



Uranie

## Plateforme Incertitude & Optimisation

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ATELIER ESNT

ORME DES MERISIERS, SACLAY

13 Février 2014



- Introduce the ROOT framework
- The Uranie platform
- Applications :
  - Launcher
  - Optimisation



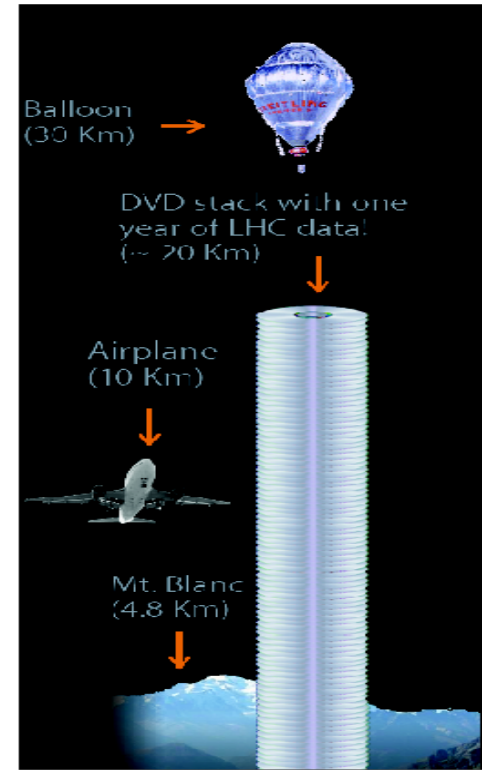


- particle accelerator
- 27 km circumference tunnel in Geneva
- 4 experiments (ATLAS, CMS, ALICE, LHCb)

Study the structure of matter

- Search for the Higgs boson
- Search for new physics

- Data quantity generated : 20 PetaBytes/year
- ROOT is the framework to store, treat and analyze this data

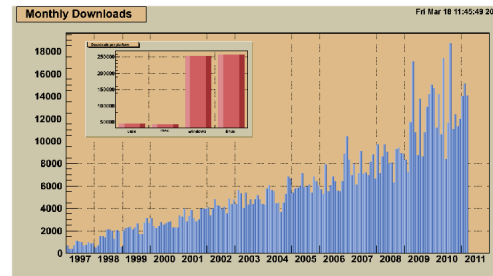
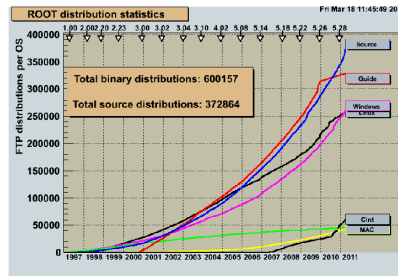


Fons Rademakers / CERN






ROOT is an object-oriented framework for large scale data analysis and data mining.

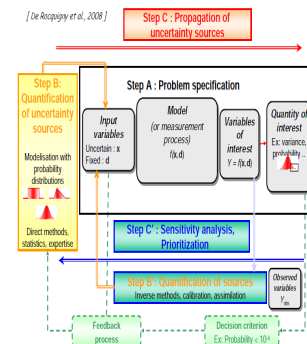
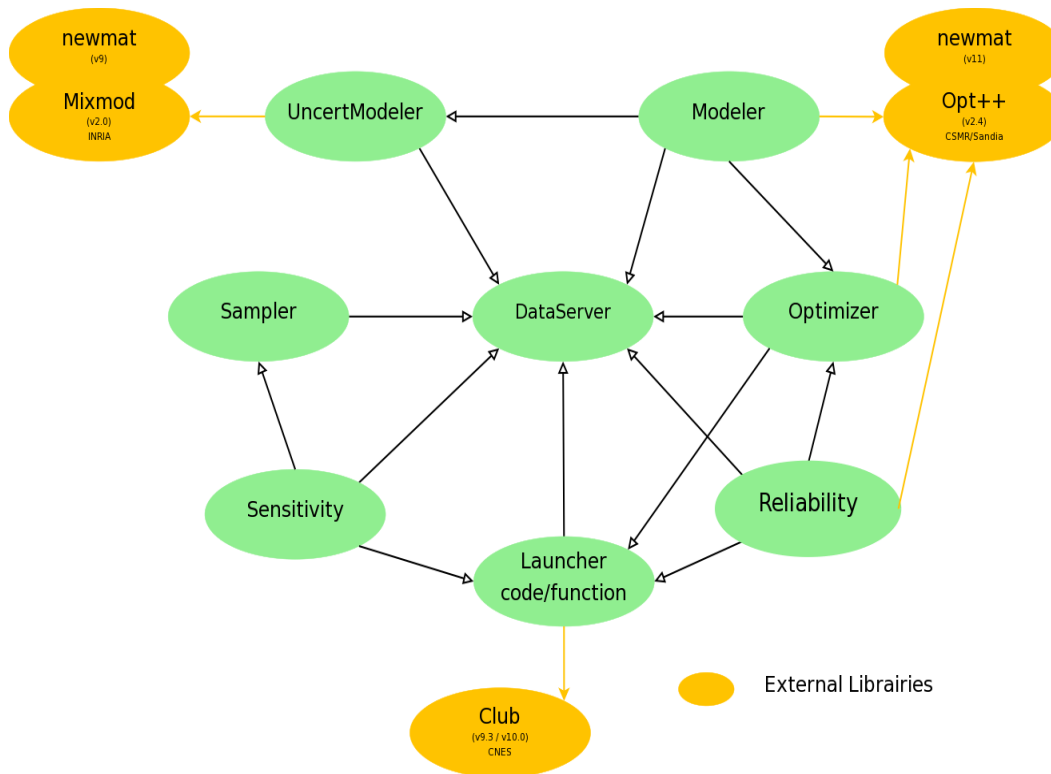
- 20 years of development (C++ with 3-4 releases/year )
- multi-platform (Unix, Windows, Mac OS X)
- Offer :
  - A **C++ interpreter**, but also python (**PyROOT**), **ruby**
  - A hierarchical object-oriented database (machine independent, highly compressed, supporting schema evolution and object versioning)
  - Shared libraries (*automatic loading with "rootmap"*)
  - Advanced statistical analysis tools (subprojects *RooStats*, *RooFit*, *TMVA*)
  - Advanced visualization tools
- **LGPL License**





-  ROOT (CERN),  MIXMOD (Gaussian Mixtures - INRIA),  
 OPT++ (Optimization - Sandia)
- Data access :
  - Flat file with header ( "Salomé Table" )
  - TTree (internal ROOT)
  - SQL Data base (MySQL, PostgreSQL, ...)
- Uncertainty/Sensitivity/Optimisation methods in URANIE
  - Design Of Experiments (SRS, LHS, ROA, qMC, MCMC, Copulas)
  - Clustering methods
  - Surrogate models (Polynomial, Artificial Neural Networks, Kriging, GLM)
  - Non Intrusive Spectrale Projection : Generalized Polynomial Chaos
  - Inverse Quantification of Uncertainty (CIRCE)
  - Sensitivity Analysis (Local, Morris, Regressions (*Pearson, Spearman*)), Sobol, FAST & RBD)
  - Optimization, Multi-Criteria (**Vizir** library : Genetic Algorithms)
  - Computing distribution (**HPC** : TGCC, CCRT)







> root myScript.C

```

emacs: myScript.C
File Edit View Cntrl Tools Options Buffers C++ Help
Open Dired Save Print Cut Copy Paste Undo Spell C/C++ Replace Mail Info Compile Debug News
myScript.C
// Create the TDataSet of the study
TDataSet * tds = new TDataSet("tdsBorehole","Launch the Borehole function");
// Add the eight attributes of the study with uniform law
tds->addAttribute( new TUniformDistribution("rw", 0.05, 0.15));
tds->addAttribute( new TUniformDistribution("tu", 100.0, 50000.0));
tds->addAttribute( new TUniformDistribution("tu", 63070.0, 115600.0));
tds->addAttribute( new TUniformDistribution("tl", 63.1, 116.0));
tds->addAttribute( new TUniformDistribution("hu", 980.0, 1110.0));
tds->addAttribute( new TUniformDistribution("hl", 700.0, 820.0));
tds->addAttribute( new TUniformDistribution("l", 1120.0, 1680.0));
tds->addAttribute( new TUniformDistribution("kw", 8655.0, 12045.0));

// Generate the sampling from the TDataSet (LHS, 1000)
TSampling *sampsLhs = new TSampling(tds, "lhs", 1000);
sampsLhs->generateSample();
tds->exportData("waterhole_sampler_lhs.dat");

// Load the analytical functions
gROOT->LoadMacro("UserFunctions.C");

// Evaluate the flowrateModel analytical function
TLauncherFunction * tlf = new TLauncherFunction(tds, flowrateModel, "", "ywo");
tlf->run();
tds->exportData("waterholelhs.dat");

// Clean the TDS
tds->deleteAttribute("ywo");
delete tds->getTuple();

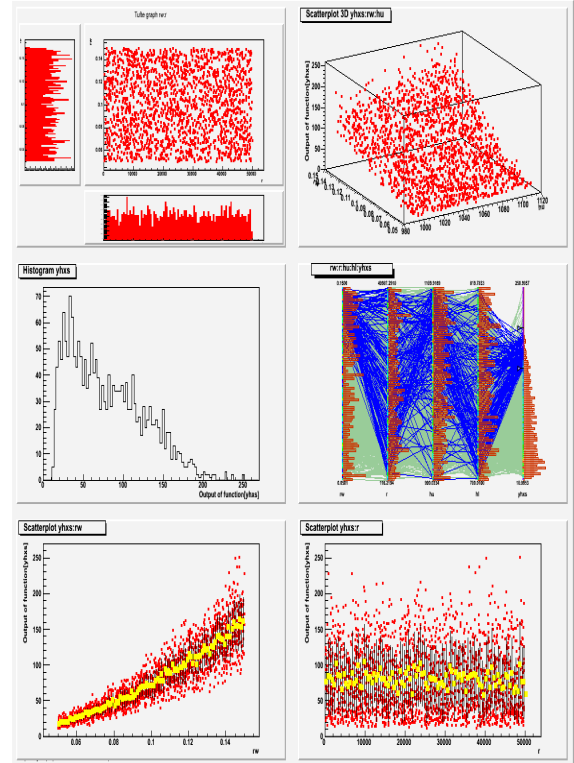
// Generate the sampling from the TDataSet (SRS, 2000)
TSampling *sampsSrs = new TSampling(tds, "srs", 2000);
sampsSrs->generateSample();

// Evaluate the HoXuSurrogateModel function
TLauncherFunction * tlFhs = new TLauncherFunction(tds, HoXuSurrogateModel, "rw::tu:tl:hu:hl:l:kw", "yhsx");
tlFhs->run();

// Visualisation
TCanvas *cCanvas = new TCanvas("c1", "Graph for the Macro launchFunctionSampling",8,118,989,830);
Canvas->Divide(2,3);
Canvas->cd(1); tds->drawTufite("rw::", "", "same");
Canvas->cd(2); tds->draw("yhsx:rw:hu");
Canvas->cd(3); tds->draw("yhsx");
Canvas->cd(4); tds->draw("rw:r:hl:hu:hsx", "", "para");
TParallelCoord* para = (TParallelCoord*)gPad->GetListOfPrimitives()->FindObject("ParallelCoord");
TParallelCoordVar* axis = (TParallelCoordVar*)para->GetVarList()->FindObject("yhsx");
axis->AddRange(new TParallelCoordRange(axis,150.0,200.0));
para->AddSelection("blue");
para->GetCurrentSelection()->SetLineColor(kBlue);
Canvas->cd(5); tds->drawProfile("yhsx:rw", "", "same");
Canvas->cd(6); tds->drawProfile("yhsx:r", "l", "same");

Canvas->SaveAs("uranieScriptGraph.png");
}
Rau----XEmacs: myScript.C //1:24 █ (C++ Font Abbrev)----L18-C2-A11-----

