

# what bothers me?

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17 mars 2014

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1. All the calculations presented here were done with the TALYS code

Actinides = deformed nuclei  $\implies$  CCC framework

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Coupled Channel Calculations  $\implies$  good OP + coupling scheme

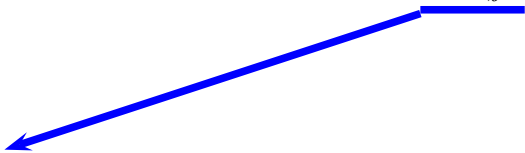


# Optical Model $\leftrightarrow \sigma_{tot}, \sigma_{SE}, \sigma_{DI}, \sigma_R$ et $T_{l,j}^{J\pi}$

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Statistical Model  $\leftrightarrow \sigma_{n,\gamma}, \sigma_{n,f}, \sigma_{n,xn}, \dots$   
+ P.E. ( $\sigma_R = \sigma_{CN} + \sigma_{PE} + \sigma_{DI}$ )

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good Opt. Pot.  $\equiv$  good tank  $\sigma_R$  and also  $T_{l,j}^{J\pi}$

Optical Model  $\leftrightarrow \sigma_{tot}, \sigma_{SE}, \sigma_{DI}, \sigma_R$  et  $T_{l,j}^{J\pi}$

But !

Are we sure to use the "best" coupling scheme ?

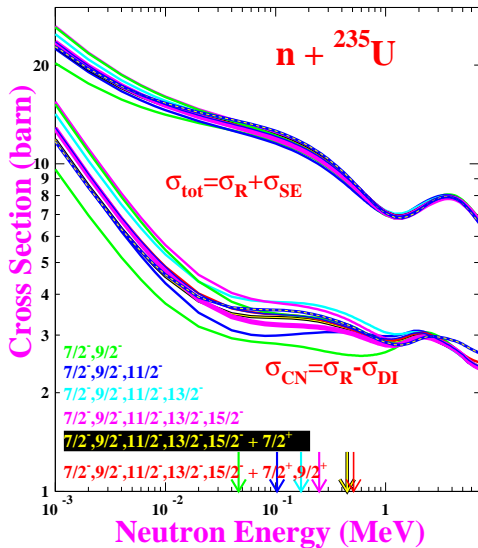
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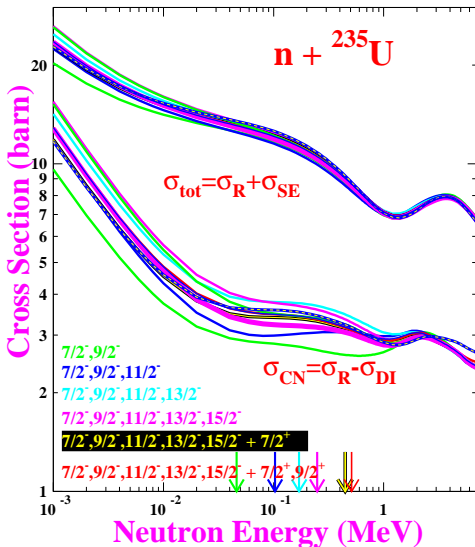
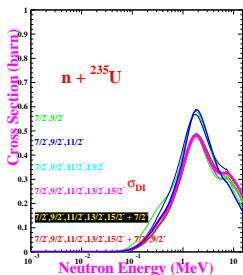


# OMP - CCC $\leftrightarrow$ which coupling scheme?

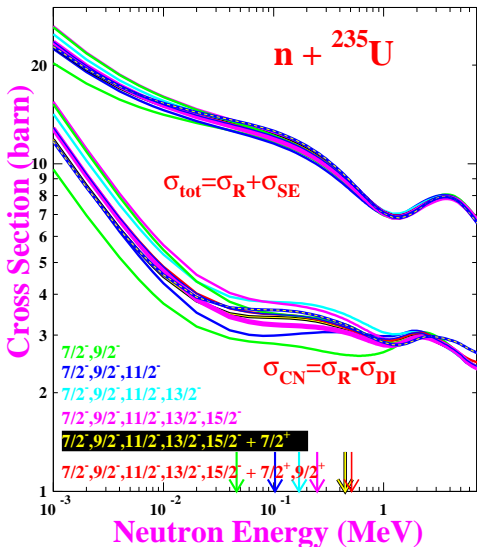
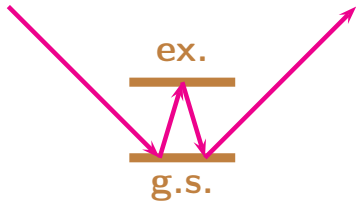
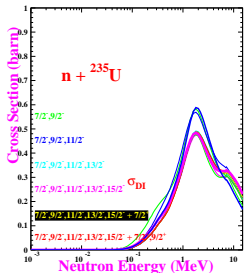




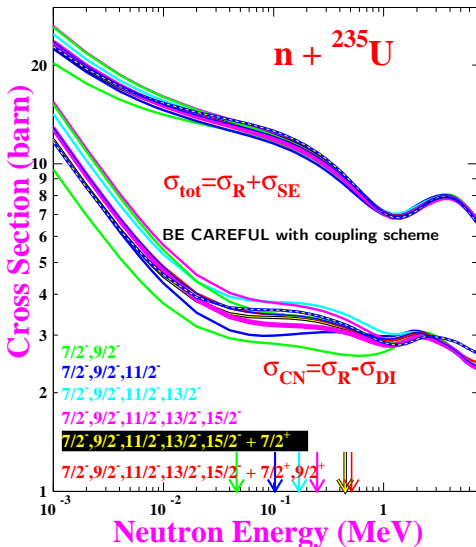
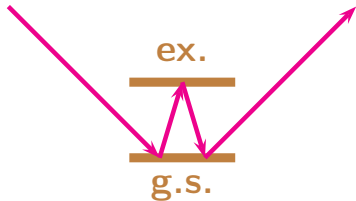
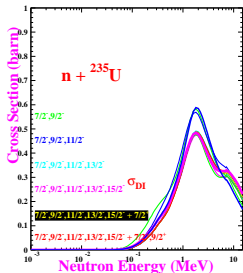
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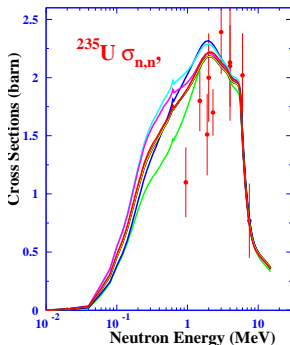
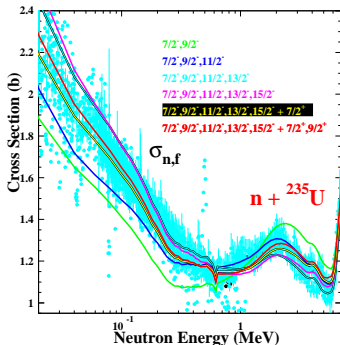
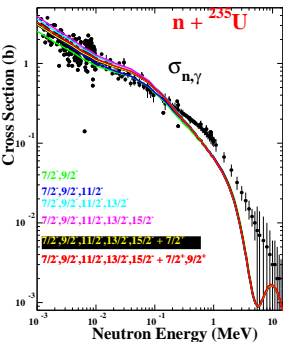


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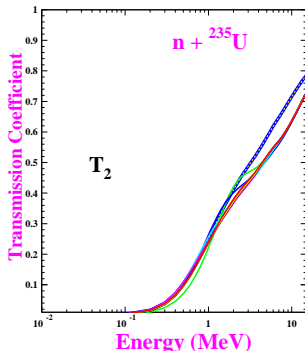
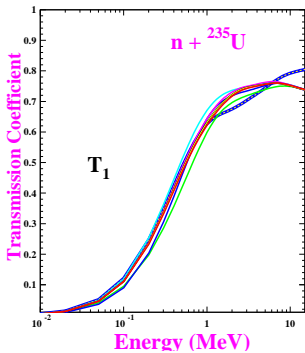
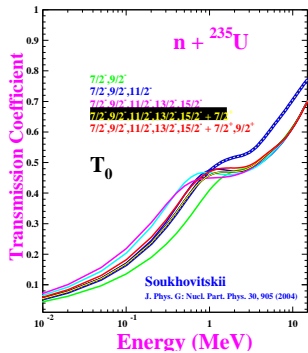
# CCC : coupling scheme effects on statistical model calculations

## Cross Sections behaviour



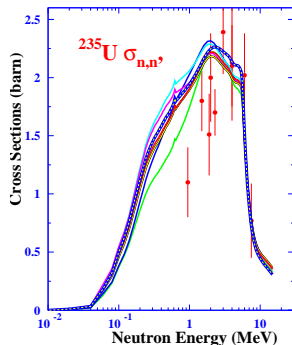
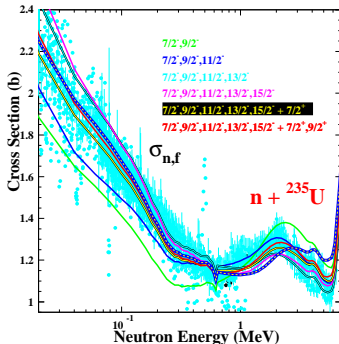
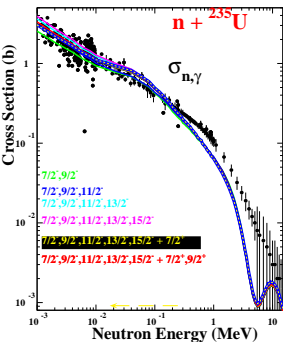
# CCC : coupling scheme effects on statistical model calculations

## Transmission Coefficients used



# CCC : optical potentiel effects on statistical model calculations

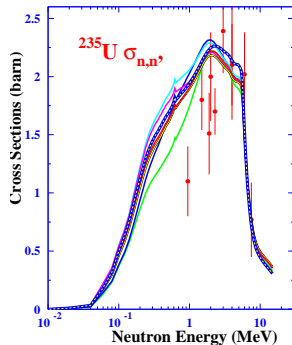
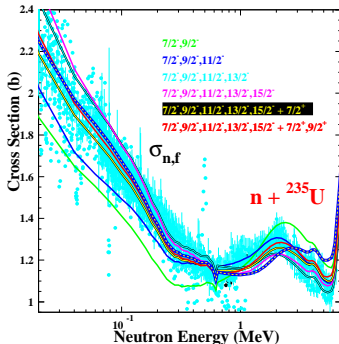
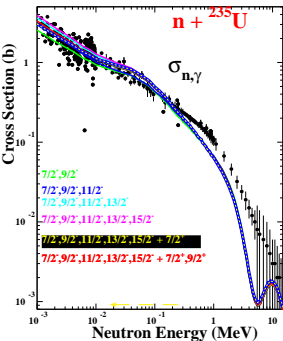
## Cross Sections behaviour



Soukhovitskii (non dispersive OP)

# CCC : optical potentiel effects on statistical model calculations

## Cross Sections behaviour



$\neq T_l \implies \neq$  Trans. States populated

Soukhovitskii (non dispersive OP)

Barrier Heights strongly OP dependent

# Once Optical Potential and coupling scheme adopted ...





we are now able to define many interesting quantities



# compound emission probabilities

For energies  $E < E_{(n,2n)}^{seuil}$  when considering compound emission processes, we get :

$$\sigma_{CN} = \sigma_R - \sigma_{DI} = \sigma_{CE} + \sigma_{n,n'} + \sigma_{n,\gamma} + \sigma_{n,f}$$

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$$\begin{aligned}\sigma_{CN} &= \sigma_{n,n} + \sigma_{n,\gamma} + \sigma_{n,f} \\ \Leftrightarrow 1 &= \frac{\sigma_{n,n}}{\sigma_{CN}} + \frac{\sigma_{n,\gamma}}{\sigma_{CN}} + \frac{\sigma_{n,f}}{\sigma_{CN}}\end{aligned}$$



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Then defining GLOBAL compound emission probability for each processes occurring in this energy range :

$$1 = P_{n,n} + P_{n,\gamma} + P_{n,f}$$

Now, for a surrogate reaction defined by an entrance channel  $EC$ , we have :

$$1 = P_{EC,n} + P_{EC,\gamma} + P_{EC,f}$$



# Use of Shannon theorem towards surrogate reactions

From another point of view, we can also define the lack of information on the compound emission processes for an emitting system (CN). When using the same notations as previously defined, according to the Shannon theorem [1], the lack of information (also called entropy) on the compound emission processes for an emitting CN is defined as :

$$H_{EC}(CN, E) = \begin{aligned} & -P_{EC,\gamma}(E) \log_2 P_{EC,\gamma}(E) \\ & -P_{EC,n}(E) \log_2 P_{EC,n}(E) \\ & -P_{EC,f}(E) \log_2 P_{EC,f}(E). \end{aligned}$$

Instead of plotting each probability of all exit channels for each studied entrance channel versus energy, this representation is more compact, and so, more clearly to read.

In addition, using these functions, Bohr independence hypothesis implies that for two different entrance channels  $EC_1$  and  $EC_2$  leading to the same CN at the same excitation energies in the same spin-parity states, the lack of information on these compound nuclei emission processes or the uncertainties on their emission processes should be identical :

$$H_{EC_1}(CN, E) = H_{EC_2}(CN, E).$$

[1] C.E Shannon, Bell System Technical Journal, 27 , 379 and 623, (1948).



we are now able to define many interesting quantities  
in order to avoid the fission channel we can begin to study some  
rare earth nuclei which are also deformed nuclei (CCC).



