

Fig. 5. Calculated RPA energy of the main II and IV giant resonances in closed shell nuclei are reported as a function of the angular momentum  $A^{-1/2}$ . Theoretical values including step by step. The well-known values of the constant  $\delta$  (ISGMR and VIGMR) are represented by rectangles, while the other theoretical values appear as very fragmented modes and are represented as long rectangles. Details of strength for these two resonances are given on the left part for the  $^{160}\text{Pb}$ ,  $^{160}\text{VIGMR}$  and  $^{160}\text{ISGMR}^*$  correspond to the second 2<sup>-</sup> and 0<sup>+</sup> modes, respectively (see the text).

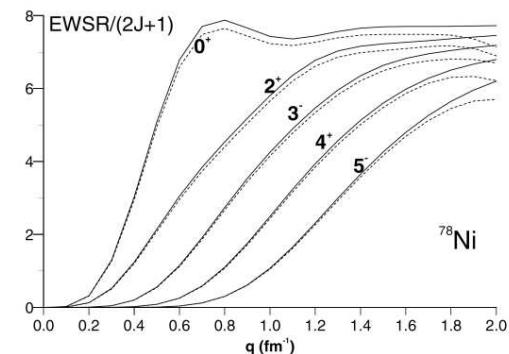
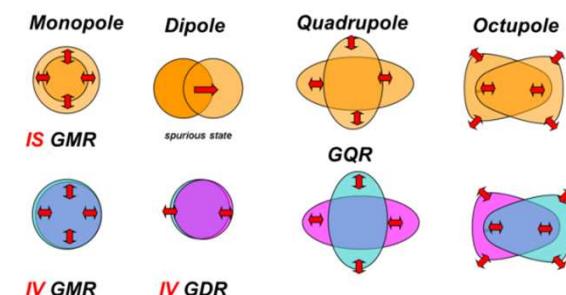
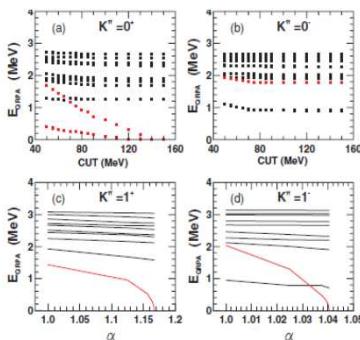
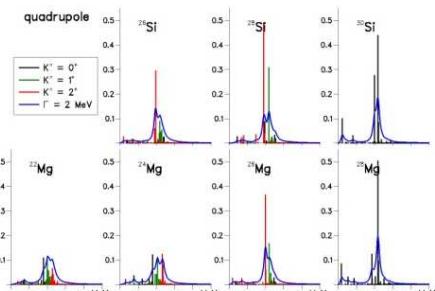
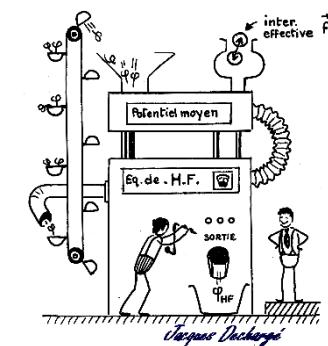
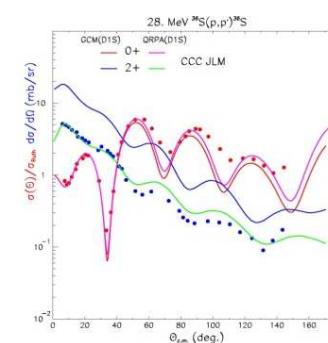


Fig. 1. Comparisons between the exact EWSR of eq. (3) (solid line) and those deduced from eq. (2) (dotted line) in  $^{78}\text{Ni}$  for the RPA states with  $J^\pi = 0^+$ ,  $2^+$ ,  $3^-$ ,  $4^+$  and  $5^-$ . The unit of the EWSR scale is  $e^2$  MeV. The abscissa  $q$  represents the transferred momentum.

# Excitations and QRPA calculations with the Gogny force



Sophie Péru  
&  
Marco Martini  
Marc Dupuis



# QRPA formalism

**HFB+QRPA**

$$\theta_n^+ = \sum_{ij} X_n^{ij} \beta_i^+ \beta_j^+ + Y_n^{ij} \beta_{\bar{j}}^- \beta_{\bar{i}}^- \quad \{\beta^+ \beta\} \text{ qp creation and annihilation operators.}$$

$\theta$  are solution of

$$\begin{pmatrix} A & B \\ B^* & A^* \end{pmatrix} \begin{pmatrix} X \\ Y \end{pmatrix} = \omega \begin{pmatrix} X \\ -Y \end{pmatrix}, \quad |n\rangle = \theta_n^+ |\tilde{0}\rangle.$$

In our approach, The effective interaction **D1S** is used both in the HFB mean field and in the QRPA matrix.