```





```
1<?xml version="1.0" encoding="iso-8859-1"?>
2<!DOCTYPE Problem SYSTEM "/uranie.dtd">
3<Problem>
4  <Header name="boreholeXML" title="Launch the Borehole function in XML" debug="0">
5    <Application name="uranie" version="1.0"/>
6  </Header>
7  <DataDictionary>
8    <DataField name="rw" law="uniform" min="0.05" max="0.15"/>
9    <DataField name="r" law="uniform" min="100.0" max="50000.0"/>
10   <DataField name="tu" law="uniform" min="63070.0" max="115600.0"/>
11   <DataField name="tl" law="uniform" min="63.1" max="116.0"/>
12   <DataField name="hu" law="uniform" min="990.0" max="1110.0"/>
13   <DataField name="hl" law="uniform" min="700.0" max="820.0"/>
14   <DataField name="l" law="uniform" min="1120.0" max="1680.0"/>
15   <DataField name="kw" law="uniform" min="9855.0" max="12045.0"/>
16 </DataDictionary>
17 <Sampler method="LHS" N="1000" export="waterhole_sampler_lhs.dat"/>
18 <Launcher macro="UserFunctions.C" function="flowrateModel" output="ymod" export="waterholelhs.dat"/>
19 <Sampler method="SRS" N="2000"/>
20 <Launcher function="HoXuSurrogateModel" input="rw:r:tu:tl:hu:hl:l:kw" output="yhxs"/>
21</Problem>
```

```
void evaluateXMLFile (TString xmlFile = "uranieproblem.xml")
{
  TXMLProblem * xmlProblem = new TXMLProblem(xmlFile);
  xmlProblem->submit();
}
```





- 110 000 lines & 234 classes
- Version of ROOT :  
v5.34.13 (2013 Nov.)  
v5.32 (2011 Dec.)
- Compilation with **cmake**  
(Linux-Makefiles/Windows-Visual Project)
- Unitary tests with **CppUnit**
- Coverage with **gcov** in CDash
- Memory check with **valgrind**
- **Exceptions** (Warning, Error, Deprecated)
- Open source since 2013/05

<http://sourceforge.net/projects/uranie>

Uranie											
No update data as of Wednesday, September 25 2013 - 00:00 CEST											
<b>Nightly</b>											
Site	Build ID	Build Name	Update Files	Configure Error	Configure Warn	Build Error	Build Warn	Not Run	Fail	Pass	Build Time
ii220576	6001	CentOS 5.5-64bit	0	0	0	3	0	0	11	11	Sep 25, 2013 - 02:00 CEST
ii222877@raona08	6002	Fedora 18-64bit	0	0	0	0	0	0	10	10	Sep 25, 2013 - 02:40 CEST
ii222796	6000	Manjaro-2012-64bit	0	0	0	0	0	0	11	11	Sep 25, 2013 - 03:30 CEST
ii214607	6004	Windows	0	0	0	0	0	0	7	7	Sep 25, 2013 - 02:30 CEST
<b>Coverage</b>											
Site	Build ID	Build Name	Percentage	LOC Tested	LOC Untested	Date					
ii220576	6001	CentOS 5.5-64bit	55.13%	49939	39781	Sep 25, 2013 - 02:00 CEST					
ii222877@raona08	6002	Fedora 18-64bit	59%	0	0	Sep 25, 2013 - 02:40 CEST					
ii222796	6000	Manjaro-2012-64bit	55.20%	45204	35802	Sep 25, 2013 - 02:31 CEST					
<b>Dynamic Analysis</b>											
Site	Build ID	Build Name	Checker	Defect Count	Date						
ii220576	6001	CentOS 5.5-64bit	Valgrind	1206	Sep 25, 2013 - 02:00 CEST						
ii222877@raona08	6002	Fedora 18-64bit	Valgrind	1161	Sep 25, 2013 - 02:45 CEST						
ii222796	6000	Manjaro-2012-64bit	Valgrind	25	Sep 25, 2013 - 02:31 CEST						

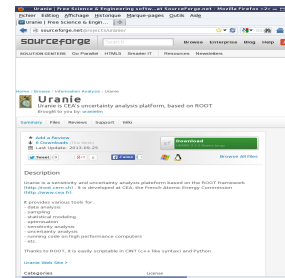
CDash reports

```

--- <WARNING> URANIE::MessageLogger : ===== WARNING =====
--- <WARNING> URANIE::MessageLogger : Depreciated constructor since v0.3 to v0.5
--- <WARNING> URANIE::MessageLogger : Using the same constructor with a TDataServer object
--- <WARNING> URANIE::MessageLogger : ===== End Of Warning =====

```

Depreciated message



Uranie SourceForge site

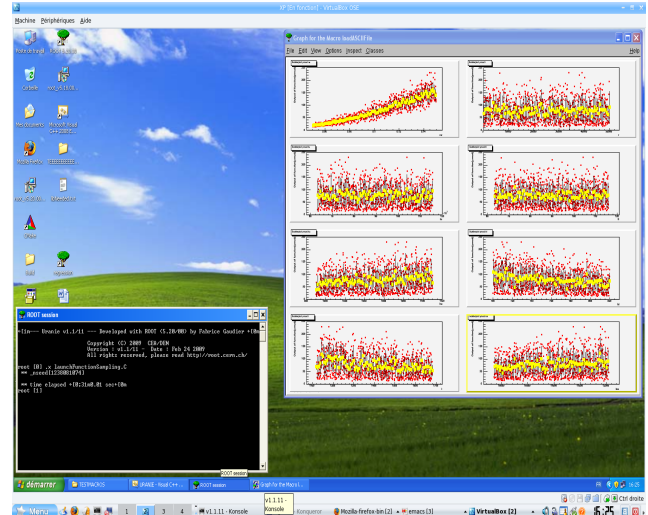
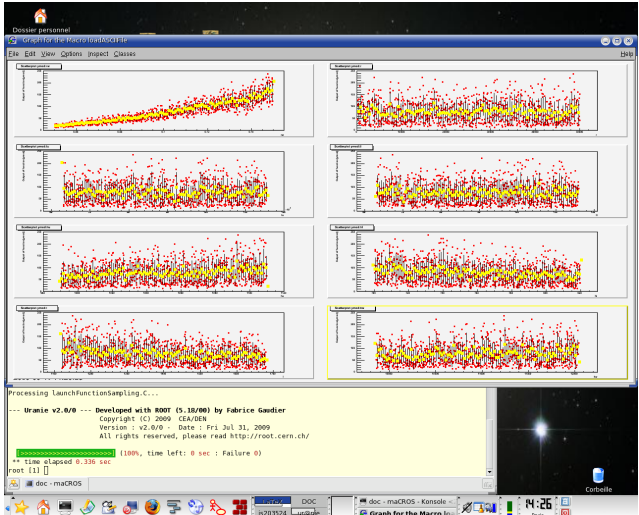
# The URANIE project : Windows



- Configure with **cmake**
- Compilation with **Visual C++** (free edition)
- with very few "#ifdef WIN32"
- Same Macro on Linux and Windows

```

...
LaunchFunction.cpp
...
int i;
...
// timer
#ifdef __GLIBC__
timer_t rValc, "Uranie Launcher");
for(int i=0; i<=n; i++) {
// get the current pattern
...
}
// Fill the input vector
...
// Evaluate y = f(x)
...
// Fill the output
...
#endif
// DrawProgressBar(iValc);
...
cout << endl << " * time elapsed * << timer.getTime() << endl;
// Clean
delete[] valInp;
delete listOfInputLeaves;
...
    
```



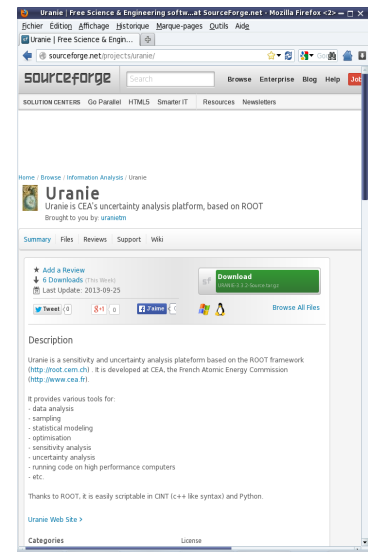


- LEONAR tool for severe accidents in french nuclear reactor (**CEA-EDF Septen**)
- PSI-Matador Methodology : Dosimetry computation in french nuclear reactor (**CEA-EDF**)
- SIVIT project : (**CEA DTCD**)
  - ◇ GUI Salomé/Uranie on Windows
- EHPOC project : Meteor/Pleiades codes (**CEA DEC**)
- Multi-criteria optimization (**CEA CESTA/CELIA**)
- Sensitivity Analysis for ThermalHydraulic codes Flica/Cathare (**Areva TA**)
- ALLIANCES platform (**CEA/ANDRA/EDF**)
  - ◇ is to provide a working environment for the simulation and analysis of phenomena to be taken into account for waste storage and disposal studies
- European project **NURESIM/NURISP**
  - ◇ The European Platform for NUclear REactor SIMulations, NURESIM, is a Common European Standard Software Platform for modeling, recording, and recovering computer data for nuclear reactors simulations





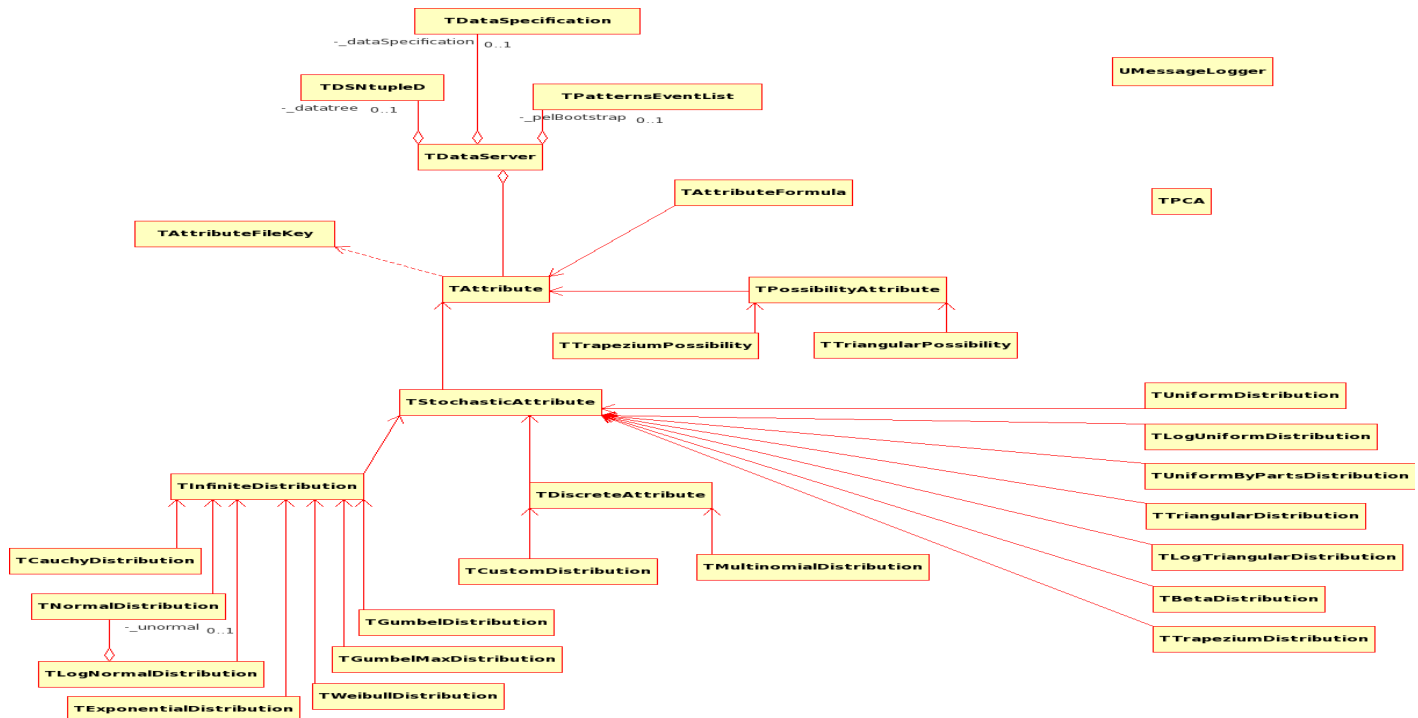
- Uranie Training sessions
  - 2013/10/14-15 : **"Optimisation user"** session - SAC Areva-TA (2)
  - 2013/09/16-18 : **"user"** session - CAD CEA/DEN (12)
  - 2013/04/2-4 : **"user"** session - SAC NURES SAFE (12)
  - 2012/10/14-17 : **"user"** session - SAC (12)
  - 2012/04/11-13 : **"user"** session - CAD CEA/DEN-DSM (12)
  - 2011/10/17-19 : **"user"** session - SAC CEA/DEN (8)
  - 2011/04/4-6 : **"user"** session - NURISP (5)
  - 2011/01/19-21 : **"user"** session - SAC CEA/DEN (12)
  - ...
  - 2008-2009 : Areva-TA (~ 10)
  - 2006-2008 : CEA/DEN (~ 50 persons)
- ROOT Training sessions at INSTN ( 12 students, 3/4 days)
  - February 2011 : **DEN-SAC**
  - February 2010 : **DEN-SAC**
- Developpment is piloted by user request
- bugtracker
- Distribution : Open source since 2013/05



