

DE LA RECHERCHE À L'INDUSTRIE



# Optimization at the multireference level

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CEA, DAM, DIF

Workshop ESNT

27 NOVEMBRE 2014

DE LA RECHERCHE À L'INDUSTRIE

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## How we fitted D1M ?

Workshop ESNT

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## Collaborators :

S. Goriely

S. Péru

M. Girod

M. Martini

J.P. Ebran

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# GENERAL MOTIVATION

Providing nuclear reaction models with « **credible and coherent** » microscopic inputs

- makes (really) sense when dealing with unmeasured target
- the sounder the underlying physics the better the predictive power
- no direct link between xs and n-n interaction for **all nuclei**
- **many inputs** needed
  - . Discrete levels properties (masses, J, p, deformation etc ...)
  - . Nuclear level densities up to 200MeV
  - . Gamma strength functions
  - . Fission properties (barriers, broken symmetries, = path)
  - . Optical potential (spherical and deformed)
- all this can be derived from nuclear structure more or less directly
- all this can be used mostly through tables
- robust codes needed
- robust methodology (recipes)
  - . to reduce human intervention while producing tables
  - . to fill gaps (even-even limitation for instance)

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All this has been done with Skm for all nuclei (S. Goriely) !

Let's do it with Gogny !

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All this has been done with Skm for all nuclei (S. Goriely) !

Let's do it with Gogny !

- ⇒ We have codes
- ⇒ We have computers
- ⇒ We have experts (not me !)
- ⇒ We have motivation (me !)



# PLAN

- Motivation



- Motivation
- The starting point : D1S, D1N

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- Results
- Perspectives

**THE STARTING POINT : D1S, D1N**

**A little bit of history**

# D1 type Gogny interaction

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- **First interaction D1 in 1980** (*Dechargé et al., PRC21 (1980) 1568*)
  - Phenomenologic effective interaction
  - 14 parameters adjusted on nuclear matter properties and few data for  $^{16}\text{O}$ ,  $^{48}\text{Ca}$ ,  $^{90}\text{Zr}$ ,  $^{208}\text{Pb}$
  - Specificity : finite range in central term :
    - ⇒ interaction usable for mean field and pairing (HFB) and beyond
  - provide globally good results
  - requires significant computation time (up to 10' for 14 H.O shells)

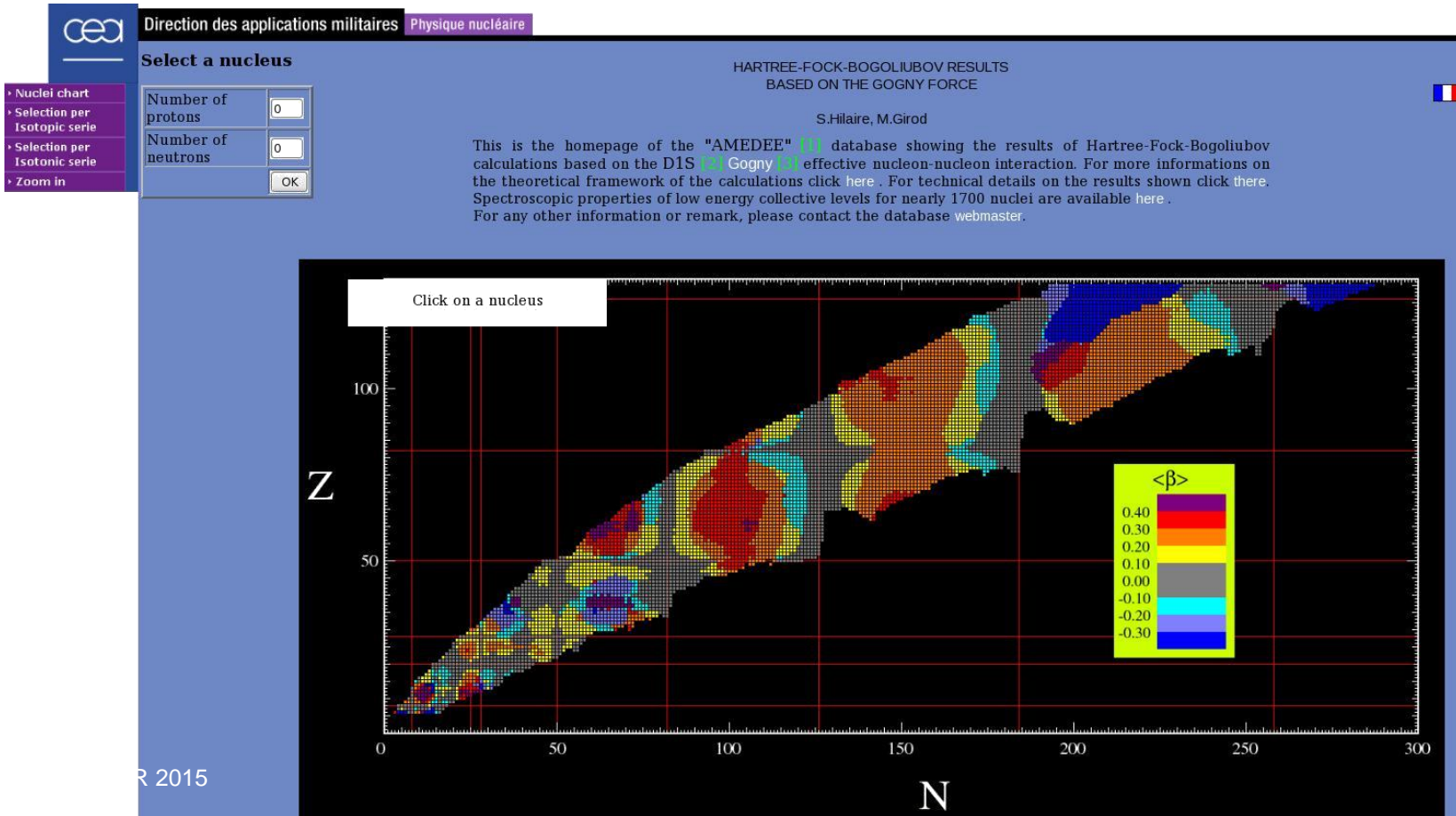
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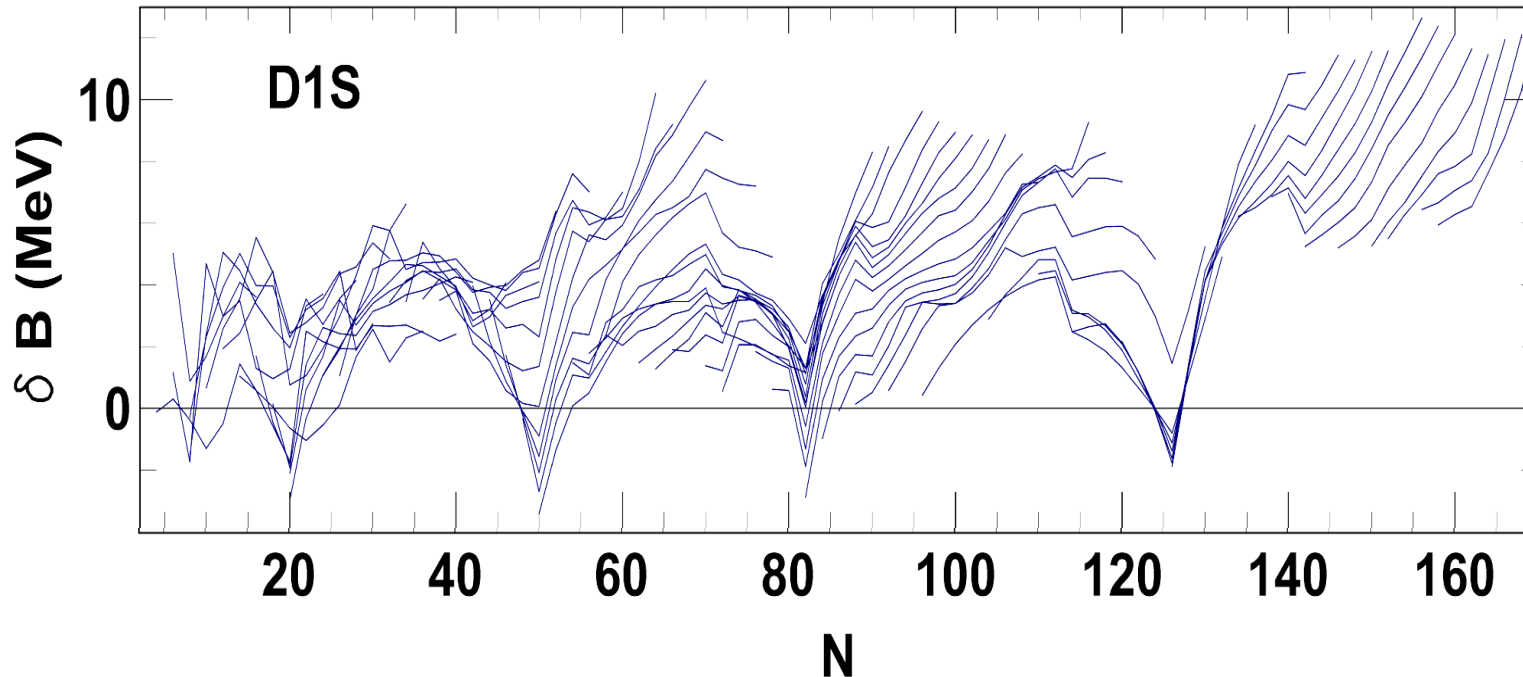
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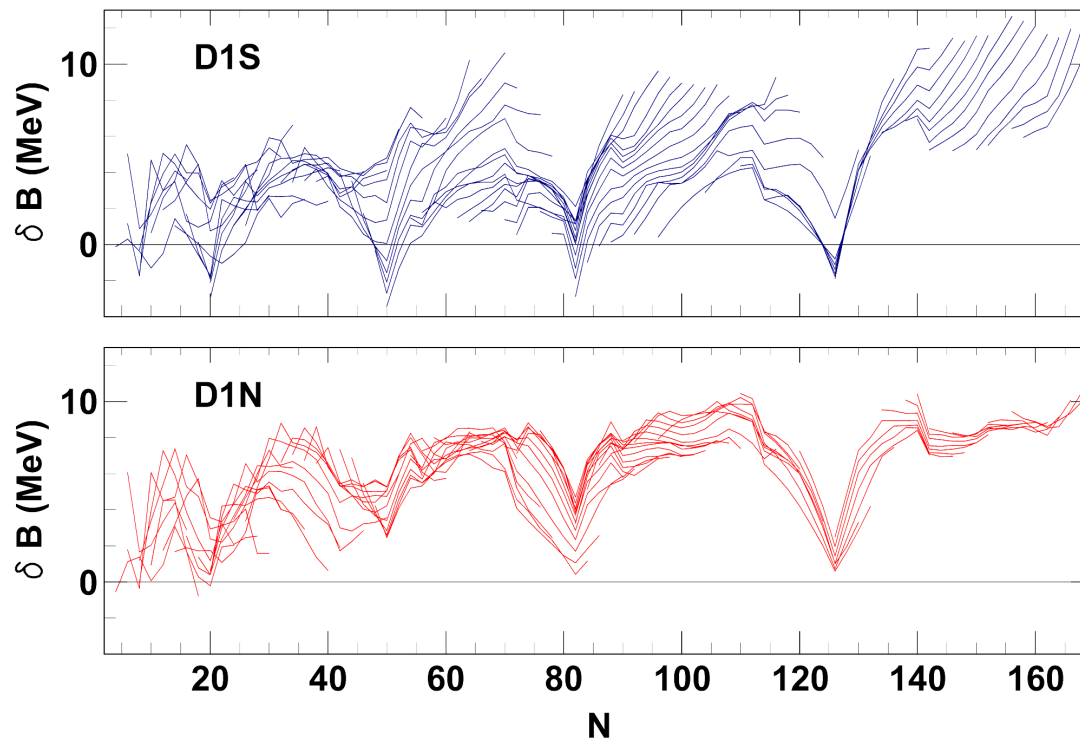
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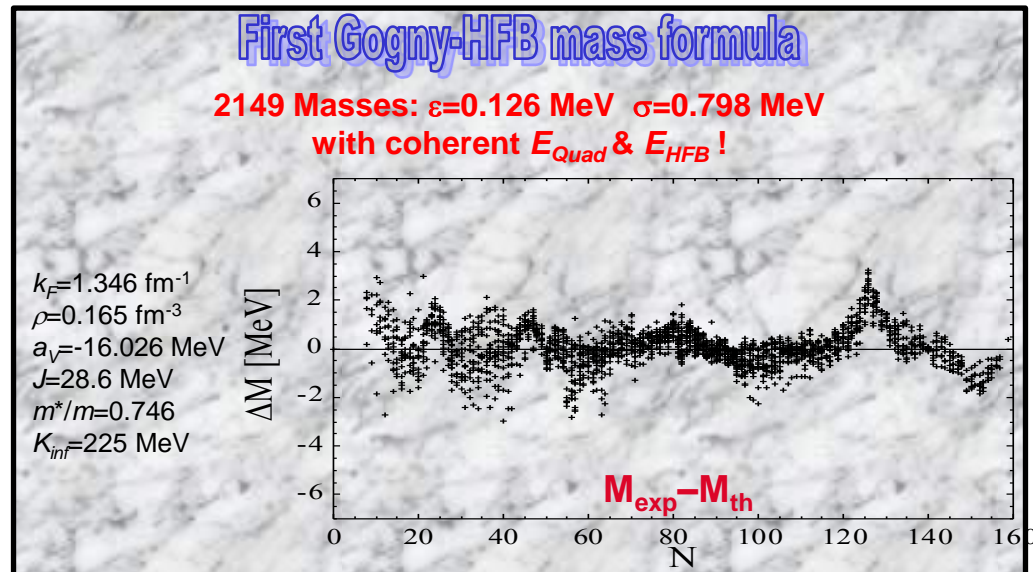
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- **D1S « benchmarking » in 2010** (*Delaroche et al., PRC 81 (2010) 014303*)

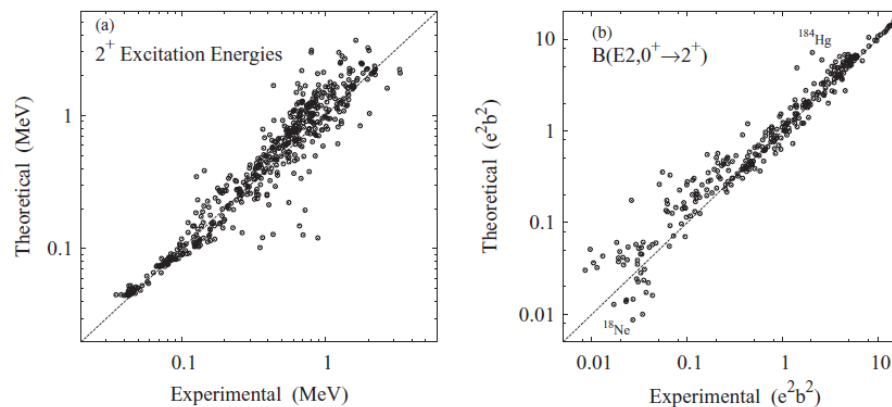


FIG. 11. (a) Theoretical  $2^+$  excitation energies of 537 even-even nuclei as a function of their experimental values. (b) Theoretical  $B(E2; 0^+ \rightarrow 2^+)$  transition strengths of 320 even-even nuclei as a function of their experimental values. Several cases showing deviations are labeled by the nucleus. Experimental data are from Refs. [56,57].

# D1 type Gogny interaction

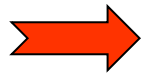
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**New interactions more frequently**



**Clear will to reduce pathologies**



**Link with computer power**



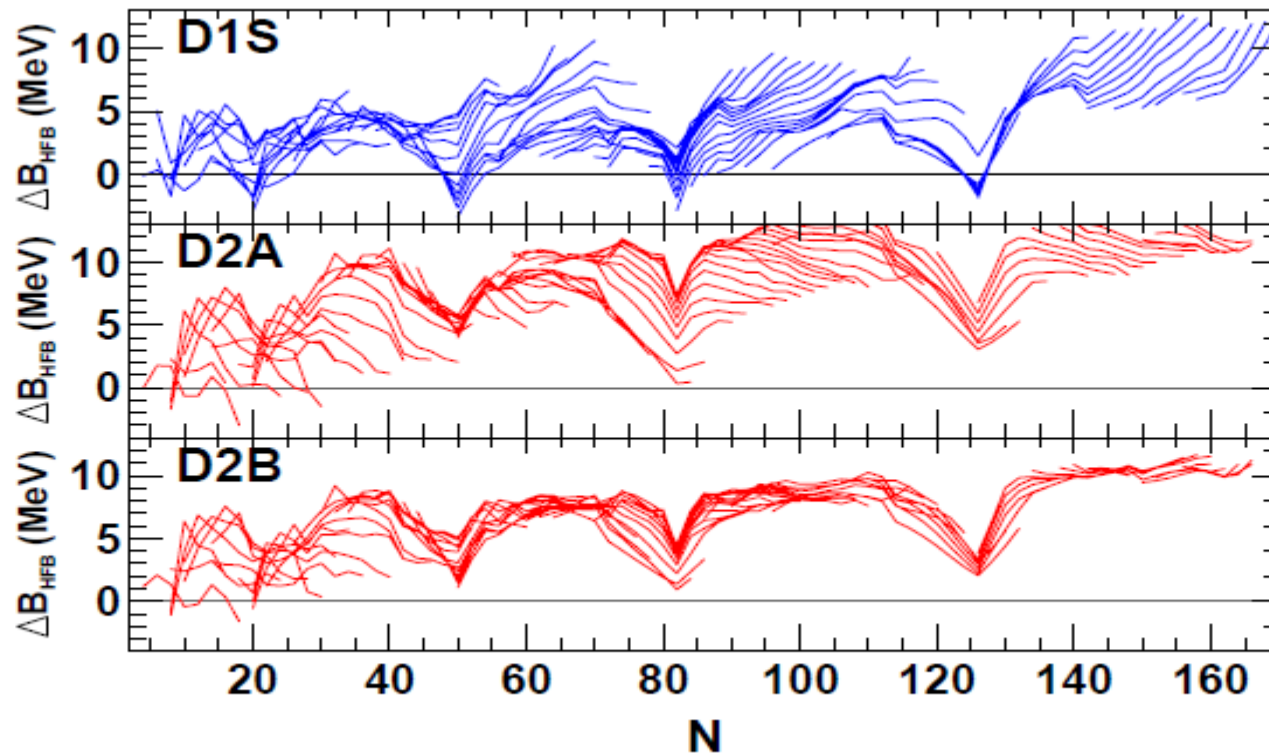
**Things have not been made in order**

# D2 type interaction(s)

D1 (1980)

D1S (1991) : surface properties improved (fission)

D2 (2007) : finite range in density dependent term (PRC 2015)



# D2 type interaction(s)

D1 (1980)

D1S (1991) : surface properties improved (fission)

D2 (2007) : finite range in density dependent term (PRC 2015)

