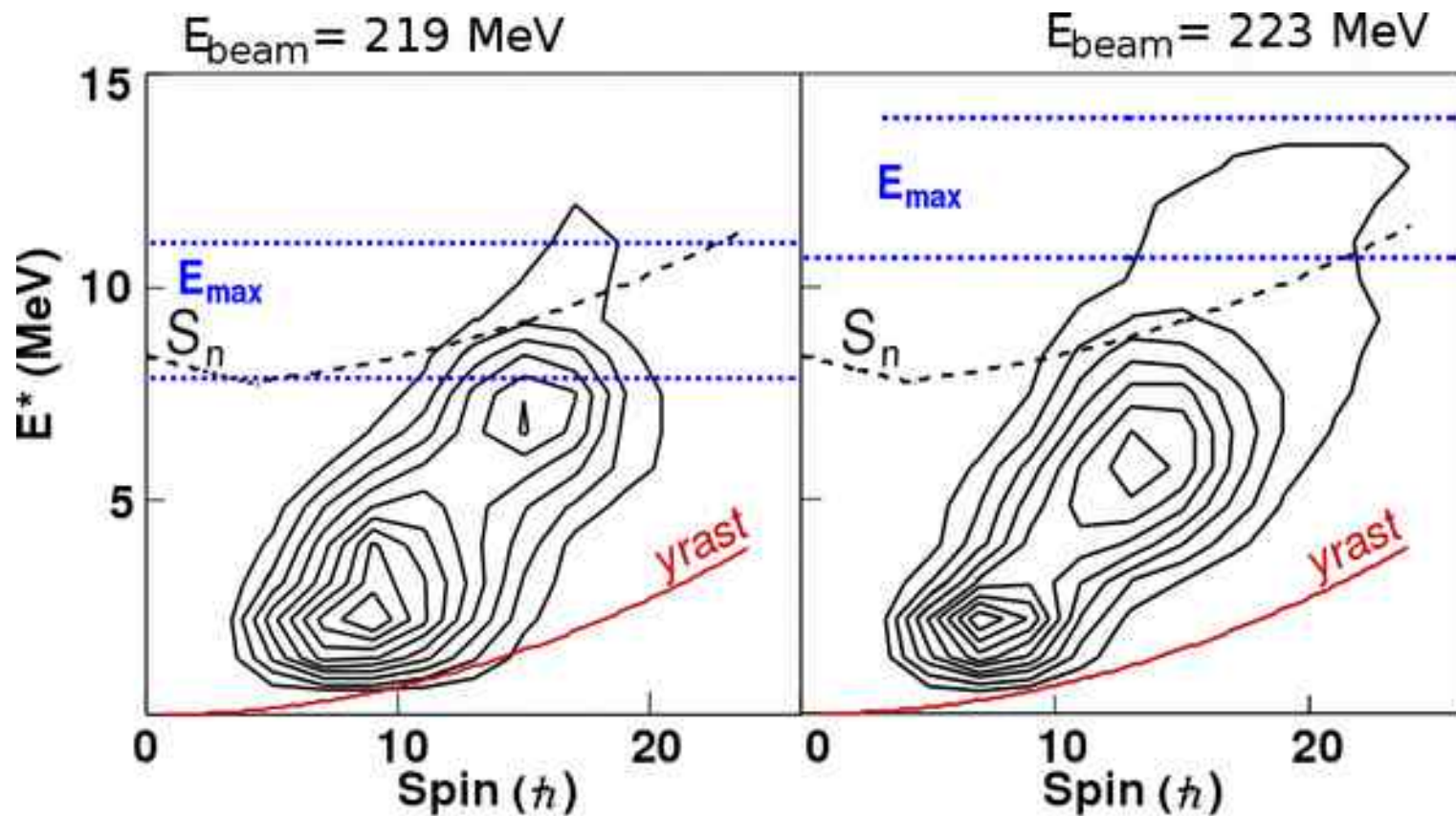
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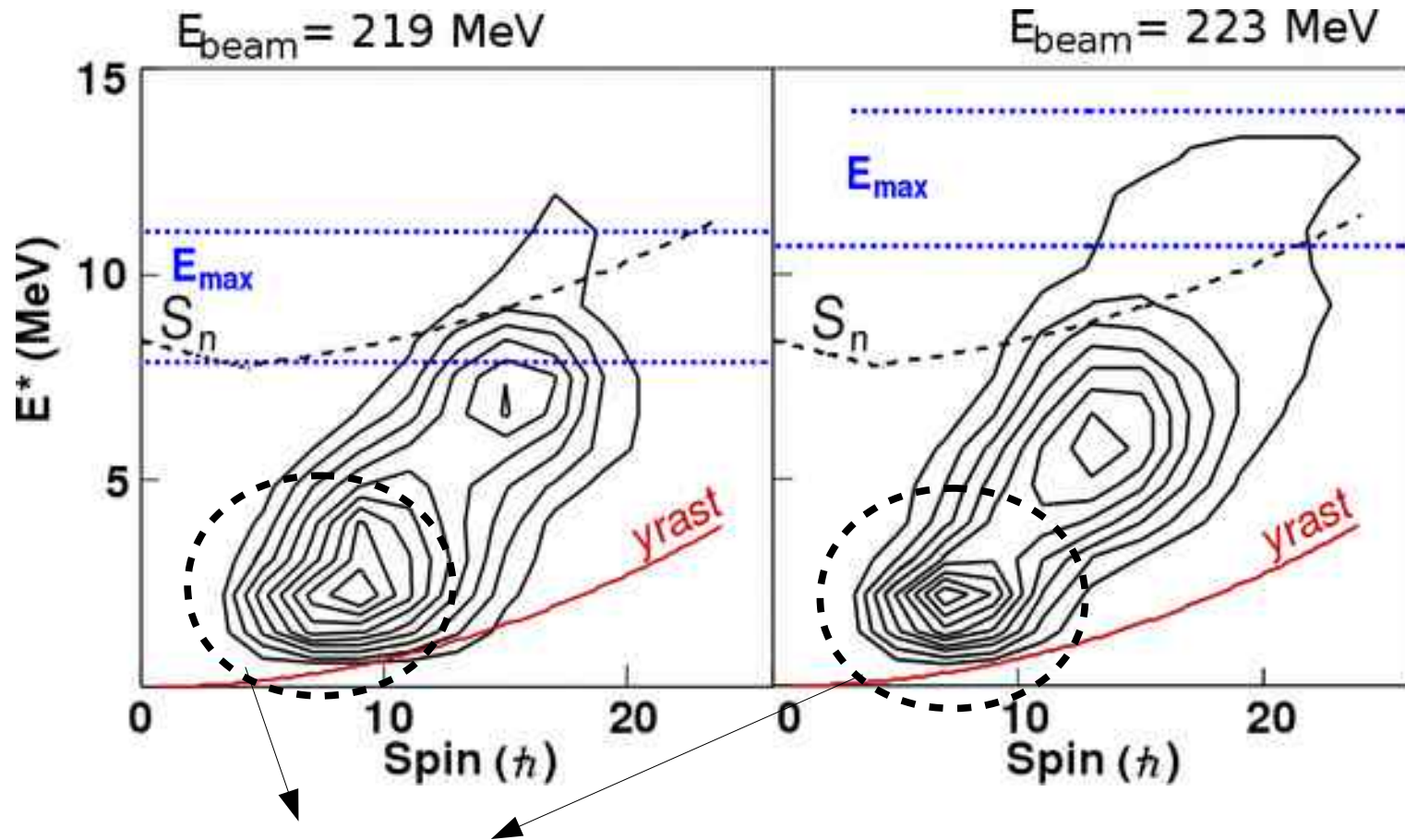
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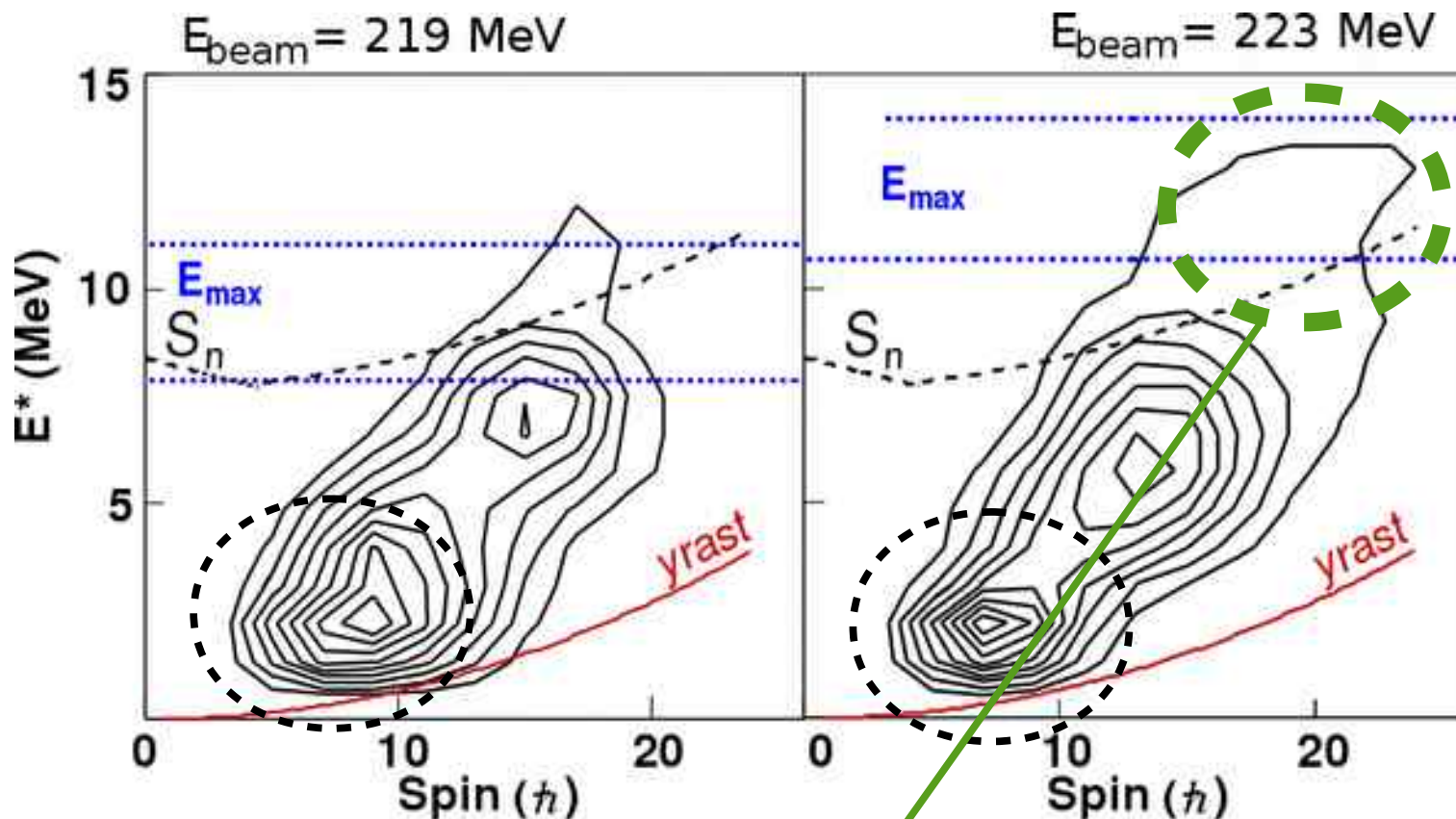
# Entry distribution