<http://sourceforge.net/projects/uranie>



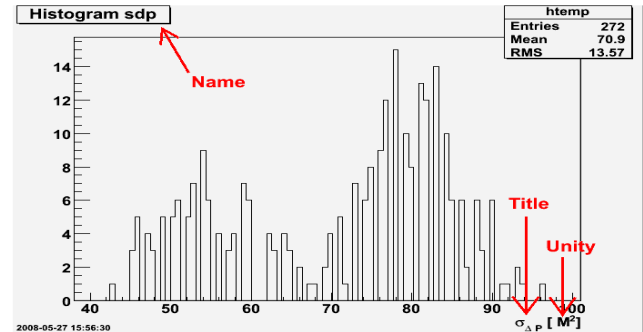
- Management of the attributes (~ variables)
- create/transform attributes
- Load data from external files/formats (ASCII, TTREE, SQL)
- Graphs and treatments specific to uncertainties





```
#NAME: geyser
#TITLE: geyser data
#DATE: Mon Mar 12 23:41:09 2007
#COLUMN_NAMES: x1| sdp
#COLUMN_TITLES: x_1| #sigma_{#Delta P}
#COLUMN_UNITS: Sec| M^{2}

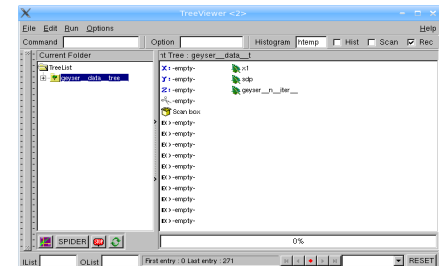
----- empty line -----
3.600 79.000
1.800 54.000
...
```



```
t ds->draw("sdp");
```

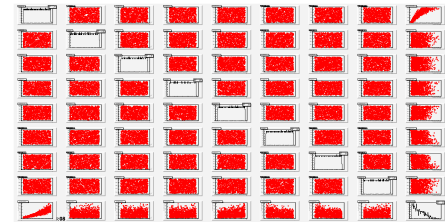
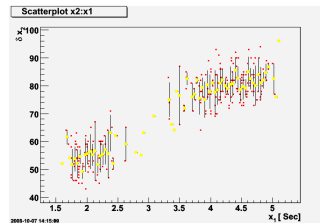
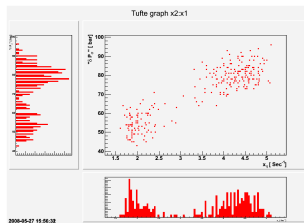
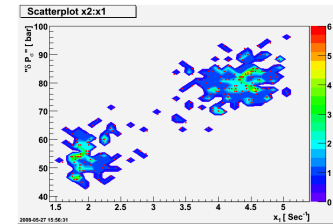
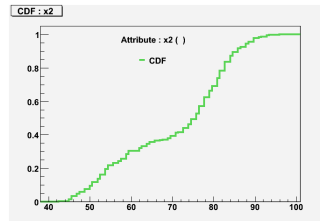
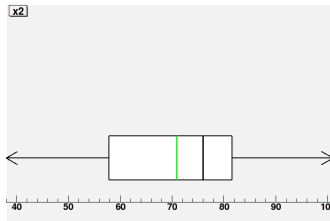
Only the "#COLUMN\_NAMES:" line is mandatory  
**WARNING** : the empty line between the header and the matrix data

```
TDataServer *tds = new TDataServer();
tds->fileDataRead("geyser.dat");
tds->draw("sdp");
tds->startViewer();
```





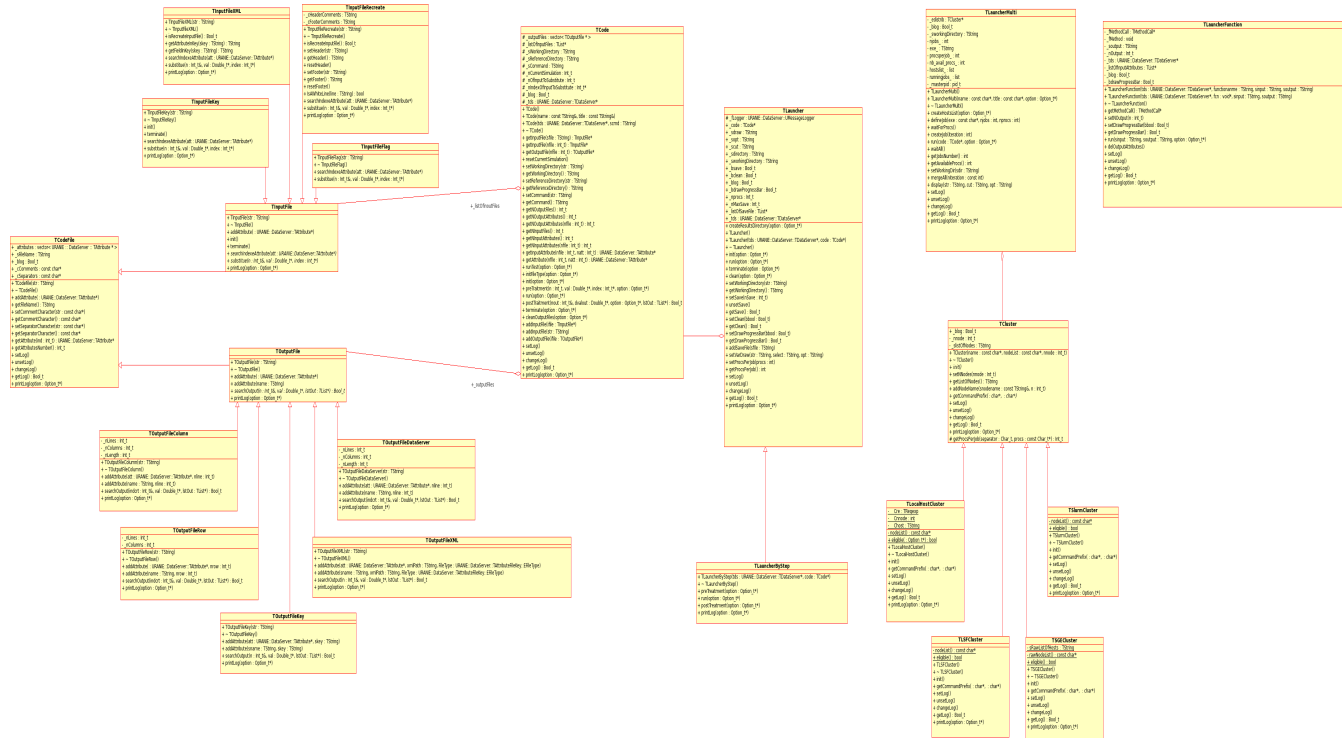
```
tds->drawBoxPlot("x2");  
tds->drawCDF("x2","x1<3.0");  
tds->drawScatterplot("x2:x1");  
tds->drawTuft("x2:x1");  
tds->drawProfile("x2:x1","", "same");  
tds->drawPairs();
```



# "Launcher" library



Distribute the model evaluations (sequential, cluster) for:  
Analytical function  
External code





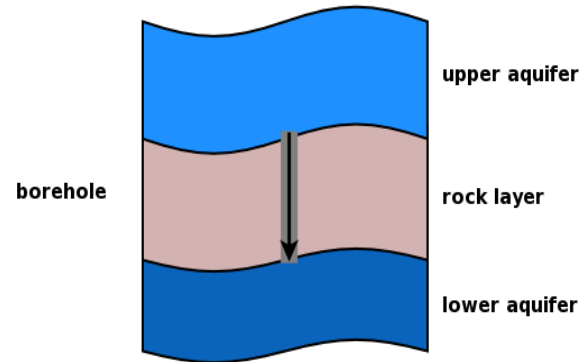


```
void myFunction (double *x, double *y)
```

Analytical function of  $R^8$  in  $R$  :

(Bernoulli's law and flow is steady-state laminar and isothermal)

$$y = \frac{2\pi T_u (H_u - H_l)}{\ln\left(\frac{r}{r_w}\right) \left[ 1 + \frac{2LT_u}{\ln\left(\frac{r}{r_w}\right) r_w^2 K_w} + \frac{T_u}{T_l} \right]}$$

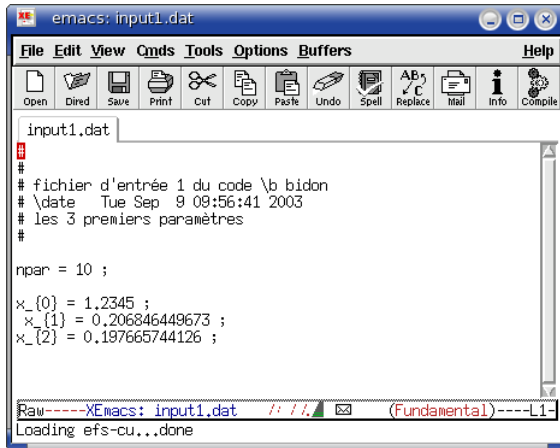


Fang, p 35

```
void flowrateModel(double *x, double *y)
{
    Double t drw = x[0], dr = x[1];
    Double t dtu = x[2], dtl = x[3];
    Double t dhu = x[4], dh1 = x[5];
    Double_t dl = x[6], dkw = x[7];

    Double t dnum = 2.0 * TMath::Pi() * dtu * ( dhu -dh1);
    Double t dlnronrw = TMath::Log( dr / drw);
    Double t dden = dlnronrw * ( 1.0 + ( 2.0 * dl * dtu ) / ( dlnronrw * drw * drw * dkw) + dtu / dtl );

    y[0] = dnum / dden;
}
```



```
emacs: input1.dat
File Edit View Cmds Tools Options Buffers Help
Open Dired Save Print Cut Copy Paste Undo Spell Replace Mail Info Compile
input1.dat
#
# fichier d'entrée 1 du code \b bidon
# \date Tue Sep 9 09:56:41 2003
# les 3 premiers paramètres
#
npar = 10 ;
x_{0} = 1.2345 ;
x_{1} = 0.206846449673 ;
x_{2} = 0.197665744126 ;
Raw----XEmacs: input1.dat  /: /: (Fundamental)---L1-
Loading efs-cu...done
```

```
TAttribute *x1 = new TAttribute("x_{1}", 0.20, 0.40);
x1->setFileKey("input1.dat");
```

```
TAttribute *x2 = new TAttribute("x2", 0.15, 0.25);
x2->setFileKey("input1.dat", "x_{2}");
```

Hypothesis : unicity of the key

```
void TAttribute::setFileKey(
    TString sfile,
    TString skey="",
    TString sformatToSubstitute="%e",
    TAttributeFileKey::EFileType FileType=TAttributeFileKey::kKey);
```



```

emacs: flowrate_input_with_flags.in
File Edit View Cmds Tools Options Buffers Help
Open Dired Save Print Cut Copy Paste Undo Spell Replace Mail Info Compile Debug News
flowrate_input_with_fl...
# INPUT FILE with FLAG for the "FLOWREATE" code
# \date 2008-04-22 12:55:17
#
new Implicit_Steady_State sch {
  frottement_pari { 0,100000 25050,000000 }
  tinit 0.0
  tmax 1000000.
  nb_pas_dt_max 1500
  dt_min 1050,000000
  dt_max 760,000000
  facsec 1000000.
  ku 10950,000000
  information_Tu Champ_Uniforme 1 89335,000000
  information_Tl Champ_Uniforme 1 89,550000
  information_L {
    precision 1400,000000
  }
  convergence {
    criterion relative_max_du_dt
    precision 1.e-6
  }
  stop_criterium {
    ch_abscissa_hu 1050
    ch_ordonate_hl 770
    c_radius 1100
  }
  Solveur Newton3 {
    max_iter_matrice 1
    max_iter_implicite 1
    data 5654321
    seuil_conv_implicite 1.e-6
    assemblage_implicite 10
  }
}
Raw-----XEmacs: flowrate_input_with_flags.in 12:35 (Fundamental)