D1N (2008) : better neutron matter EOS description

D1M (2009) : better description of binding energies and  $Q_{\text{reaction}}$

➡ **New interactions more frequently**

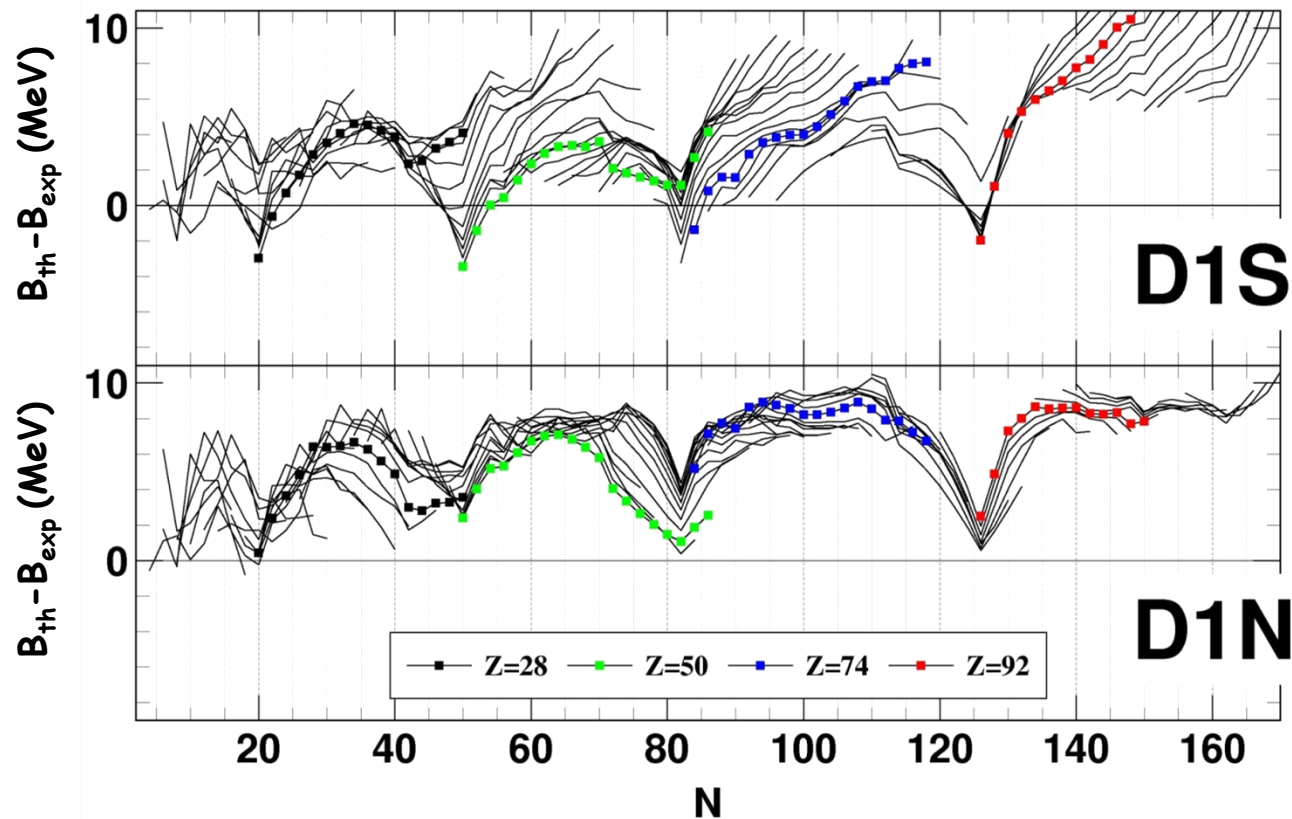
➡ **Clear will to reduce pathologies**

➡ **Link with computer power**

➡ **Things have not been made in order**



## Summary : D1S, D1N



⇒ Challenge in 2008 : Reduce the r.m.s of binding energies differences  
 Other properties similar or better  
 Cope with local criticisms  
 Obey Bruyères Golden Rule

## *ONE SHALL ONLY DESIGN EFFECTIVE INTERACTIONS*

- ❖ for both mean field and beyond mean field predictions*
- ❖ for all nuclei*
- ❖ for all nuclear properties*

⇒ Challenge in 2008 : Reduce the r.m.s of binding energies differences  
Other properties similar or better  
Cope with local criticisms  
Obey Bruyères Golden Rule

# **METHODOLOGY, CODES**

# Methodology used to fit D1S or D1N

$$\begin{aligned}
 v_{12} = & \sum_{j=1}^2 \exp \left[ - \left( \frac{|\vec{r}_1 - \vec{r}_2|}{\mu_j} \right)^2 \right] (W_j + B_j P_\sigma - H_j P_\tau - M_j P_\sigma P_\tau) \\
 & + t_3 (1 + x_3 P_\sigma) \delta (r_1 - r_2) \rho^\alpha \left( \frac{r_1 + r_2}{2} \right) \\
 & + i W_{ls} \overleftarrow{\nabla}_{12} \cdot \delta (r_1 - r_2) \wedge \overrightarrow{\nabla}_{12} \cdot (\vec{\sigma}_1 + \vec{\sigma}_2) \\
 & + \frac{(1 - 2\tau_1^z)(1 - 2\tau_2^z)}{4} \frac{e^2}{|\vec{r}_1 - \vec{r}_2|}
 \end{aligned}$$

➔ **Finite range** : avoid pathologies “beyond HF” due to unrealistic behavior of 0-range forces at high relative momenta

## Methodology used to fit D1S or D1N

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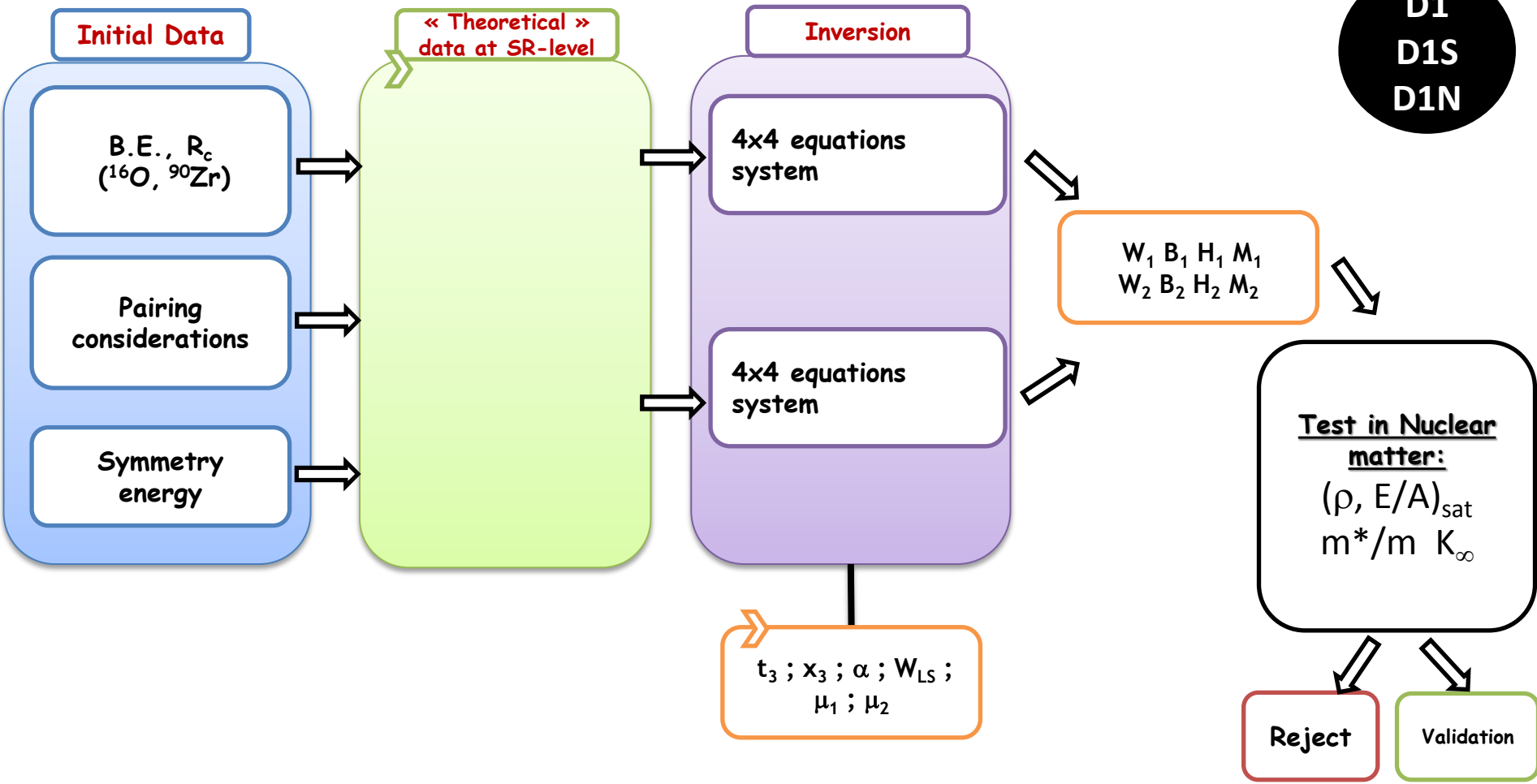
**14 parameters to fit**

➔ **Finite range** : avoid pathologies “beyond HF” due to unrealistic behavior of 0-range forces at high relative momenta

# Methodology used to fit D1S or D1N

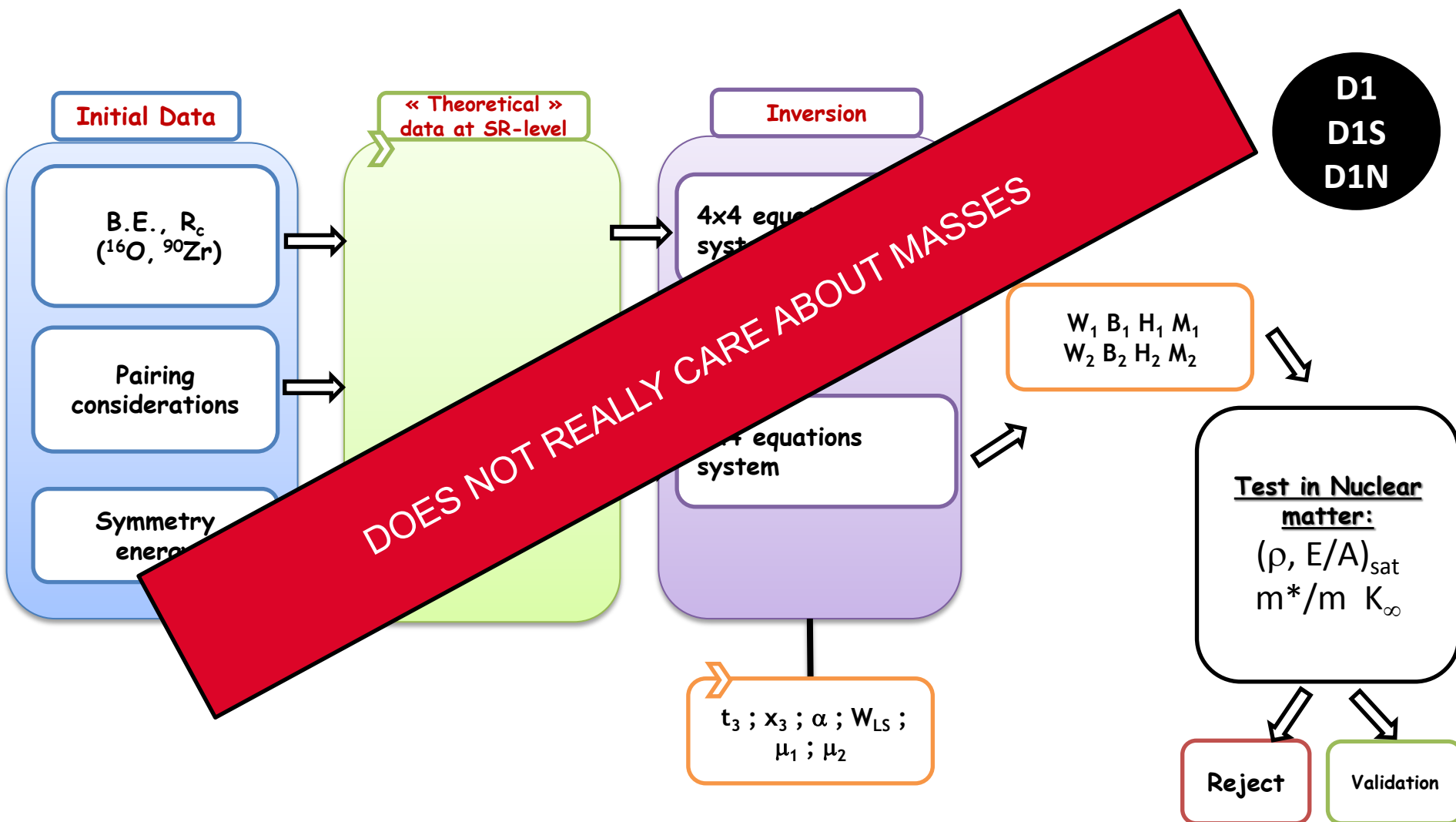
⇒ “Traditional” method involving small set of magic nuclei (!!!) at SR-level

**D1**  
**D1S**  
**D1N**



# Methodology used to fit D1S or D1N

⇒ “Traditional” method involving small set of magic nuclei (!!!) at SR-level



## How can we compute binding energies ?

$$B = B(N_0) + \Delta_\infty + \Delta_{\text{quad}}$$

⇒ Infinite basis correction : code AMEDEC

$$\Delta_\infty = E(N_0) - E(N = +\infty)$$

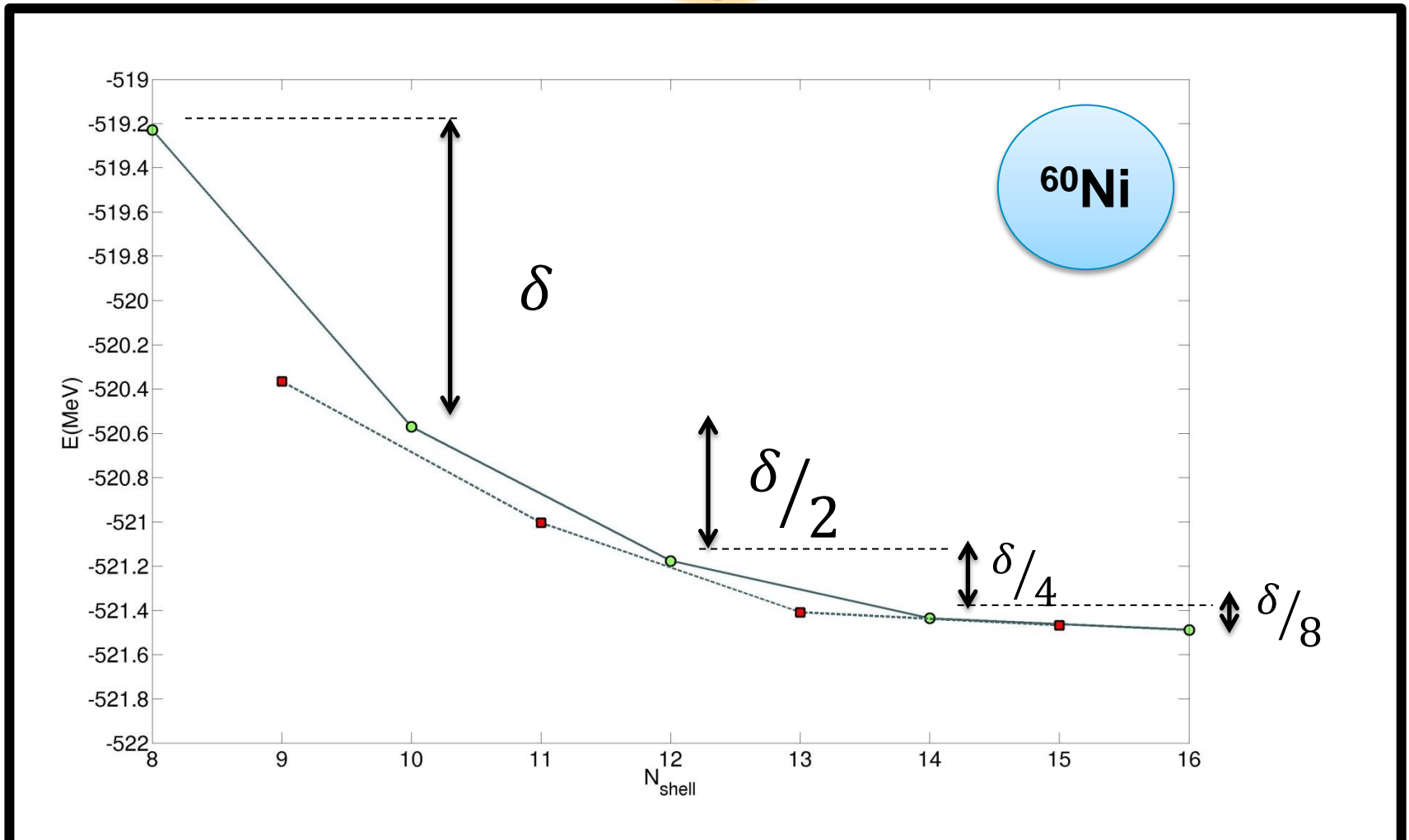
⇒ Assumption

$$\Delta_\infty = 2[E(N_0) - E(N_0 + 2)]$$



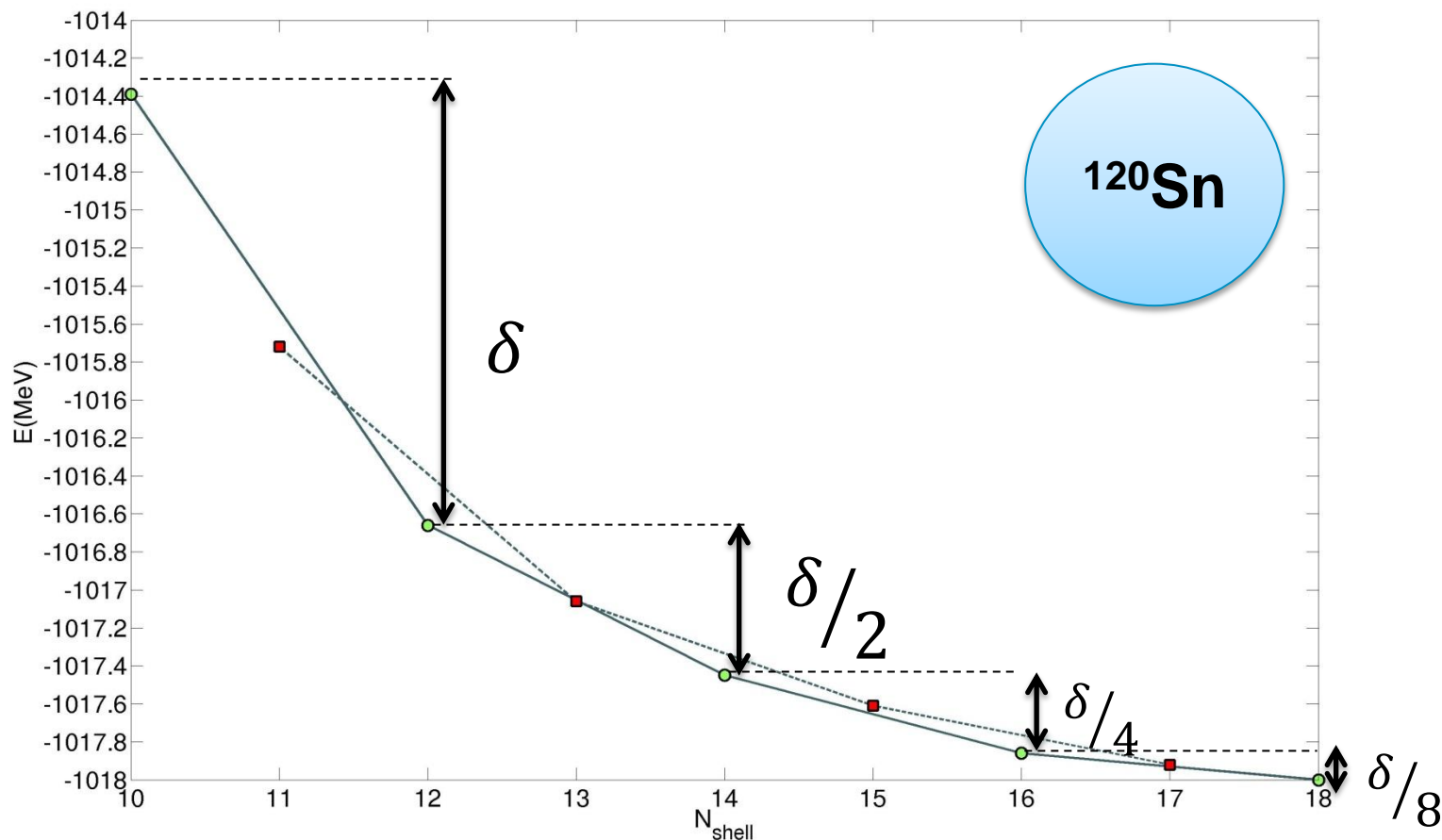
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## How can we compute binding energies ?