Isomer events: reconstructed at the wrong  $I, E^*$



# Entry distribution

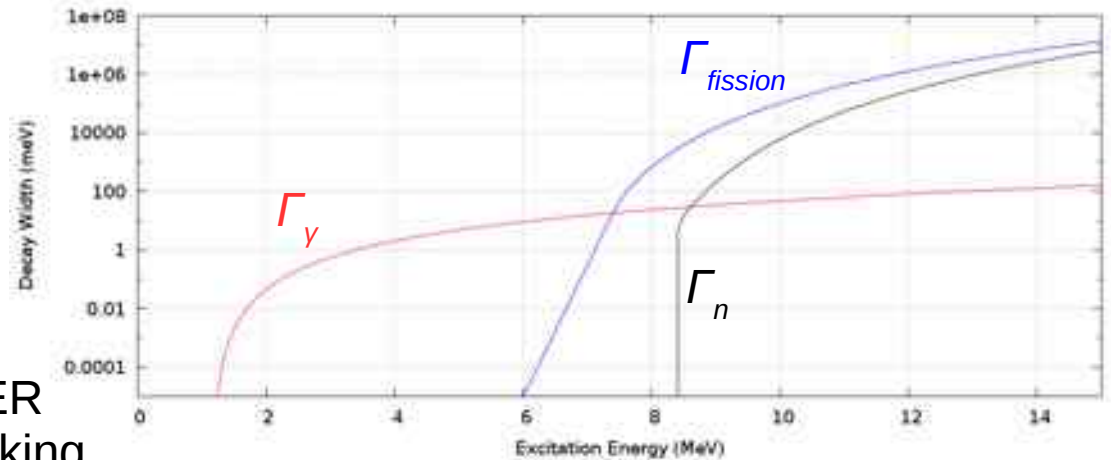


Tail toward high  $E^*$  from random summing with reaction background

# Maximum $E^*$ at a given spin ?

$$N_{\gamma}(E^*) = \frac{\Gamma_{\gamma}(E^*)}{\Gamma_{total}(E^*)} \times D(E^*)$$

If we control for the population of the ER  $D(E^*)$ , then the fall of  $N_{\gamma}$  reflects the taking over of gamma decay by fission.



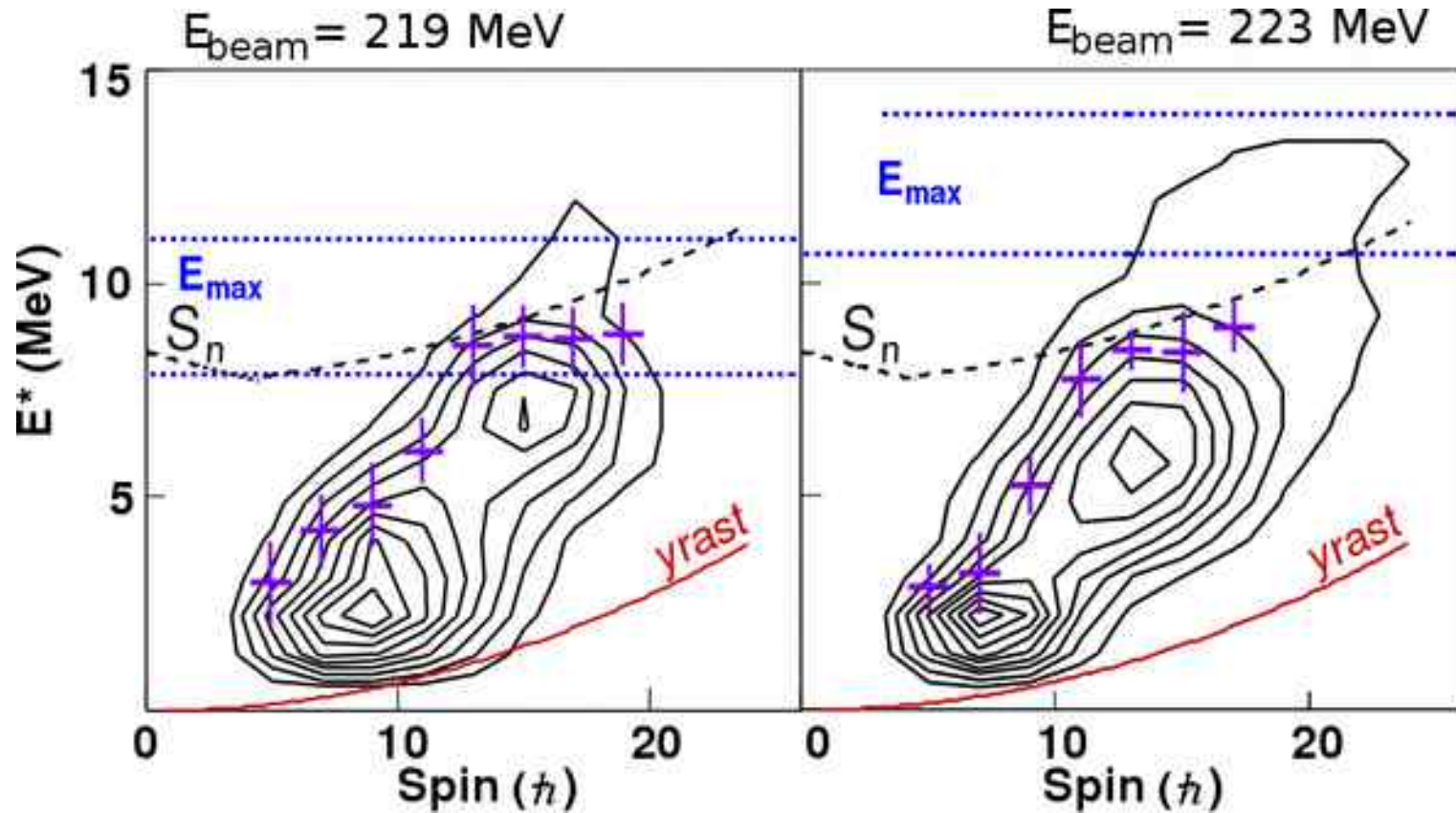
To account for the distribution of formed ER, study with calculation codes :