```

Original file

```

emacs: flowrate_input_with_flags.in
File Edit View Cmds Tools Options Buffers Help
Open Dired Save Print Cut Copy Paste Undo Spell Replace Mail Info Compile Debug News
flowrate_input_with_ke... flowrate_input_with_fl...
# INPUT FILE with FLAG for the "FLOWREATE" code
# \date 2008-04-22 12:55:17
#
new Implicit_Steady_State sch {
  frottement_pari { @rw@ @r@ }
  tinit 0.0
  tmax 1000000.
  nb_pas_dt_max 1500
  dt_min @hu@
  dt_max @hl@
  facsec 1000000.
  ku @kw@
  information_Tu Champ_Uniforme 1 @tu@
  information_Tl Champ_Uniforme 1 @tl@
  information_L {
    precision @l@
  }
  convergence {
    criterion relative_max_du_dt
    precision 1.e-6
  }
  stop_criterium {
    ch_abscissa_hu 1050
    ch_ordonate_hl 770
    c_radius 1100
  }
  Solveur Newton3 {
    max_iter_matrice 1
    max_iter_implicite 1
    data 5654321
    seuil_conv_implicite 1.e-6
    assemblage_implicite 10
  }
}
Raw-----XEmacs: flowrate_input_with_flags.in 12:34 (Fundamental)

```

User Flag file

```

attrw->setFileFlag("myfile.in", "@tu@" );
attrw->setFileKey("myfile.in", "@tu@", "%f", TAttributeFileKey::kFlag);

```

Hypothesis : unicity of the key not required but intervention of the user



```
[file ../../flowrate_input_with_xml.xml does not exist]
```

```
...
```

```
attrw->setFileXMLAttribute("input.xml", "wall_friction/@rw");
```

```
atthu->setFileXMLField("input.xml", "parameter[tonode='mesh and toport='dt_hu']/value/double");
```

Hypothesis : unicity of the key not required and no intervention of the user



- **TAttributeFileKey::kNewRow** 4<sup>th</sup> argument in the **setFileKey** method

```
2.481733e+02 6.112975e-03 1.055352e-06 2.635758e-03 2.217372e+02 1.888999e+00 ...
```

- **TAttributeFileKey::kNewColumn** 4<sup>th</sup> argument in the **setFileKey** method

```
2.481733e+02  
6.112975e-03  
...
```

- **TAttributeFileKey::kNewKey** 4<sup>th</sup> argument in the **setFileKey** method

```
t = 2.481733e+02 ;  
kl = 6.112975e-03 ;  
kc = 1.055352e-06 ;  
...
```

Hypothesis : The input files does not exist



- **TOutputFileRow** class

```
0.20E+05 0.5579978E-25 0.2789989E-25  
0.30E+05 0.5121863E-20 0.2560931E-20  
0.40E+05 0.8212720E-17 0.4106360E-17  
0.50E+05 0.1432418E-14 0.7162090E-15  
...
```

- **TOutputFileColumn** class

```
0.20E+05 0.30E+05 0.40E+05 0.50E+05 ....  
0.5579978E-25 0.5121863E-20 0.8212720E-17 0.1432418E-14 ...  
0.2789989E-25 0.2560931E-20 0.4106360E-17 0.7162090E-15 ...  
...
```



- **TOutputFileKey** class

```
yhat = 3.591931e+01;  
d = 2.415401e+03;  
...
```

- **TOutputFileDataServer** class

```
#COLUMN_NAMES: yhat | d  
  
3.591931e+01 2.415401e+03  
...
```



- PC multicores

```
launcher->run("localhost=5");
```

- Cluster (SLURM, LSF, SGE)

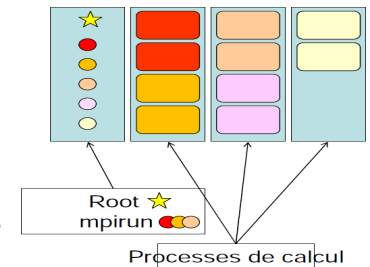
```
#BSUB -n 10
#BSUB -J FlowrateSampling
#BSUB -o FlowrateSampling.out
#BSUB -e FlowrateSampling.err
source /home/cont002/uranie/uranie-titane.cshrc
rm -f FlowrateSampling.out FlowrateSampling.err
root -l -q lanceurFLOWRATE_SAMPLING.C
```

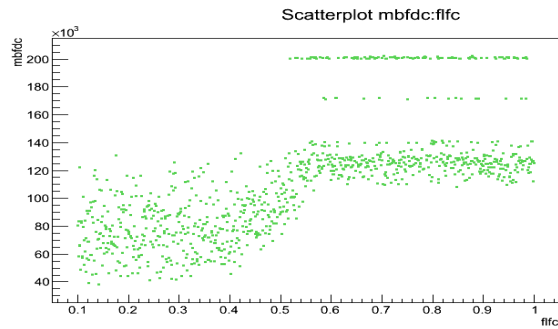
> bsub < BsubFile

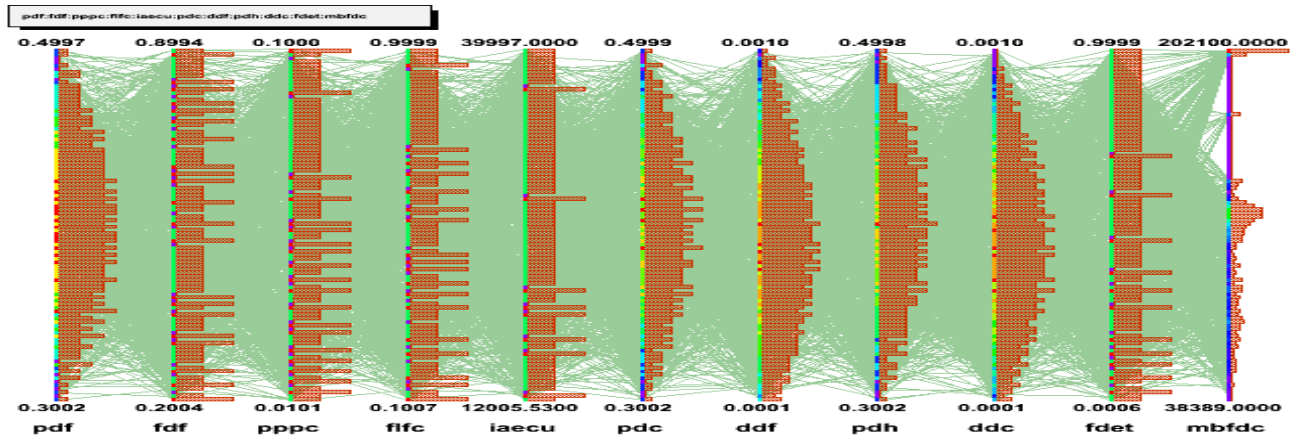
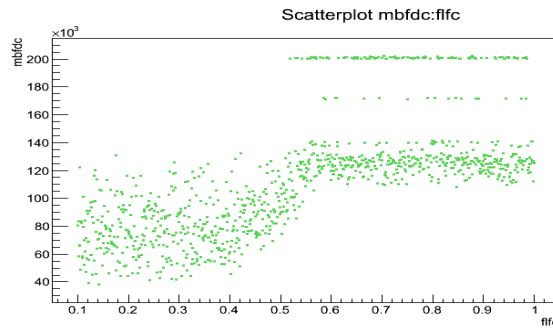




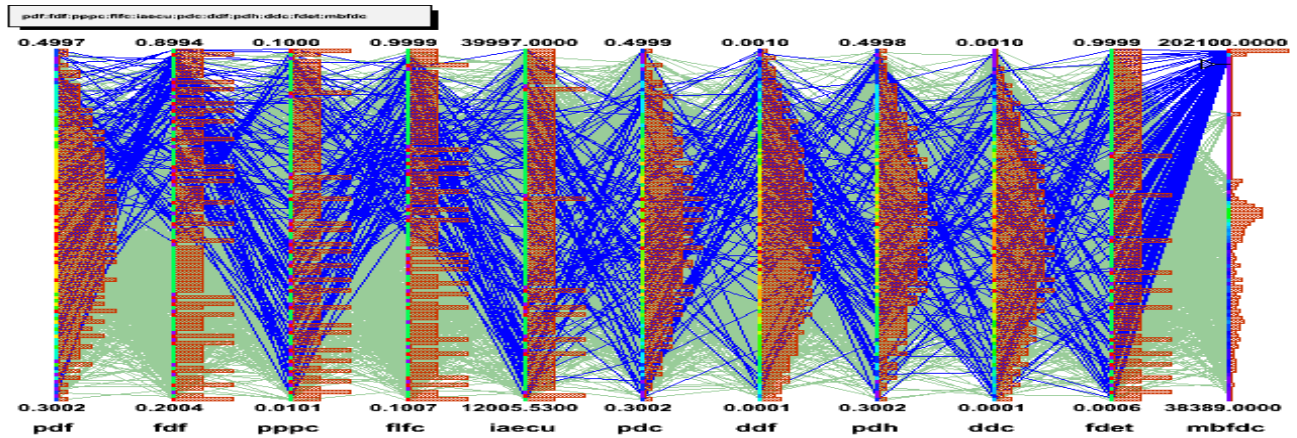
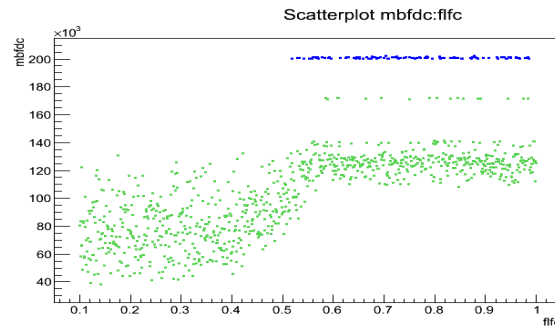
- Le mécanisme de lancement des calculs dans URANIE est transparent pour l'utilisateur : le script URANIE est le même que l'on soit sur un poste de travail ou sur le CCRT;
- La séquence est la suivante :
  - Le plan d'expérience est généré (en fonction de la méthode et des incertitudes sur les paramètres d'entrée)
  - URANIE analyse la machine locale à l'aide de variables d'environnement et déduit le nombre de processeurs disponibles
  - Un pool de processeurs est ensuite géré pour répartir les calculs au fur et à mesure sur les processeurs disponibles
- Travail réalisé par les équipes du Support Applicatif CCRT;
- Difficulté liée au fait qu'il est impossible de lancer *mpirun* depuis *mpirun*;
- Méthode choisie :
  - Le noeud maître gère la distribution des calculs au fur et à mesure;
  - Lorsqu'un groupe de processeurs est disponible, le process maître est forké et lance un *mpirun*;
  - La fin de l'exécution du cas est détectée en analysant l'état du process fils.