# Shannon theorem - non fissile nuclei : 2 exit channels

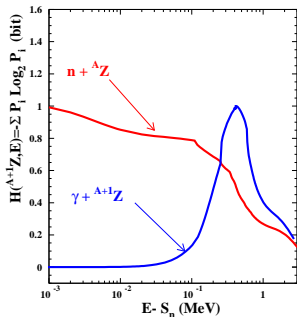


Figure : Lack of information on the compound emission processes,  $H_\gamma(A+1Z, E)$  and  $H_n(A+1Z, E)$  related to a given entrance channel  $EC = \gamma$  or  $EC = n$ , plotted versus  $E - S_n$ .

$$\begin{aligned}
 H_{EC}(CN, E) &= -P_{EC,\gamma}(E) \log_2 P_{EC,\gamma}(E) \\
 &\quad -P_{EC,n}(E) \log_2 P_{EC,n}(E) \\
 &= -P_{EC,\gamma}(E) \log_2 P_{EC,\gamma}(E) \\
 &\quad -(1 - P_{EC,\gamma}(E)) \times \\
 &\quad \log_2(1 - P_{EC,\gamma}(E)).
 \end{aligned}$$

When, (for the  $EC_1 = \gamma$ ),  $\gamma$  emission is the most important emission process then :

$$P_{EC_1,\gamma}(E) \approx 1, \quad P_{EC_1,n}(E) = 1 - P_{EC_1,\gamma}(E) \approx 0$$

and

$$H_{EC_1}(CN, E) = 0$$

For the  $EC_1 = \gamma$  and  $EC_2 = n$  entrance channels, the lack of information on the compound emission processes is maximum when :

$$P_{EC,\gamma}(E) = P_{EC,n}(E) = \frac{1}{2}$$

[since  $h = -p \log_2 p - (1 - p) \log_2(1 - p)$  is maximum for  $p = \frac{1}{2}$ ].



# Shannon theorem - non fissile nuclei : 2 exit channels

$$H_{EC}(CN, E) = -P_{EC,\gamma}(E) \log_2 P_{EC,\gamma}(E) - P_{EC,n}(E) \log_2 P_{EC,n}(E)$$

becomes here :

$$H_{EC}(CN, E) = -P_{EC,\gamma}(E) \log_2 P_{EC,\gamma}(E) - (1 - P_{EC,\gamma}(E)) \log_2 (1 - P_{EC,\gamma}(E))$$

Shannon Theorem translation of Bohr independence hypothesis :

$$H_{EC1}(CN, E) = H_{EC2}(CN, E).$$

BUT HERE :

$$H_n(^{156}\text{Gd}, E) \neq H_\gamma(^{156}\text{Gd}, E)$$

AND HERE ALSO FOR  $SR = (p, p'\gamma)$  :

$$\begin{array}{ccc} H_n(^{156}\text{Gd}, E) & \neq & H_{(p,p'\gamma)}(^{156}\text{Gd}, E) \\ & \Downarrow & \\ J_n, \pi_n & \neq & J_{SR}, \pi_{SR} \\ & \text{or at least} & \end{array}$$

Bohr independence hypothesis failed for  $E \sim S_n$  with incident n since  $W \neq 1$

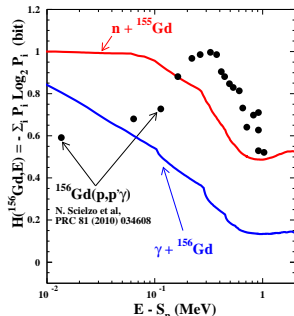


Figure : Lack of information on the compound emission processes,  $H_\gamma(^{156}\text{Gd}, E)$  and  $H_n(^{156}\text{Gd}, E)$  and,  $H_{(p,p'\gamma)}(^{156}\text{Gd}, E)$  related to a given entrance channel, plotted versus  $E - S_n$  ( $S_n = 8.536$  MeV).

# Interest of Shannon information for the 2 exit channels case

$$H_{EC}(CN, E) = -P_{EC,\gamma}(E) \log_2 P_{EC,\gamma}(E) - P_{EC,n}(E) \log_2 P_{EC,n}(E)$$

becomes here :

$$H_{EC}(CN, E) = -P_{EC,\gamma}(E) \log_2 P_{EC,\gamma}(E) - (1 - P_{EC,\gamma}(E)) \log_2 (1 - P_{EC,\gamma}(E))$$

Shannon Theorem translation of Bohr independence hypothesis :

$$H_{EC1}(CN, E) = H_{EC2}(CN, E).$$

BUT HERE :

$$H_n(^{176}\text{Lu}, E) \neq H_\gamma(^{176}\text{Lu}, E)$$

AND HERE ALSO FOR  $SR = ^{174}\text{Yb}(^3\text{He}, p)^{176}\text{Lu}$  :

$$\begin{array}{ccc} H_n(^{176}\text{Lu}, E) & \neq & H_{SR}(^{176}\text{Lu}, E) \\ & \Downarrow & \\ J_n, \pi_n & \neq & J_{SR}, \pi_{SR} \\ & \text{or at least} & \end{array}$$

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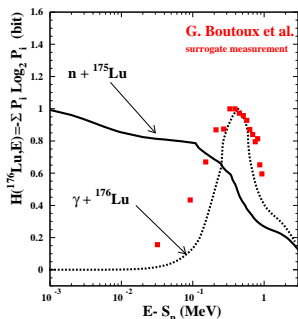


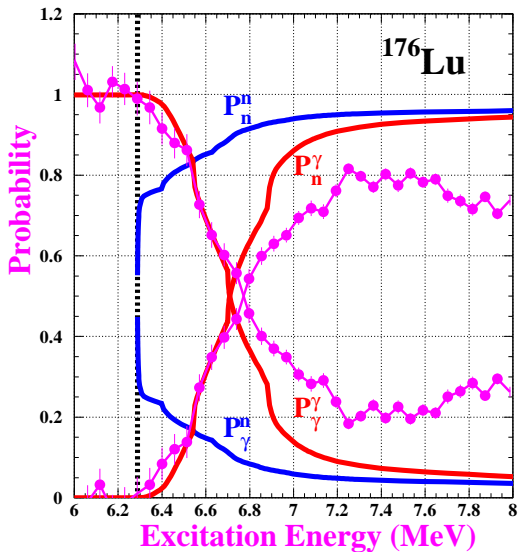
Figure : Lack of information on the compound emission processes,  $H_\gamma(^{176}\text{Lu}, E)$  and  $H_n(^{176}\text{Lu}, E)$  and,  $H_{SR}(^{176}\text{Lu}, E)$  related to a given entrance channel, plotted versus  $E - S_n$ .

$$P_{EC,\gamma} + P_{EC,n} = 1$$



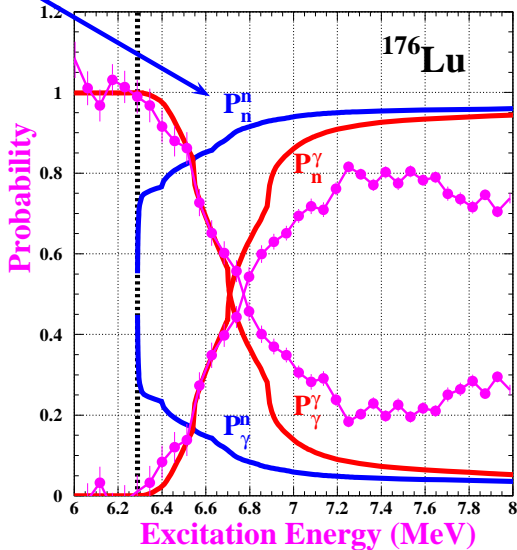
$$P_{EC,n} = 1 - P_{EC,\gamma}$$

# E.D.P.S : the only 2 exit channels case



# E.D.P.S : the only 2 exit channels case

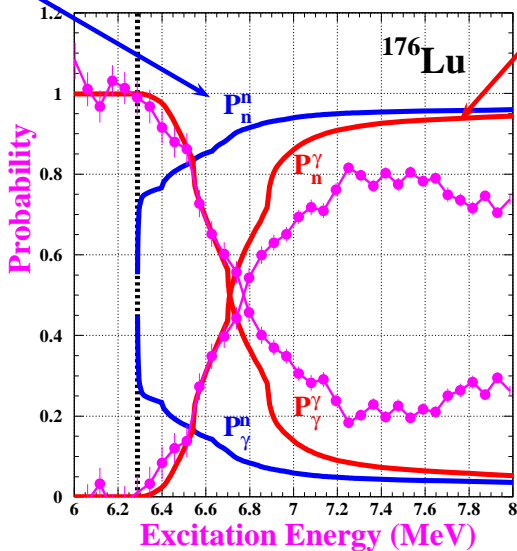
calc.  $^{175}\text{Lu}(n, n)^{175}\text{Lu}$



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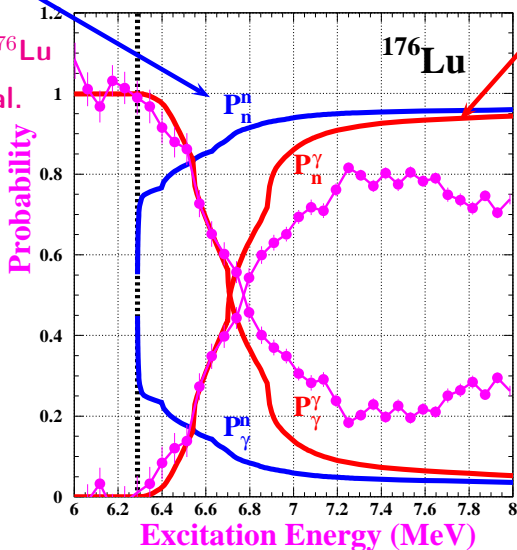
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G. Boutoux et al.

CENBG



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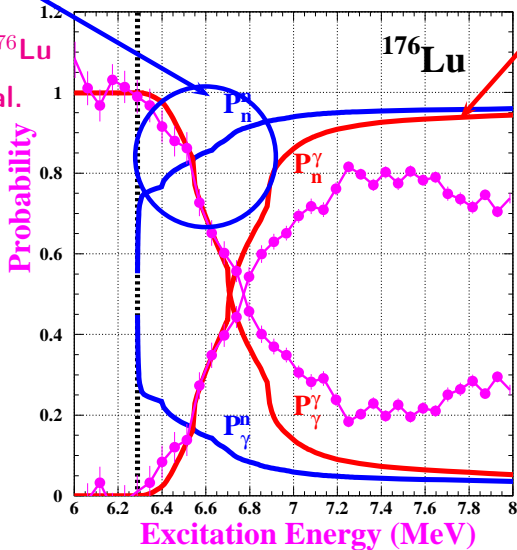
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structures =  
opening channels





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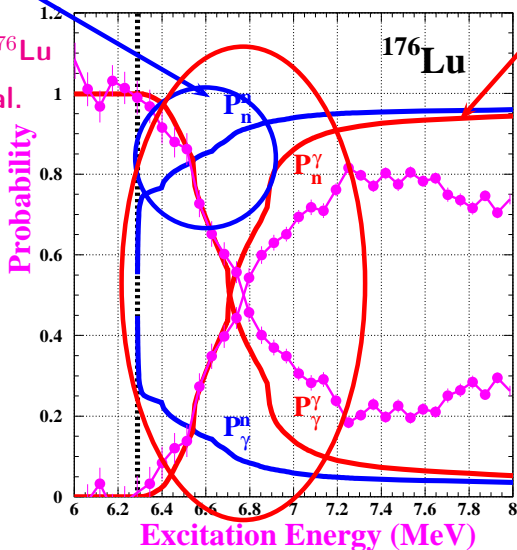
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id. for  $P_n^\gamma$  et  $P_n^{SR}$



$$P_{EC,\gamma} + P_{EC,n} = 1$$



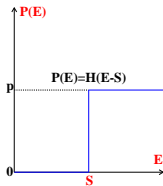
$$P_{EC,n} = 1 - P_{EC,\gamma}$$

But neutron emissions on discrete states = threshold reactions

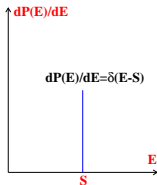
⇒ interest of energy derivative study :

$$\frac{dP_{EC,n}}{dE} = -\frac{dP_{EC,\gamma}}{dE}$$

# Inelastic neutron emission probability



**Figure :** *Inelastic neutron emission probability for populating an  $E = S$  energy state (Heaviside function) = threshold reaction.*



**Figure :** *Energy derivative of the inelastic neutron emission probability for populating an  $E = S$  energy state (Dirac distribution = energy distribution of populated states).*

# Energy distribution of populated states

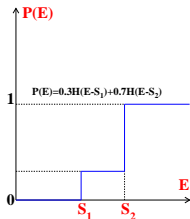


Figure : Inelastic neutron emission probability for populating two energy states  $E = S_1$  and  $E = S_2$  (Heaviside functions)= threshold reactions.

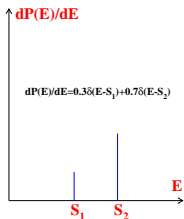
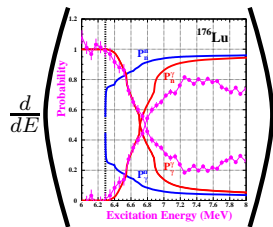


Figure : Energy derivative of the Inelastic neutron emission probability for populating two energy states  $E = S_1$  and  $E = S_2$  (Dirac distributions = energy distribution of populated states).