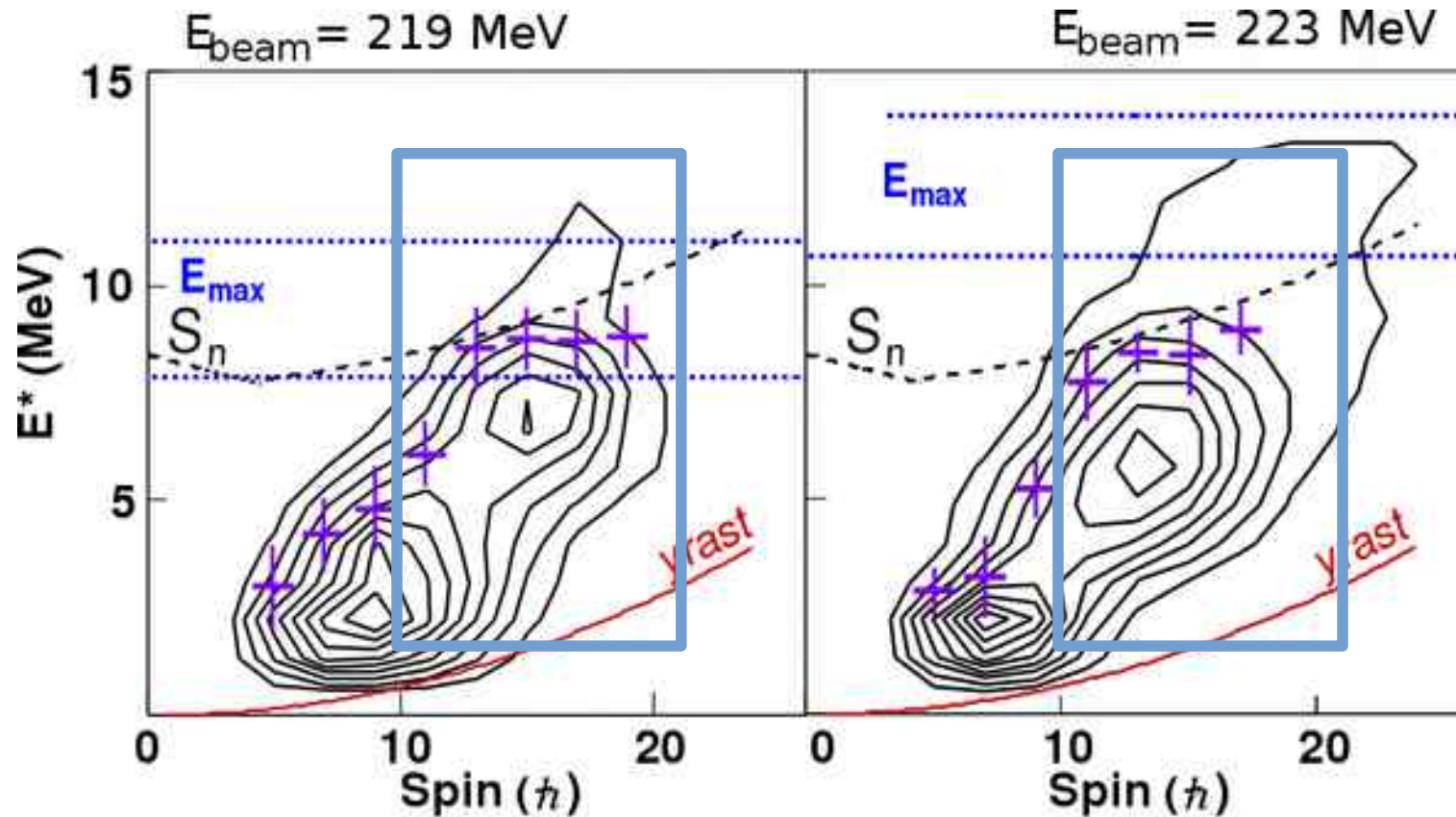
- NRV,
- KEWPIE2.

Extract relationship between the energy  $E_{1/2}$  where  $N_{\gamma}(E^*, I)=1/2$  and  $E_{saddle}(I) : \Delta(I) = E_{1/2} - E_{saddle}$