$$B = B(N_0) + \Delta_\infty + \Delta_{\text{quad}}$$

$$\Delta_{\text{quad}} = ESR - EMR$$

⇒ GCM + GOA : code THEOPHIL + KUMAR

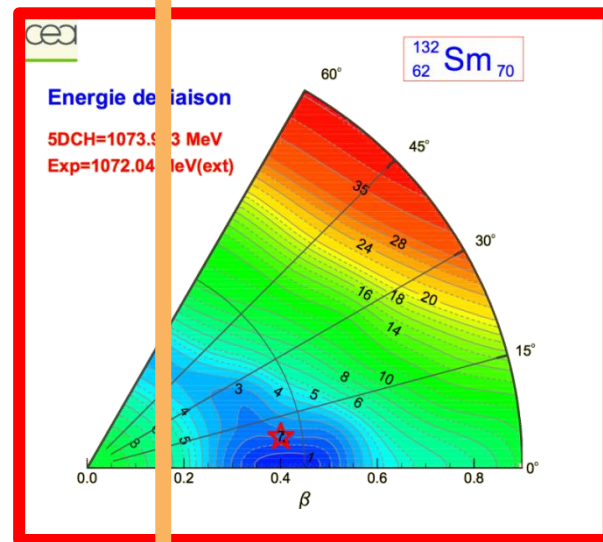
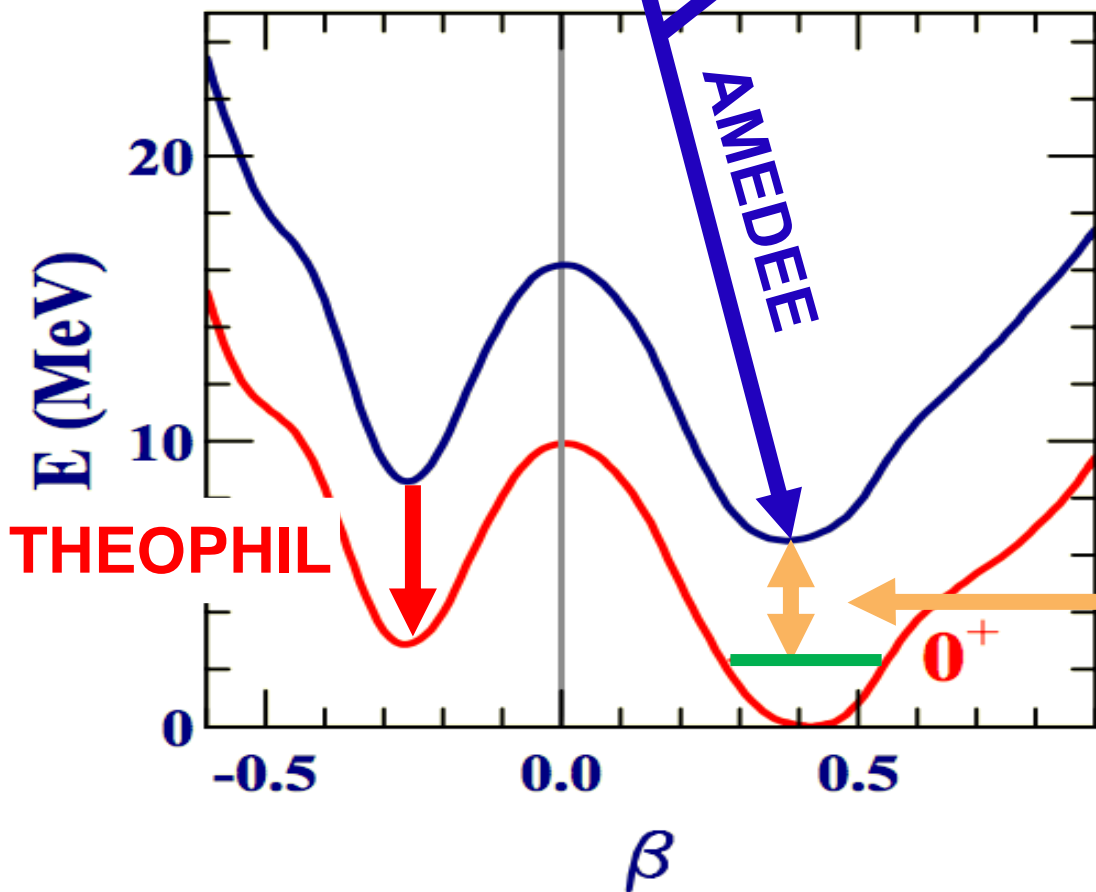
$$\hat{\mathcal{H}}_{\text{coll}} = -\frac{\hbar^2}{2} \sum_{i,j} \frac{\partial}{\partial q_i} [M^{-1}(q)]_{ij} \frac{\partial}{\partial q_j} + \mathcal{V}(q)$$

⇒ M. Girod and B. Grammaticos, Nucl. Phys. **A330** 40 (1979)

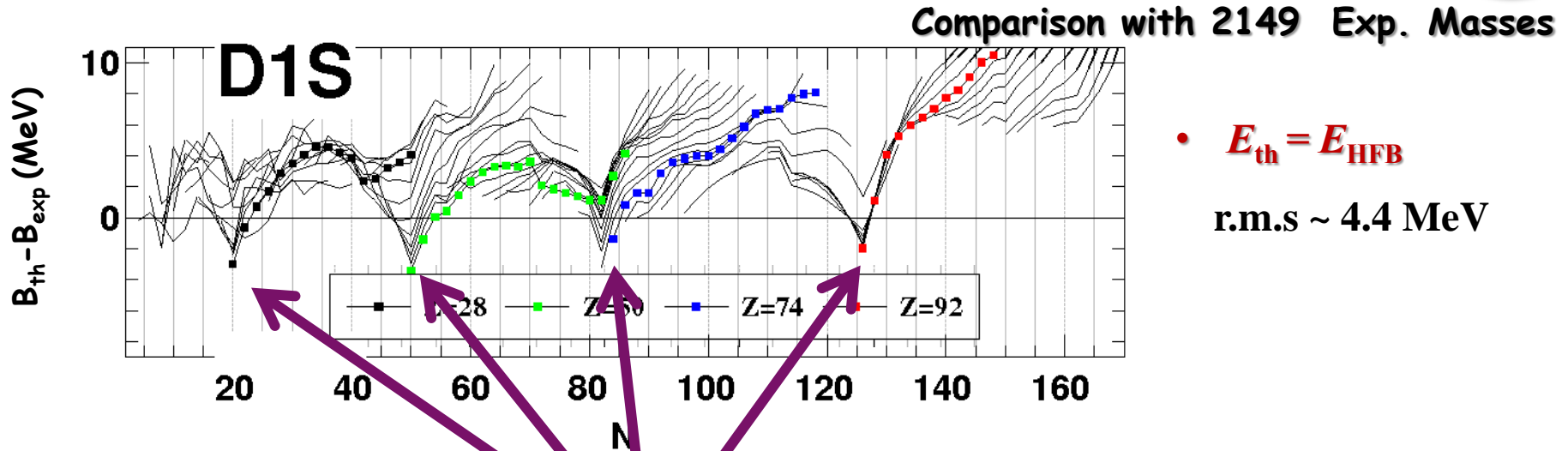
⇒ J. Libert, M. Girod and J.-P. Delaroche, Phys. Rev. **C60** 054301 (1999)

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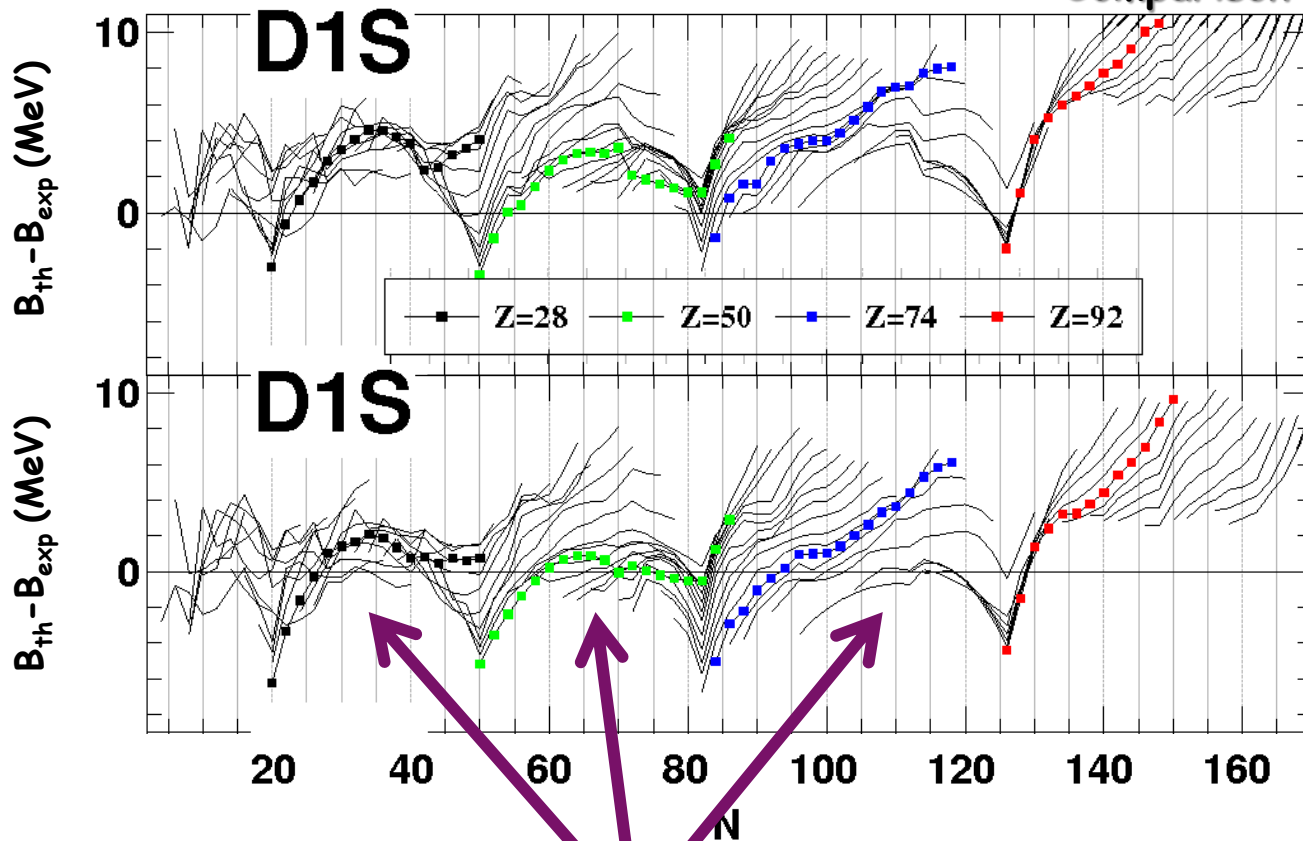
KUMAR



- $E_{th} = E_{HFB}$   
r.m.s ~ 4.4 MeV

Adjustment performed  
without  
infinite basis effect estimation  
⇒ Overbinding of 1-3 MeV

Comparison with 2149 Exp. Masses

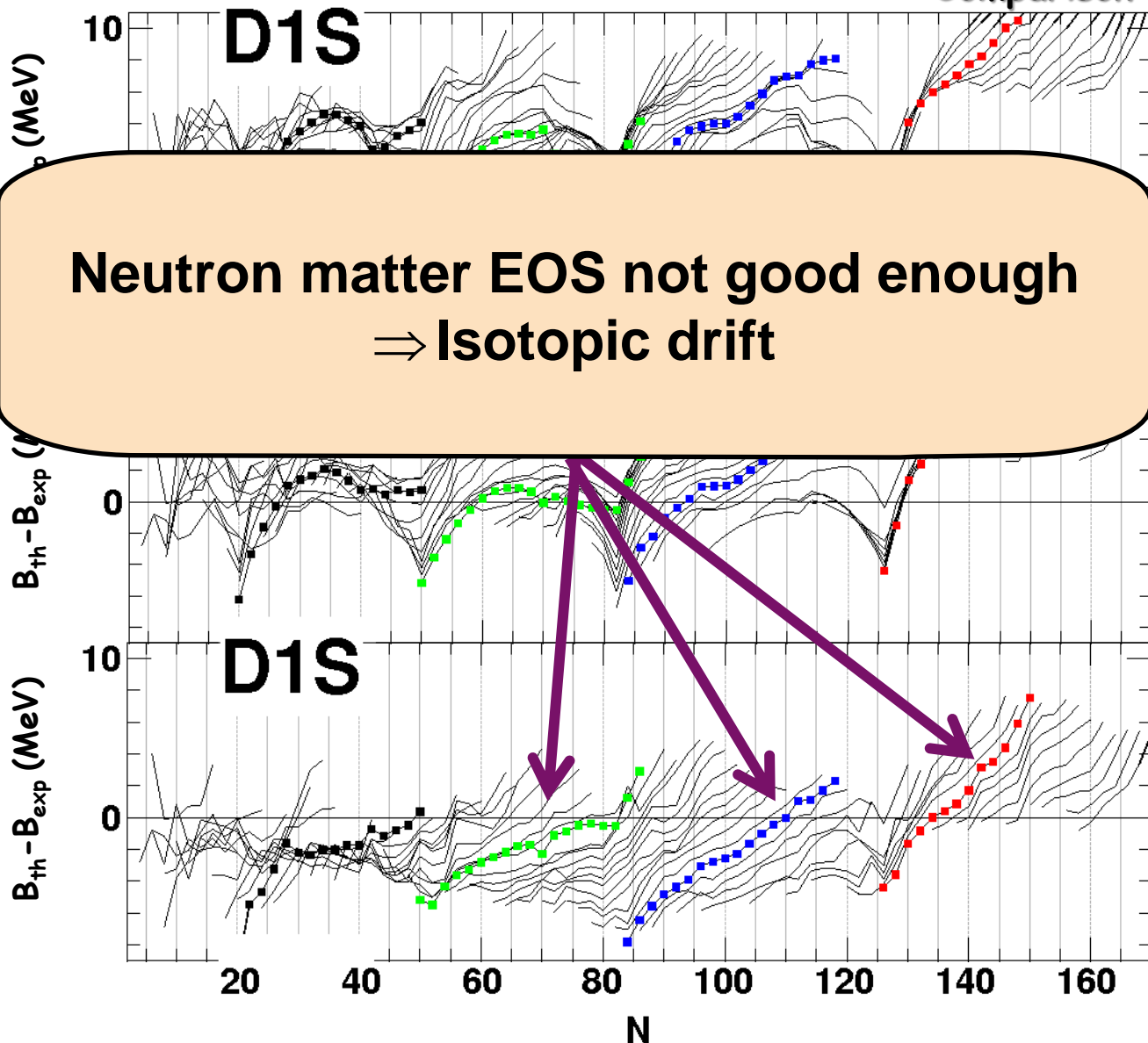


- $E_{th} = E_{HFB}$   
r.m.s ~ 4.4 MeV

- $E_{th} = E_{HFB} - \Delta_{\infty}$   
r.m.s ~ 2.6 MeV

Quadrupole correlations missing  
⇒ Arches between magic nuclei

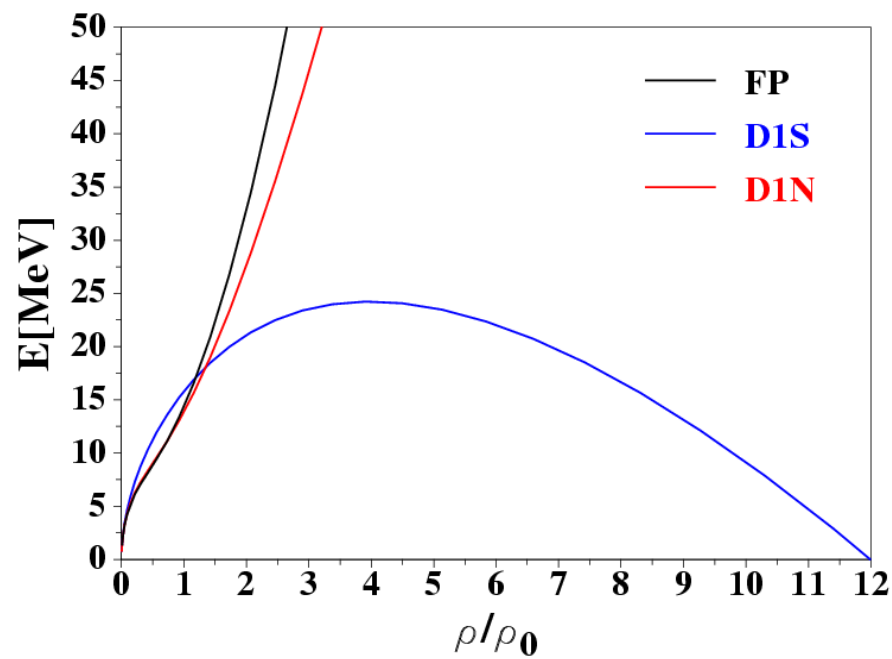
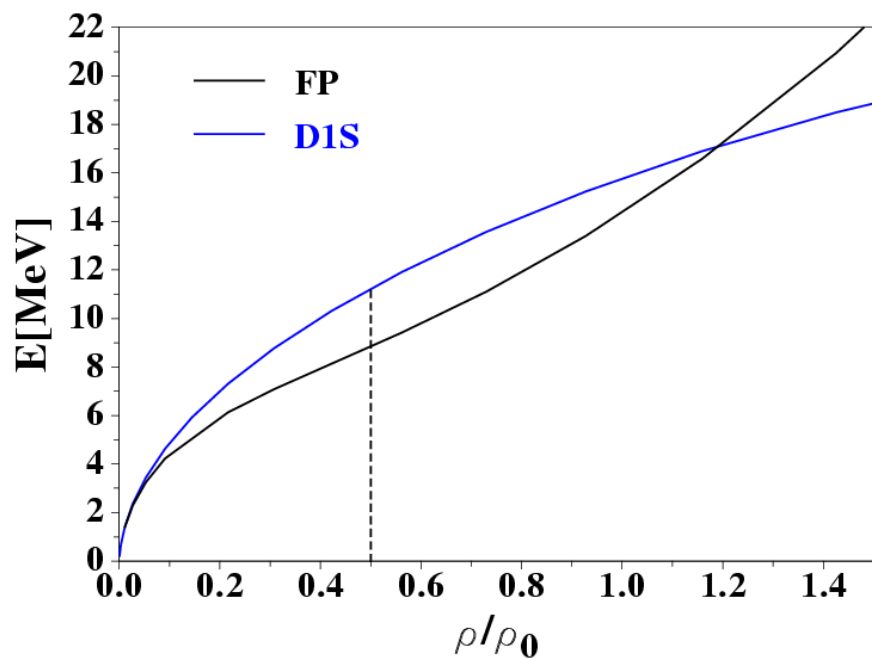
Comparison with 2149 Exp. Masses