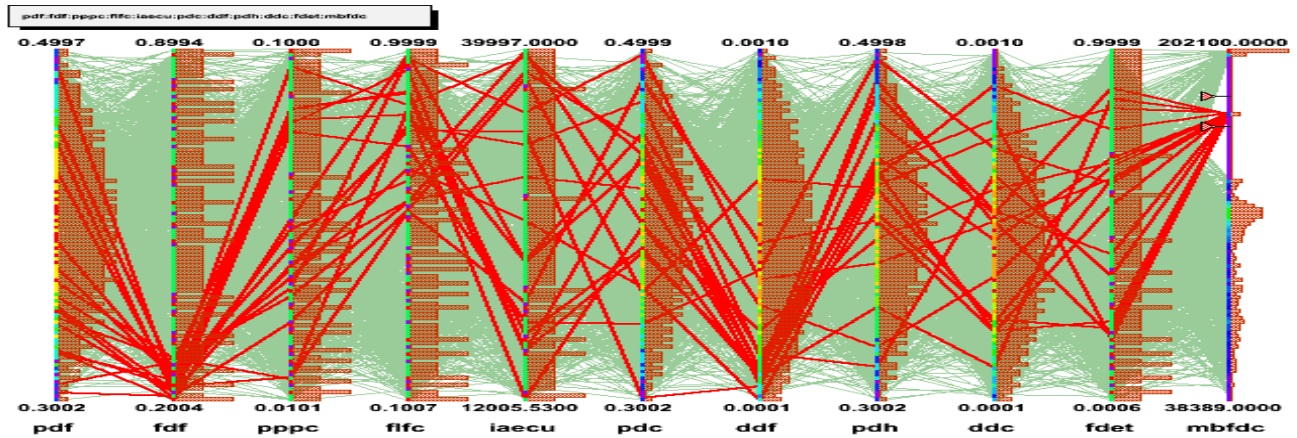
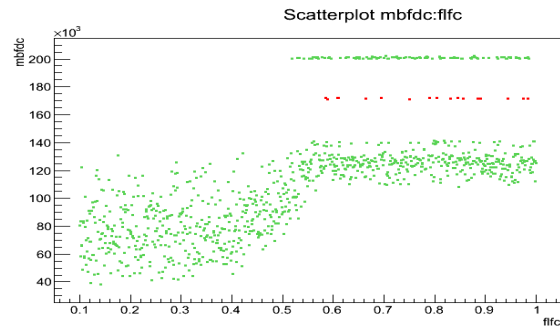


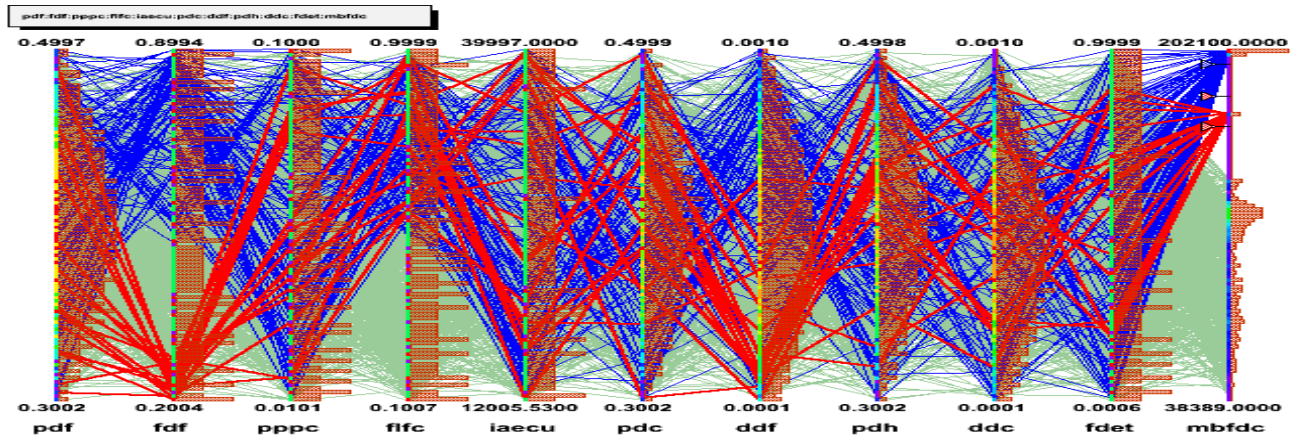
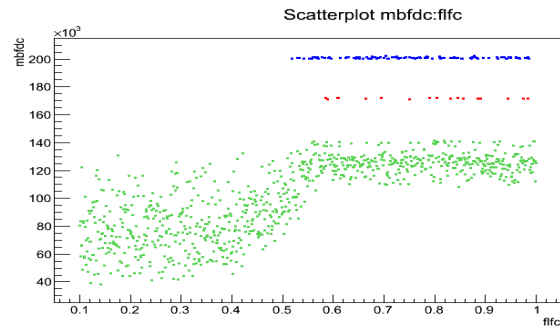




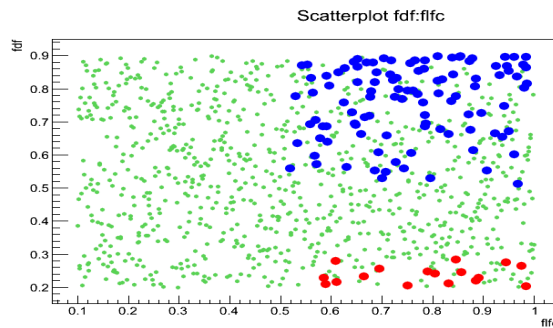
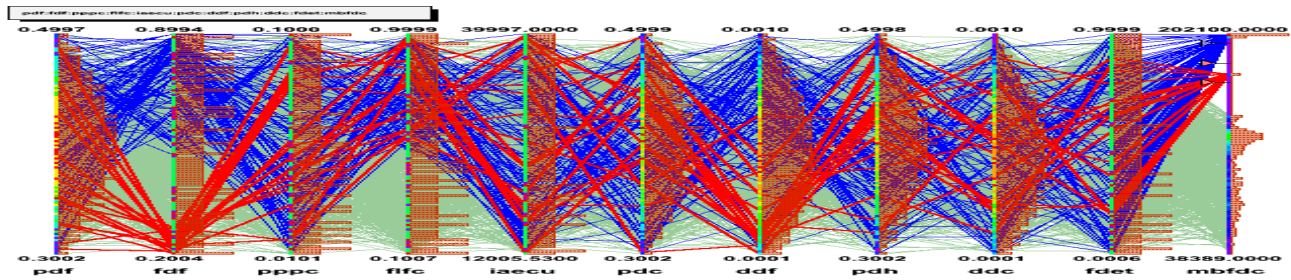
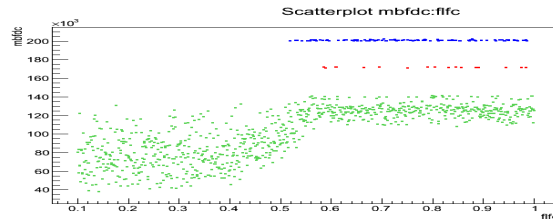
```
tds->Draw("pdf:ddf:pppc:flfc:iaecu:pcdc:ddf:pdh:ddc:fdet:mbfdc", "", "para");
```

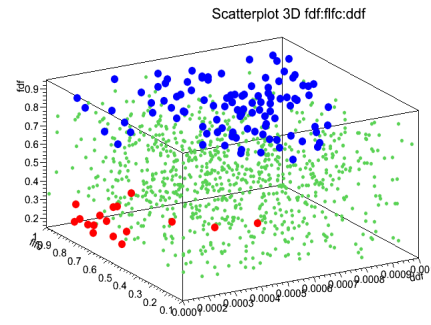
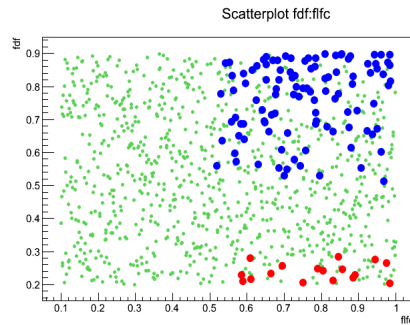
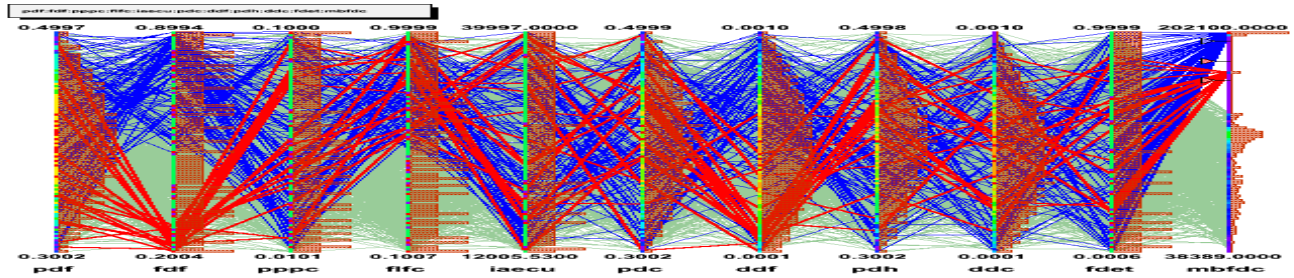
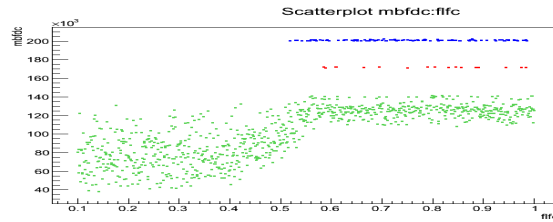
















- Context

Make Sensitivity Analysis with Surrogate Model : Artificial Neural Networks ("ANN")

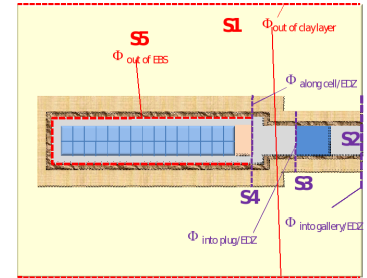
- CPU time single calculation :  $1 < t < 5$  hours (Cluster)

- Original DataSet

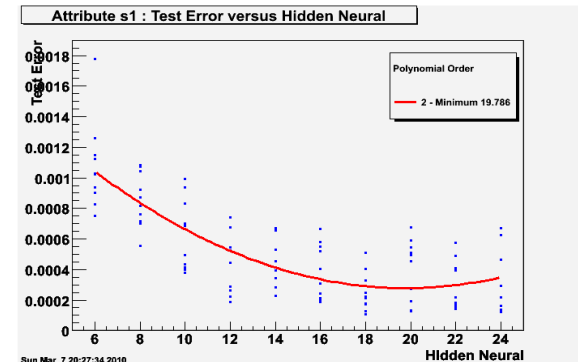
- $nX = 17$  input variables
- $nY = 5$  output variables
- Build the 5 ANN :  $nS = 1500$  patterns

- Neural networks

- different architectures (MLP)
- Input with a logarithm PDF  $x := \log(x)$
- Output  $y := \frac{1}{1+\log(y)}$
- cross validation
- Validate the 5 ANN on another dataset with  $nS = 1000$  patterns



Guillaume Pépin (ANDRA)





First Order :

$$S_i = \frac{Var[IE[Y | x_i]]}{Var[Y]}$$

1. Regression Analysis  $\hat{y} = b_0 + \sum b_i x_i$

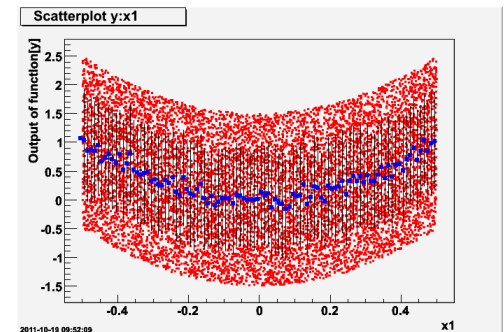
- on the Values : "SRC" ("Standardised Regression Coefficient")
- on the Ranks : "SRRC" ("Standardised Rank Regression Coefficient")

The regression is valid when  $R^2 = \frac{\sum(\hat{y}_i - \bar{y})^2}{\sum(y_i - \bar{y})^2}$  close to 1.0 ( $\geq 0.7$ )