$$\Delta(0 \hbar) \approx 1 \text{ MeV}$$

$$\Delta(20 \hbar) \approx 0 \text{ MeV}$$

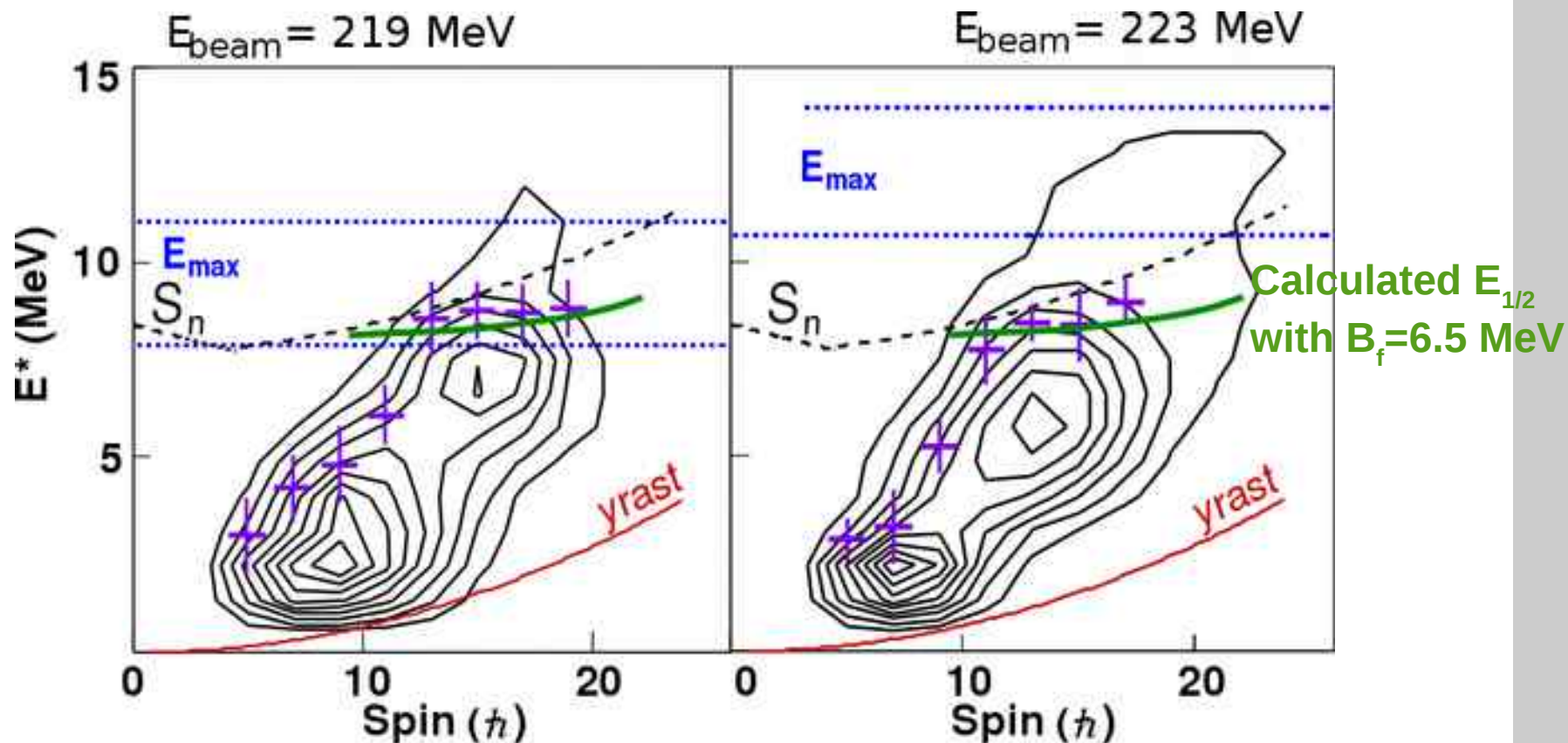




### Range of interest for the Entry distribution

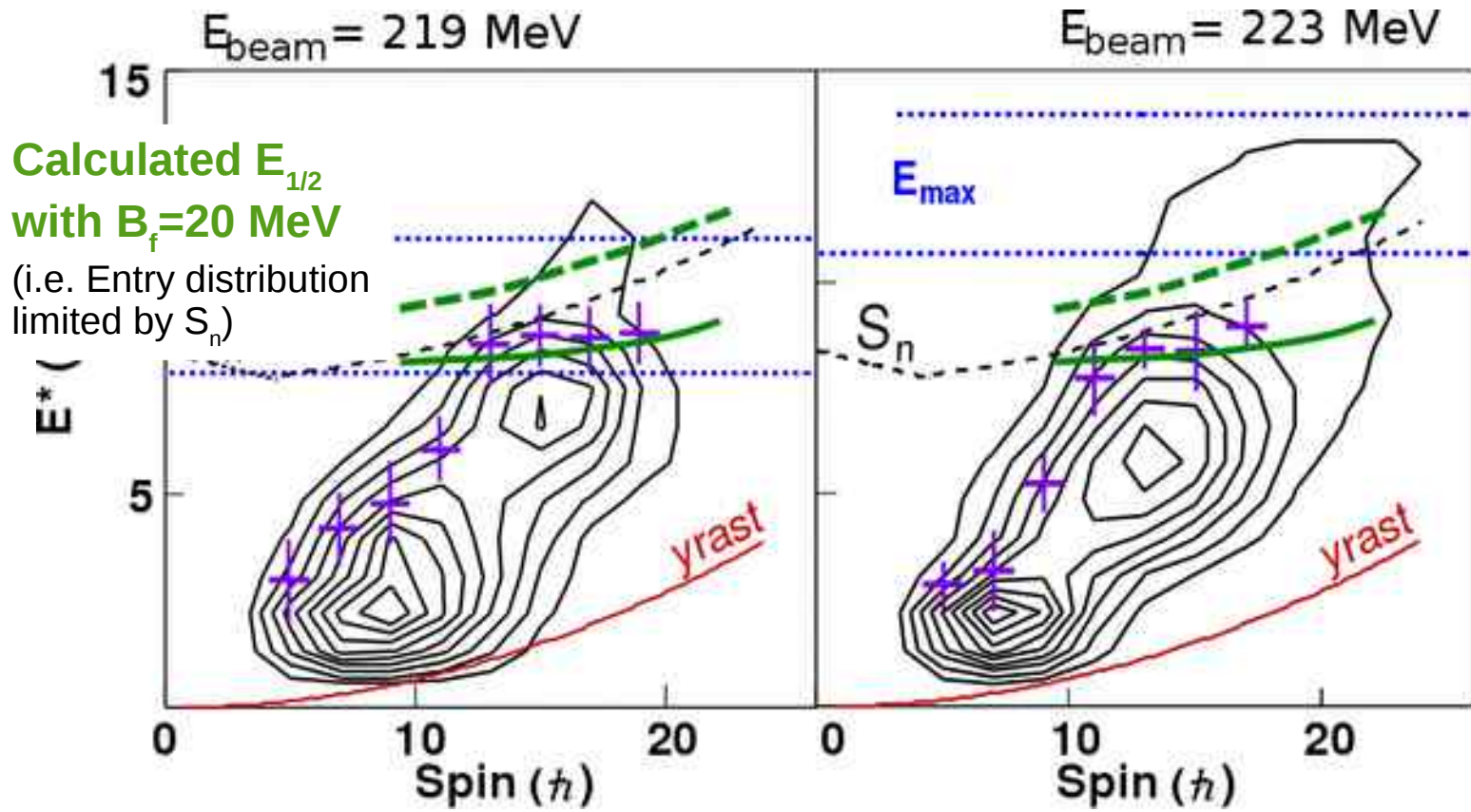
Where the fission has an impact on the entry distribution

# $E_{1/2}$ : experiment vs. calculation



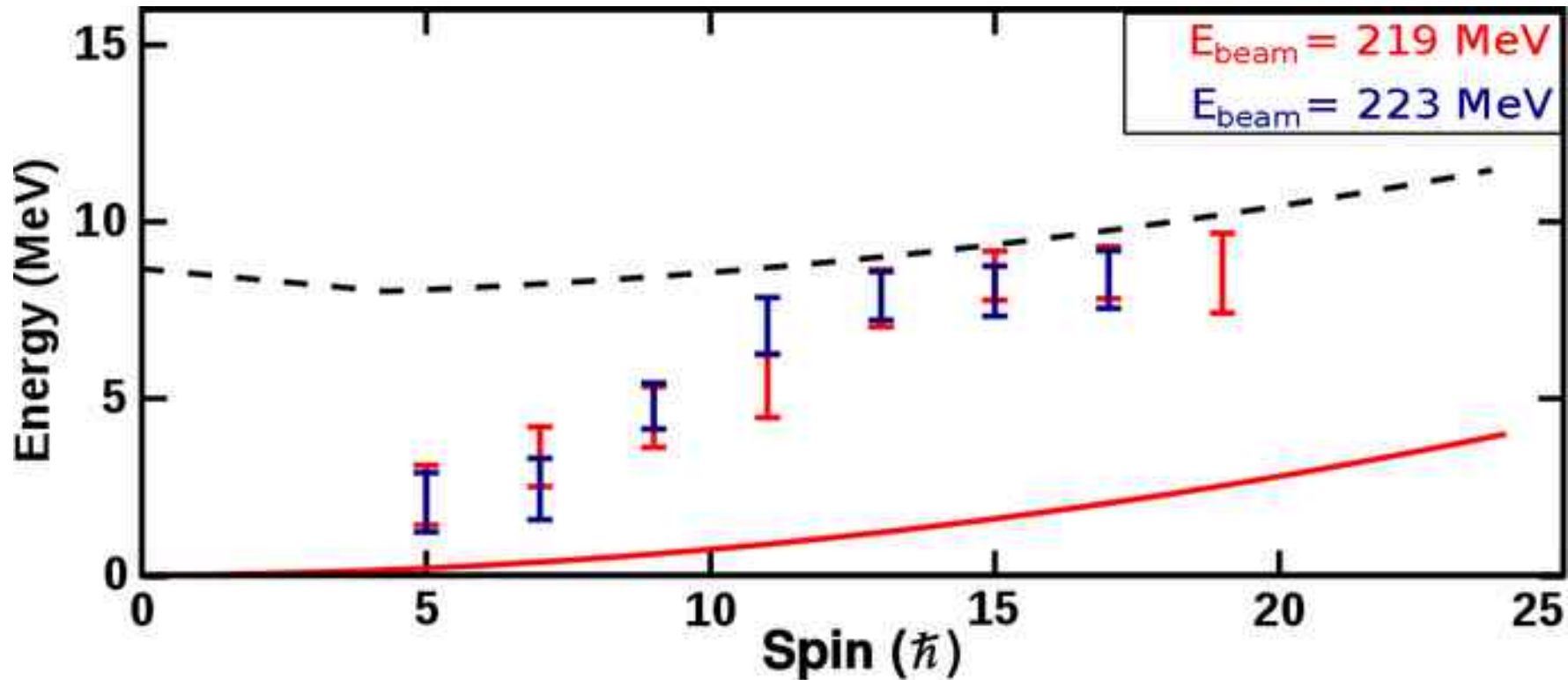
Calculated  $E_{1/2}$   
with  $B_f = 6.5 \text{ MeV}$