Neutron matter EOS not good enough  
=> Isotopic drift

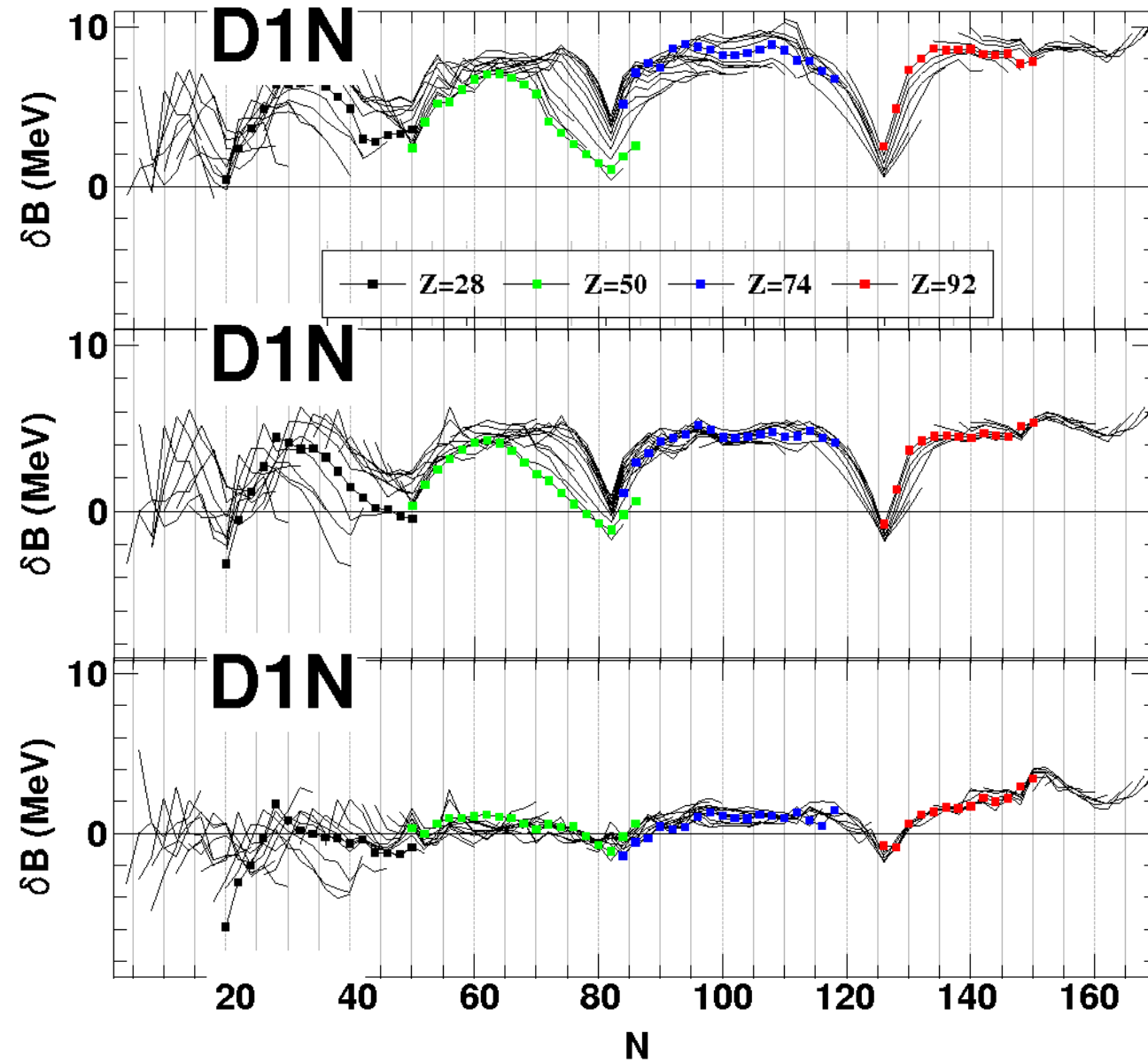
- $E_{th} = E_{HFB}$   
r.m.s ~ 4.4 MeV
- $E_{th} = E_{HFB} - \Delta_{\infty}$   
r.m.s ~ 2.6 MeV
- $E_{th} = E_{HFB} - \Delta_{\infty} - \Delta_{quad}$   
r.m.s ~ 2.9 MeV

# D1N : better neutron matter EOS !



⇒ F. Chappert, M. Girod & S. Hilaire, Phys. Lett. B668 (2008) 420.





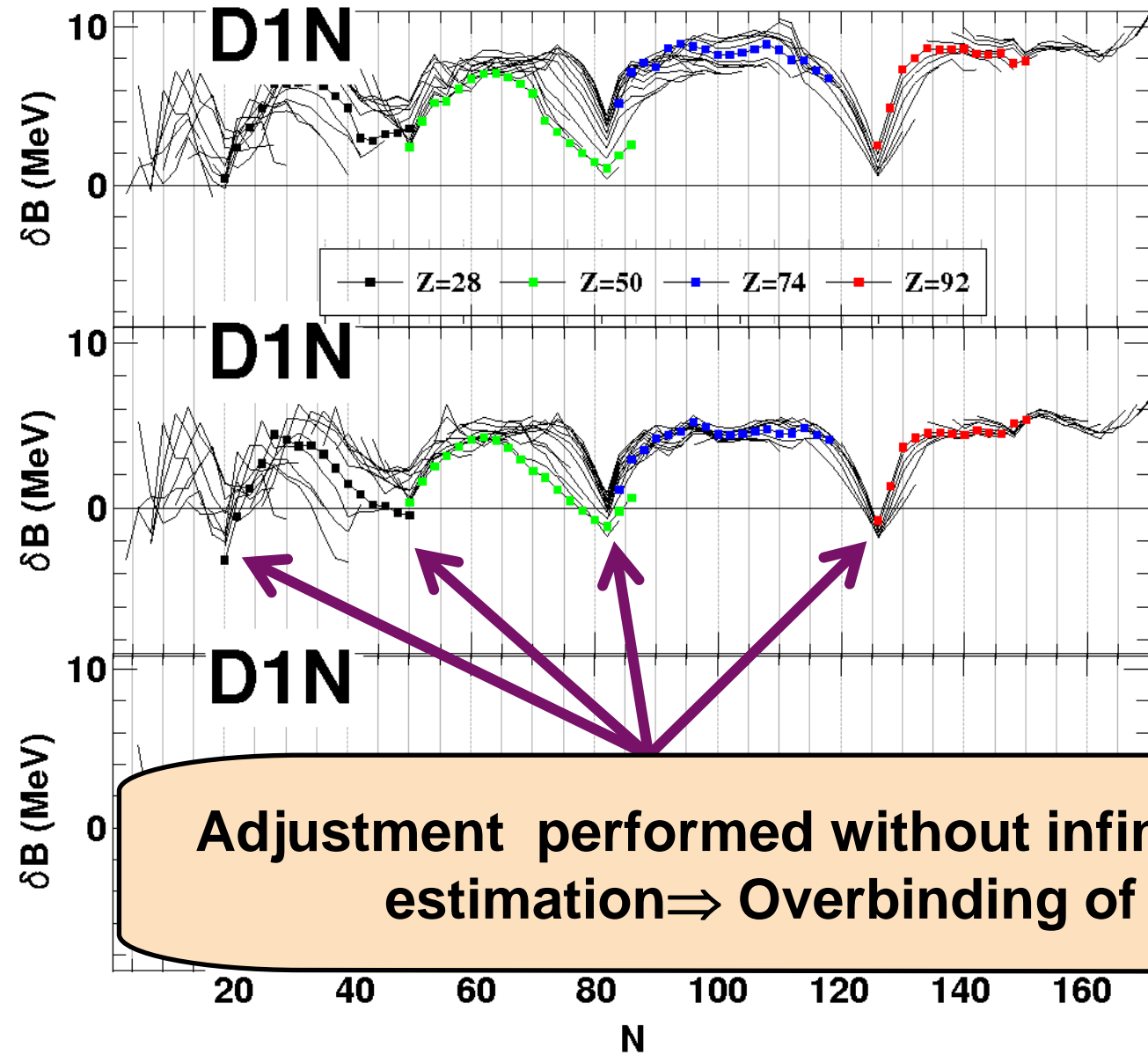
- $E_{th} = E_{HFB}$

r.m.s ~ 2.5 MeV

- $E_{th} = E_{HFB} - \Delta_{\infty}$

- $E_{th} = E_{HFB} - \Delta_{\infty} - \Delta_{quad}$

r.m.s ~ 1 MeV



- $E_{th} = E_{HFB}$   
r.m.s  $\sim 2.5$  MeV

- $E_{th} = E_{HFB} - \Delta_{\infty}$

- $E = E_{HFB} - \Delta_{\infty} - \Delta_{med}$

Adjustment performed without infinite basis effect estimation  $\Rightarrow$  Overbinding of 1-3 MeV

# The new fitting procedure

⇒ Make use of the huge data on masses and incorporate a minimum of effectivity in the functional ⇒ MR-level = the best formalism we can use

Parameters kept constant: 4 (can be included in the fit)

4

$\mu_1=0.7-0.8 ; \mu_2=1.2 ; x_3=1 ; \alpha=1/3$  (0.2-0.5 investigated)

D1M

Parameters constrained: 3

- $J \sim 29 - 32$  MeV to reproduce at best neutron matter EoS
- $K \sim 230 - 240$  MeV as expected from exp. breathing mode data
- $k_F$  kept constant to reproduce charge radii at best (manually adjusted)

Parameters directly fitted to nuclear masses at MR-level: 7

5

$(a_v, m^*, W_1, M_1, B_2, H_2, W_{so})$

Matrix inversion gives the rest

5

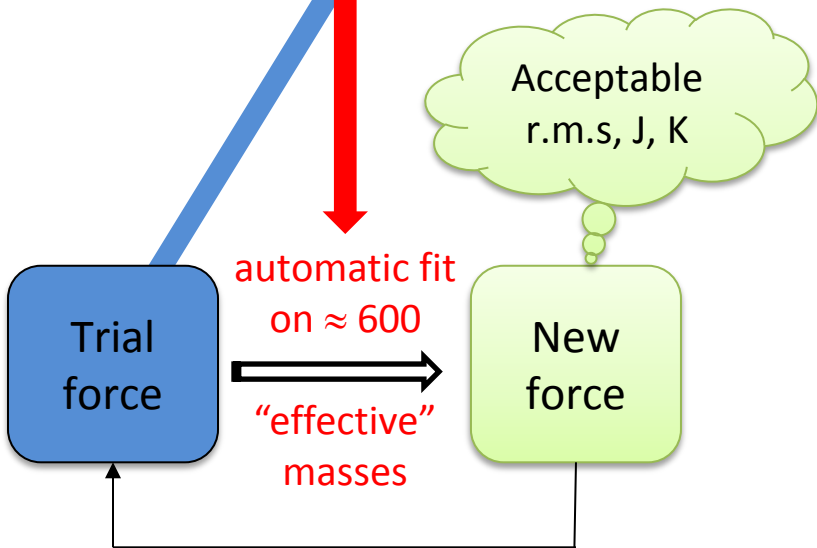
$(a_v, J, m^*, K, k_F) \longleftrightarrow (B_1, H_1, W_2, M_2, t_3)$

# The new fitting procedure

$$\{B_{exp} + \Delta_{\infty} + \Delta_{quad}\}$$

For 1/3 of 2149 exp masses (Audi *et al* 2003) excluding N=Z, N=Z±1, N=Z±2 nuclei

Interpolated for odd-odd and odd-even using neighboring even-even nuclei

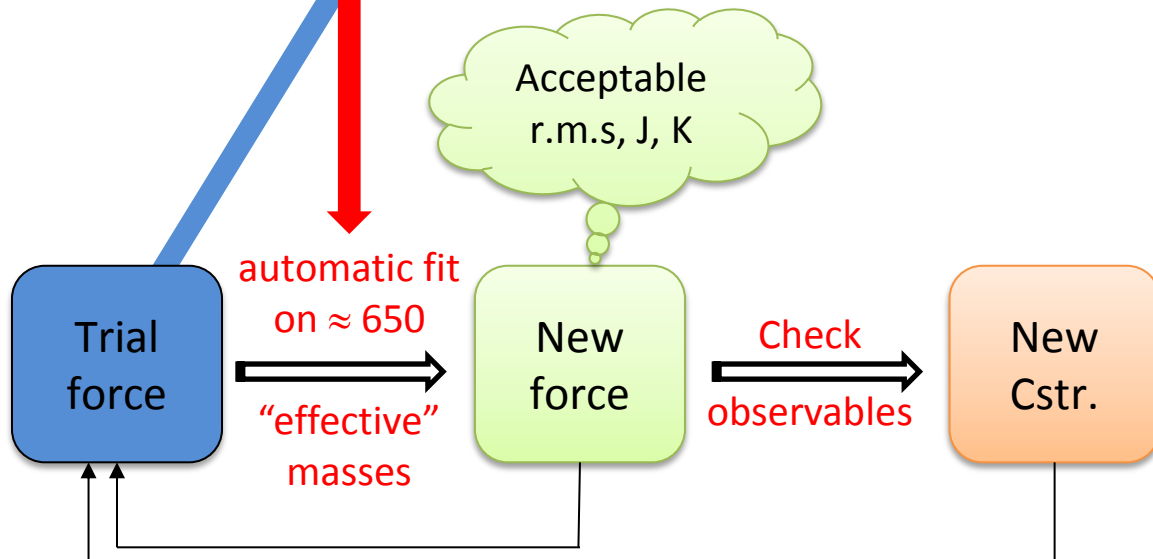


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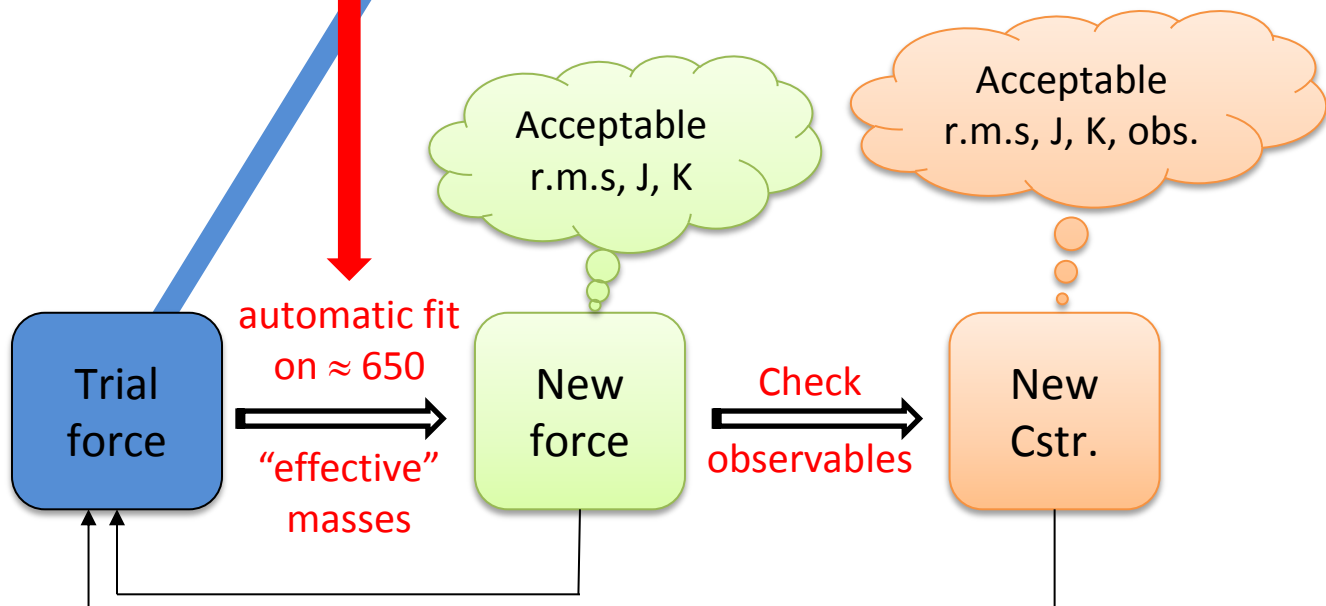


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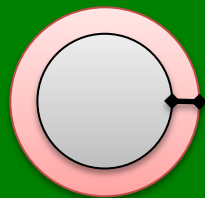


# The new fitting procedure

$$\{B_{exp} + \Delta_{\infty} + \Delta_{quad}\}$$

For ex  
neig

≈ 200/782 exp. charge radii  
with dynamical correction  
Play on  $k_F$  to adjust globally



r.m.s, J, K

Acc  
r.m.s

Landau Parameters (stability, sum rules,  
 $G_0 \sim 0$ ;  $G_0' \sim 0.9-1$  (Borzov et al. 1981))

Trial  
force

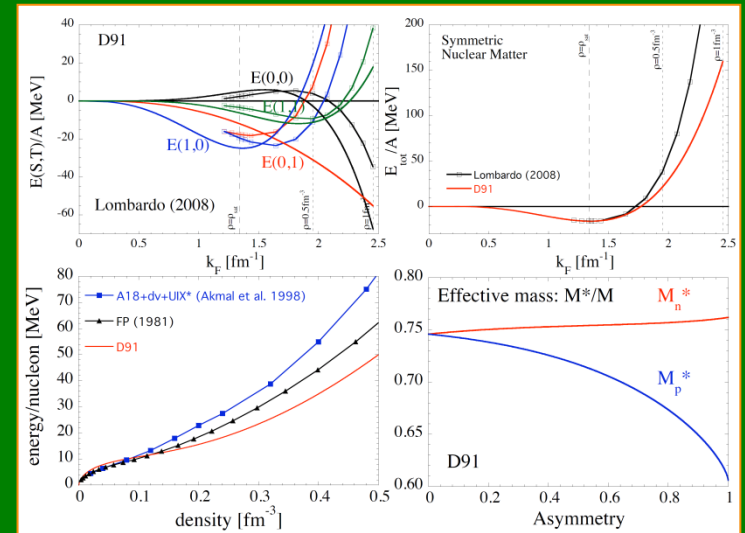
automatic fit  
on ≈ 650  
"effective"  
masses

New  
force

Check  
observables

New  
Cstr.