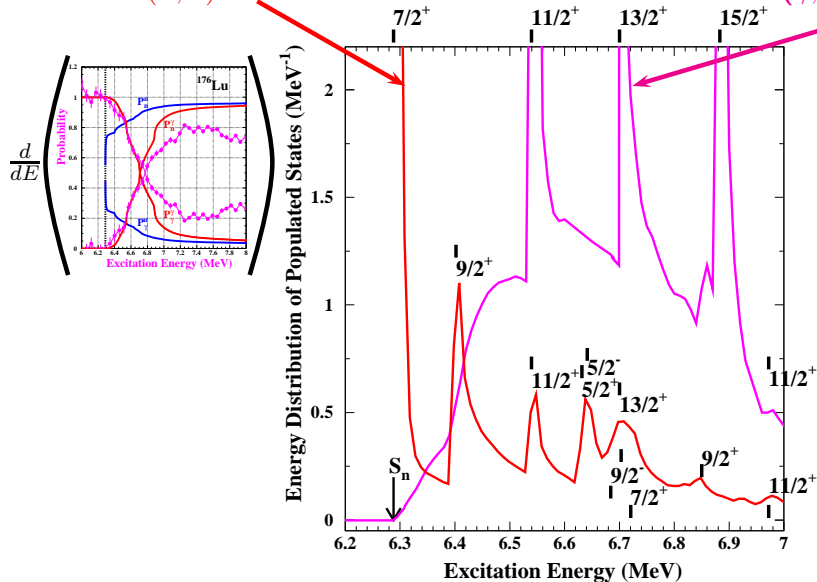
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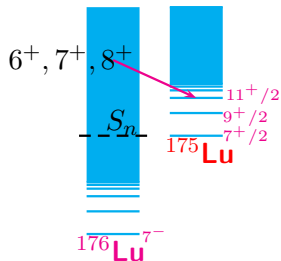
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# Spin/Parity states reached

absorption :  $\gamma + {}^{176}\text{Lu}$  : composition :  $1(-) + 7^-$  states :  $6^+, 7^+, 8^+$  states pop. after n-emission :  $\frac{11^+}{2}, \frac{13^+}{2}$   
 $\frac{15^+}{2}, \frac{17^+}{2}$



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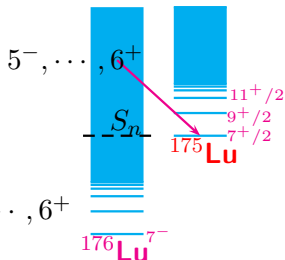
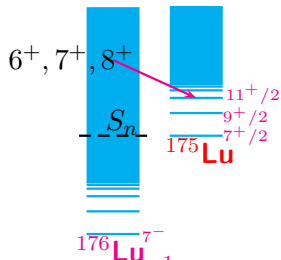
$\gamma + {}^{176}\text{Lu}$  :

$1(-) + 7^{-}$

$6^{+}, 7^{+}, 8^{+}$

$\frac{11}{2}^{+}, \frac{13}{2}^{+}$

$\frac{15}{2}^{+}, \frac{17}{2}^{+}$



$(l = 0, 2) : 1^{+}, \dots, 6^{+}$

$n + {}^{175}\text{Lu}$  :

$\frac{1}{2} + (l = 0) + \frac{7}{2}^{+}$

$\frac{1}{2} + (l = 1) + \frac{7}{2}^{+}$

$\frac{1}{2} + (l = 2) + \frac{7}{2}^{+}$

$\frac{1}{2}^{+}, \dots, \frac{13}{2}^{+}$

$\frac{1}{2}^{-}, \dots, \frac{13}{2}^{-}$

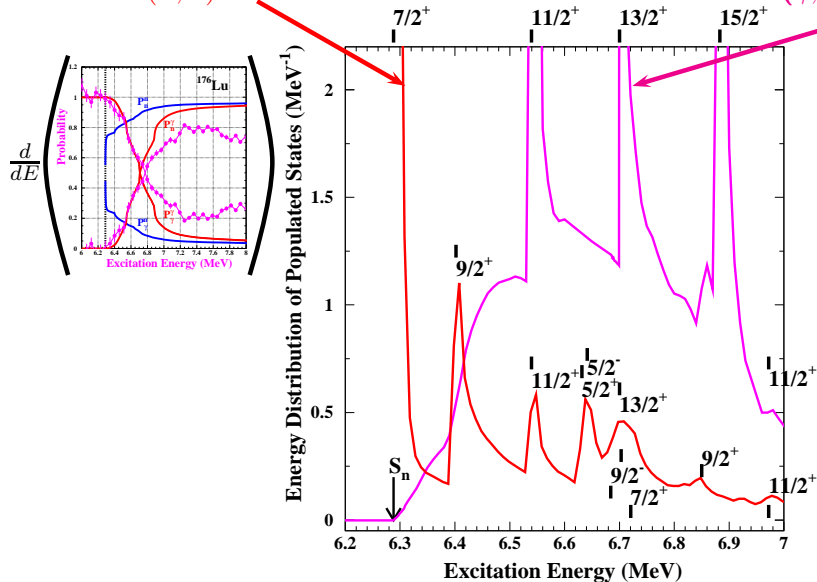
$(l = 1) : 2^{-}, \dots, 5^{-}$



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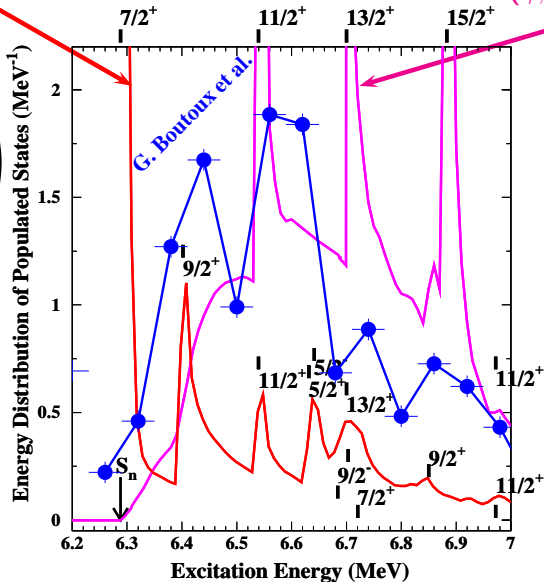
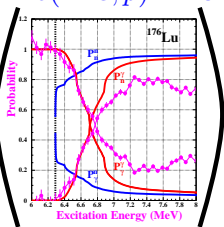
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$\frac{d}{dE}$



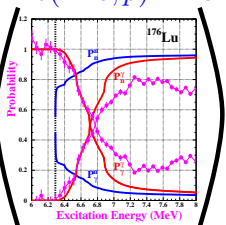
# E.D.P.S : the only 2 exit channels case

$^{175}\text{Lu}(n, n)^{175}\text{Lu}$

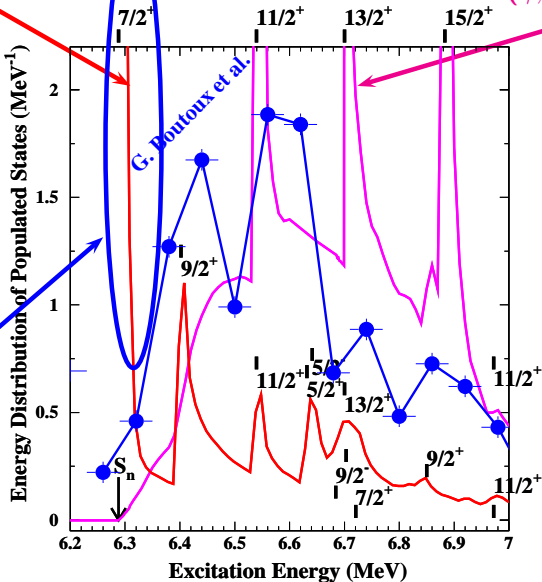
$^{176}\text{Lu}(\gamma, n)^{175}\text{Lu}$

$^{174}\text{Yb}(^3\text{He}, p)^{176}\text{Lu}$

$\frac{d}{dE}$



$CE^{175}\text{Lu}_{gs}$

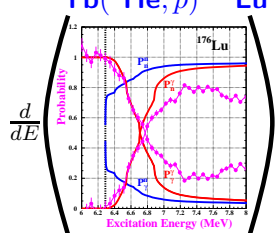


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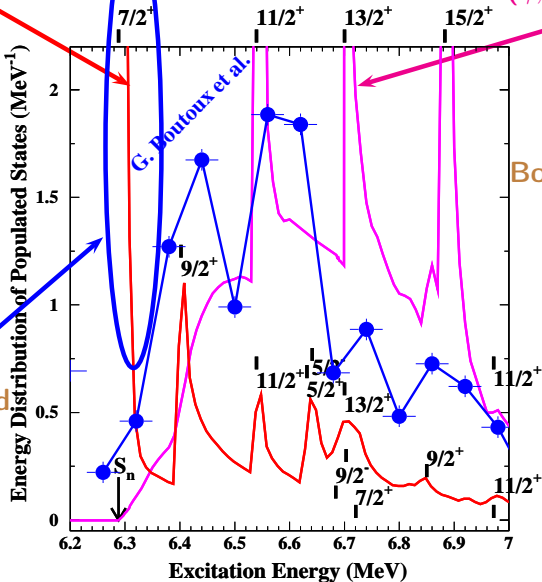
$^{176}\text{Lu}(\gamma, n)^{175}\text{Lu}$

$^{174}\text{Yb}(^3\text{He}, p)^{176}\text{Lu}$



$CE^{175}\text{Lu}_{gs}$

$\frac{dP_n}{dE} \rightarrow J\pi$  populated



Bohr-ography

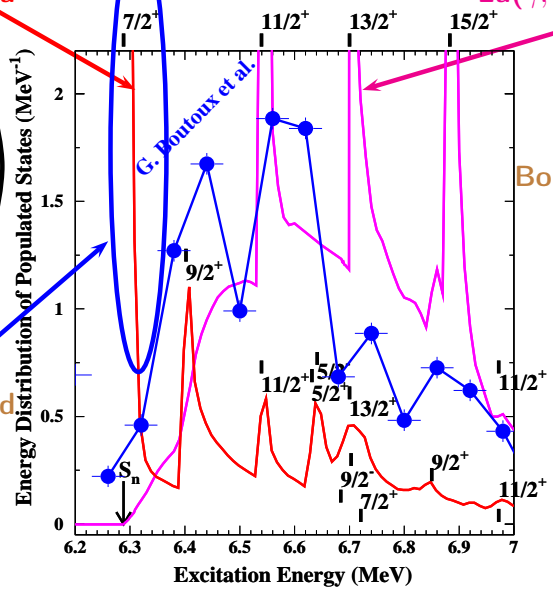
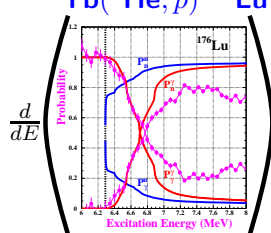


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$^{174}\text{Yb}(^3\text{He}, p)^{176}\text{Lu}$



Bohr-ography

CE  $^{175}\text{Lu}_{gs}$

$\frac{dP_n}{dE} \rightarrow J\pi$  populated  
surrogate

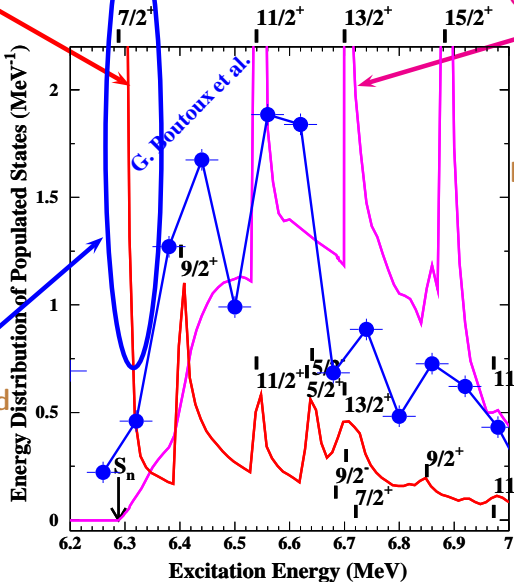
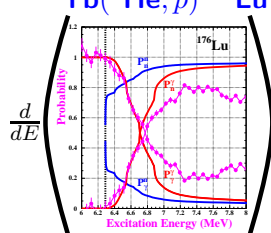


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$^{175}\text{Lu}(n, n)^{175}\text{Lu}$

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$^{174}\text{Yb}(^3\text{He}, p)^{176}\text{Lu}$



Bohr-ography

$CE^{175}\text{Lu}_{gs}$

$\frac{dP_n}{dE} \rightarrow J\pi$  populated

~~sub-gate~~



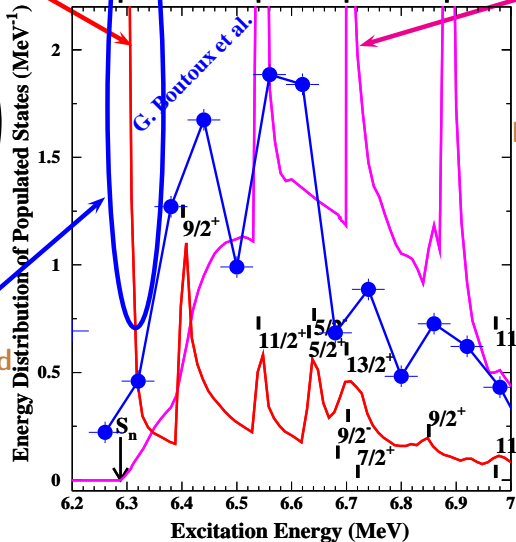
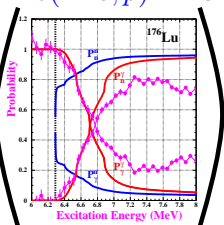
# E.D.P.S : the only 2 exit channels case

$^{175}\text{Lu}(n, n)^{175}\text{Lu}$

$^{176}\text{Lu}(\gamma, n)^{175}\text{Lu}$

$^{174}\text{Yb}(^3\text{He}, p)^{176}\text{Lu}$

$$\frac{d}{dE}$$



Bohr-ography

$CE^{175}\text{Lu}_{gs}$

$\frac{dP_n}{dE} \rightarrow J\pi$  populated

~~substate~~  
forget it

even for fission!

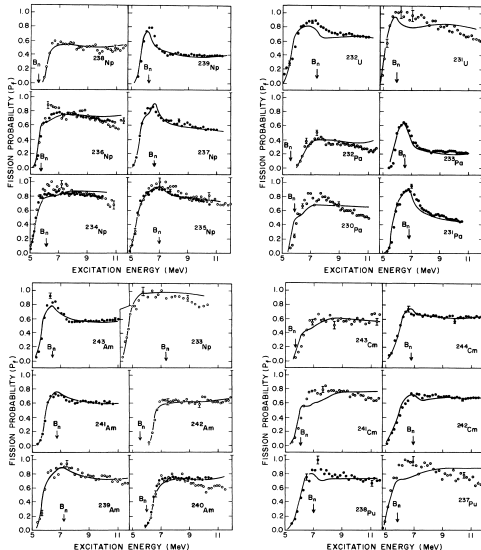


# Fission barriers distributions

2376

GAVRON, BRITT, KONECNY, WEBER, AND WILHELMY

13



fission Probabilities from

Gavron et al. : Phys. Rev. C 13 p. 2374 (1976)

FIG. 2. Measured fission probabilities: open circles, from ( $^3\text{He}, f$ ) reactions; closed circles, from ( $^4\text{He}, d, f$ ) reactions; full lines, model fits as discussed in the text.