# $E_{1/2}$ : experiment vs. calculation



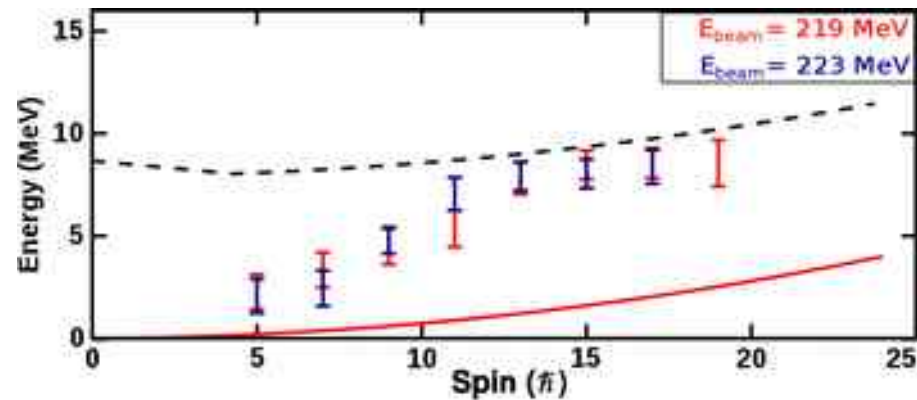
# Extracting $E_{\text{saddle}}$ (I)

- Multiple unfoldings to take care of statistical variation in the process,
- For each resulting entry distribution, extract  $E_{1/2}$ ,



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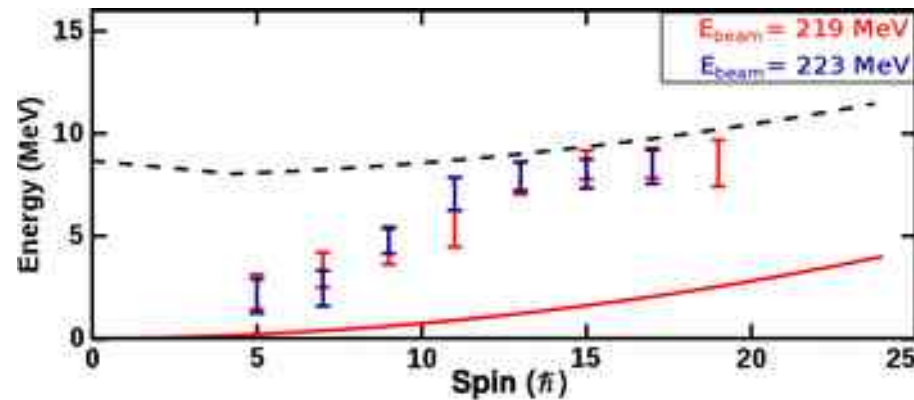


For  $I$  in [13, 19], fit on 
$$E_{\text{saddle}}(I) = B_f(0) + \frac{I(I+1)}{2J_{\text{saddle}}}$$



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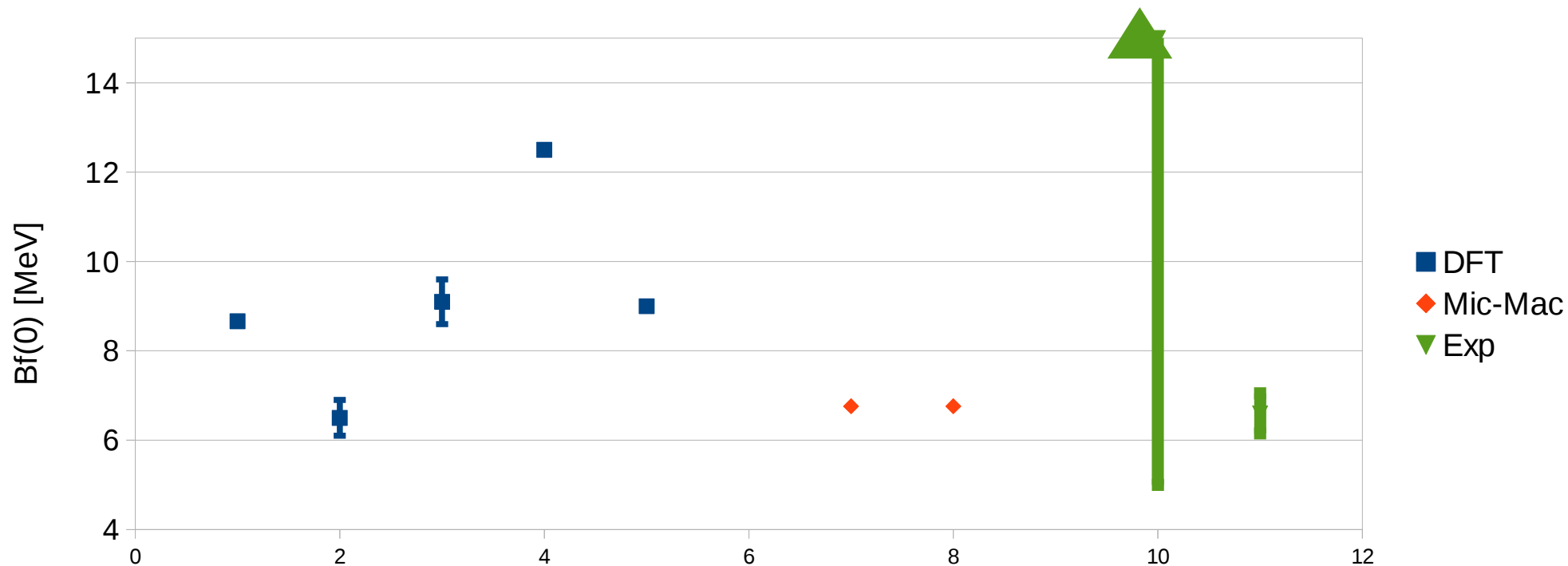
For  $I$  in [13, 19], fit on 
$$E_{\text{saddle}}(I) = B_f(0) + \frac{I(I+1)}{2J_{\text{saddle}}}$$

$$B_f(0) = 6.6 \pm 0.9 \text{ MeV}$$

$$J_{\text{saddle}} = 125 \pm 60 \text{ } \hbar^2/\text{MeV}$$

(corr = 0,95)

# Results compared to existing predictions



- 1 J.L. Egido, L. M. Robledo, Phys. Rev. Lett. 85, 1198.
- 2 J.P. Delaroche et al., Nuclear Physics A 771 (2006) 103.
- 3 L. Bonnaeu, et al., Eur. Phys. J. A 21, 391 (2004).
- 4 T. Duguet et al., Nuclear Physics A 679 (2001) 427.
- 5 M. Warda and J. L. Egido, Phys. Rev. C 86, 014322. 2012

- 7 M. Kowal et al., Phys. Rev. C 82, 014303.
- 8 P. Moller et al., Phys. Rev. C 79, 064304.
- 10 P. Reiter, et al., Phys. Rev. Lett. 82, 509 (1999).
- 11 G. Henning et al., Phys. Rev. Lett. 113, 262505

## Looking to the future

- Experimental improvements
- Data interpretation and theory

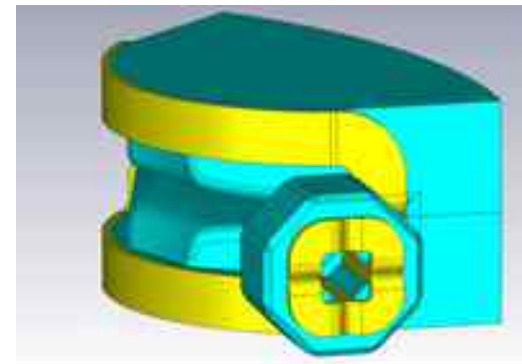
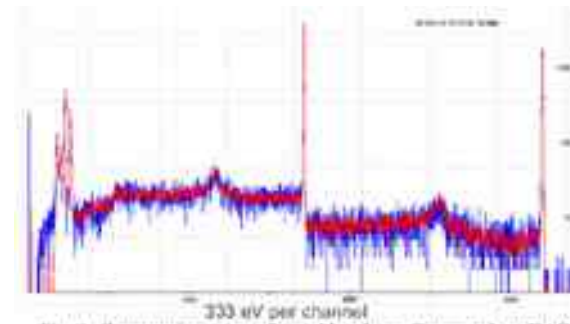
Coming soon...