## Nuclear Matter Properties



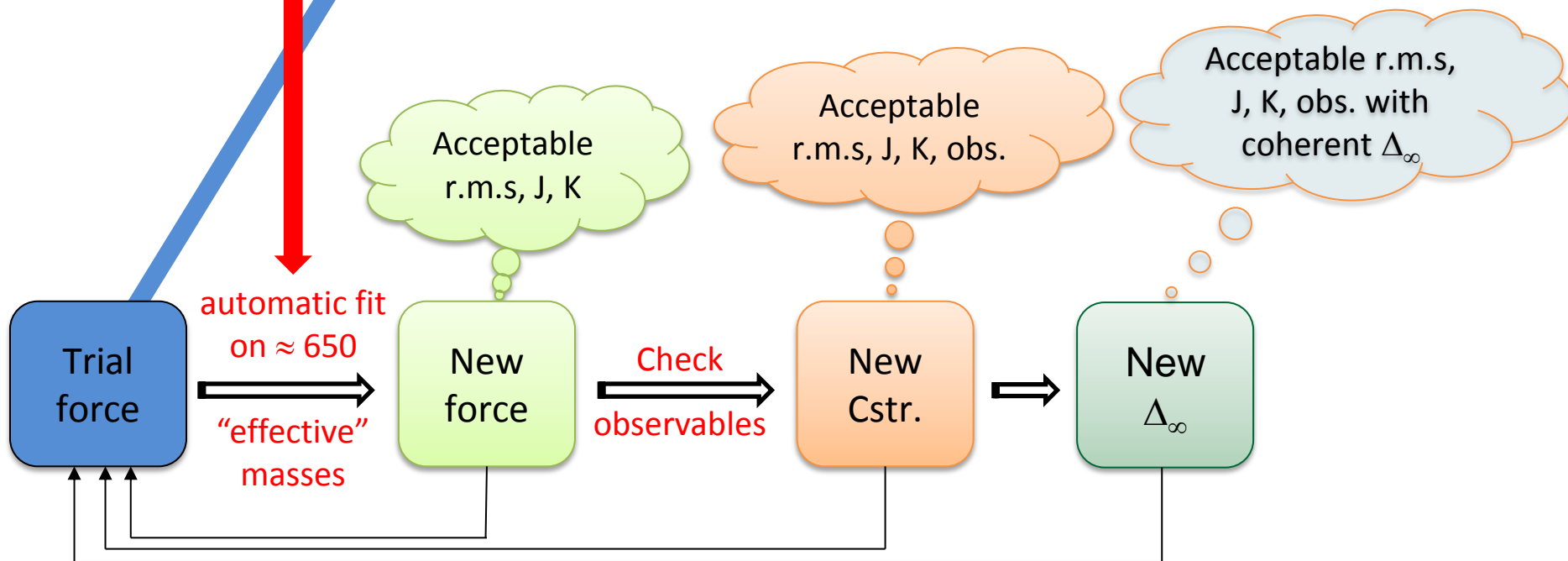
+

# The new fitting procedure

$$\{B_{exp} + \Delta_{\infty} + \Delta_{quad}\}$$

For 1/3 of 2149 exp masses (Audi *et al* 2003) excluding  $N=Z, N=Z\pm 1, N=Z\pm 2$  nuclei

Interpolated for odd-odd and odd-even using neighboring even-even nuclei





# The new fitting procedure

$$\{B_{exp} + \Delta_{\infty} + \Delta_{quad}\}$$

For 1/3 of 2149 exp masses (Audi *et al* 2003) excluding N=Z, N=Z±1, N=Z±2 nuclei

Interpolated for odd-odd and odd-even using neighbors

Acceptable rms, J, K, obs. with coherent  $\Delta_{\infty}$  and  $\Delta_{quad}$

Acceptable r.m.s, J, K

rms, J, K, obs. with coherent  $\Delta_{\infty}$

Trial force

automatic fit on  $\approx 650$  "effective" masses

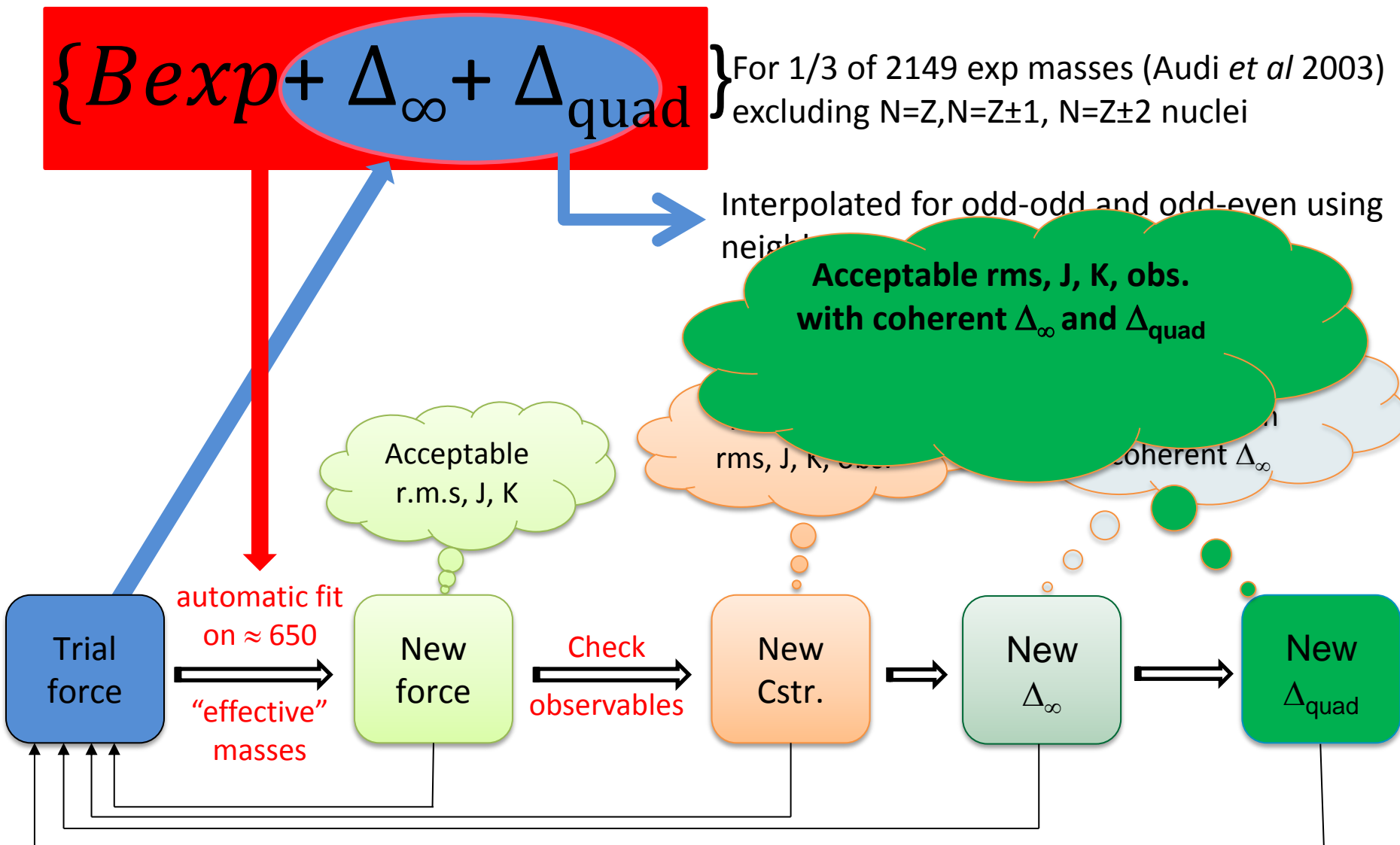
New force

Check observables

New Cstr.

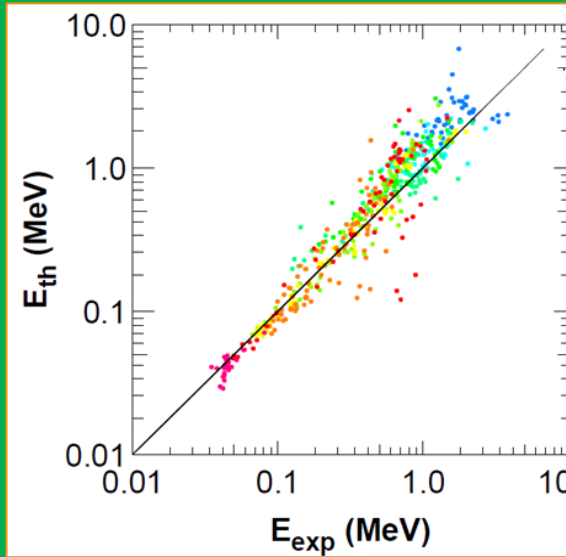
New  $\Delta_{\infty}$

New  $\Delta_{quad}$



# Procedure

## Energy of 2+ levels



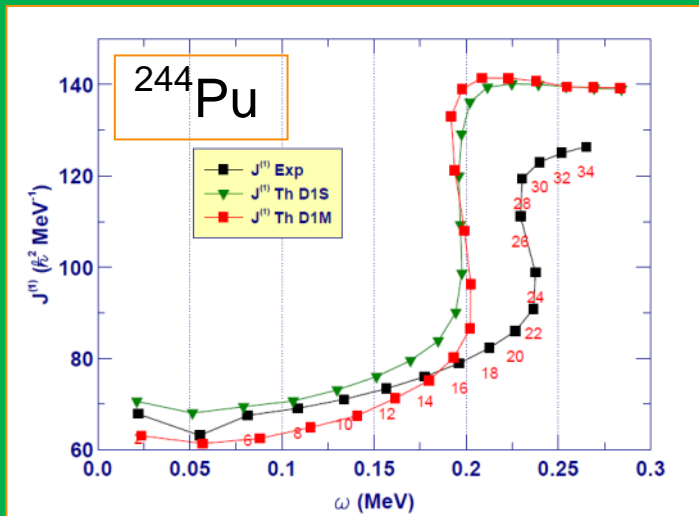
For 1/3 of 2149 exp masses (Audi *et al* 2003) excluding N=Z, N=Z±1, N=Z±2 nuclei

Interpolated for odd-odd and odd-even using neighbors

Acceptable rms, J, K, obs. with coherent  $\Delta_\infty$  and  $\Delta_{quad}$

+  
New observables

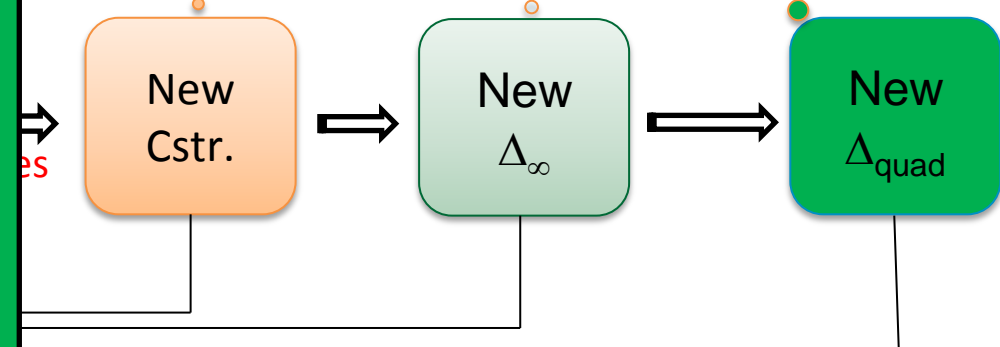
## Moment of inertia



New Cstr.

New  $\Delta_\infty$

New  $\Delta_{quad}$



# The new fitting procedure : time scales

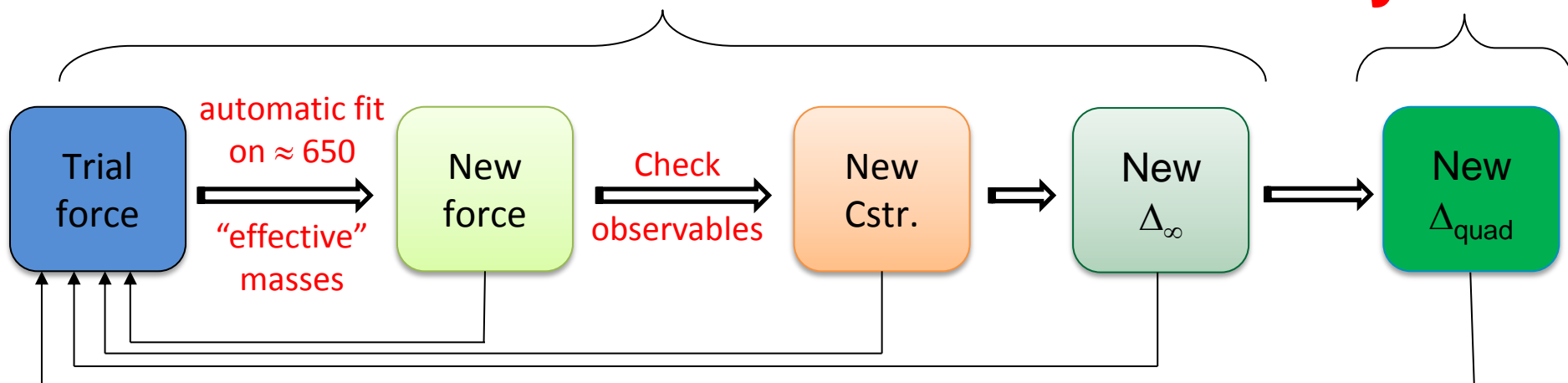
$$\{B_{exp} + \Delta_{\infty} + \Delta_{quad}\}$$

For 1/3 of 2149 exp masses (Audi *et al* 2003) excluding N=Z, N=Z±1, N=Z±2 nuclei

Interpolated for odd-odd and odd-even using neighboring even-even nuclei

**SR**  
months

**MR**  
years



r.m.s(F45)~1.36 MeV with  $E_{\text{Quad}}(\text{D1N})$  but ~2.68 MeV with  $E_{\text{Quad}}(\text{F45})$

r.ms.(F60)~0.97 MeV with  $E_{\text{Quad}}(\text{F45})$  but ~1.32 MeV with  $E_{\text{Quad}}(\text{F60})$

r.m.s(F78)~0.90 MeV with  $E_{\text{Quad}}(\text{F60})$  but ~1.08 MeV with  $E_{\text{Quad}}(\text{F78})$

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**SLOW CONVERGENCE (1 year)**

**COHERENCE DEGRADING r.m.s**

# Convergence issues : next steps on TERA

CCRT : 4 Interactions in 1 year

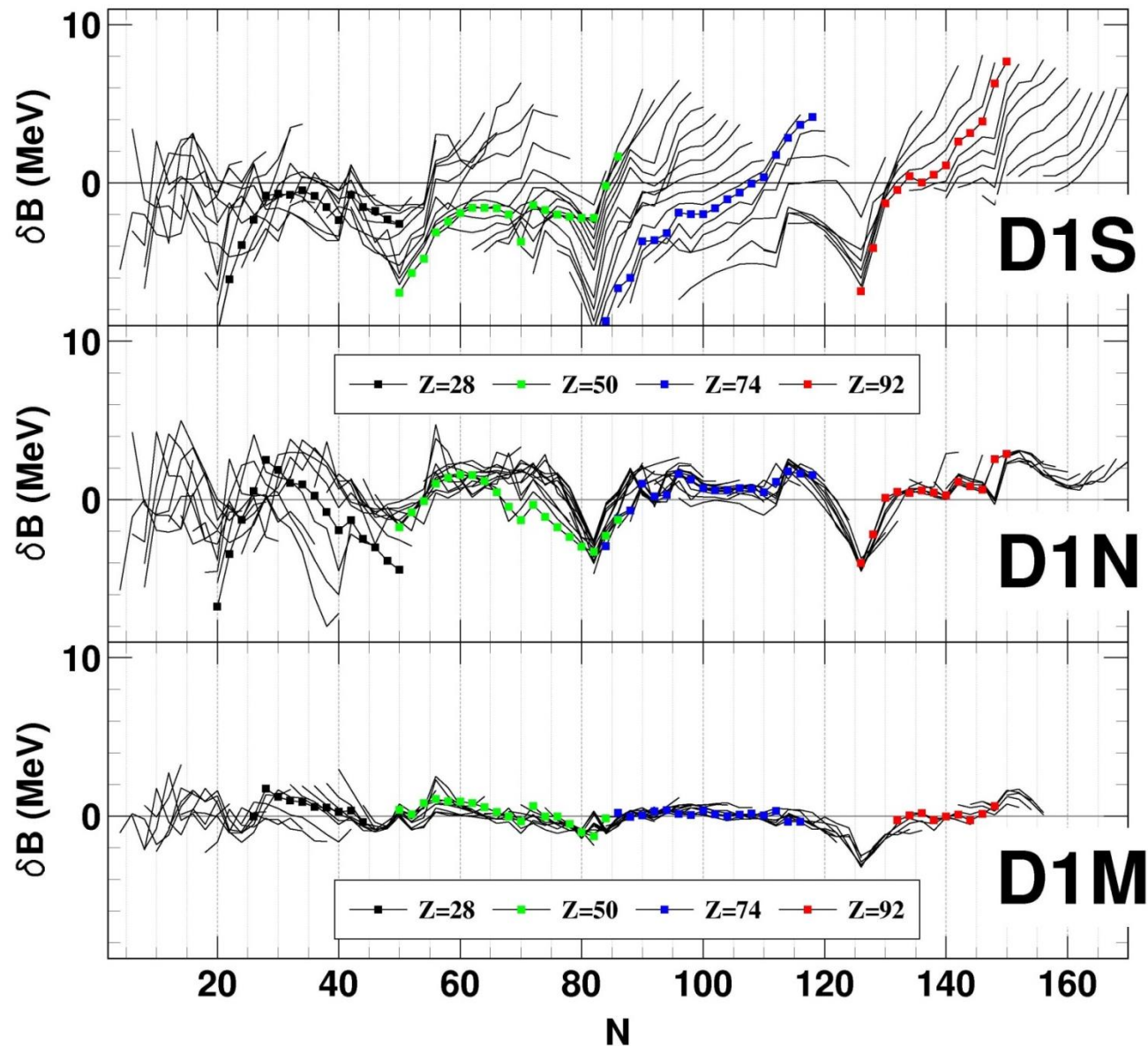
TERA : 15 Interactions in 3 months

	r.m.s masses	r.m.s radii
D08	1.027 MeV	0.0302 fm
D19	1.026 MeV	0.0328 fm
D23	0.857 MeV	0.0302 fm
D28	0.990 MeV	0.0377 fm
D32	0.846 MeV	0.0378 fm
D36	0.954 MeV	0.0385 fm
D38	0.939 MeV	0.0358 fm
D39	0.909 MeV	0.0377 fm
D44	0.853 MeV	0.0312 fm
D45	1.364 MeV	0.0295 fm
D52	0.813 MeV	0.0308 fm
D59	0.893 MeV	0.0304 fm

	r.m.s masses	r.m.s radii
F45	1.365 MeV	0.0295 fm
F60	1.376 MeV	0.0299 fm
F78	1.049 MeV	0.0321 fm
F87	1.360 MeV	0.0299 fm
F91	1.262 MeV	0.0386 fm
F101	1.319 MeV	0.0320 fm