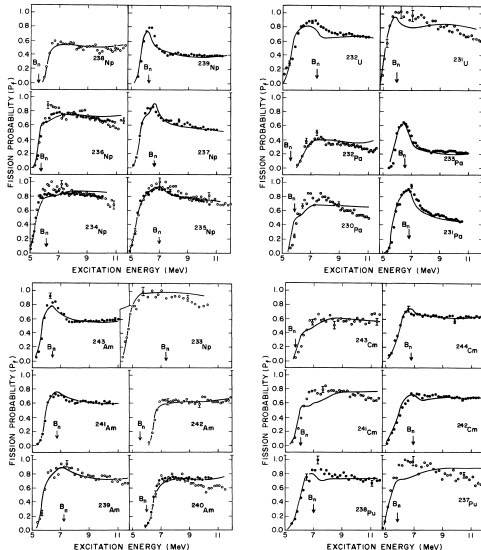
# Fission barriers distributions

$$P_f \rightarrow 1!!!$$

2376

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# Fission barriers distributions

$$P_f \rightarrow 1!!!$$

$^{231}\text{U}$

fission Probabilities from

Gavron et al. : Phys. Rev. C 13 p. 2374 (1976)

2376

GAVRON, BRITT, KONECNY, WEBER, AND WILHELMY

13

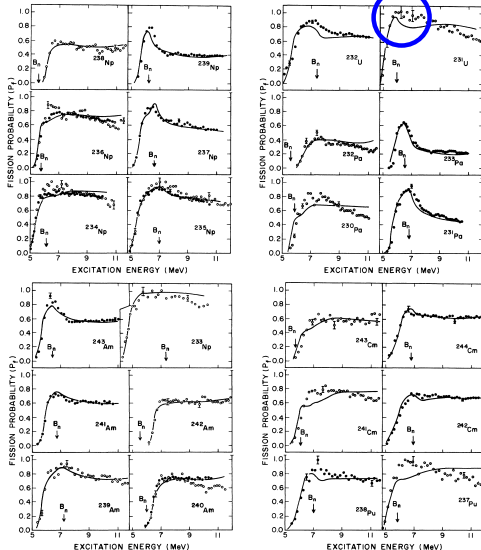


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# Fission barriers distributions

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$^{231}\text{U}$

$^{233,234,235}\text{Np}$

fission Probabilities from

Gavron et al. : Phys. Rev. C 13 p. 2374 (1976)

2376

GAVRON, BRITT, KONECNY, WEBER, AND WILHELMY

13

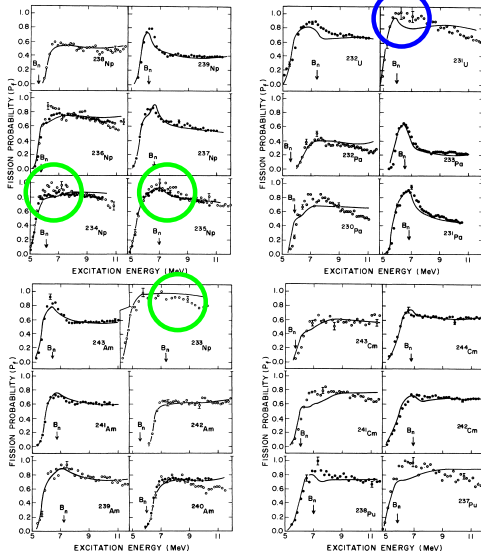


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# Fission barriers distributions

$$P_f \rightarrow 1!!!$$

$^{231}\text{U}$

$^{233,234,235}\text{Np}$

$^{237}\text{Pu}$

fission Probabilities from

Gavron et al. : Phys. Rev. C 13 p. 2374 (1976)

2376

GAVRON, BRITT, KONECNY, WEBER, AND WILHELMY

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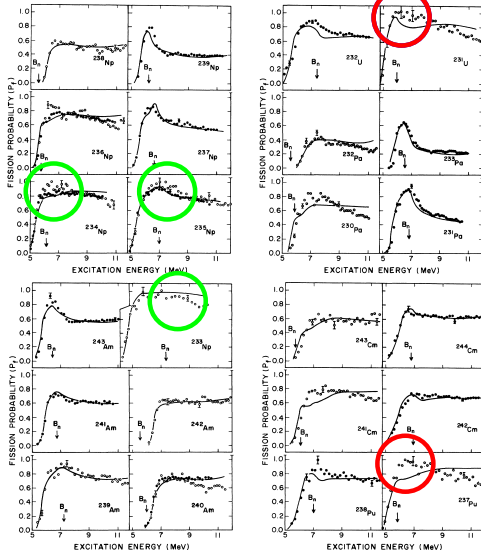


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# Fission barriers distributions

$$P_f \rightarrow 1!!!$$

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$^{233,234,235}\text{Np}$

$^{237}\text{Pu}$

$\Rightarrow \neq J_{SR}\pi_{SR}$  populated

fission Probabilities from

Gavron et al. : Phys. Rev. C 13 p. 2374 (1976)

2376

GAVRON, BRITT, KONECNY, WEBER, AND WILHELMY

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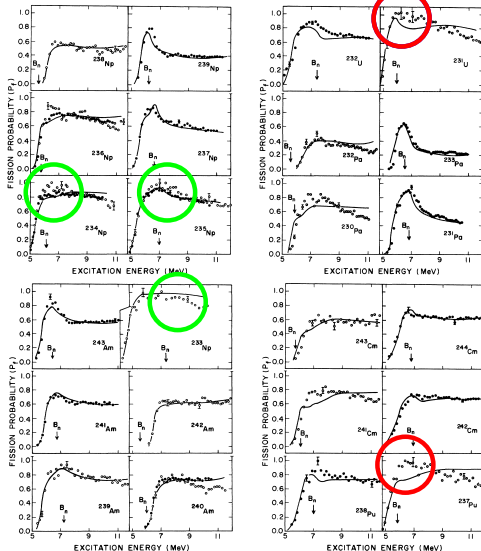


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additionnally  
 $(^3\text{He}, t) \neq (^3\text{He}, d)$

fission Probabilities from

Gavron et al. : Phys. Rev. C 13 p. 2374 (1976)

2376

GAVRON, BRITT, KONECNY, WEBER, AND WILHELMY

13

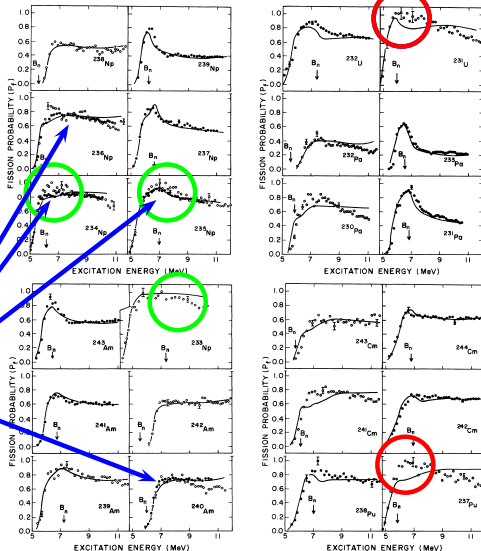


FIG. 2. Measured fission probabilities: open circles, from  $(^3\text{He}, f)$  reactions; closed circles, from  $(^3\text{He}, d)$  reactions; full lines, model fits as discussed in the text.



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$^{237}\text{Pu}$

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additionnally  
 $(^3\text{He}, t) \neq (^3\text{He}, d)$

$P_f \rightarrow 1 \Rightarrow P_n \rightarrow 0$   
 no neutron emissions!!!

fission Probabilities from

Gavron et al. : Phys. Rev. C 13 p. 2374 (1976)

2376

GAVRON, BRITT, KONECNY, WEBER, AND WILHELMY

13

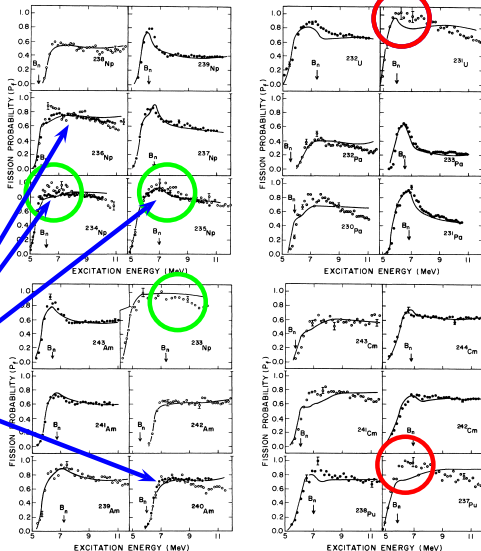


FIG. 2. Measured fission probabilities: open circles, from  $(^3\text{He}, t)$  reactions; closed circles, from  $(^3\text{He}, d)$  reactions; full lines, model fits as discussed in the text.



# Fission barriers distributions

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additionnally  
 $(^3\text{He}, t) \neq (^3\text{He}, d)$

**BUT**

fission Probabilities from

Gavron et al. : Phys. Rev. C 13 p. 2374 (1976)

2376

GAVRON, BRITT, KONECNY, WEBER, AND WILHELMY

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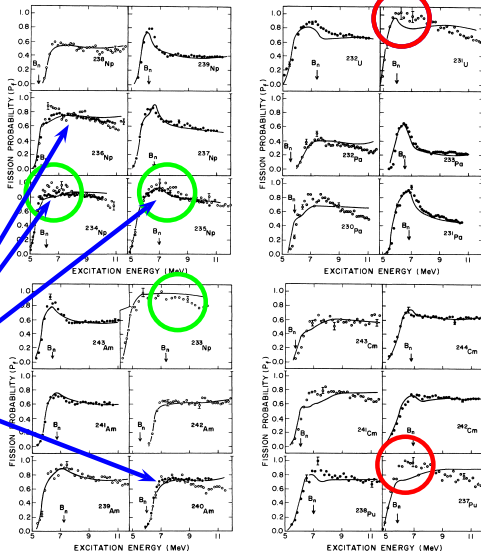


FIG. 2. Measured fission probabilities: open circles, from  $(^3\text{He}, f)$  reactions; closed circles, from  $(^3\text{He}, d)$  reactions; full lines, model fits as discussed in the text.





# Fission barriers distributions = interest of surrogate reactions

Like in heavy ions fusion reactions

it is very interesting to study the energy derivative :

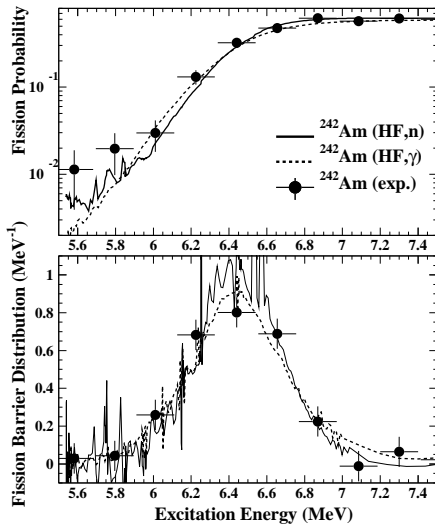
$$\begin{array}{c} \Downarrow \\ \frac{dP_{EC,f}}{dE} = D_f(E) \\ \Downarrow \end{array}$$

$D_f(E)$  defines fission barriers distributions



# Fission barriers distributions

$$D_f(E) = \frac{dP_f(E)}{dE}$$



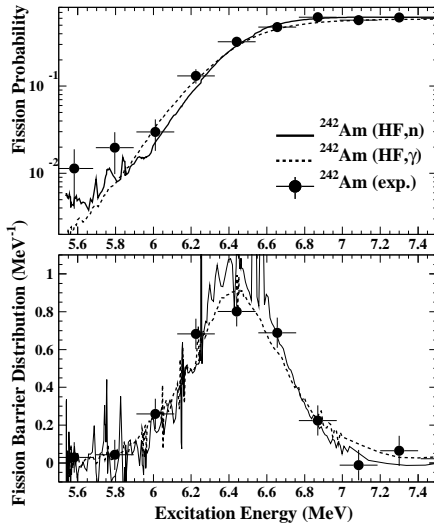
$SR = ({}^3\text{He}, \alpha f)$

# Fission barriers distributions

$$D_f(E) = \frac{dP_f(E)}{dE}$$

↓

$$\langle B \rangle = \frac{\int E D_f(E) dE}{\int D_f(E) dE}$$



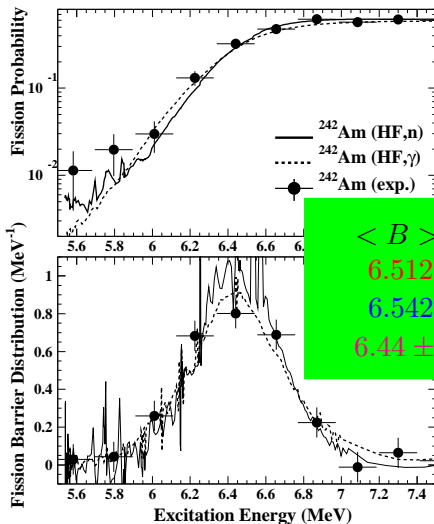
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$$D_f(E) = \frac{dP_f(E)}{dE}$$

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SR = ( $^3\text{He}, \alpha f$ )