## Digital Gammisphere

- Make use of GRETINA digitizer
- Will allow higher count rate
- resolve difficulties with calorimetry

## AGFA

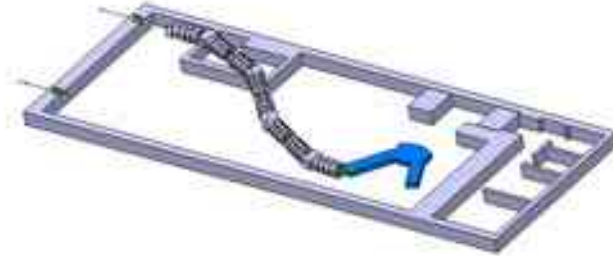
- Argonne Gas Filled Analyzer
- Quadrupole + Dipole
- Short length and large acceptance
- improve recoil detection efficiency (70% foreseen for  $^{254}\text{No}$ )



# Experimental improvements elsewhere

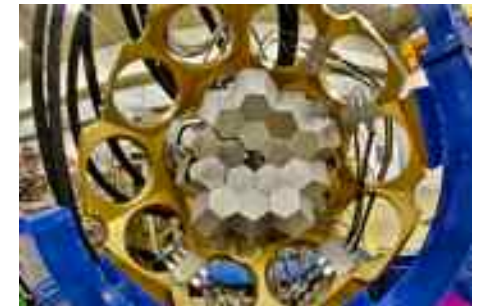
## S<sup>3</sup>

- Super Separator Spectrometer
  - Good reaction product separation
  - Diversity of focal plane instrumentation
- But... Calorimetry at the target position ?



## AGATA or GRETA

- Arrays of Ge crystal with pulse shape analysis and tracking
- May be useful for calorimetry once reaching  $4\pi$

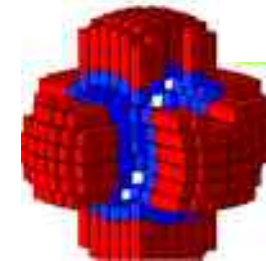


## PARIS

- Photon Array for studies with Radioactive Ion and Stable beams
- Medium resolution spectroscopy and calorimetry of  $\gamma$ -rays in large energy range
- Aimed at reaction mechanism studies

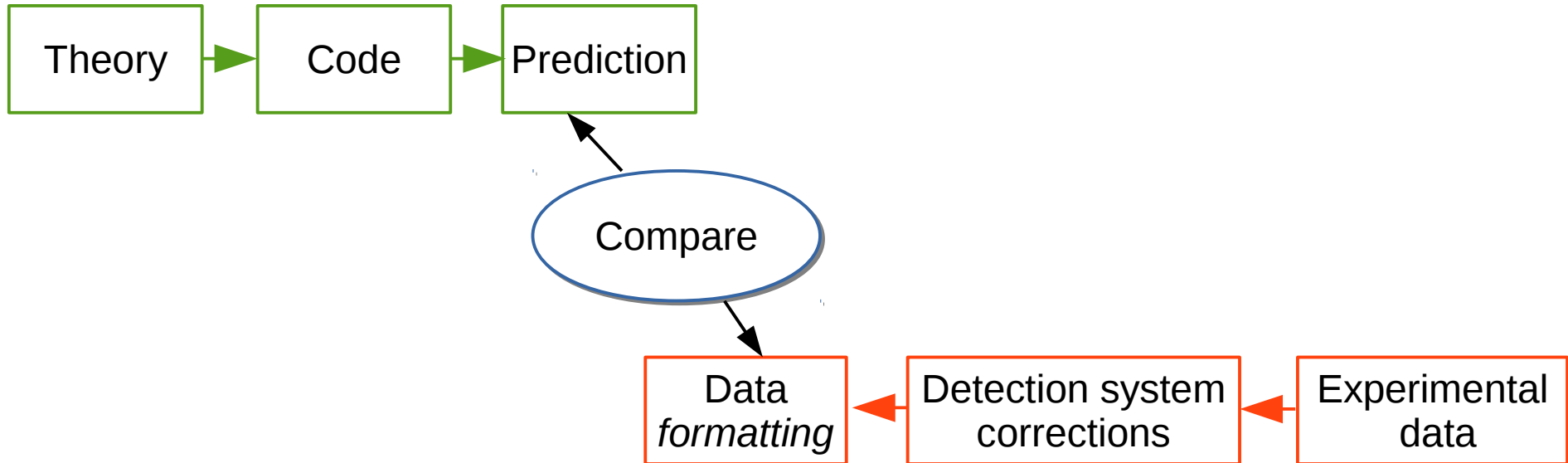
## Your favorite Gamma array and separator ?

- Some energy resolution and detection efficiency required
- Try it!



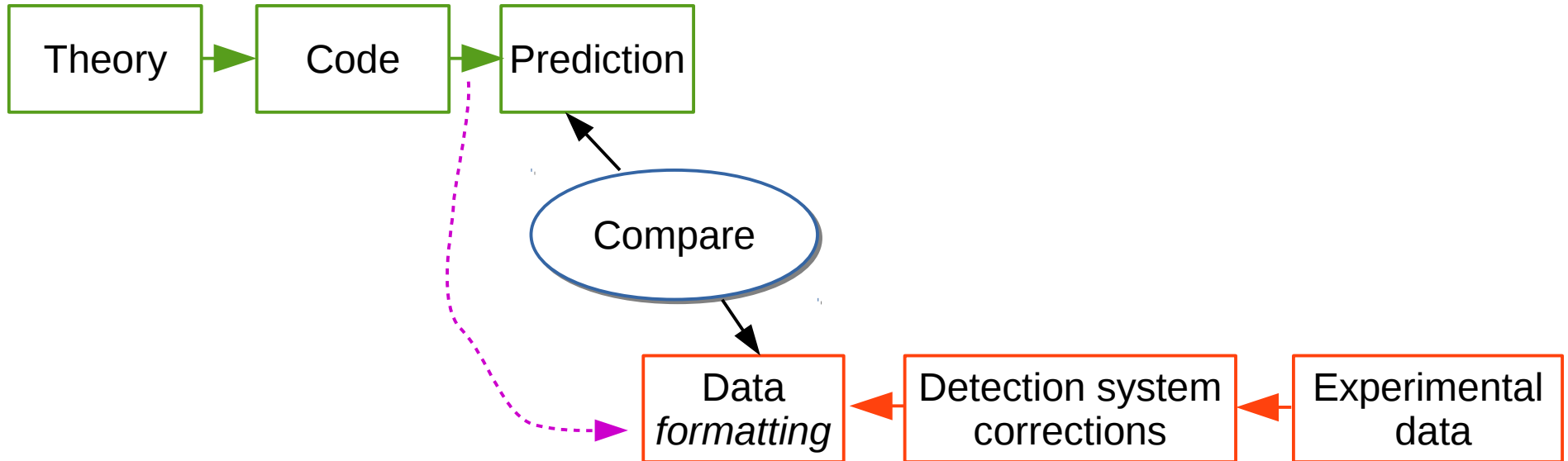
# Data interpretation

Interpretation scheme followed in this work:



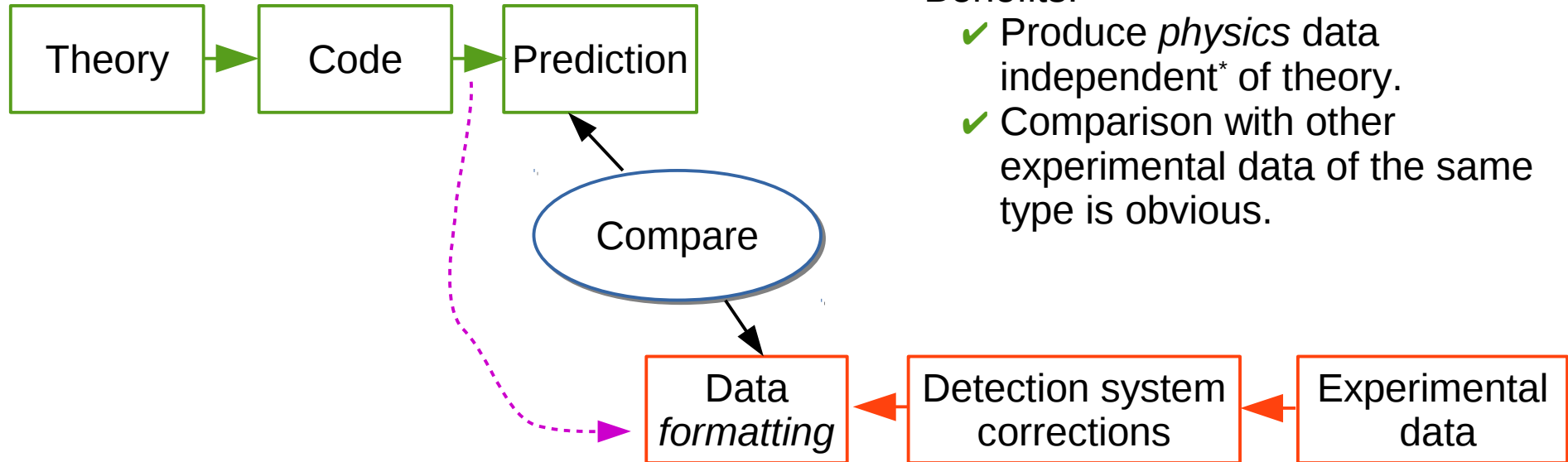
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Benefits:

- ✓ Produce *physics* data independent\* of theory.
- ✓ Comparison with other experimental data of the same type is obvious.

Limitations:

- ✗ Formatted data is not an observable (case of  $B_f$ ).
- ✗ Some assumptions on physics used.



# Data interpretation

**Interpretation scheme: Experimental data is a benchmark of theory**

Theory

Experimental  
data

# Data interpretation

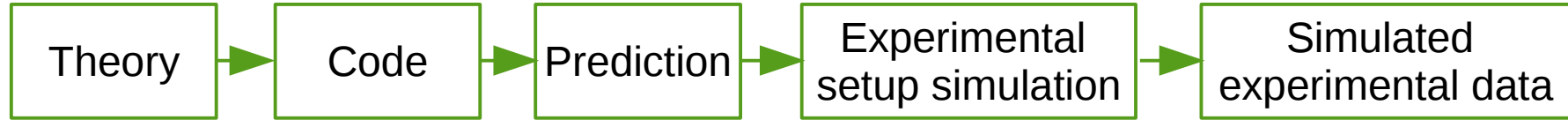
Interpretation scheme: Experimental data is a benchmark of theory



Experimental  
data

# Data interpretation

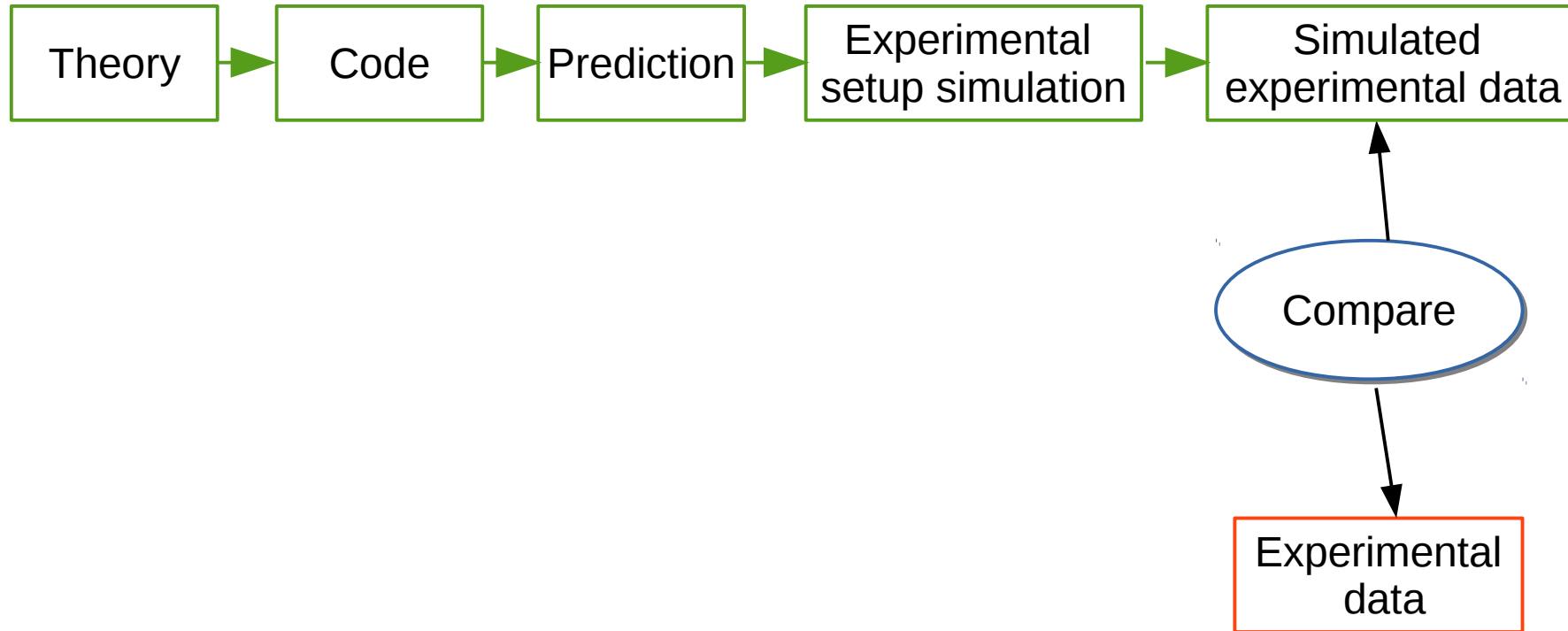
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Experimental data