# RESULTS

# Major goal reached : first Gogny mass model !



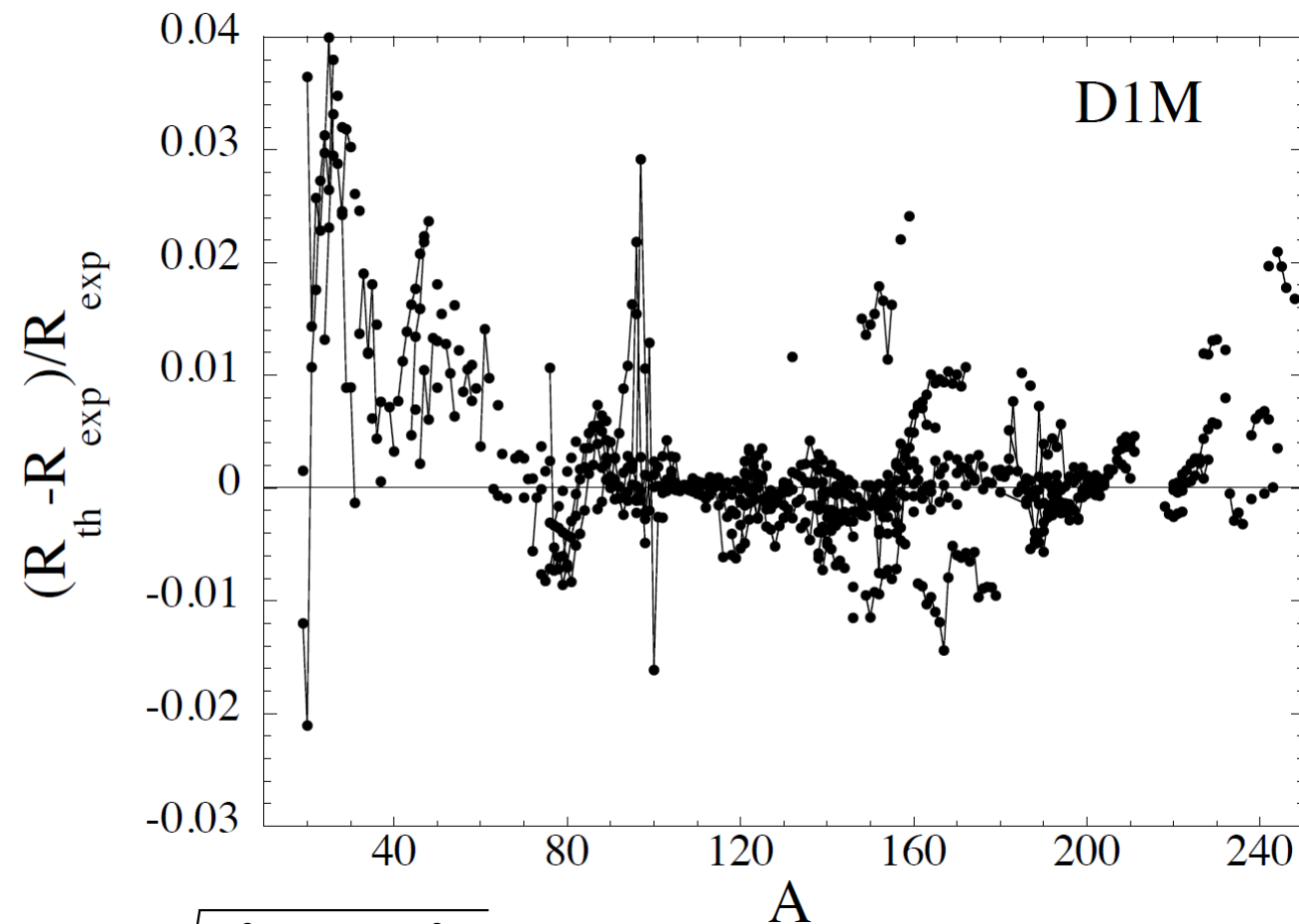
r.m.s ~ 3 MeV

r.m.s ~ 1 MeV

r.m.s = 0.798 MeV



## Comparison with 707 Exp. Charge Radii



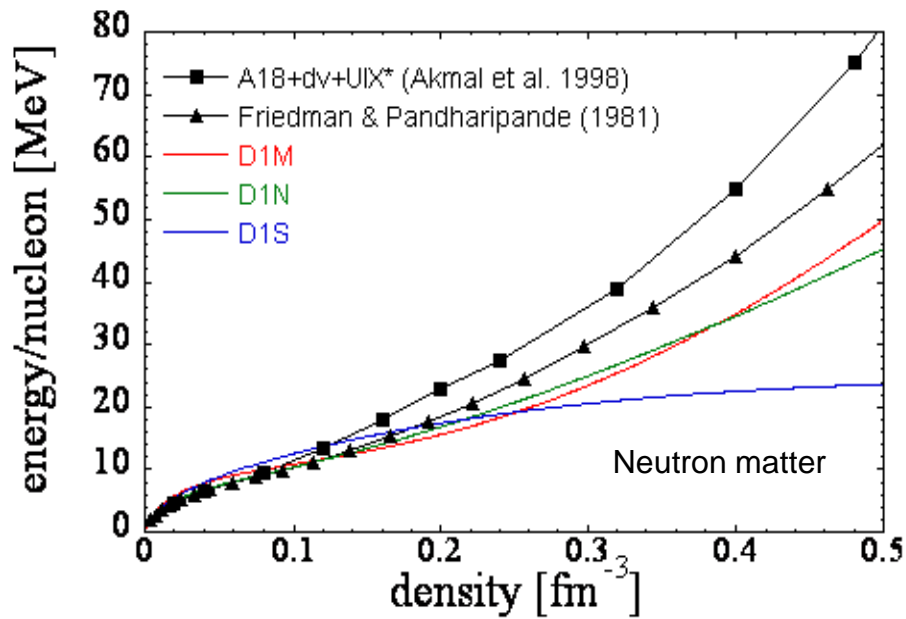
r.m.s = 0.031 fm

$$R_{ch} = \sqrt{R_{HFB}^2 + \Delta R_{corr}^2}$$

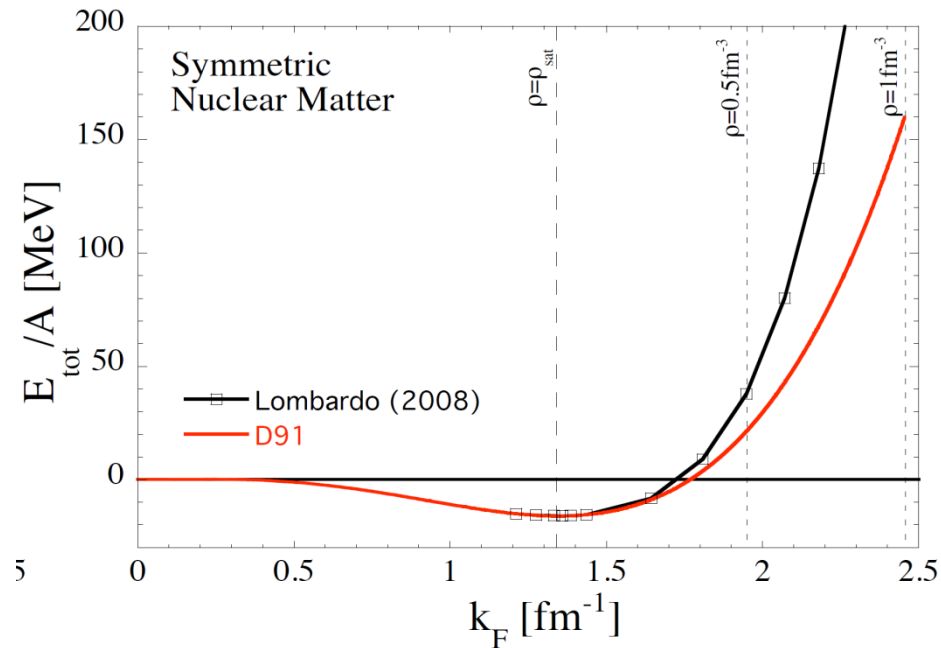
$$\Delta R_{corr} = \sqrt{R_{dyn}^2 - R_{HFB}^2}$$

$k_F=1.346 \text{ fm}^{-1}$     $J=28.6 \text{ MeV}$     $m^*/m=0.746$     $K_{inf}=225 \text{ MeV}$

## Neutron matter EOS

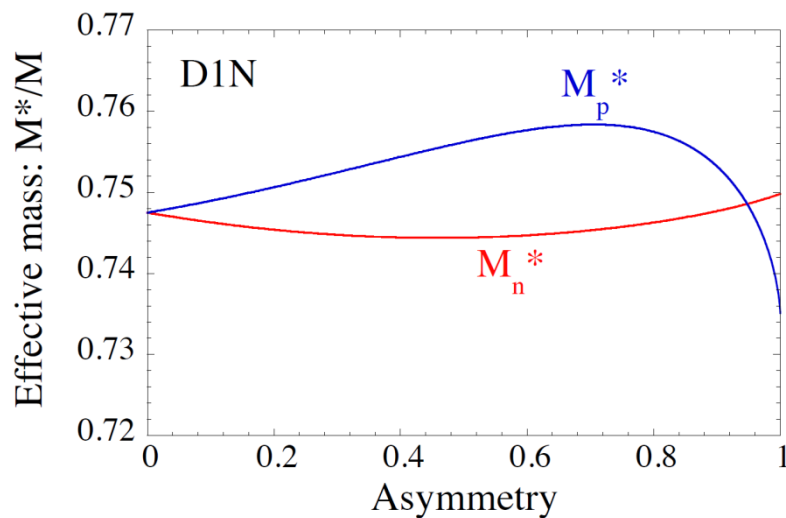
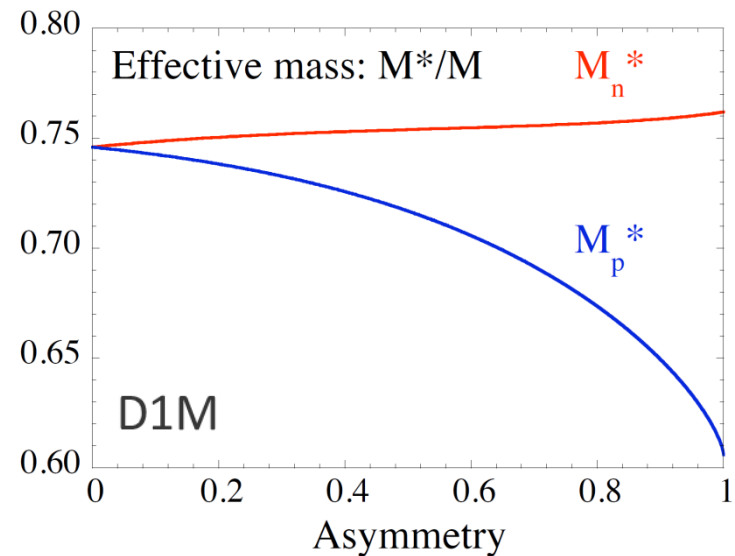
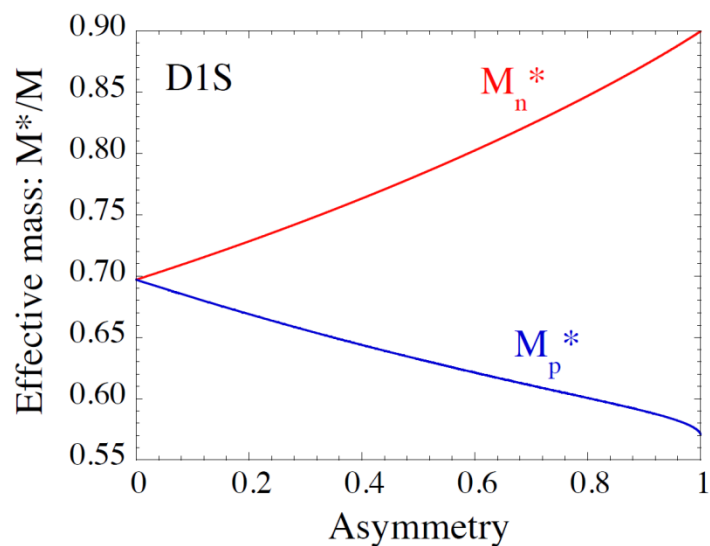


## Symmetric nuclear matter EOS



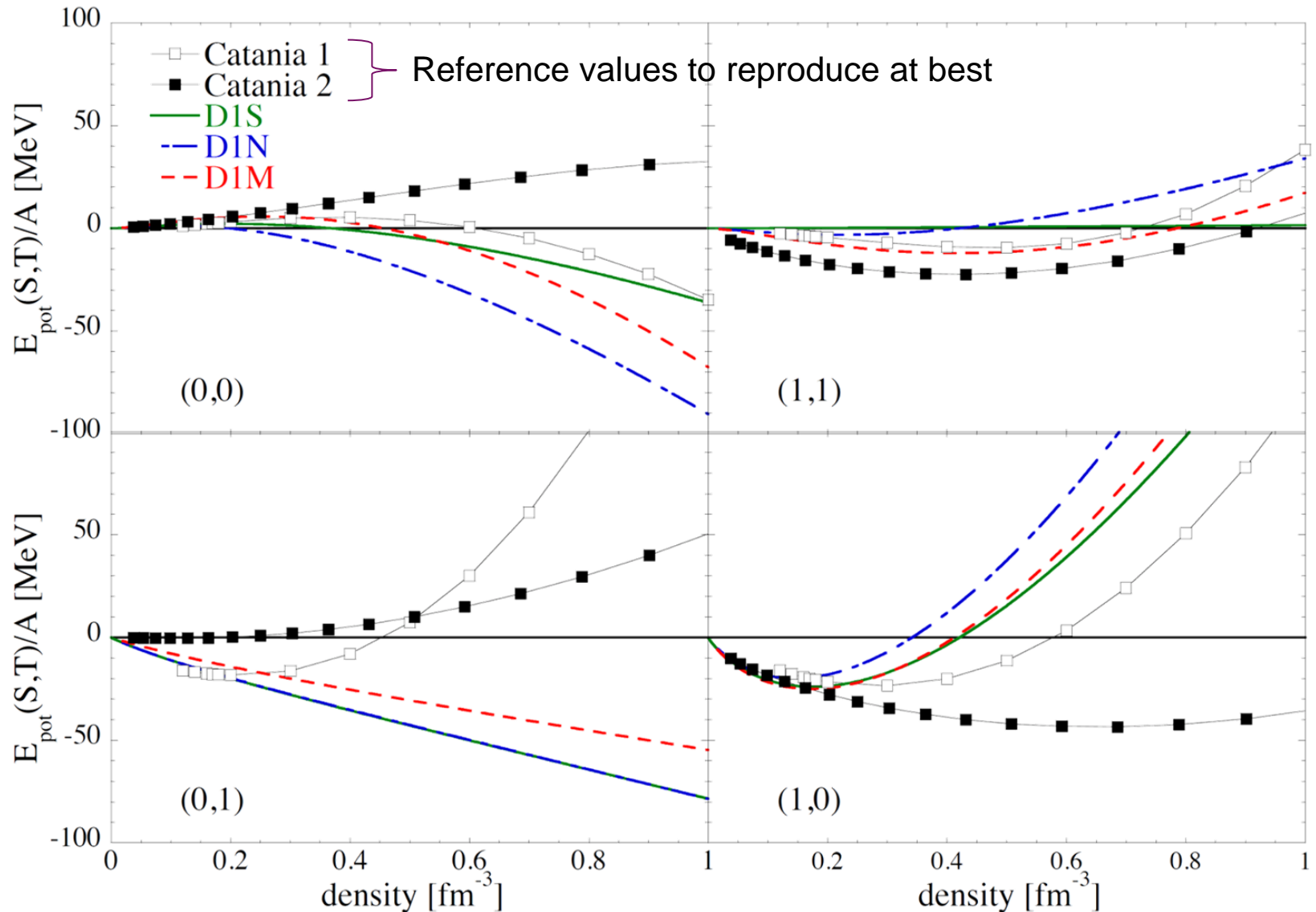
# NUCLEAR MATTER : effective masses

$k_F=1.346 \text{ fm}^{-1}$   $J=28.6 \text{ MeV}$   $m^*/m=0.746$   $K_{inf}=225 \text{ MeV}$

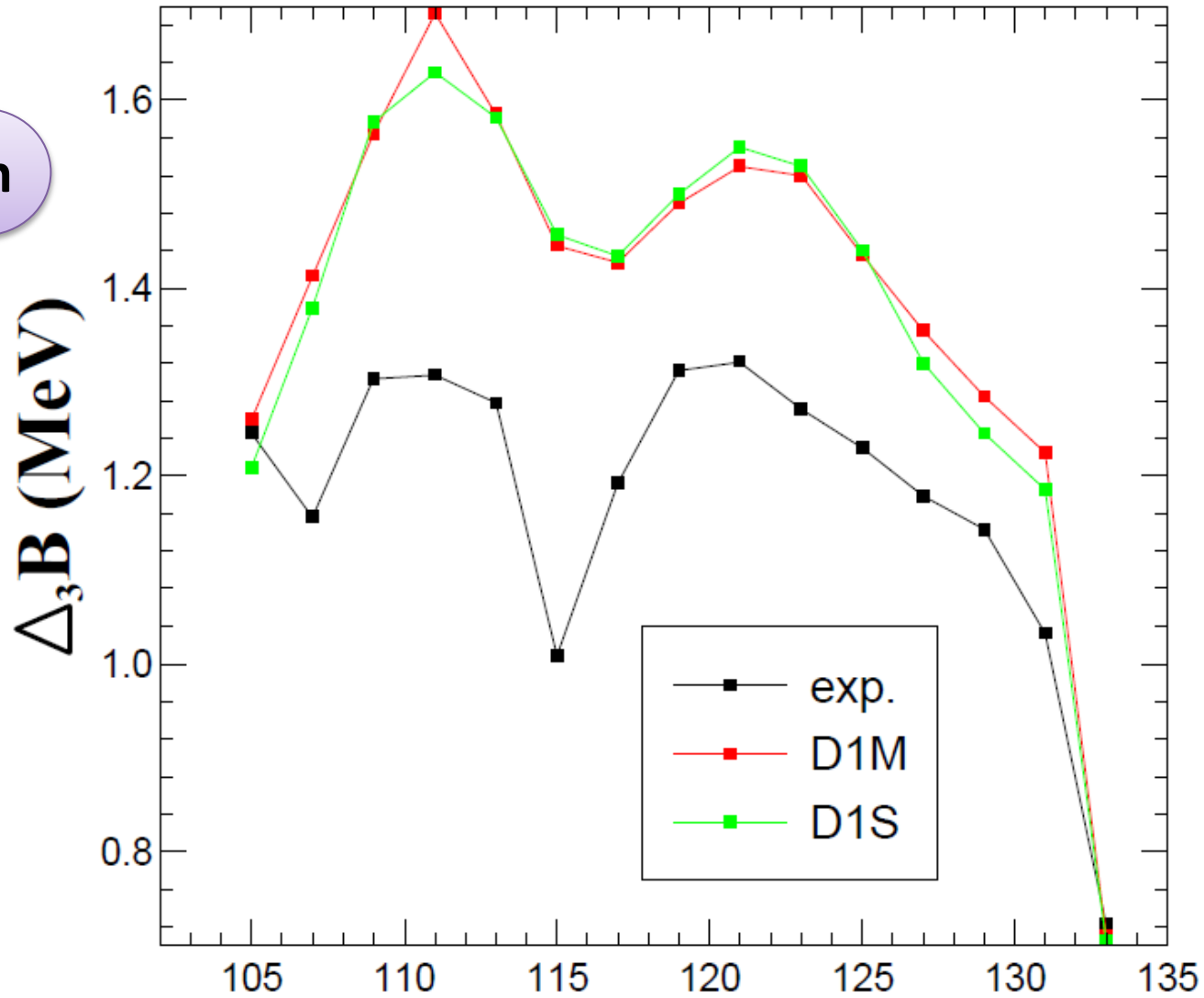


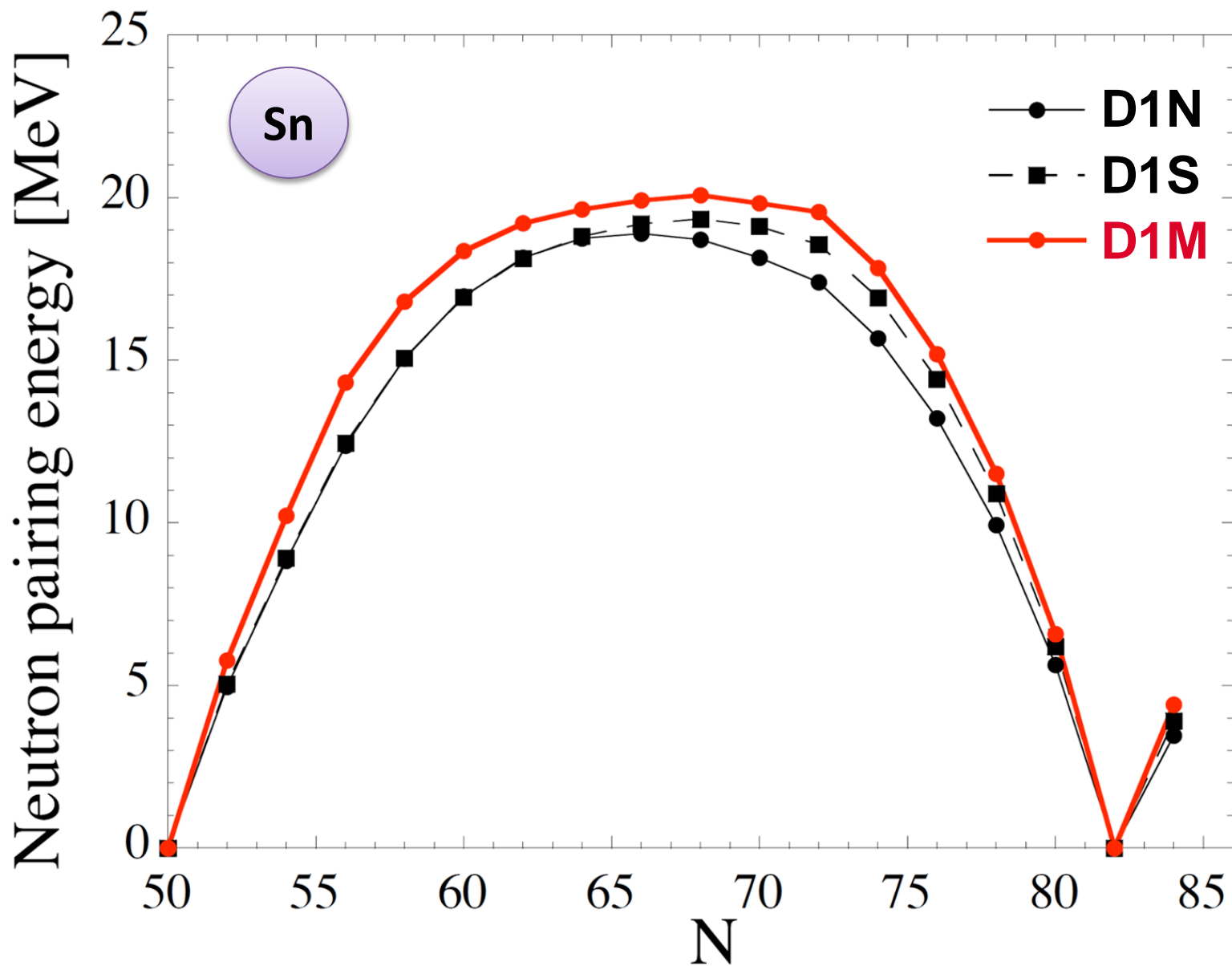
# NUCLEAR MATTER EOS in the 4 (S,T) channels