# Fission barriers distributions

$$D_f(E) = \frac{dP_f(E)}{dE}$$



$$\langle B \rangle = \frac{\int ED_f(E)dE}{\int D_f(E)dE}$$

consistency  
between *EC*

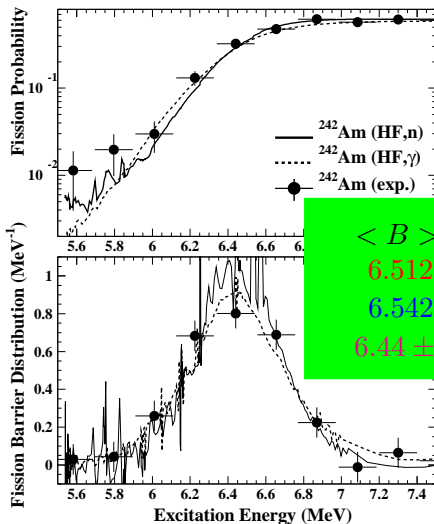
HOPE

surrogate for  
fission



$\langle B^{exp} \rangle$

completely exp.  
using no model



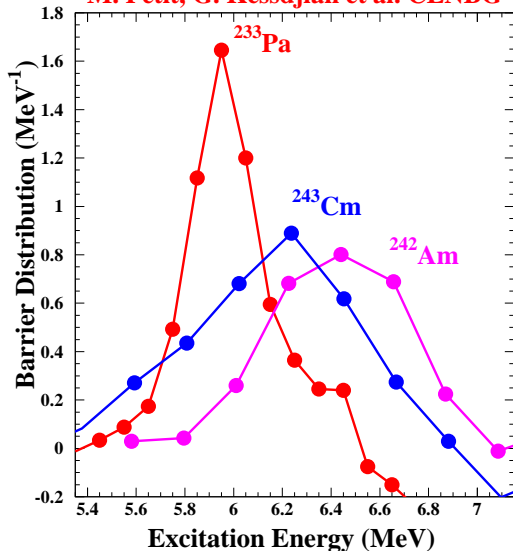
$SR = ({}^3\text{He}, \alpha f)$

$\langle B \rangle$	reaction
6.512	$n, f$
6.542	$\gamma, f$
$6.44 \pm 0.11$	SR

# Fission barriers distributions

$$D_f(E) = \frac{dP_f(E)}{dE}$$

M. Petit, G. Kessedjian et al. CENBG



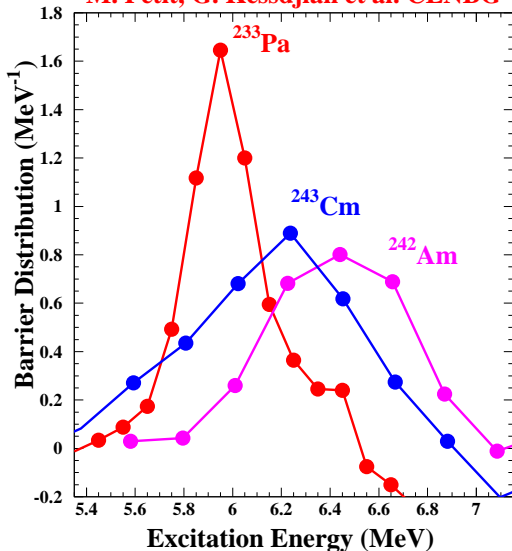
# Fission barriers distributions

$$D_f(E) = \frac{dP_f(E)}{dE}$$

⇓

$$\langle B \rangle = \frac{\int ED_f(E)dE}{\int D_f(E)dE}$$

M. Petit, G. Kessedjian et al. CENBG



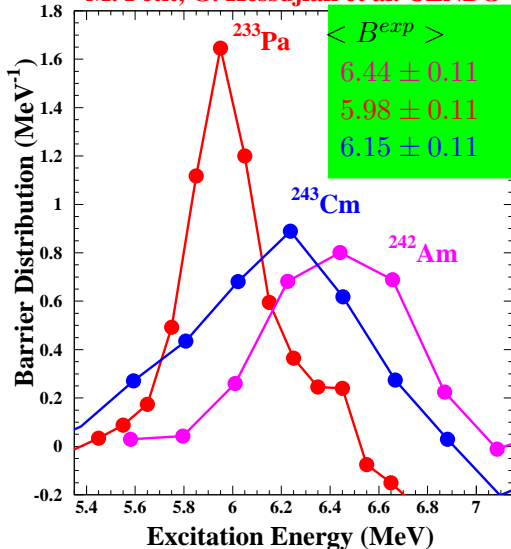
# Fission barriers distributions

$$D_f(E) = \frac{dP_f(E)}{dE}$$

↓

$$\langle B \rangle = \frac{\int ED_f(E)dE}{\int D_f(E)dE}$$

M. Petit, G. Kessedjian et al. CENBG



$\langle B^{exp} \rangle$

$6.44 \pm 0.11$

$5.98 \pm 0.11$

$6.15 \pm 0.11$

Bjorn-Lynn

$6.5 \pm 0.2$

$6.1 \pm 0.3$

$6.4 \pm 0.3$





# Fission barriers distributions

$$D_f(E) = \frac{dP_f(E)}{dE}$$

↓

$$\langle B \rangle = \frac{\int ED_f(E)dE}{\int D_f(E)dE}$$

HOPE

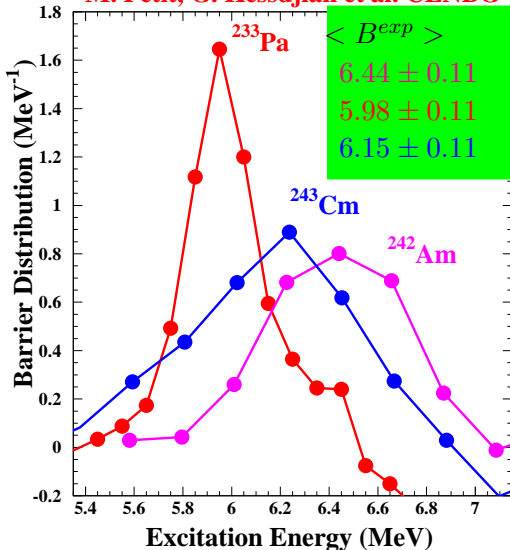
surrogate for  
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↓

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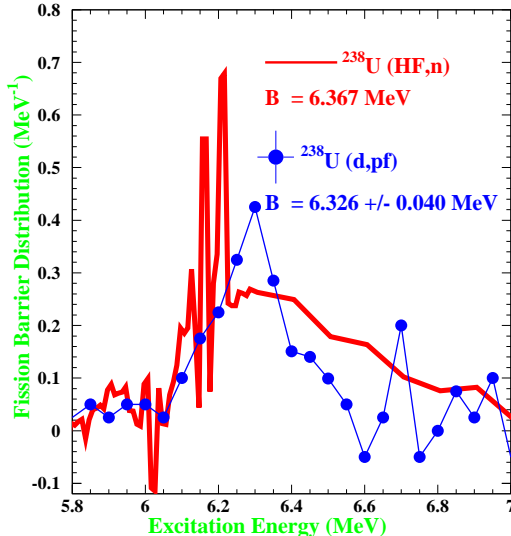
more accessible to Harmonic

cea

# Fission barriers distributions

$$D_f(E) = \frac{dP_f(E)}{dE}$$

$P_f(E) = Q$ . Ducasse et al. CENBG ND2013



$SR = (d, pf)$

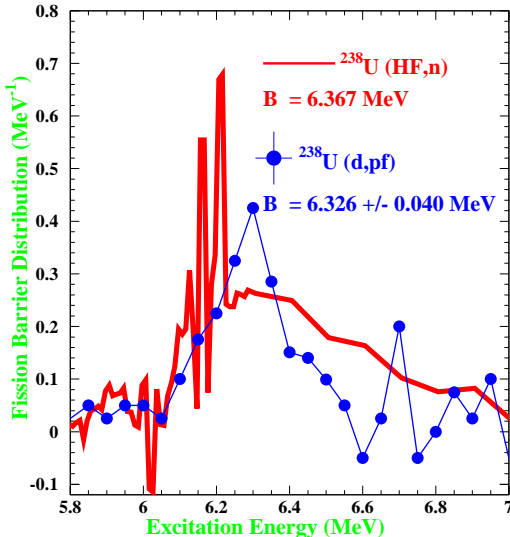
# Fission barriers distributions

$$D_f(E) = \frac{dP_f(E)}{dE}$$

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$$\langle B \rangle = \frac{\int E D_f(E) dE}{\int D_f(E) dE}$$

$P_f(E) = Q$ . Ducasse et al. CENBG ND2013



$SR = (d, pf)$

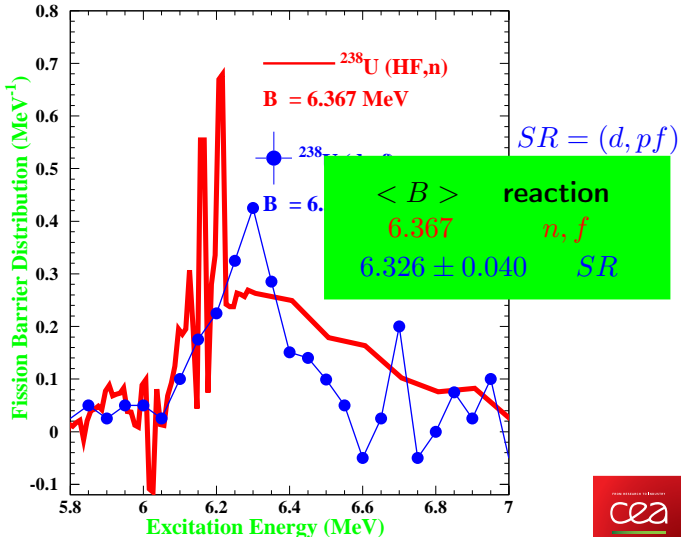
# Fission barriers distributions

$$D_f(E) = \frac{dP_f(E)}{dE}$$

↓

$$\langle B \rangle = \frac{\int ED_f(E)dE}{\int D_f(E)dE}$$

$P_f(E) = Q$ . Ducasse et al. CENBG ND2013



# Fission barriers distributions

$$D_f(E) = \frac{dP_f(E)}{dE}$$

↓

$$\langle B \rangle = \frac{\int ED_f(E)dE}{\int D_f(E)dE}$$

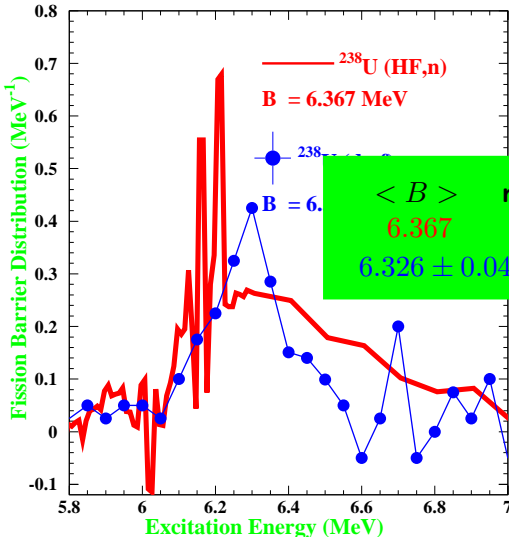
consistency  
between *EC*

HOPE  
surrogate for  
fission

↓

$\langle B^{exp} \rangle$   
completely exp.  
using no model

$P_f(E) = Q$ . Ducasse et al. CENBG ND2013



$\langle B \rangle$  reaction  
6.367  $n, f$   
6.326 ± 0.040  $SR$

# Fission barriers distributions (interest of surrogate)

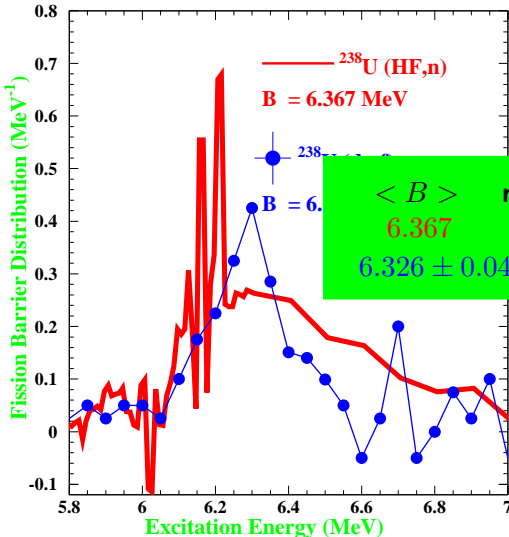
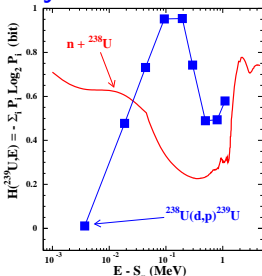
$$D_f(E) = \frac{dP_f(E)}{dE}$$



$$\langle B \rangle = \frac{\int E D_f(E) dE}{\int D_f(E) dE}$$

Since  $P_f$  and  $P_\gamma$   
simul. measured  
by Ducasse et al.

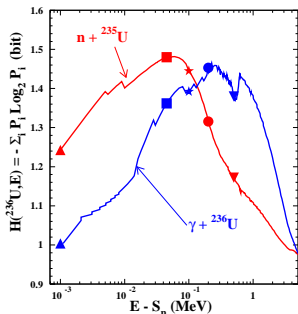
$P_f(E) = Q$ . Ducasse et al. CENBG ND2013



$SR = (d, pf)$

$\langle B \rangle$  reaction  
6.367  $n, f$   
6.326 ± 0.040  $SR$

# Use of Shannon theorem for : $n + {}^{235}\text{U} \leftrightarrow \gamma + {}^{236}\text{U}$



**Figure :** Lack of information  $H_\gamma({}^{236}\text{U}, E)$  et  $H_n({}^{236}\text{U}, E)$  on compound emissions processes, related to a given entrance channel EC, (plotted versus  $E - S_n$ ).

$$H_{EC}(CN, E) = -P_{EC,\gamma}(E) \log_2 P_{EC,\gamma}(E) - P_{EC,n}(E) \log_2 P_{EC,n}(E) - P_{EC,f}(E) \log_2 P_{EC,f}(E).$$

Bohr independence hypothesis in term of Shannon theorem re-writes :

$$H_{EC1}(CN, E) = H_{EC2}(CN, E).$$

**BUT HERE :**

$$\begin{array}{ccc} H_n({}^{236}\text{U}, E) & \neq & H_\gamma({}^{236}\text{U}, E) \\ & \Downarrow & \\ J_n, \pi_n & \neq & J_\gamma, \pi_\gamma \end{array}$$

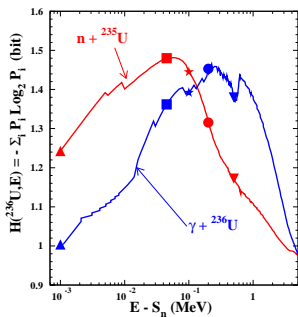
or at least

**Bohr independence hypothesis failed for  $E \sim S_n$  with incident  $n$  since  $W > 1$**

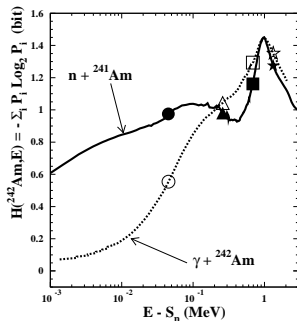
**Do not use Weisskopf-Ewing approximation !**



# Use of Shannon theorem for : $n + {}^{235}\text{U} \leftrightarrow \gamma + {}^{236}\text{U}$



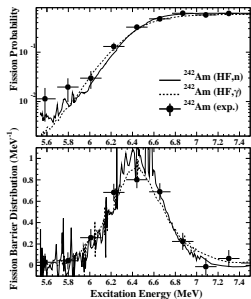
**Figure :** Lack of information  $H_\gamma({}^{236}\text{U}, E)$  et  $H_n({}^{236}\text{U}, E)$  on compound emissions processes, related to a given entrance channel  $EC$ , (plotted versus  $E - S_n$ ).