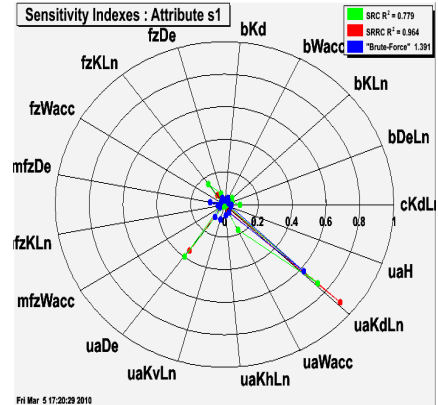
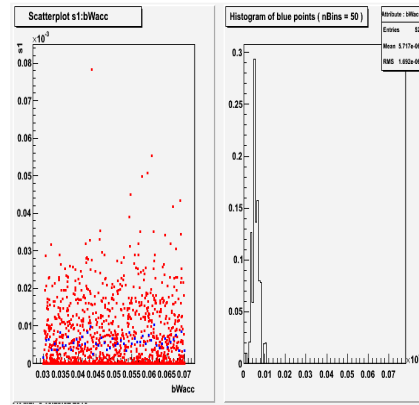
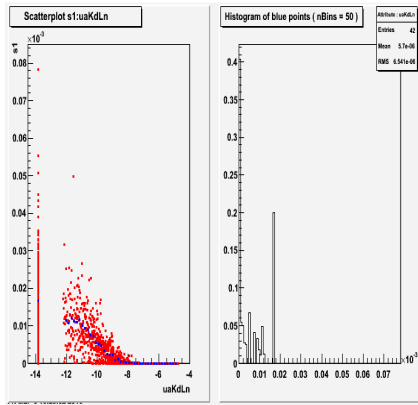
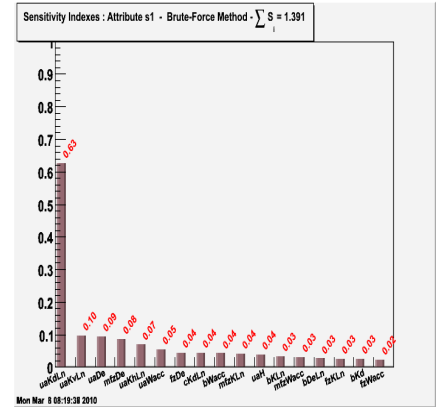
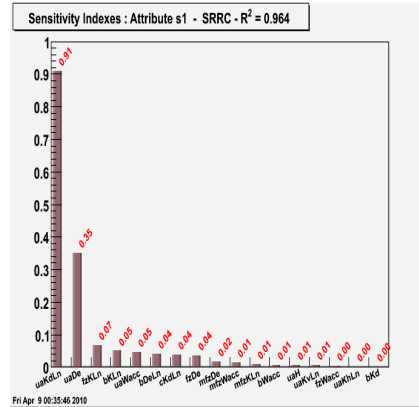
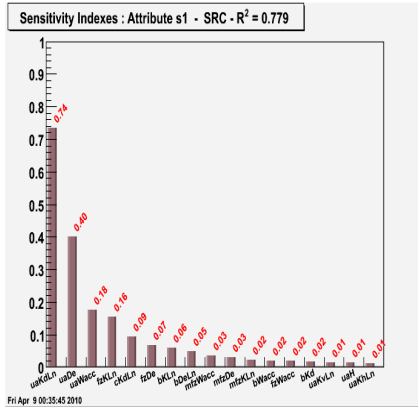
2. Brute-Force Method

Cost :  $nX * nCV * nPts$

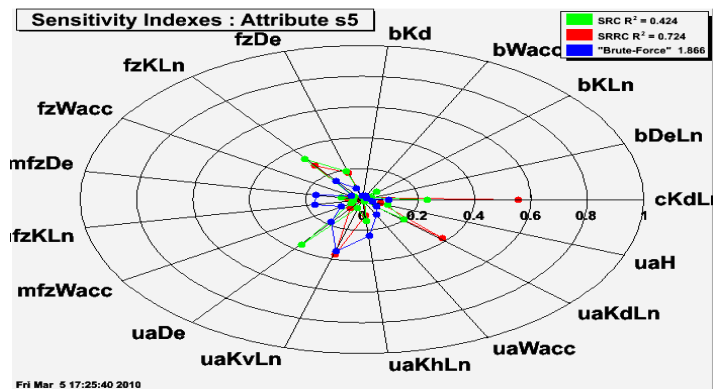
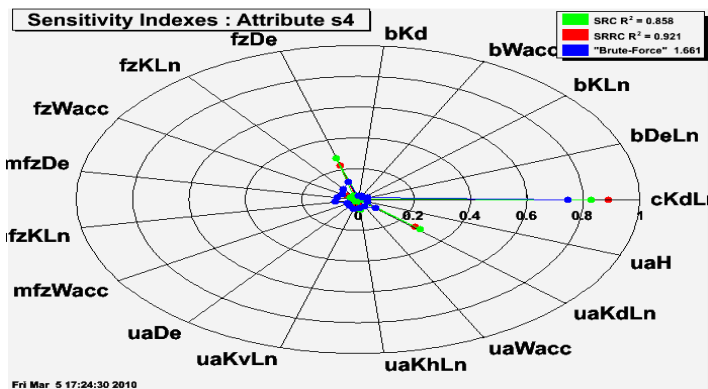
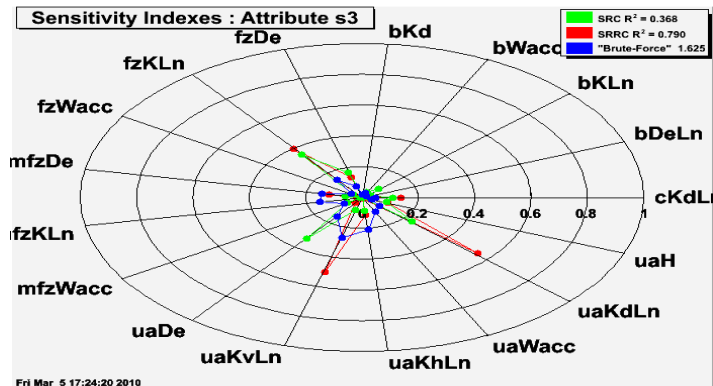
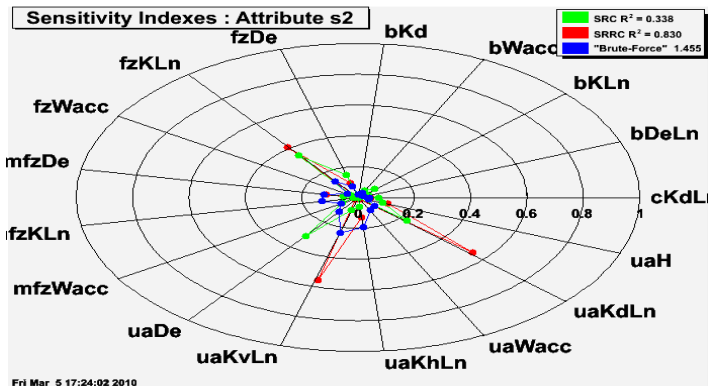
- $nX$  = number of inputs parameters
- $nCV$  = n. of conditionnal values
- $nPts$  = n. of pts over cond. values



# Original Database (nS = 1500) & "s1"



# Original Database (nS = 1500) & other outputs

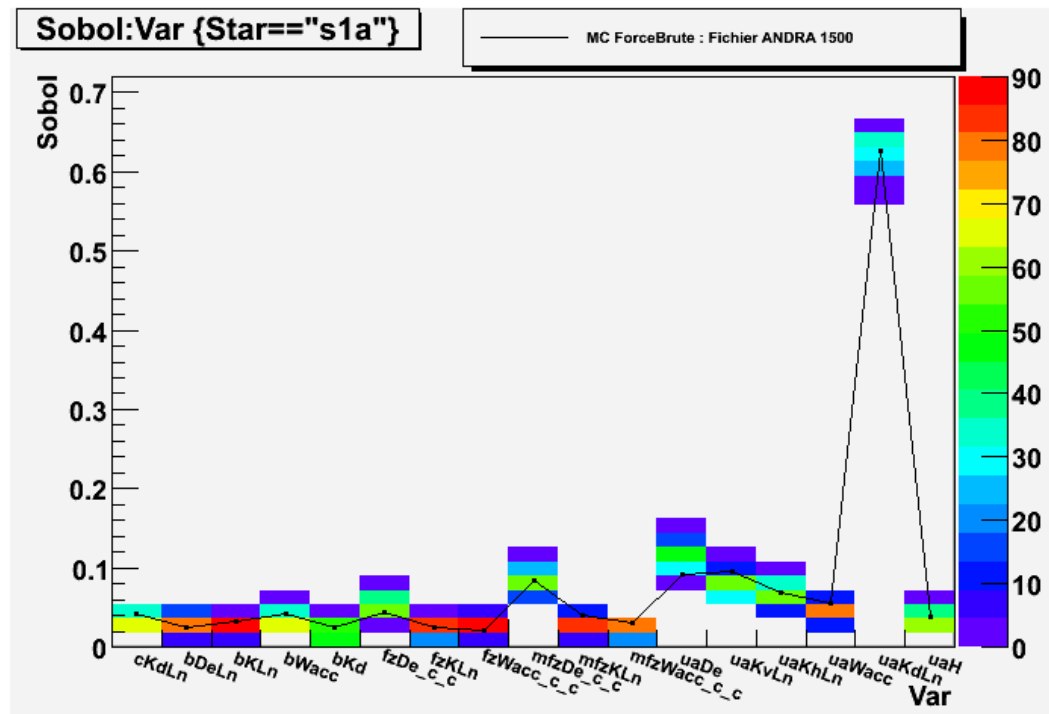


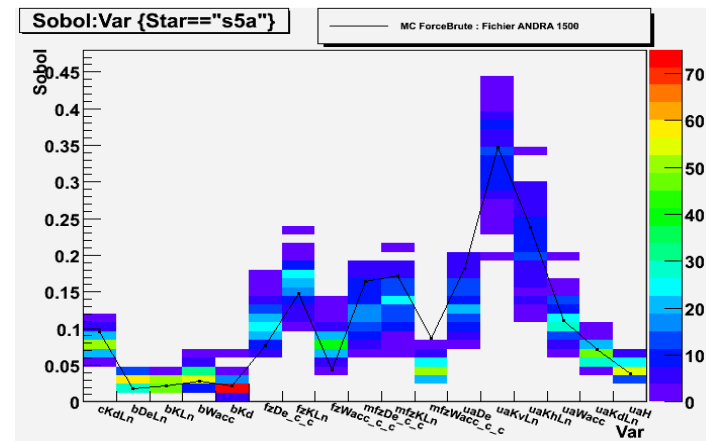
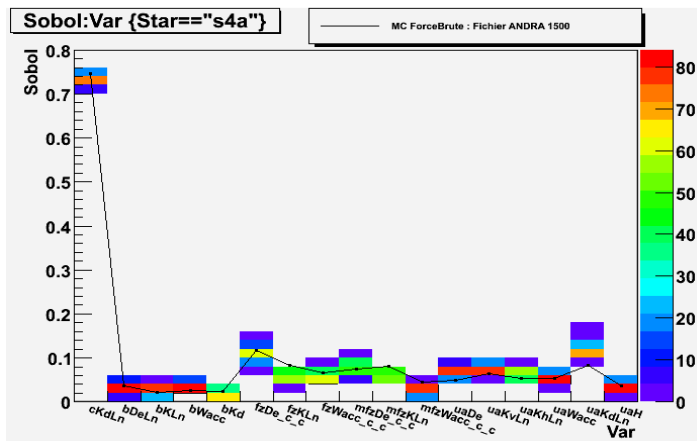
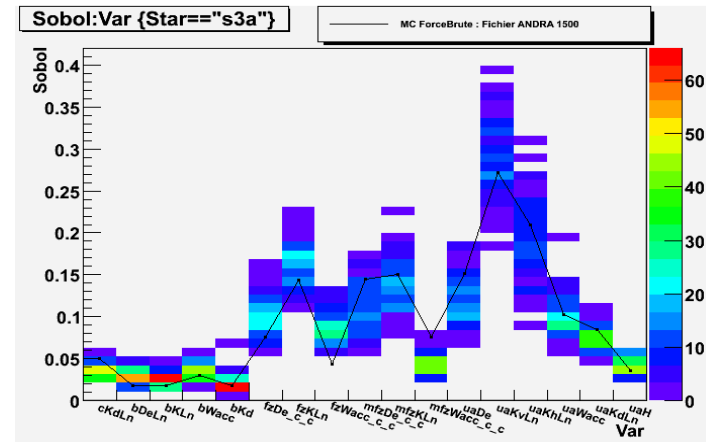
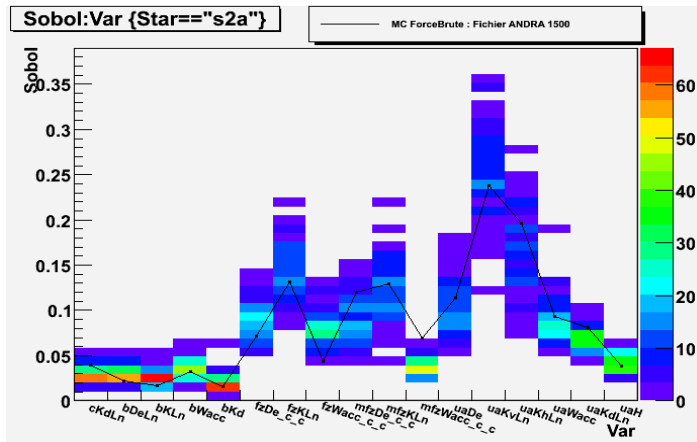