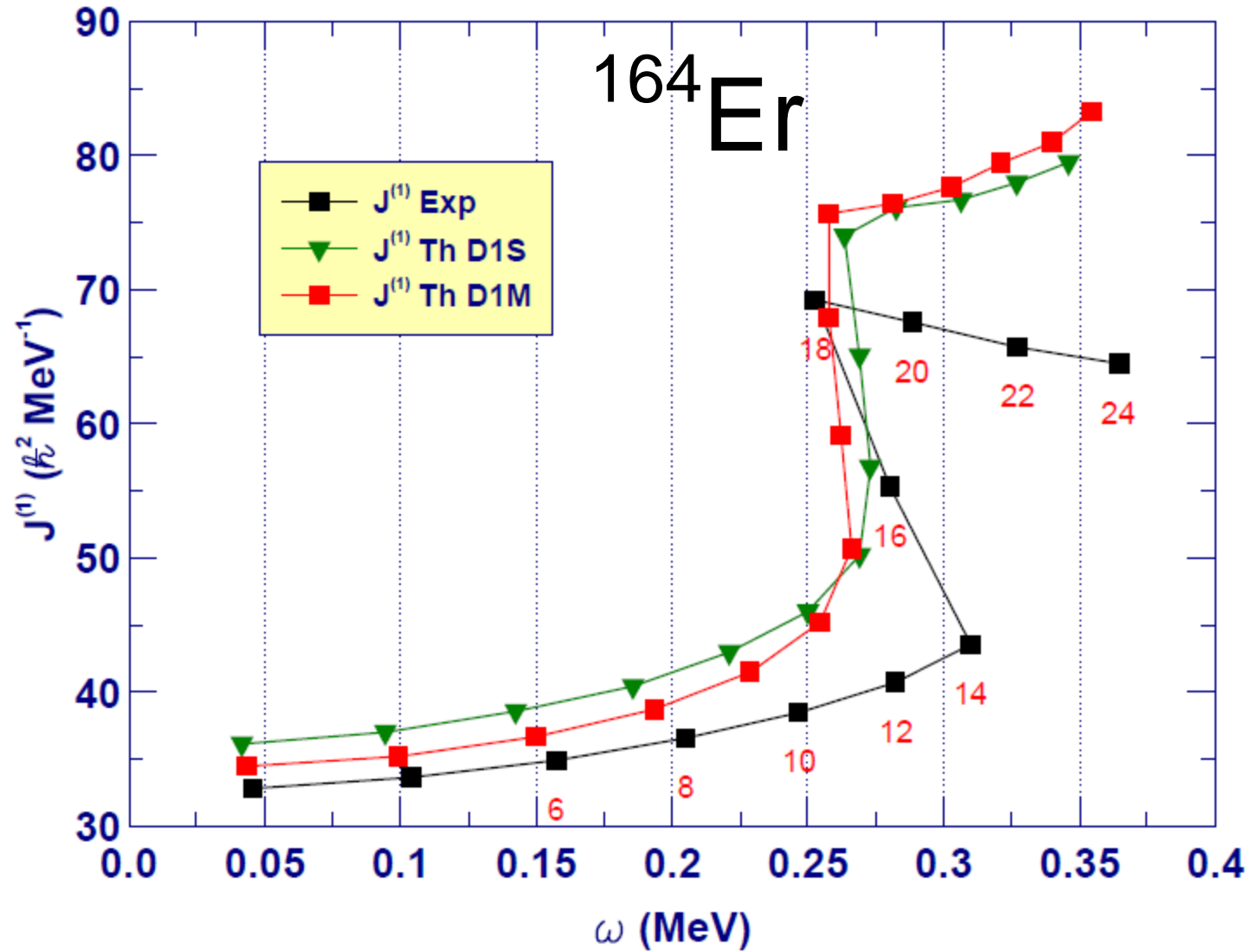
$k_F=1.346 \text{ fm}^{-1}$   $J=28.6 \text{ MeV}$   $m^*/m=0.746$   $K_{inf}=225 \text{ MeV}$

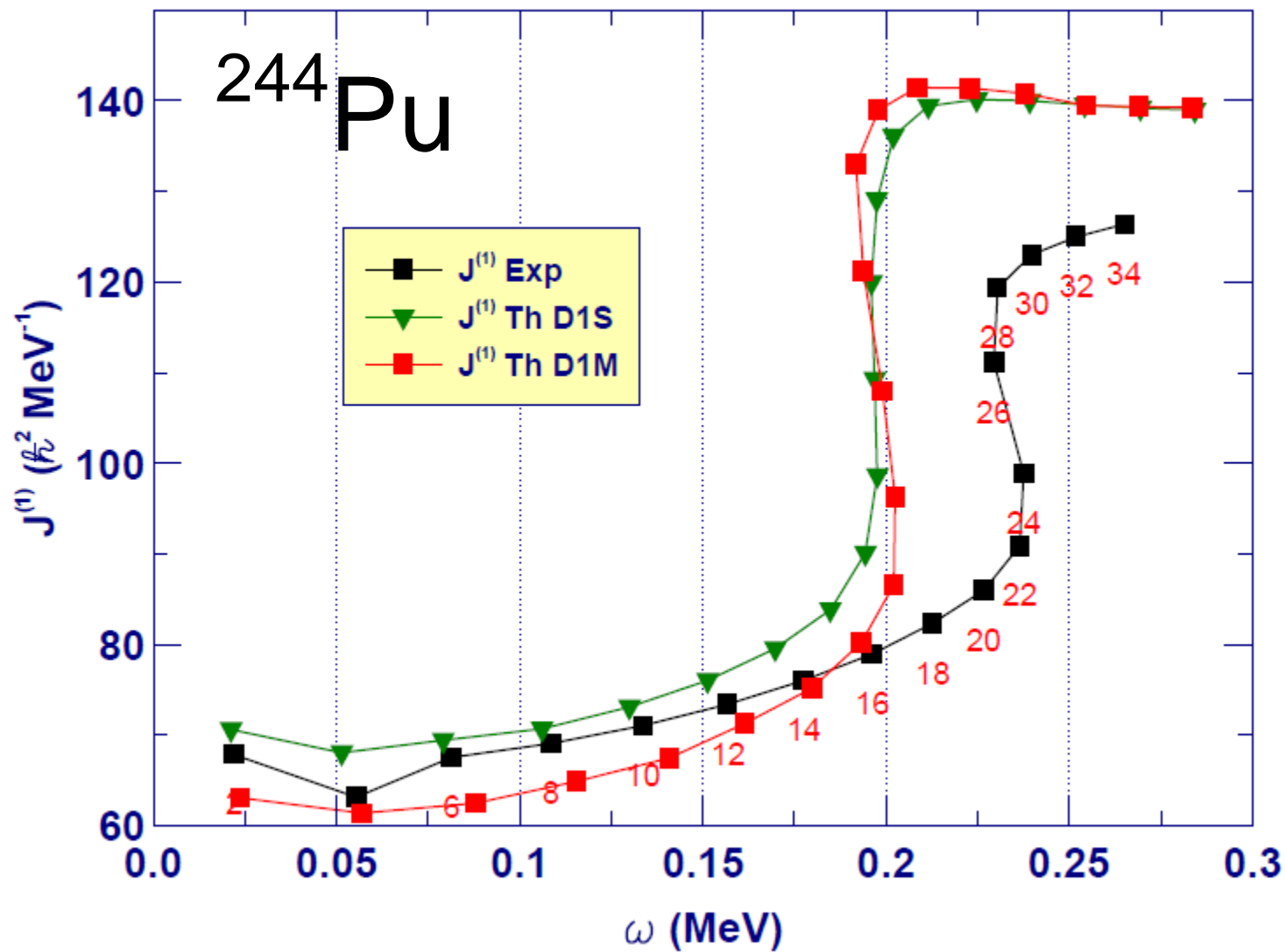


Sn





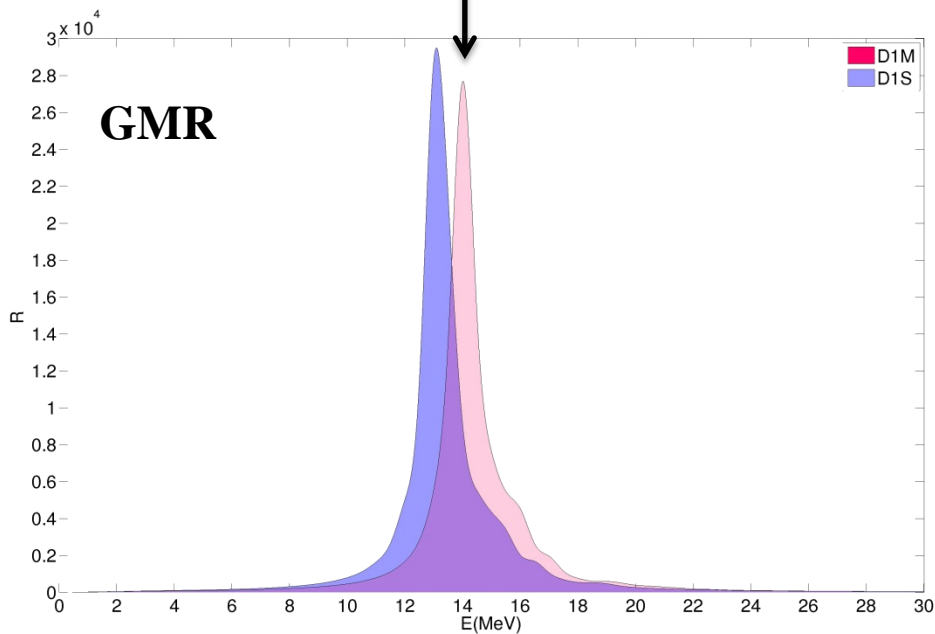






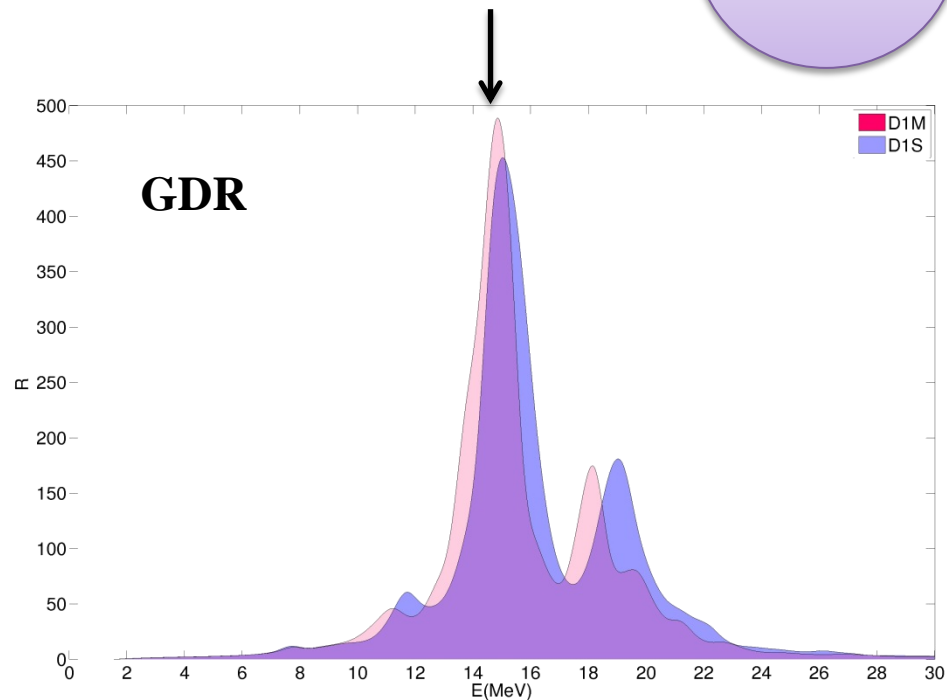


14.25 MeV



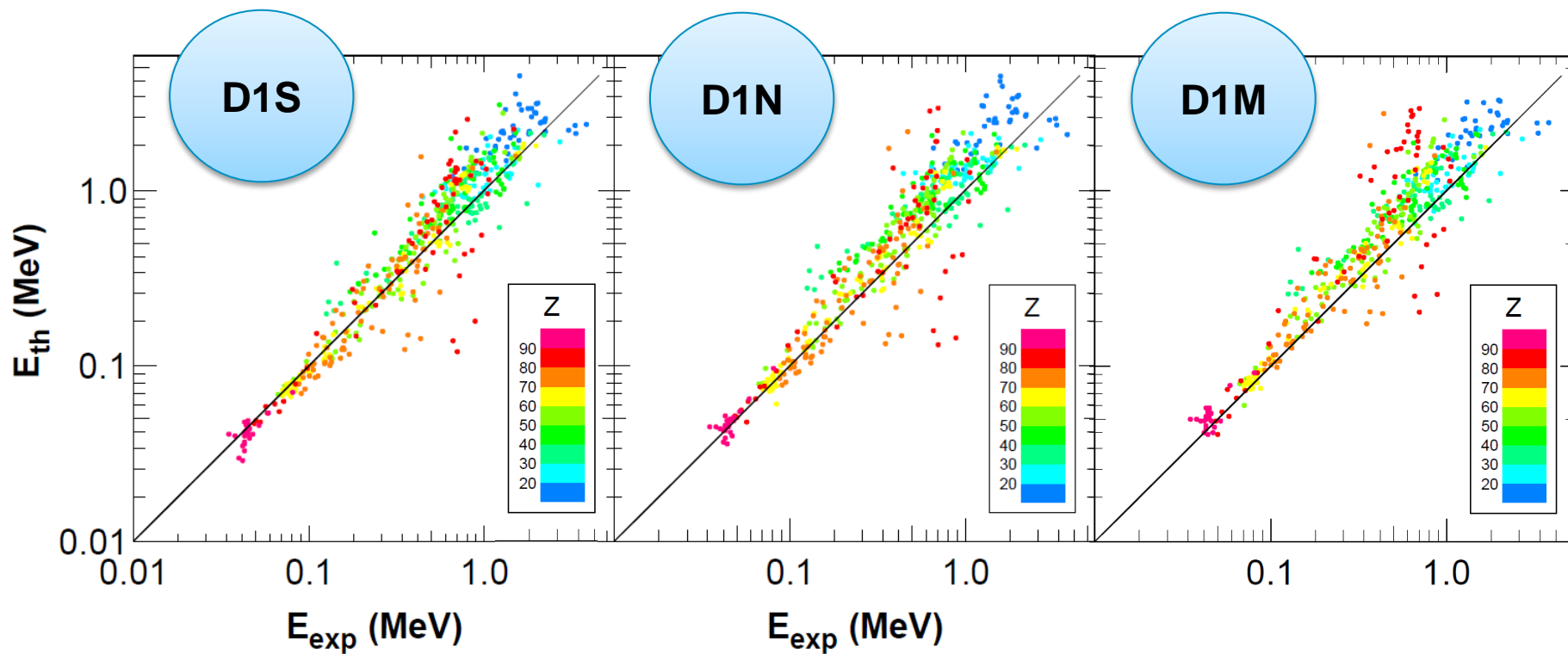
$E_{\text{exp}} = 14.17 \text{ MeV}$  D. H. Youngblood et al.,  
Phys. Rev. Lett. 82, 691 (1999).

15.85 MeV

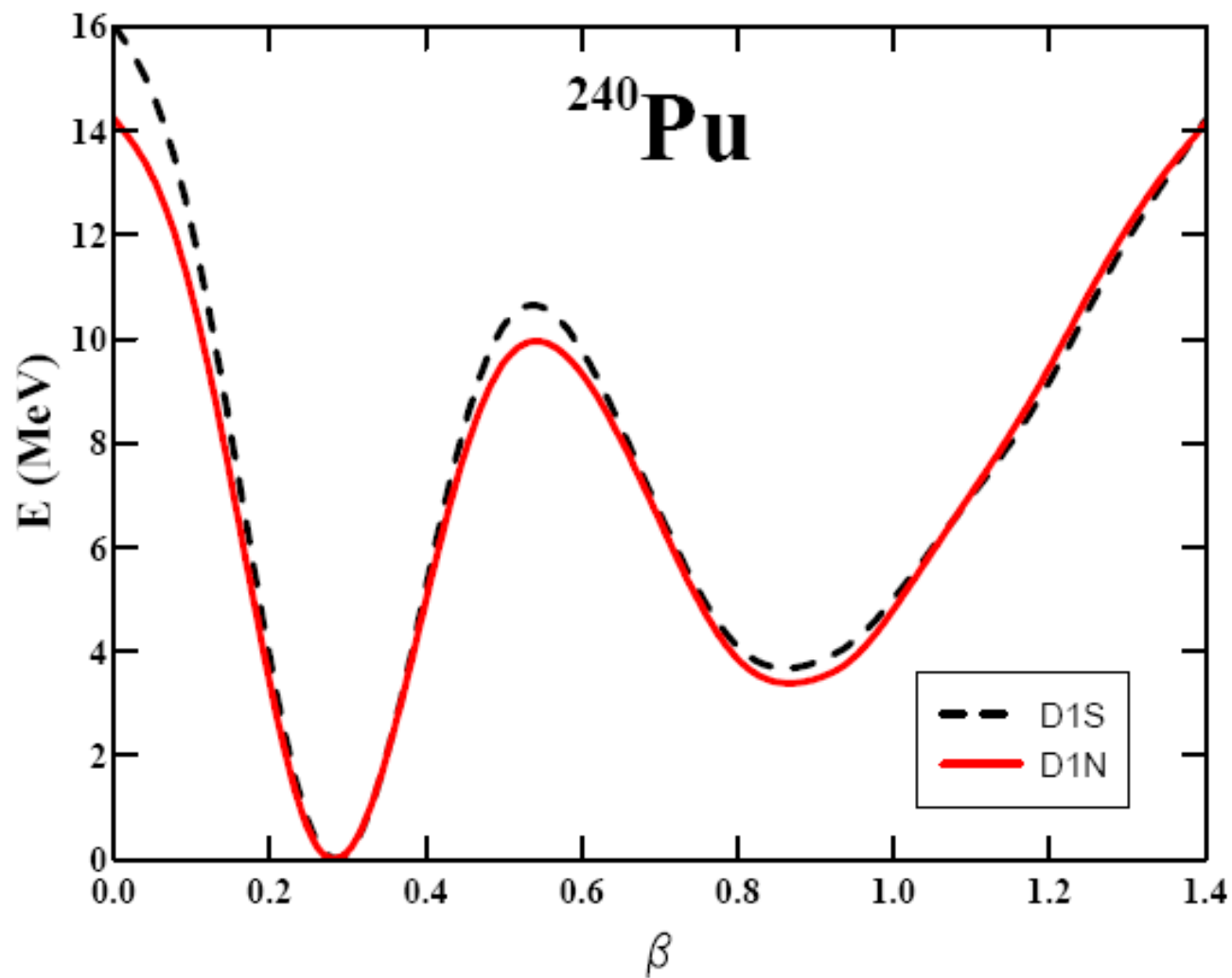


$E_{\text{exp}} = 13.43 \text{ MeV}$  B. L. Berman and S. C. Fultz,  
Rev. Mod. Phys. 47, 713 (1975).