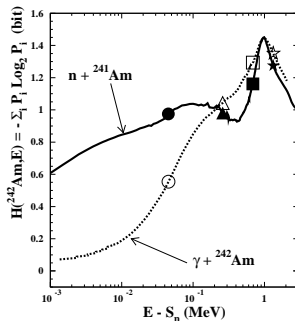
**Figure :** Lack of information  $H_\gamma({}^{242}\text{Am}, E)$  et  $H_n({}^{242}\text{Am}, E)$  on compound emissions processes, related to a given entrance channel  $EC$ , (plotted versus  $E - S_n$ ).



# Use of Shannon theorem for : $n+^{235}\text{U} \leftrightarrow \gamma+^{236}\text{U}$

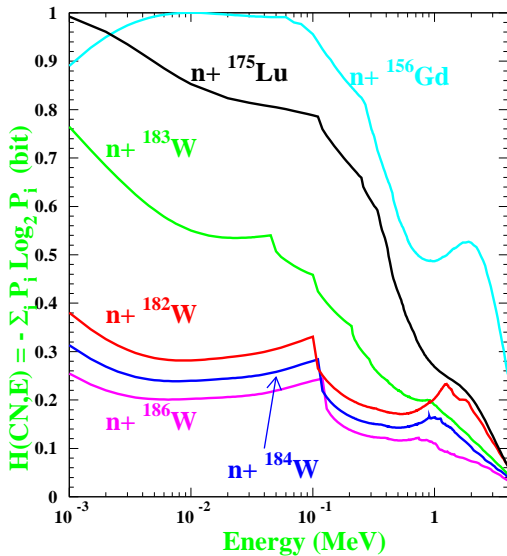


**Figure :** (top) Fission probabilities of <sup>242</sup>Am CN formed by different EC : (n, f), (γ, f) and SR (<sup>3</sup>He, αf), plotted versus excitation energy. (bottom) fission barriers distributions.

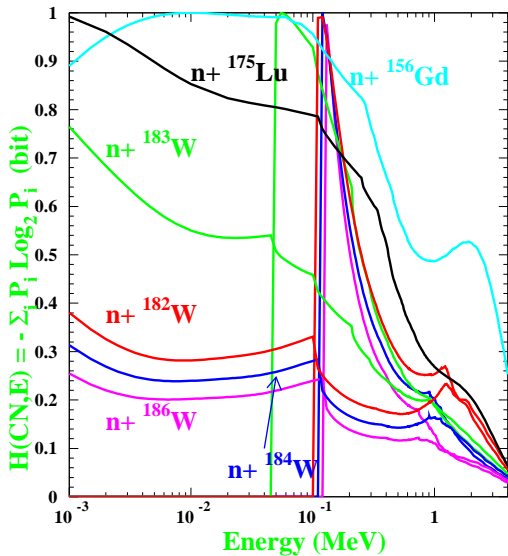


**Figure :** Lack of information  $H_\gamma(^{242}\text{Am}, E)$  et  $H_n(^{242}\text{Am}, E)$  on compound emissions processes, related to a given entrance channel EC, (plotted vs  $E - S_n$ ).

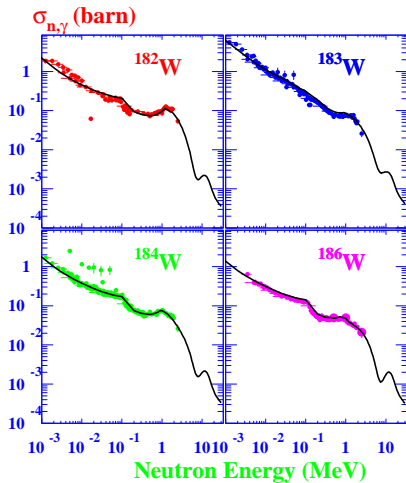
## back to rare earth nuclei : the W isotopes



# Lack of information on comp./non-elas. emission processes



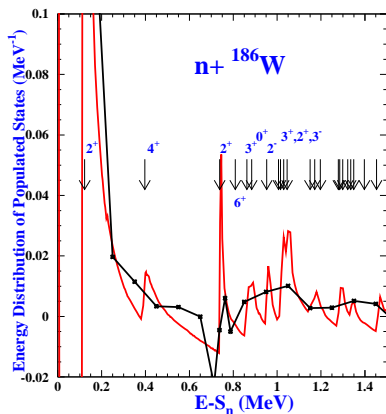
# capture the way to inelastic scattering



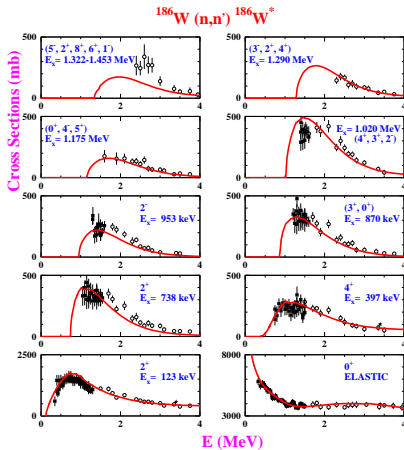
energy derivative of calculated capture probability

energy derivative of measured capture probability

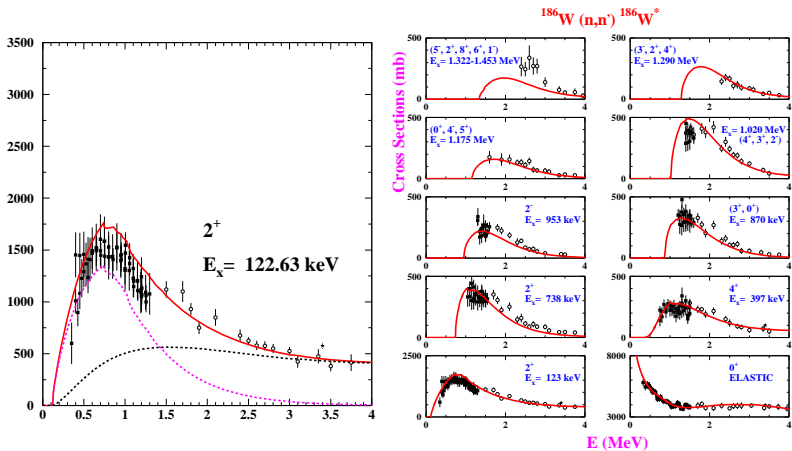
$$P_{\gamma} = \frac{\sigma_{n,\gamma}}{\sigma_{CN}} \text{ with } \sigma_{CN} = 3 \text{ b}$$



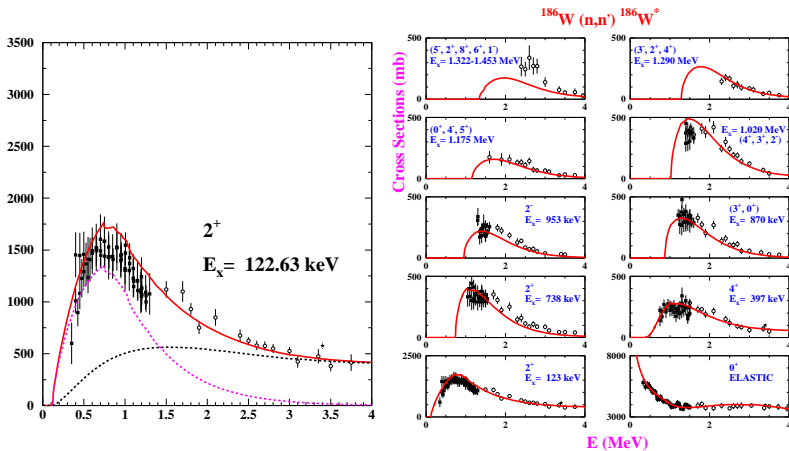
D.Lister et al., P.T. Guenther et al. (ANL)



D.Lister et al., P.T. Guenther et al. (ANL)

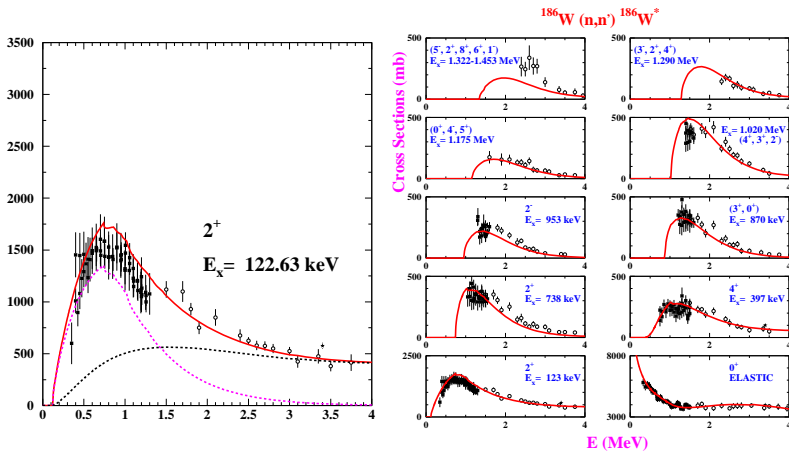


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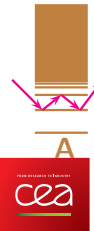
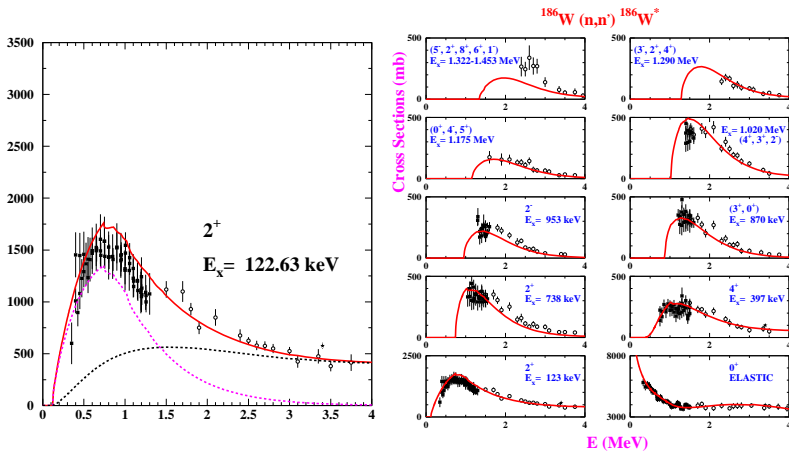




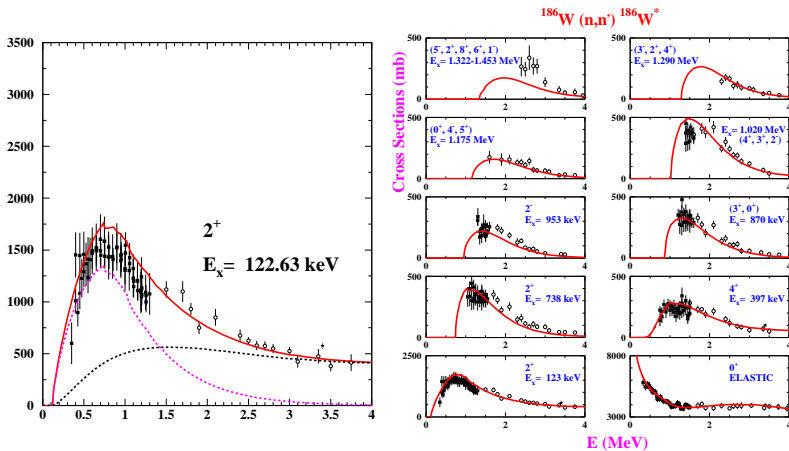
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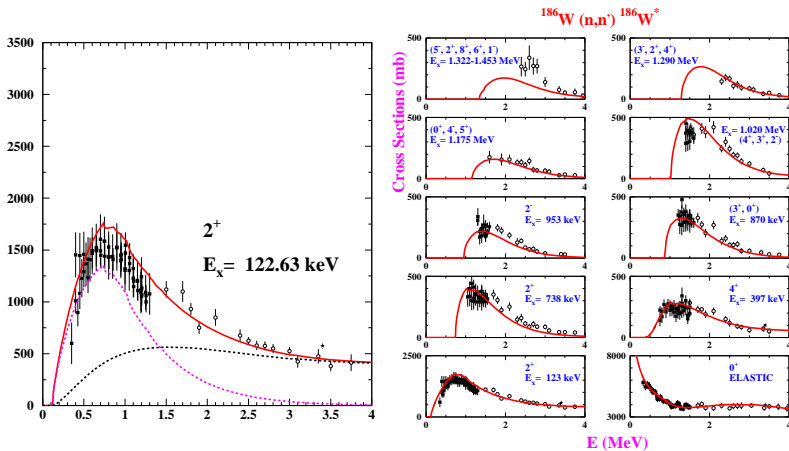
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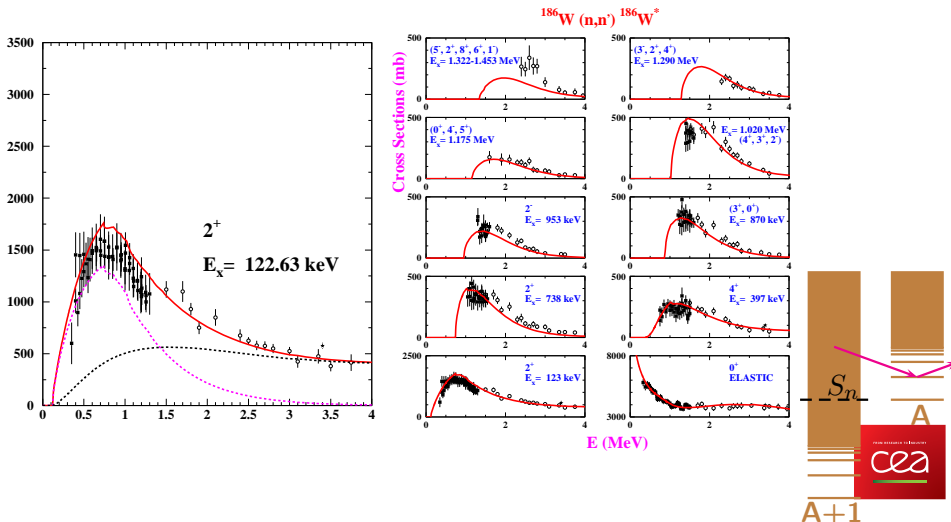
D. Lister et al., P.T. Guenther et al. (ANL)