Design  $nL = 100$  databases with size  $nS = 1500$  points

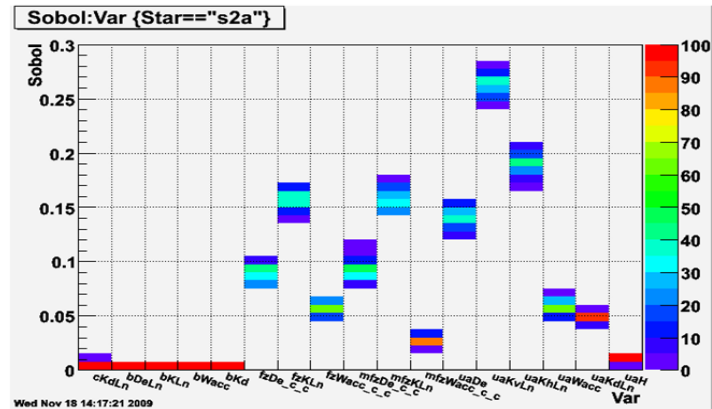
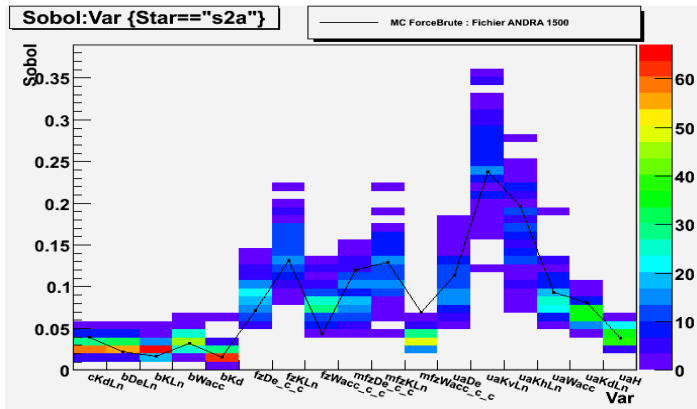
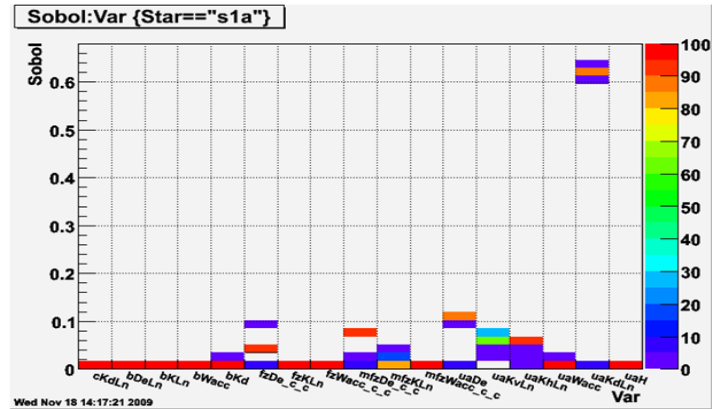
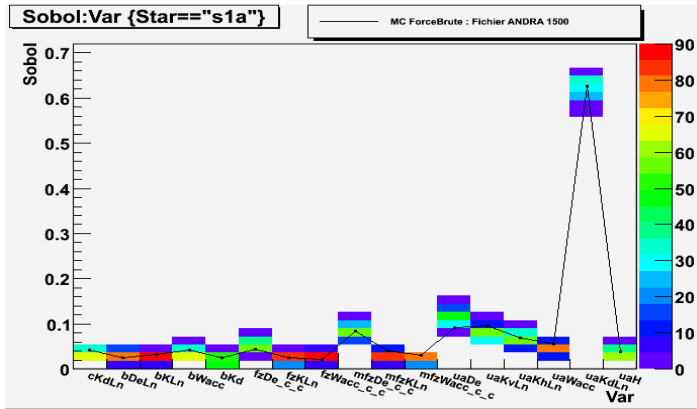
Simulate these databases using ANN surrogate models

Compute the first order SI by the Brute-Force method





# Same with $nS = 20000$ ( « s1 » and « s2 » )

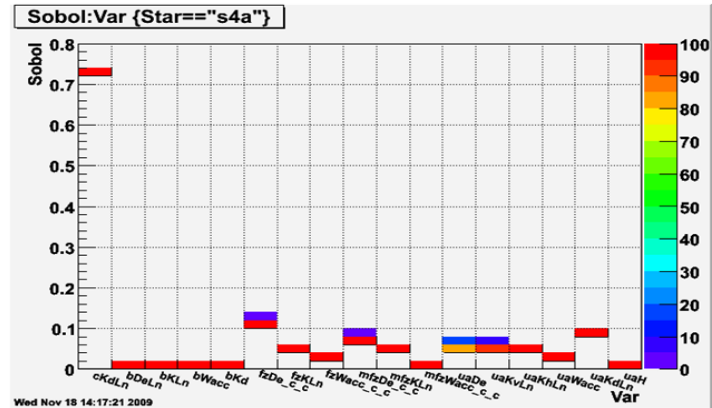
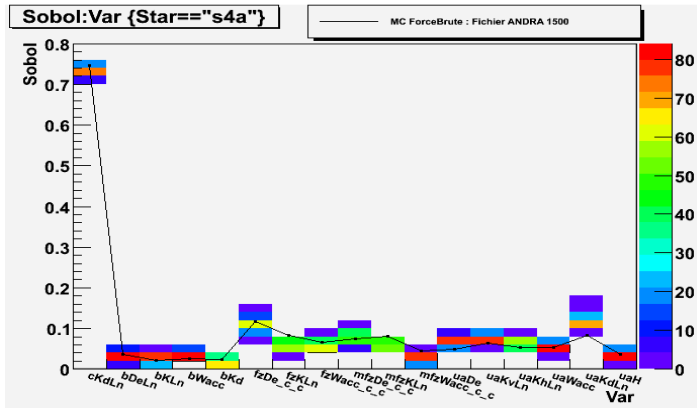
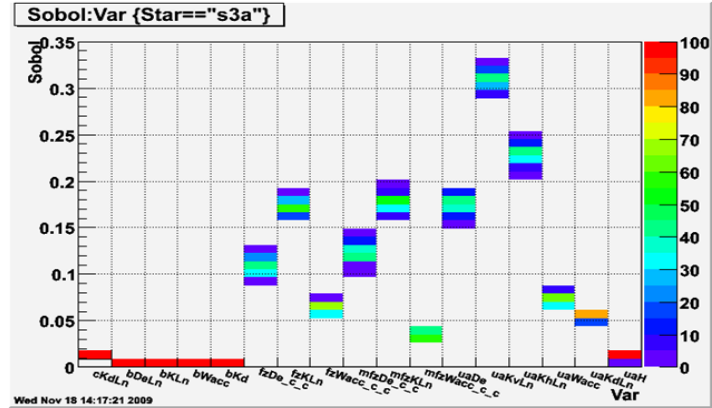
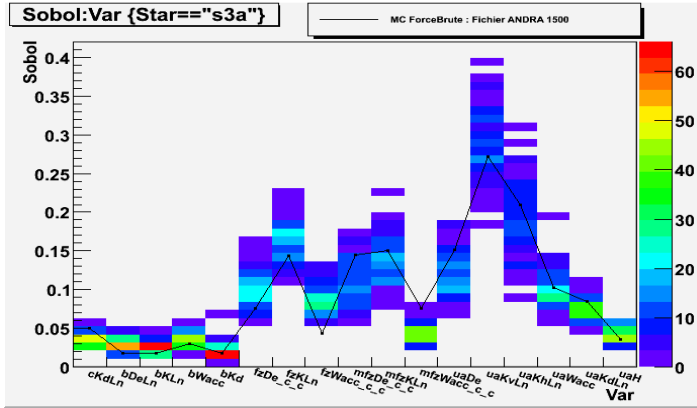


1 500 points

20 000 points



# Same with $nS = 20000$ ( « s3 » and « s4 » )



1 500 points

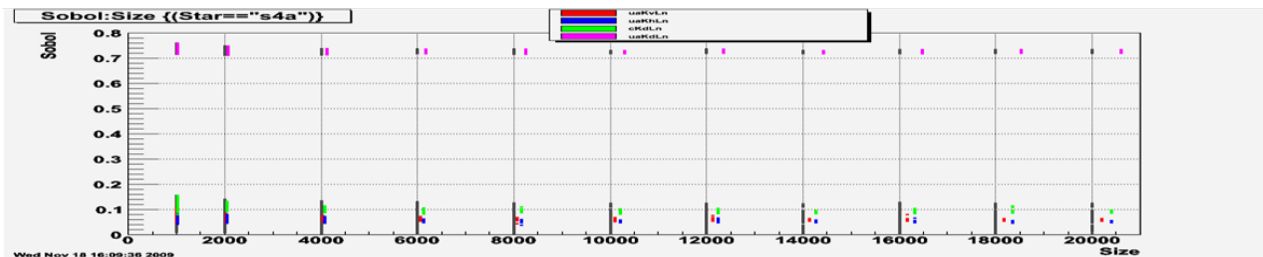
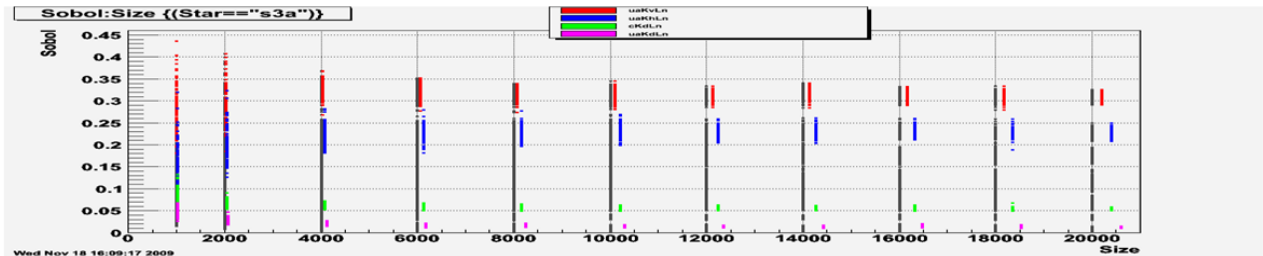
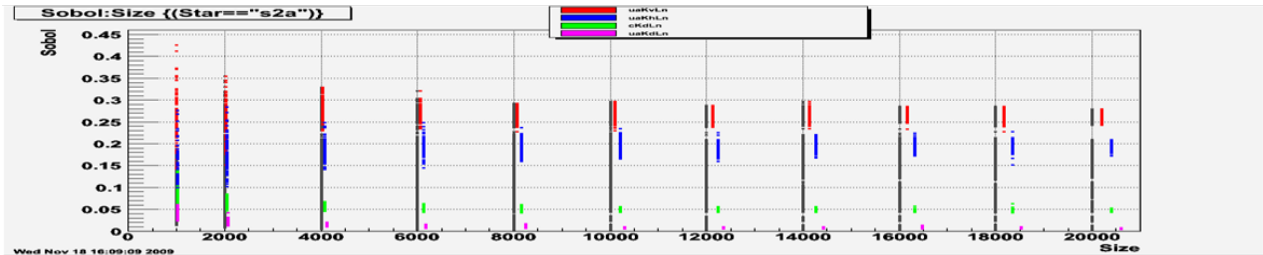
20 000 points





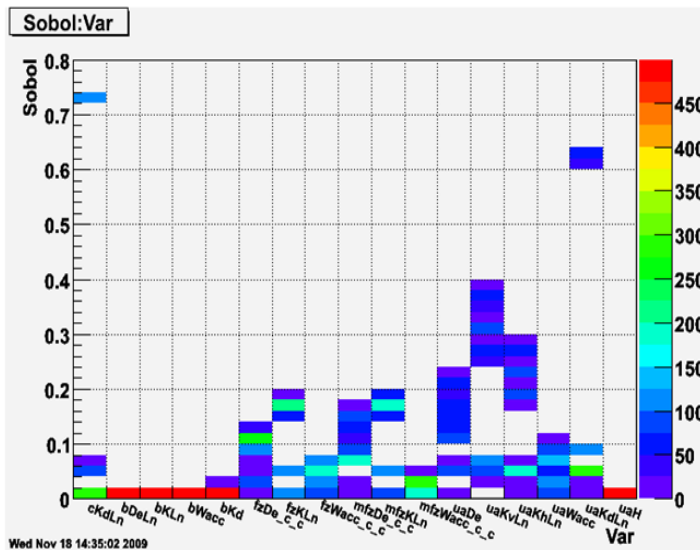


Same loop ( $nL = 100$  DoE) but for  $nS=2000$  to 20000 by step 2000 :