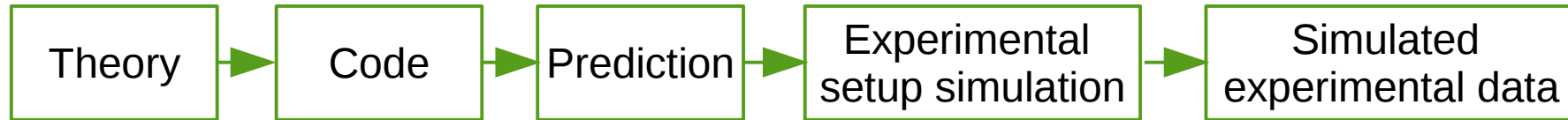
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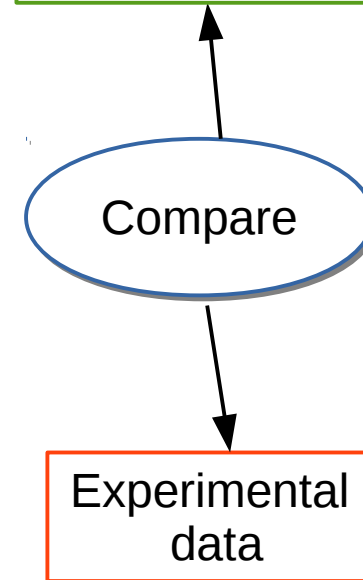
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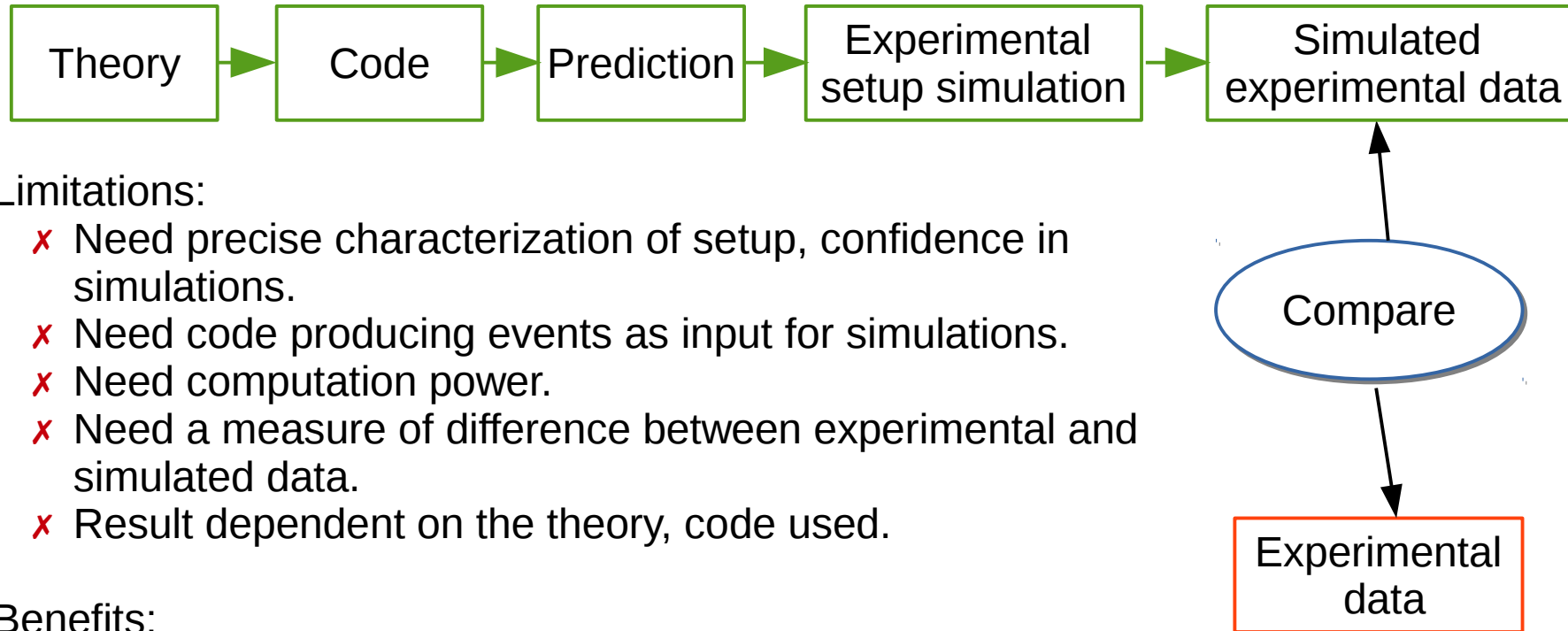
### Limitations:

- ✗ Need precise characterization of setup, confidence in simulations.
- ✗ Need code producing events as input for simulations.
- ✗ Need computation power.
- ✗ **Need a quantitative measure of difference between experimental and simulated data.**
- ✗ Result dependent on the theory, code used.



# Data interpretation

## Interpretation scheme: Experimental data is a benchmark of theory



### Limitations:

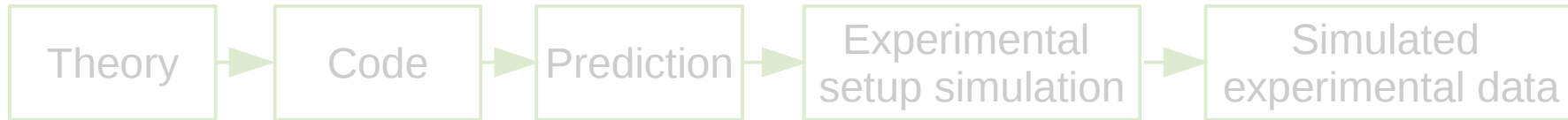
- ✗ Need precise characterization of setup, confidence in simulations.
- ✗ Need code producing events as input for simulations.
- ✗ Need computation power.
- ✗ Need a measure of difference between experimental and simulated data.
- ✗ Result dependent on the theory, code used.

### Benefits:

- ✓ Takes into account the full physics, event by event.
- ✓ Can test many codes, theories with one data set.
- ✓ **Allow exploration of model parameters, production of uncertainty, covariance data.**

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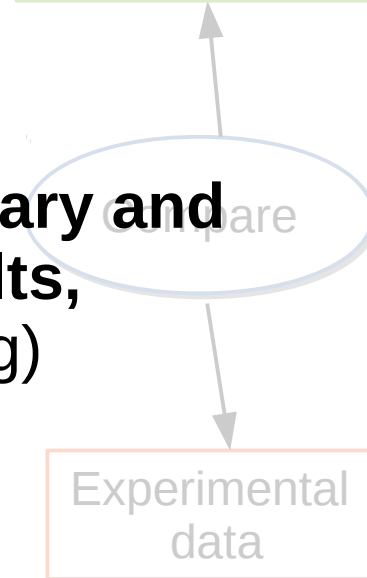
Limitations:

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- ✗ Need code producing results compatible with the data.
- ✗ Need a measure of difference between experimental and simulated data.
- ✗ Result dependent on the theory, code used.

Benefits:

- ✓ Takes into account the full physics, event by event.
- ✓ Can test many codes, theories with one data set.
- ✓ **Allow exploration of model parameters, production of uncertainty, covariance data.**

**The two schemes are complementary and should yield converging results, (otherwise, something's wrong)**



## Conclusion and perspective

- ✓ Calorimetry experiment allowed the successful extraction of  $^{254}\text{No}$ 's  $B_f$
- ✓  $B_f(0) = 6,6 \pm 0,9 \text{ MeV}$ ,  $J_{\text{saddle}} = 125 \pm 60 \text{ } \hbar^2/\text{MeV}$
- ✓ Experimental  $B_f$  in *better* agreement with mic-mac prediction than DFT



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- ? What other measurement can benchmark fission barrier (and other) properties ?
- ? How **accurately** can we measure, predict them ?

## Read more:

- P. Reiter, T. L. Khoo, et al., Phys. Rev. Lett. 84, 3542 (2000).
- A. Heinz, T. Khoo, P. Reiter, et al., Nucl. Phys. A682, 458 (2001).
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- G. Henning, Ph.D. thesis, Université Paris Sud, 2012.
- G. Henning, A. Lopez-Martens, T.L. Khoo, D. Seweryniak et al., Phys. Rev. Lett. 113, 262505(2014)

Greg Henning,<sup>1,2,\*</sup> T. L. Khoo,<sup>2</sup> A. Lopez-Martens,<sup>1</sup> D. Seweryniak,<sup>2</sup> M. Alcorta,<sup>2</sup> M. Asai,<sup>3</sup>  
B. B. Back,<sup>2</sup> P. Bertone,<sup>2</sup> D. Boilley,<sup>4,5</sup> M. P. Carpenter,<sup>2</sup> C. J. Chiara,<sup>2,6</sup> P. Chowdhury,<sup>7</sup> B. Gall,<sup>8</sup>  
P. T. Greenlees,<sup>9</sup> G. Gurdal,<sup>10</sup> K. Hauschild,<sup>1</sup> A. Heinz,<sup>11</sup> C. R. Hoffman,<sup>2</sup> R. V. F. Janssens,<sup>2</sup>  
A. V. Karpov,<sup>12</sup> B. P. Kay,<sup>2</sup> F. G. Kondev,<sup>2</sup> S. Lakshmi,<sup>7</sup> T. Lauristen,<sup>2</sup> C. J. Lister,<sup>7</sup> E. A. McCutchan,<sup>2</sup>  
C. Nair,<sup>2</sup> J. Piot,<sup>8</sup> D. Potterveld,<sup>2</sup> P. Reiter,<sup>13</sup> N. Rowley,<sup>14</sup> A. M. Rogers,<sup>2</sup> and S. Zhu<sup>2</sup>

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