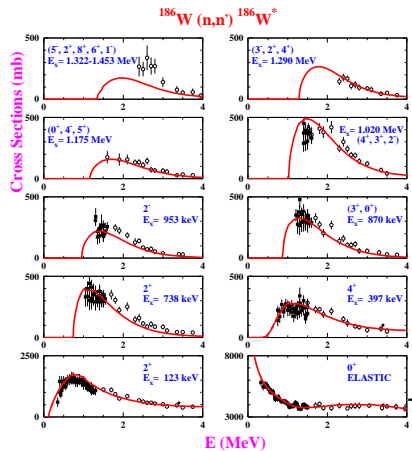
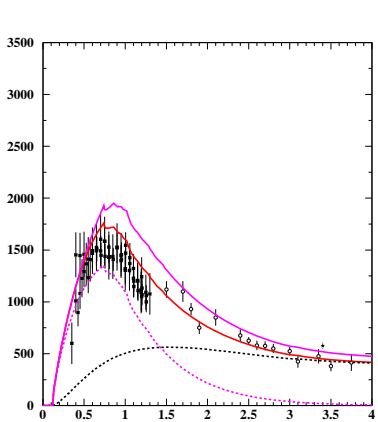
D. Lister et al., P.T. Guenther et al. (ANL)



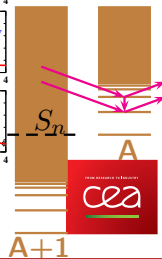
D.Lister et al., P.T. Guenther et al. (ANL)



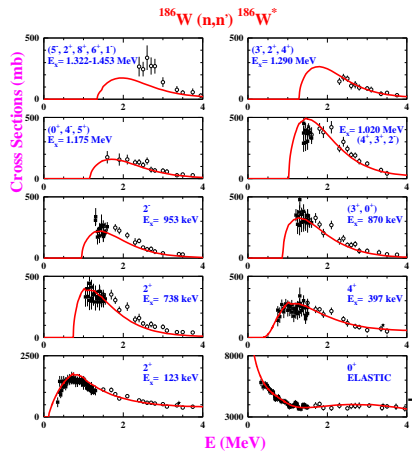
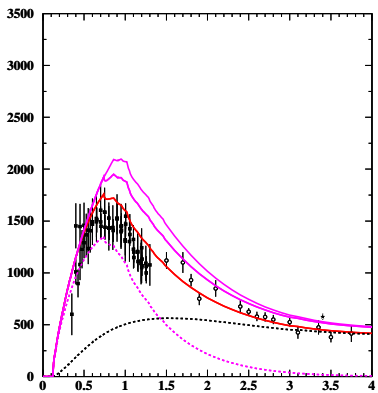
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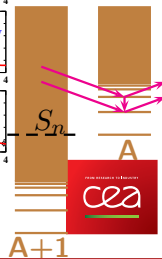
Weighted by right branching ratio



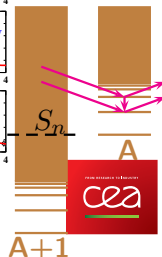
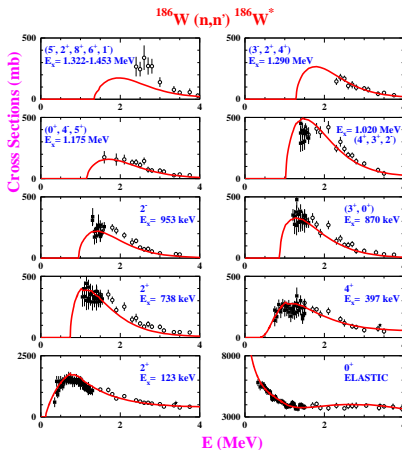
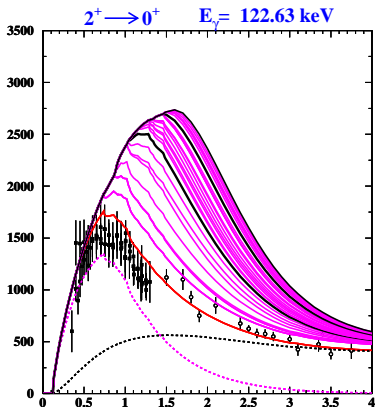
D.Lister et al., P.T. Guenther et al. (ANL)



Weighted by right branching ratio

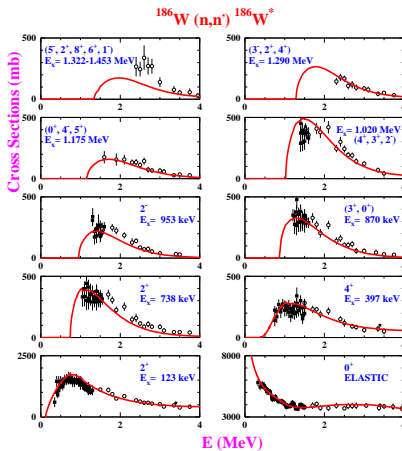
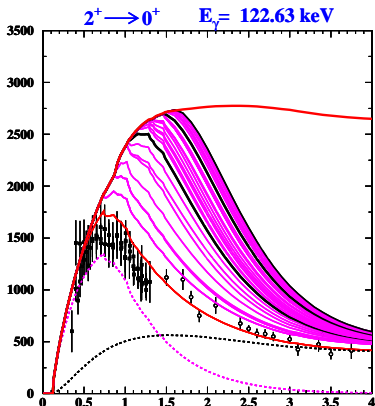


D.Lister et al., P.T. Guenther et al. (ANL)

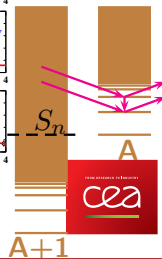




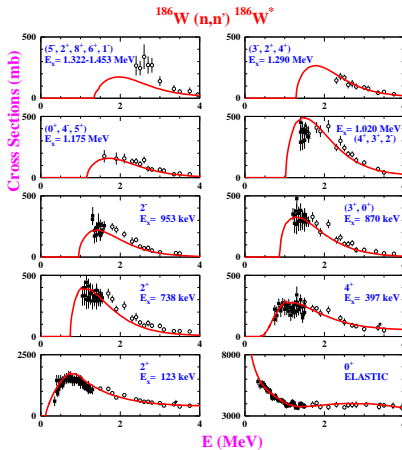
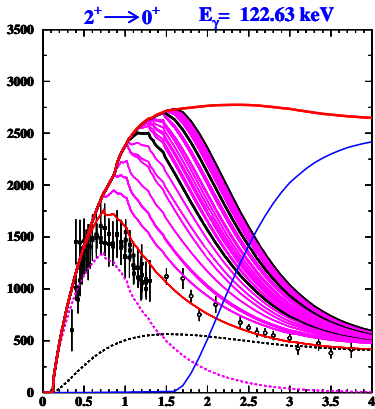
D.Lister et al., P.T. Guenther et al. (ANL)



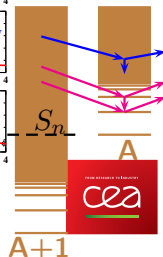
Weighted by right branching ratio



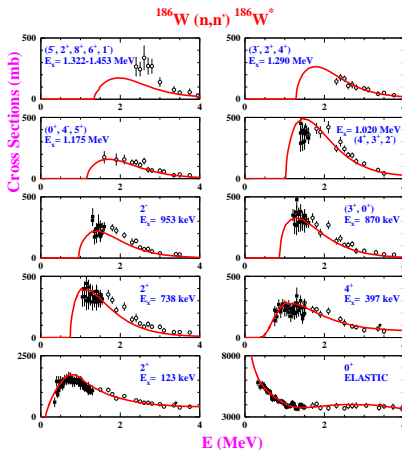
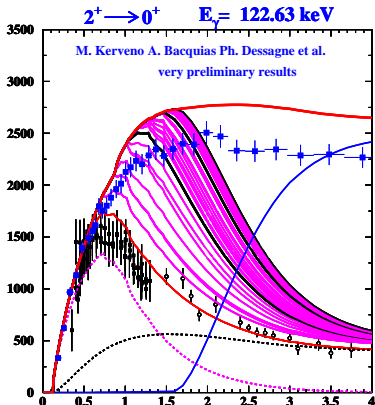
D.Lister et al., P.T. Guenther et al. (ANL)



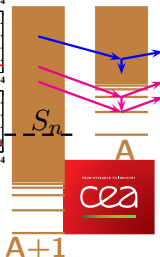
Weighted by right branching ratio



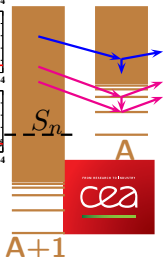
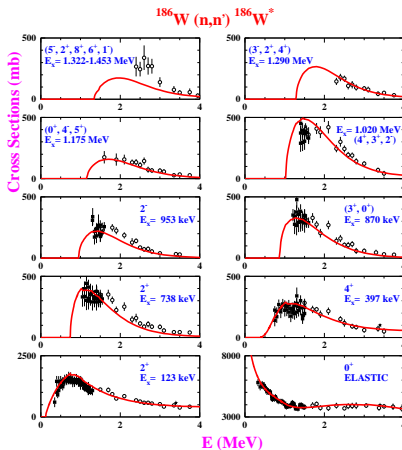
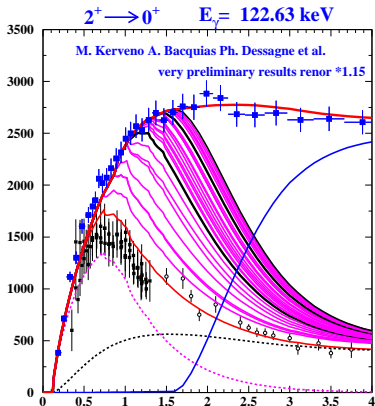
Branching ratios?? D.Lister et al., P.T. Guenther et al. (ANL)



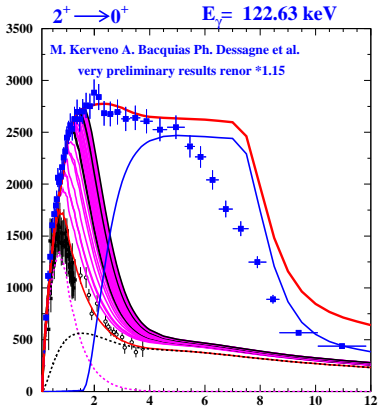
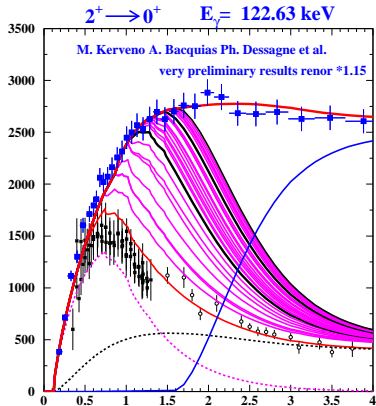
Weighted by right branching ratio



Branching ratios?? D.Lister et al., P.T. Guenther et al. (ANL)



## Branching ratios?? Spin distributions of PE models??



Back to actinides inelastic cross section :

Back to actinides inelastic cross section : the special  $^{238}\text{U}$  case!!!!



Back to actinides inelastic cross section : the special  $^{238}\text{U}$  case!!!!