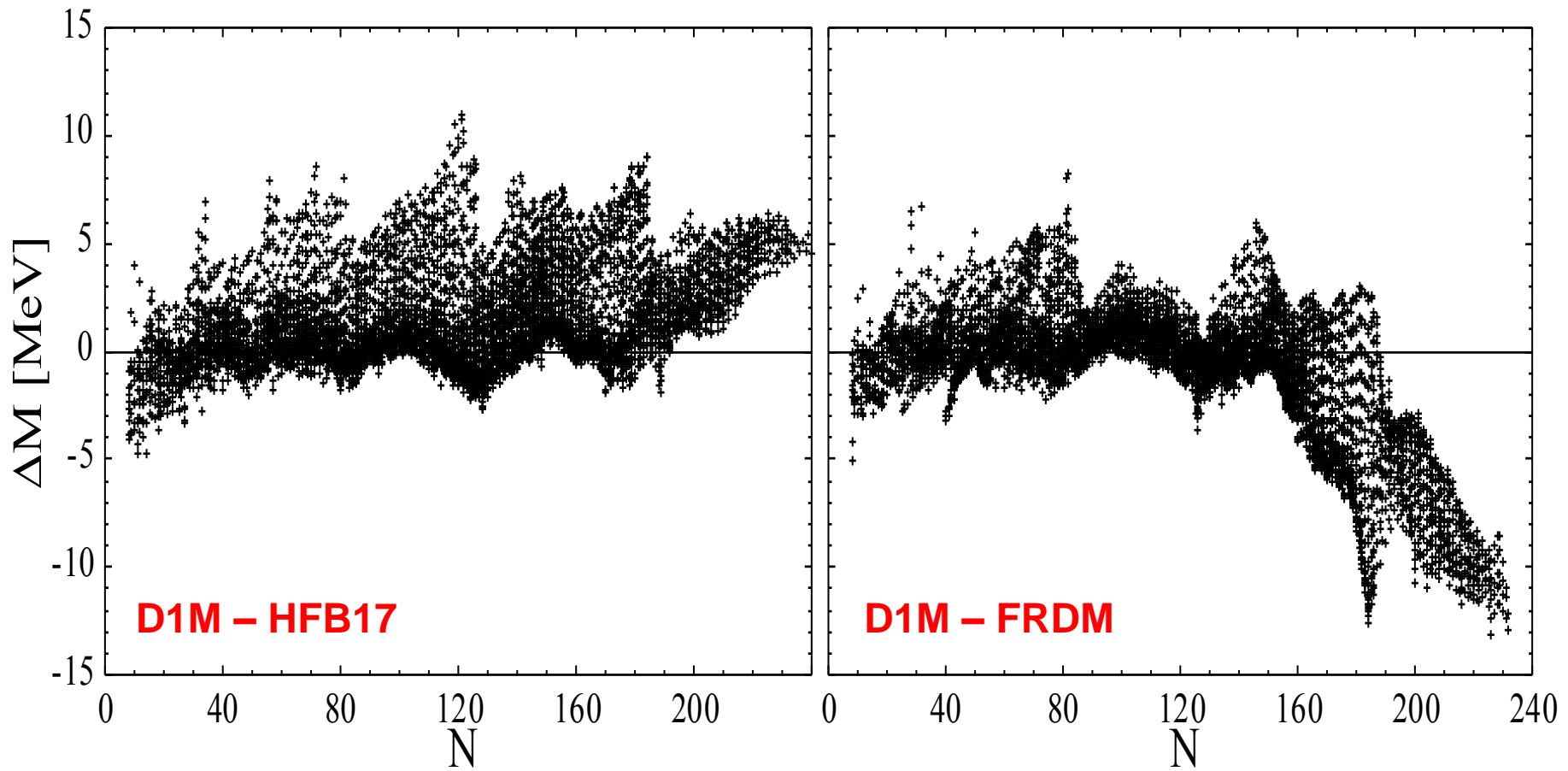
## Excitation energies of the first $2^+$ for 519 e-e nuclei

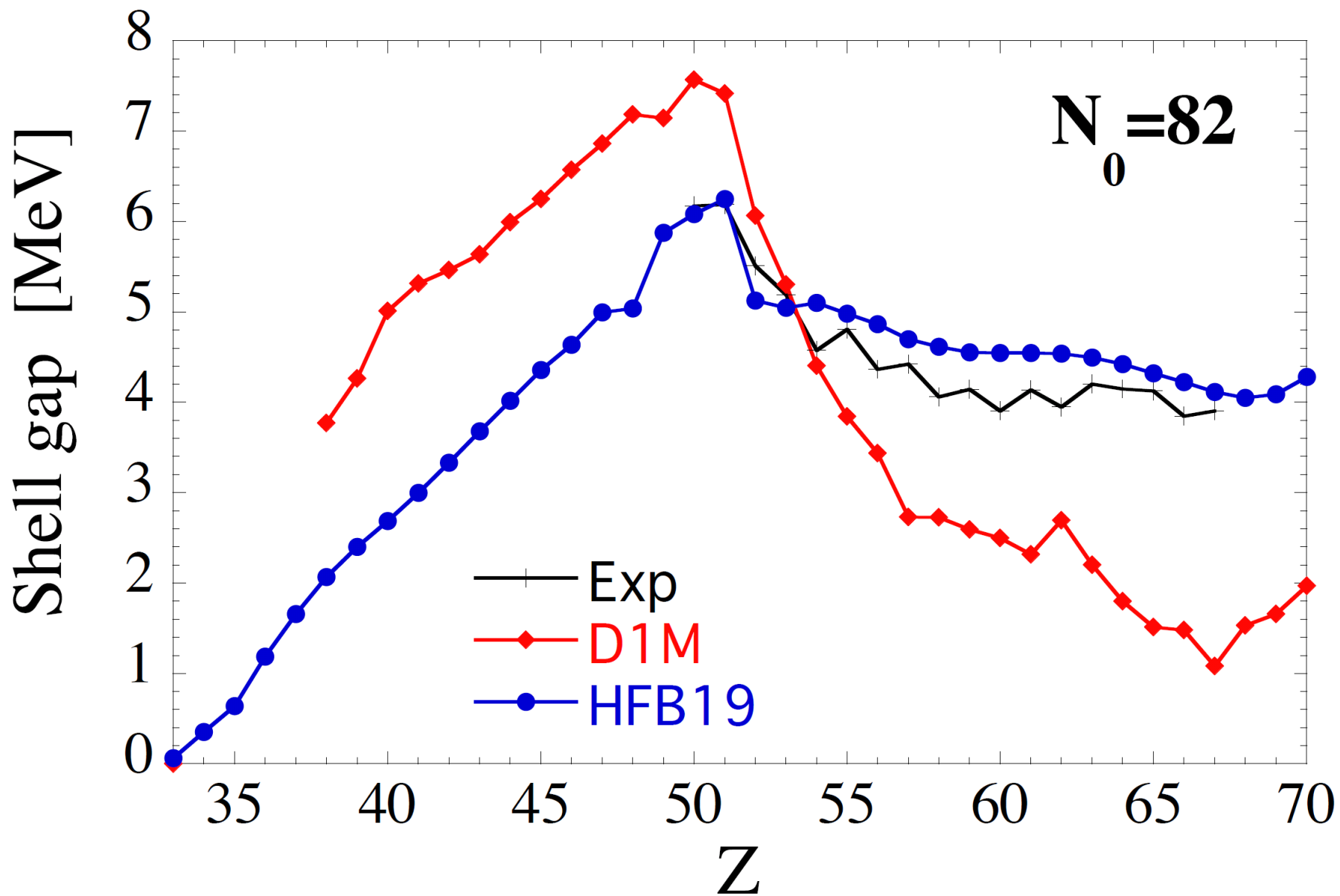


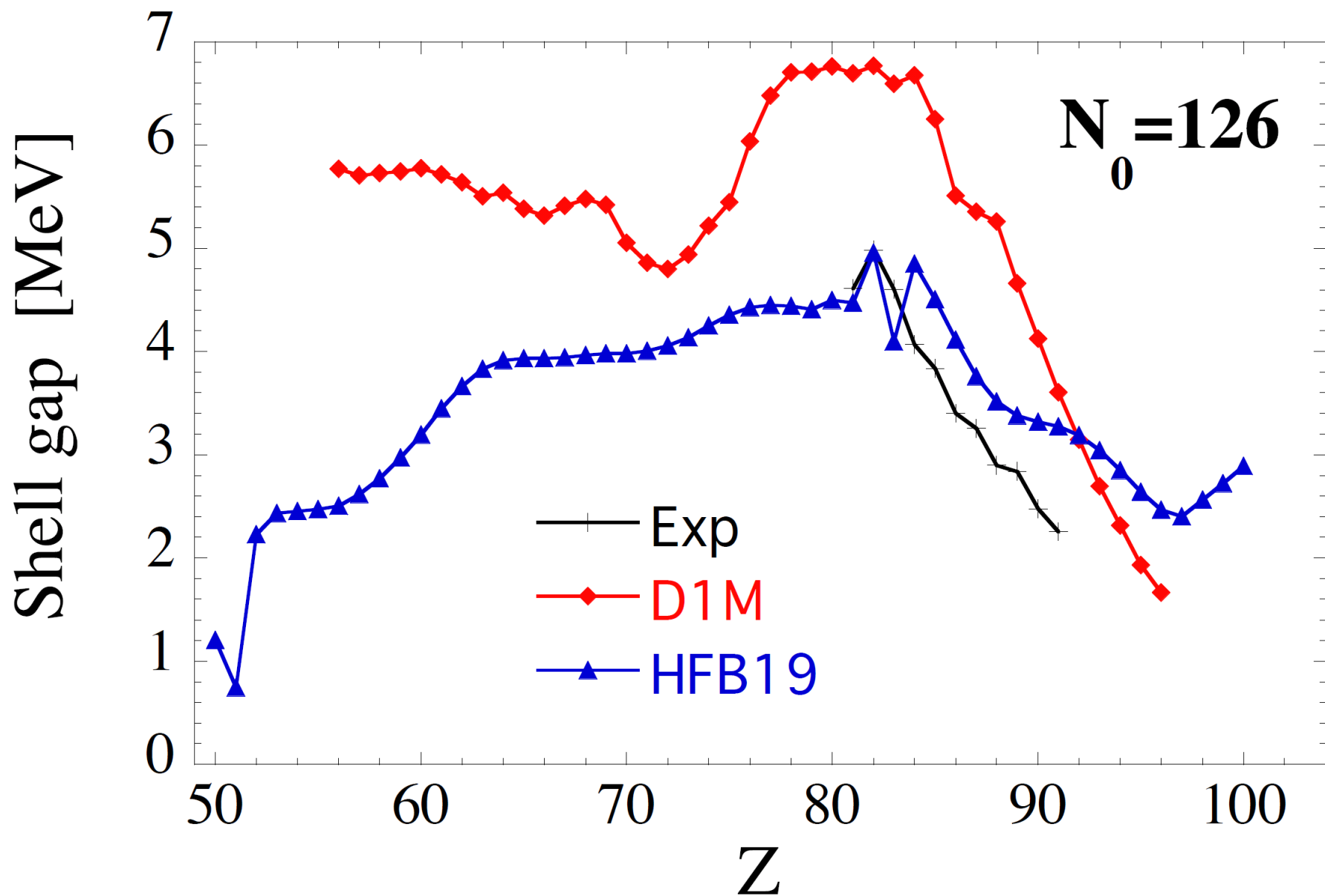
# FISSION BARRIERS



# COMPARISON WITH OTHER MASS FORMULAE







PHYSICAL REVIEW C 90, 017302 (2014)

## Predictive power of nuclear-mass models

Adam Sobiczewski<sup>1,2,3,\*</sup> and Yuri A. Litvinov<sup>2</sup>

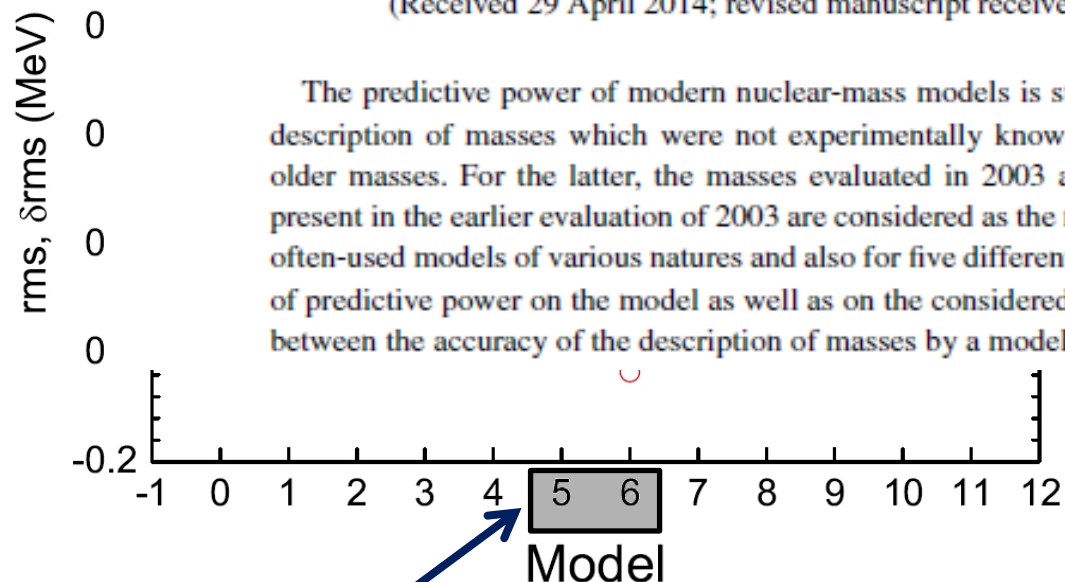
<sup>1</sup>National Centre for Nuclear Research, Hoża 69, 00-681 Warsaw, Poland

<sup>2</sup>GSI Helmholtzzentrum für Schwerionenforschung GmbH, 64291 Darmstadt, Germany

<sup>3</sup>Helmholtz Institute Mainz, 55099 Mainz, Germany

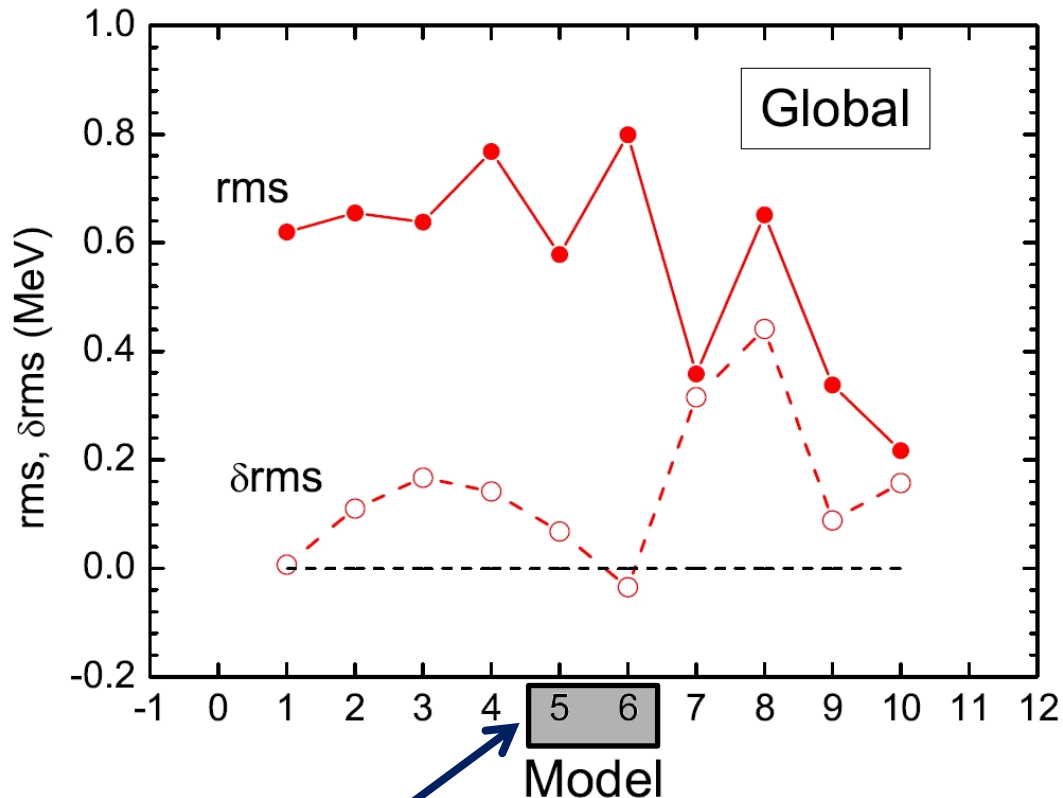
(Received 29 April 2014; revised manuscript received 16 June 2014; published 14 July 2014)

The predictive power of modern nuclear-mass models is studied. To quantify this property, we compare the description of masses which were not experimentally known at the time of the model adjustment to that of older masses. For the latter, the masses evaluated in 2003 are taken. The masses evaluated in 2012 and not present in the earlier evaluation of 2003 are considered as the new ones. The predictive power is analyzed for ten often-used models of various natures and also for five different regions in the nuclear chart. A strong dependence of predictive power on the model as well as on the considered region of nuclei is observed. No clear correlation between the accuracy of the description of masses by a model and its predictive power is found.



Microscopic models

Comparison between several mass models adjusted with 2003 exp and tested with 2012 exp masses



## Current status

**rms < 1 MeV (masses  $\approx$  GeV)**

**micro  $\sim$  macro**

**micro more predictive**

**Microscopic models**



# PERSPECTIVES

# FURTHER IMPROVEMENTS

3 axes

D1 type with less approximations  
(**exact Coulomb exchange and pairing**)

New analytical form  
D2  
(F. Chappert thesis  
+ accepted in PRC)

Finite range everywhere  
DG  
(no code yet)



JPE and SP under pressure !



HFB3 under development !  
D2N available ?  
DG to do !

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Finite range everywhere  
DG  
(no code yet)

## + Sensitivity analysis v.s number of major shells

- **N basis =  $N(N-1) \Delta_\infty$  values  $\Rightarrow$  mean r.m.s and dispersion**
- **$\Delta_{\text{quad}}$  also sensitive to basis size**
- **Beyond 5DCH ?**
- **Same with RMF ?**

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The 11<sup>th</sup> commandment :

*ONE SHALL ONLY DESIGN EFFECTIVE INTERACTIONS*

- ❖ *for both mean field and beyond mean field predictions*
- ❖ *for all nuclei*
- ❖ *for all nuclear properties*