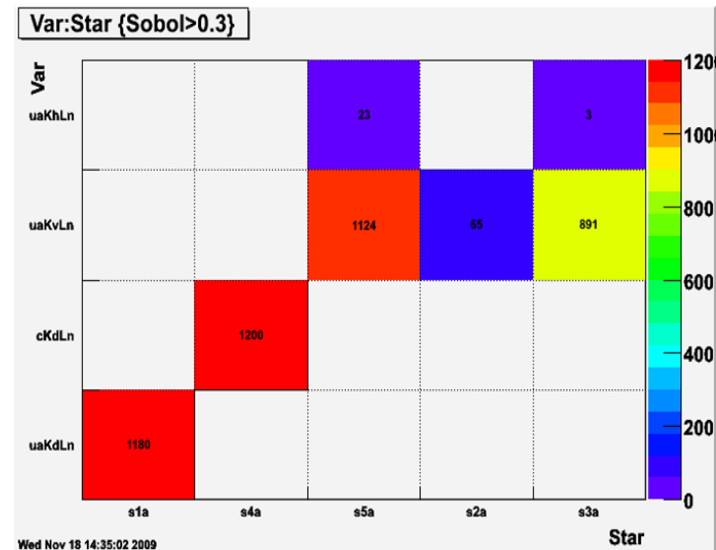




1. 5 inputs parameters are not influence (first order) on all the 5 outputs
2. Only 4 inputs parameters are sensitives (for all 5 outputs)



ttre->Draw("Sobol:Var", "", "BOXCOL2Z")



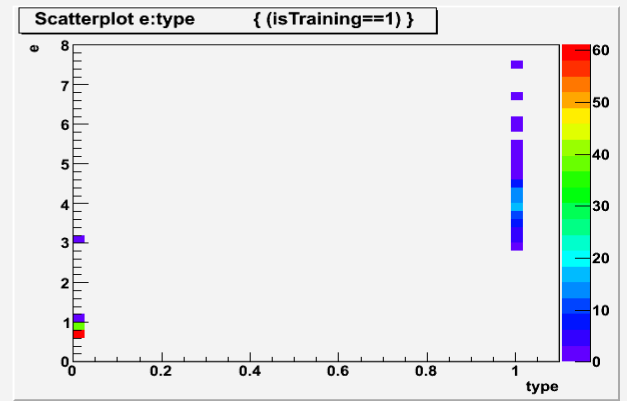
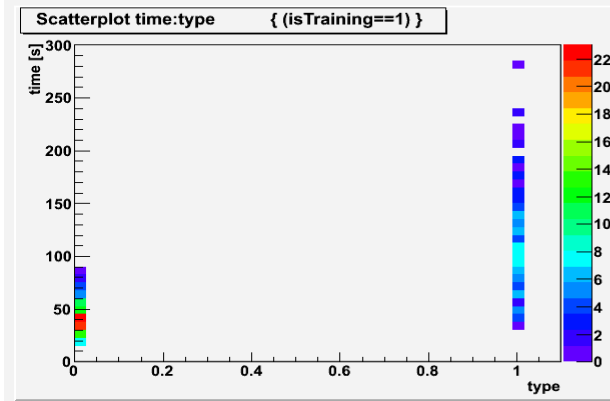
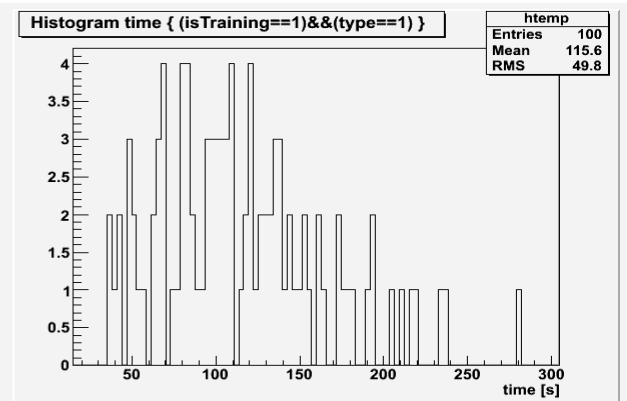
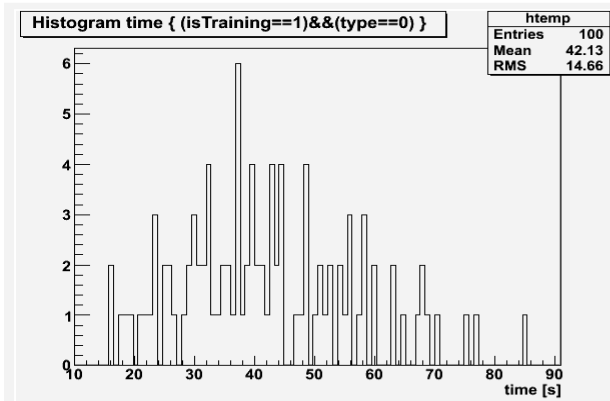
ttre->Draw("Var:Star", "Sobol>0.3", "BOXCOL2Ztext")

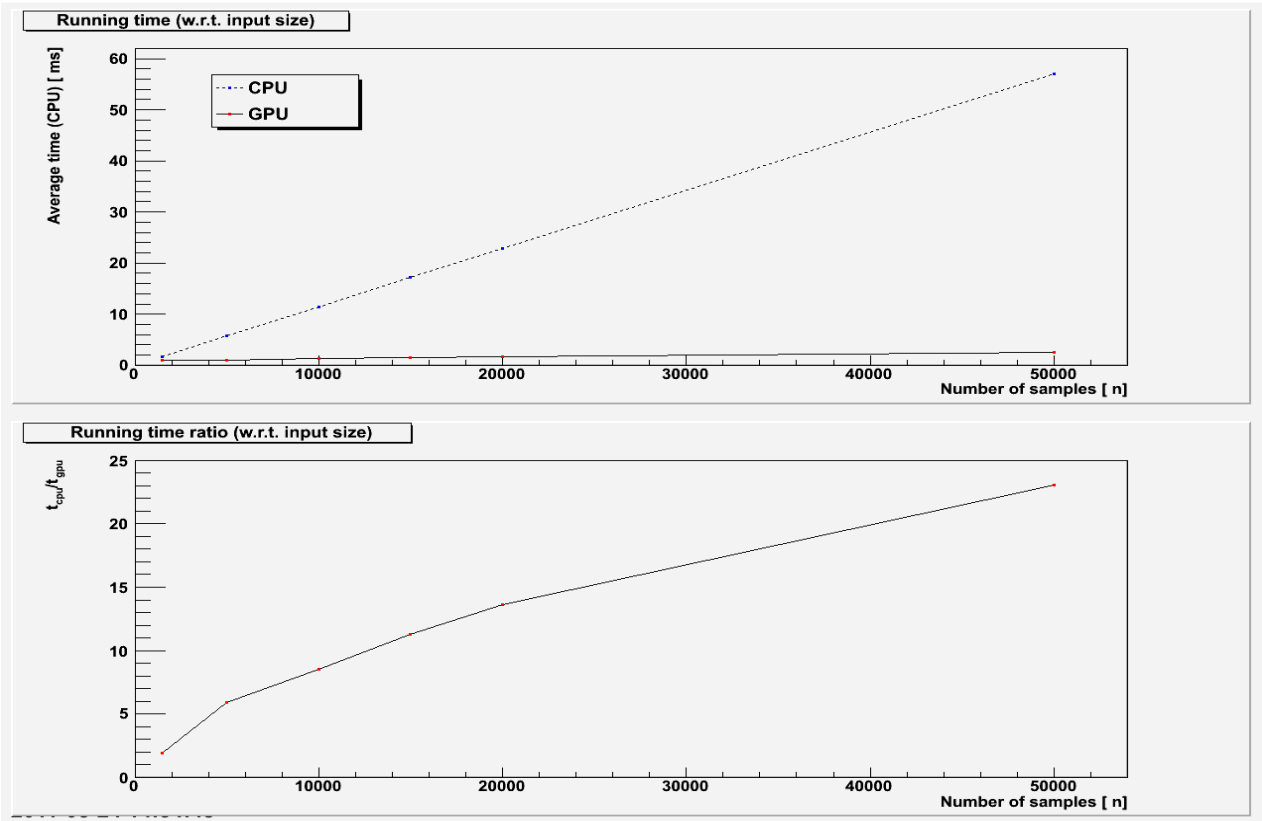


- Output : **st4** with  $nH = 16$  neurons in the hidden layer ( $\mathbb{R}^{17} \rightarrow \mathbb{R}^{16} \rightarrow \mathbb{R}$ )
- Learning :
  - 1 database with 1 400 patterns
  - 100 learning
- Running :
  - 6 databases with 1 500, 5 000, 10 000, 20 000 and 50 000 patterns
  - 10 running for each databases
- criteria for comparison : time ( $t$ ) and error ( $e$ )
  1. CPU : 2 quadri cores Xeon 5500 (Boost.uBLAS)
  2. GPU : 8 Fermi Tesla C2050 (CUDA/cuBLAS)



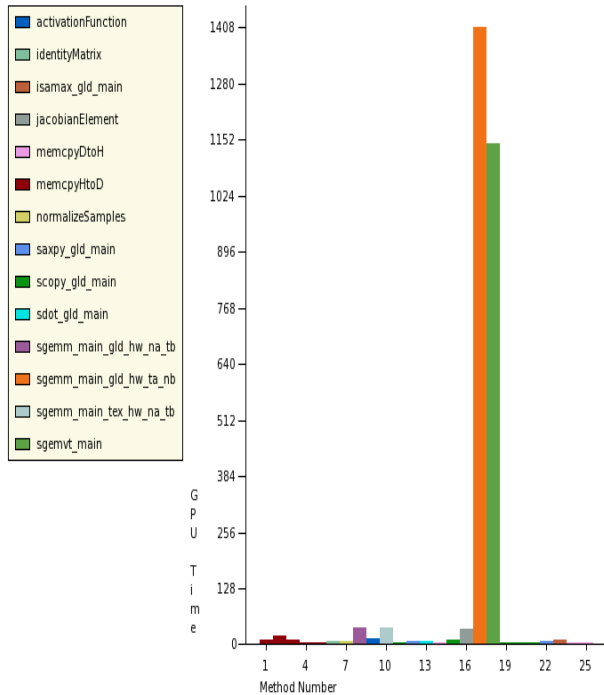
Mean : GPU 42 s versus CPU 115 s



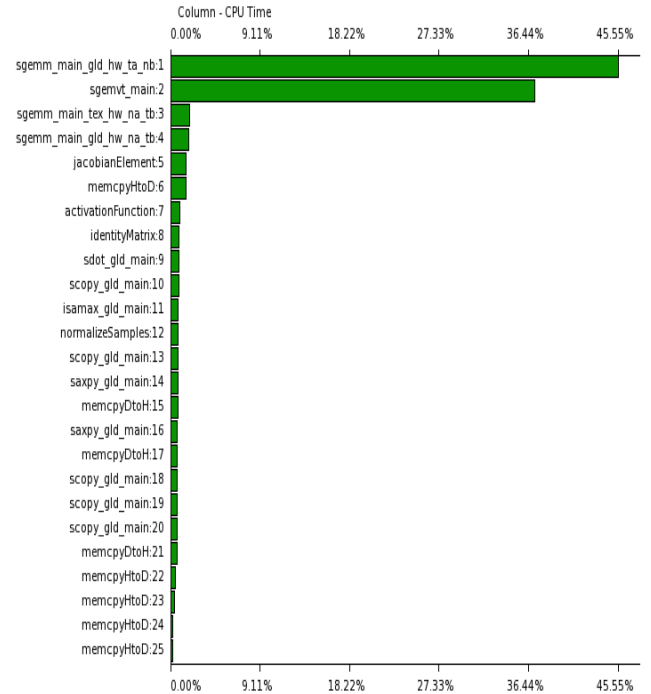




Height Plot



Column ( CPU Time ) Plot





1. GPU is 2 → 23 faster than CPU for evaluation ANN
2. GPU is only 3 faster than CPU for learning ANN for small database  
same speed-up for large database ?
3. main time consumer : matrix computing