An "inelasti-genic" nucleus





For energies  $E < E_{(n,2n)}^{threshold}$ , we can write :

$$\sigma_R = \sigma_{CE} + \sigma_{n,n'} + \sigma_{n,\gamma} + \sigma_{n,f}$$

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and finally :

$$\sigma_R - \sigma_{CE} = \sigma_{n,n'} + \sigma_{n,\gamma} + \sigma_{n,f} = \sigma_{non-elas}$$

$$1 = \frac{\sigma_{n,n'}}{\sigma_{non-elas}} + \frac{\sigma_{n,\gamma}}{\sigma_{non-elas}} + \frac{\sigma_{n,f}}{\sigma_{non-elas}}$$

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$$1 = \frac{\sigma_{n,n'}}{\sigma_{non-elas}} + \frac{\sigma_{n,\gamma}}{\sigma_{non-elas}} + \frac{\sigma_{n,f}}{\sigma_{non-elas}}$$

For each non-elastic process GLOBAL probabilities can be defined :

$$1 = P_{n,n'}^{non-elas} + P_{n,\gamma}^{non-elas} + P_{n,f}^{non-elas}$$

For energies  $E < E_{(n,2n)}^{threshold}$ , we can write :

$$\sigma_R = \sigma_{CE} + \sigma_{n,n'} + \sigma_{n,\gamma} + \sigma_{n,f}$$

and finally :

$$\sigma_R - \sigma_{CE} = \sigma_{n,n'} + \sigma_{n,\gamma} + \sigma_{n,f} = \sigma_{non-elas}$$

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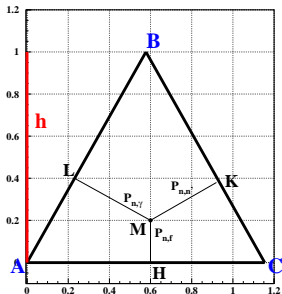
These probabilities are also directly deduced from evaluated files :

$$\sigma_{non-elas} = MF_3MT_4 + MF_3MT_{102} + MF_3MT_{18}$$

$$1 = \frac{MF_3MT_4}{\sigma_{non-elas}} + \frac{MF_3MT_{102}}{\sigma_{non-elas}} + \frac{MF_3MT_{18}}{\sigma_{non-elas}}$$



# Dalitz Representation



**Figure :** Dalitz representation of non-elastic processes in the energy range 1 keV

$$\langle E \rangle < E_{(n,2n)}^{threshold}$$

For these three open channels a Dalitz representation can be used. Indeed for an equilateral triangle  $ABC$  ( $AB = AC = BC$ ) with height  $h$ , each point  $M$  inside this triangle satisfies the following property :

$$MH + MK + ML = h$$

where  $H, K, L$  are the  $M$  orthogonal projections on each side  $[AC]$ ,  $[BC]$  et  $[AB]$  respectively. When assuming :

$$MH = P_{n,f}^{non-elas}, ML = P_{n,\gamma}^{non-elas},$$

$$MK = P_{n,n'}^{non-elas} \text{ with } h = 1$$

$$MH + MK + ML = P_{n,n'}^{non-elas} + P_{n,\gamma}^{non-elas} + P_{n,f}^{non-elas} = 1$$

Then each set

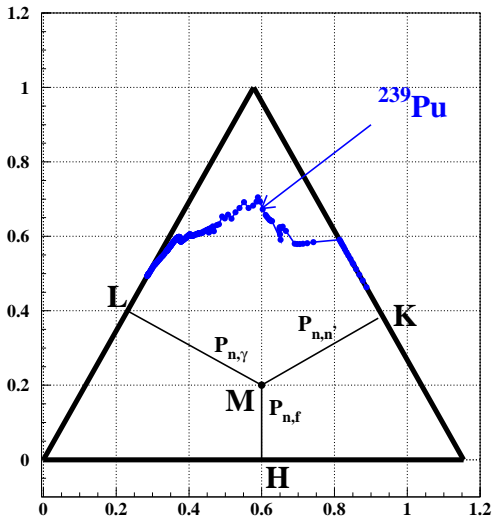
$$(E, \sigma_{n,n'}, \sigma_{n,\gamma}, \sigma_{n,f}) =$$

$$(E, MF_3MT_4, MF_3MT_{102}, MF_3MT_{18})$$

of an evaluated file can be represented by a corresponding point  $M$  inside an equilateral triangle  $ABC$  with unitary height ( $h = 1$ ). And finally an evaluated file will display a path inside this equilateral triangle.

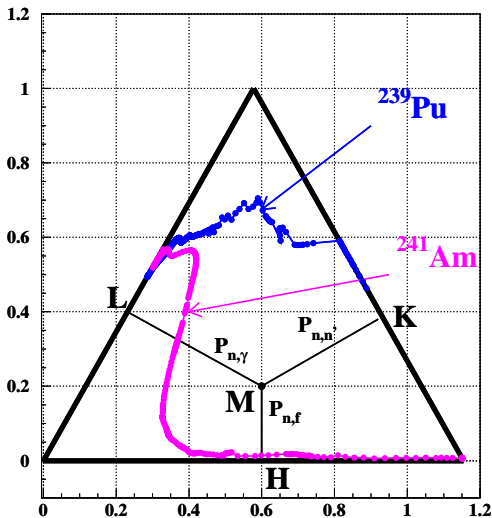
# Dalitz Representation of non-elastic processes on 1 keV

$\langle E \rangle < E_{(n,2n)}^{threshold}$  energy range



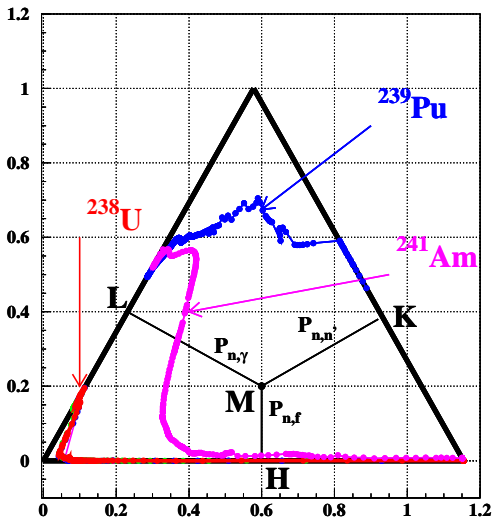
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# Dalitz Representation of non-elastic processes on 1 keV

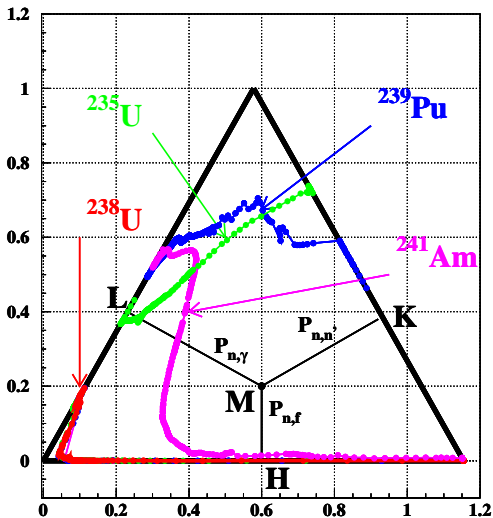
$\langle E \rangle < E_{(n,2n)}^{threshold}$  energy range





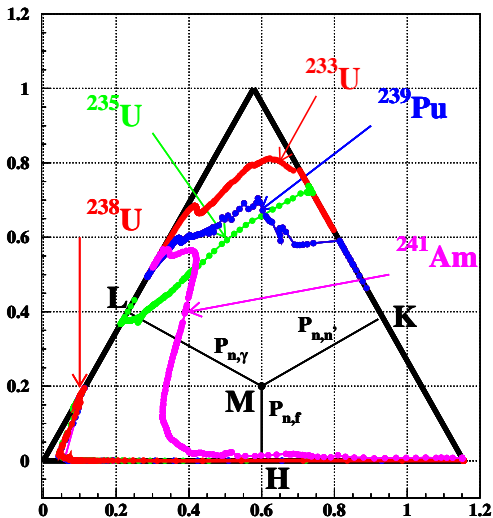
# Dalitz Representation of non-elastic processes on 1 keV

$\langle E \rangle < E_{(n,2n)}^{threshold}$  energy range



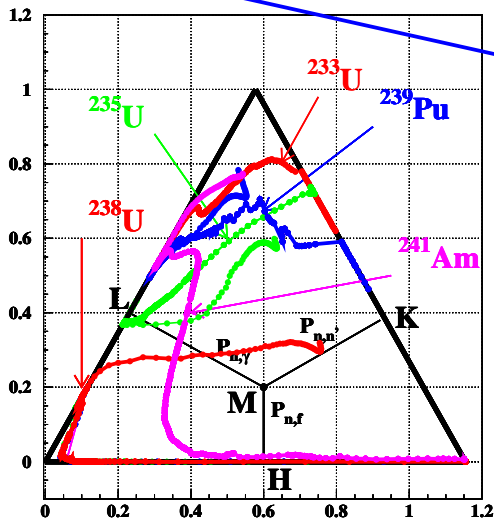
# Dalitz Representation of non-elastic processes on 1 keV

$\langle E \rangle < E_{(n,2n)}^{threshold}$  energy range



# Dalitz Representation of non-elastic processes on 1 keV

$\langle E \rangle < E_{(n,2n)}^{threshold}$  energy range



$E_{(n,3n)}^{threshold}$

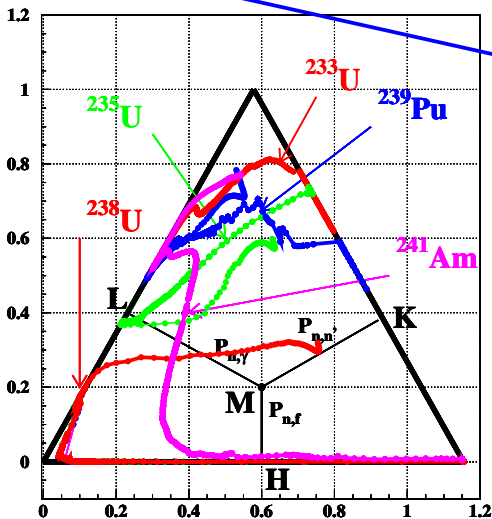
$P_{n,\gamma}^{non-elas} \approx 0$

$P_{n,\gamma}^{non-elas} \leftrightarrow P_{n,2n}^{non-elas}$



# Dalitz Representation of non-elastic processes on 1 keV

$\langle E \rangle < E_{(n,2n)}^{threshold}$  energy range



$E_{(n,3n)}^{threshold}$

$$P_{n,\gamma}^{non-elas} \approx 0$$

$$P_{n,\gamma}^{non-elas} \leftrightarrow P_{n,2n}^{non-elas}$$

For  $^{238}\text{U}$  always

$$P_{n,n'}^{non-elas} > P_{n,f}^{non-elas}$$

and mostly

$$P_{n,2n}^{non-elas} > P_{n,f}^{non-elas}$$

$\Rightarrow$   $^{238}\text{U}$  prefers  $n$ -emissions as fission



# Dalitz Representation - $^{238}\text{U}$ (BRC - ENDF-B/VII)

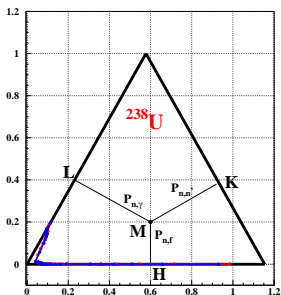


Figure : Dalitz representation of non-elastic processes in the energy range  $50 \text{ keV} < E < E_{(n,2n)}^{\text{threshold}}$ . Here were considered the same energy points (between BRC and ENDF-B/VII) joined by black straight lines.

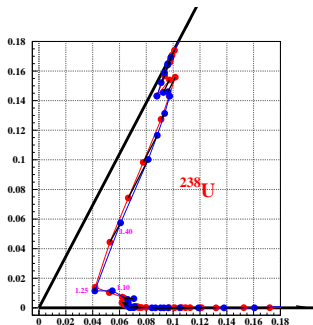


Figure : Dalitz representation of non-elastic processes for energies  $0.2 < E < 1.3 \text{ MeV}$ . Here were considered the same energy points (between BRC and ENDF-B/VII) joined by black straight lines.

# Dalitz Representation - $^{238}\text{U}$ (BRC - ENDF-B/VII)

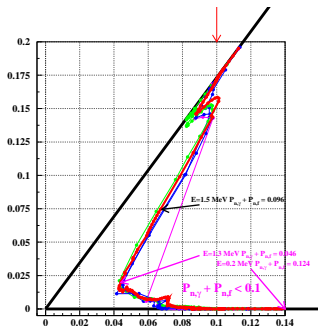


Figure : Dalitz representation of non-elastic processes for energies  $0.2 < E < 1.3$  MeV and for different evaluations : BRC - ENDF-B/VII - JENDL4.0 - JEFF3.1. All Eval. are nearly the same

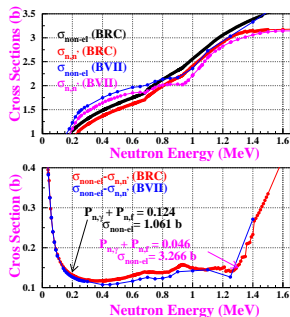


Figure : Top : evaluated (BRC - ENDF-B/VII) inelastic cross sections compared to the BRC non-elastic cross section for energies  $0.2 < E < 1.3$  MeV. Bottom : sum of capture and fission cross sections for energies  $0.2 < E < 1.3$  MeV.



$\sigma_{BRC} \neq \sigma_{ENDF-B/VII}$  but identical prob. (=ratio).

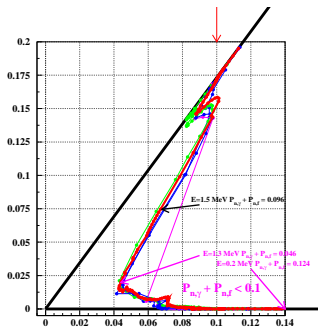


Figure : Dalitz representation of non-elastic processes for energies  $0.2 < E < 1.3$  MeV and for different evaluations : **BRC** - **ENDF-B/VII** - **JENDL4.0** - **JEFF3.1**. All Eval. are nearly the same

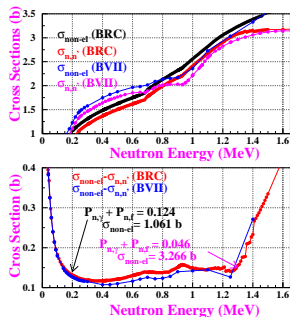


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## $^{238}\text{U}$ surprising effect

In the energy range  $0.2 < E < 1.3$  MeV :

$$\sigma_{n,n'} \approx \sigma_{non-elas}$$

or more precisely

$$\sigma_{non-elas} \times 90\% < \sigma_{n,n'} < \sigma_{non-elas} \times 95\%$$

OK, but in this energy range  $\sigma_{non-elas}$  depends on **OMP choices** :  
**coupling scheme effects**  
**and deformation parameters of course.**





OMP : Dispersive OP

Choice of Coupling Scheme

$(n, xn\gamma)$  : What about Branching ratios

$(n, xn\gamma)$  : What about Spin Distributions in the PE models

Inelastic XS (waste XS?)

Measurements of this XS would be of great interest But effectively experimental limits (to separate Inel. scat. to the low-lying states from the elast. scat.)

$^{238}\text{U}$  : an "inelasti-genic" nucleus

Surrogate Reactions : Forget it, but nevertheless interesting to deduce fission barriers height