In axial symmetry , QRPA states **{θ+}** are obtained for each block **K<sup>π</sup>** (K<sup>π</sup>≤J<sup>π</sup>)

## Restoration of rotational symmetry for deformed states

$$|JM(K)\rangle = \frac{\sqrt{2J+1}}{4\pi} \int d\Omega D_{MK}^J(\Omega) R(\Omega) |\theta_K\rangle + (-)^{J-K} D_{M-K}^J(\Omega) R(\Omega) |\bar{\theta}_K\rangle$$

We want to calculate:  $\langle \tilde{0} | \hat{Q}_{\lambda\mu} | JM(K) \rangle$  for all QRPA states (K ≤ J)

For example: J<sup>π</sup> = 2<sup>+</sup>  $\hat{Q}_{20} = \sum r^2 (Y_{20})$  In intrinsic frame  $r^2 Y_{\lambda\mu} = \sum_v D_{\mu\nu}^\lambda r^2 Y_{\lambda\nu}$

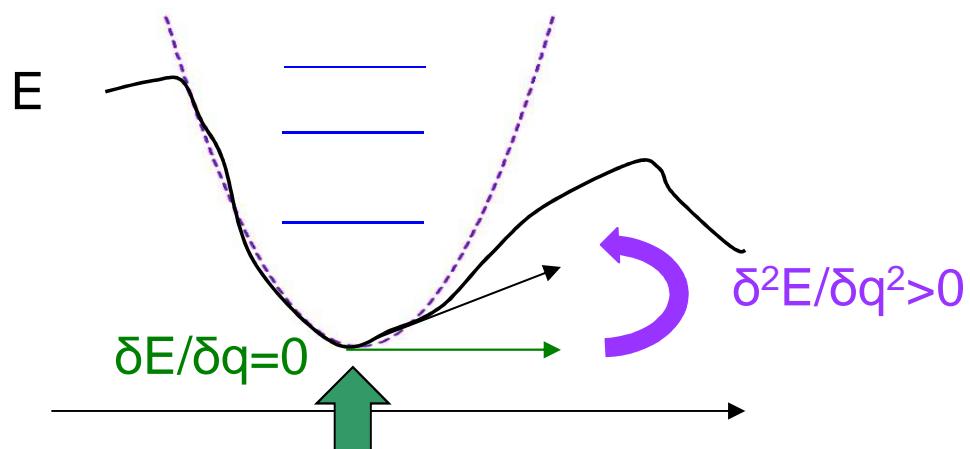
Using rotational approximation and relations for 3j symbols

$$\langle \tilde{0} | \hat{Q}_{20} | JM(K) \rangle = \frac{1}{\sqrt{5}} \langle 0 | \hat{Q}_{20} | \theta_K \rangle \delta_{K,0} + \frac{\sqrt{3}}{\sqrt{5}} \langle 0 | \hat{Q}_{2-1} | \theta_K \rangle \delta_{K,\pm 1} + \frac{\sqrt{3}}{\sqrt{5}} \langle 0 | \hat{Q}_{22} | \theta_K \rangle \delta_{K,\pm 2}$$

Using time reversal symmetry, three independent calculations (K<sup>π</sup> = 0<sup>+</sup>, 1<sup>+</sup>, 2<sup>+</sup>) are needed.

RPA approaches describe  
all multipolarities and all parities,  
collective states and individual ones,  
low energy and high energy states  
with the same accuracy.

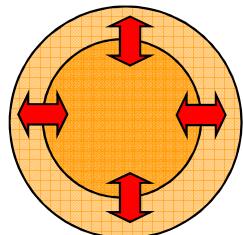
Within the small amplitude approximation, i.e. « harmonic » nuclei



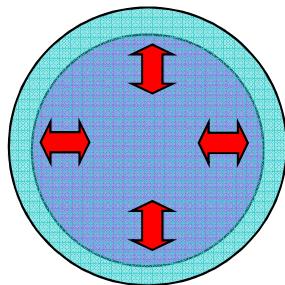
# High energy collective states: giant resonances

Giant resonances are related to nuclear matter properties

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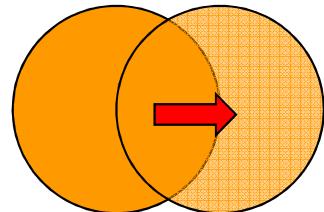


**IS GMR**

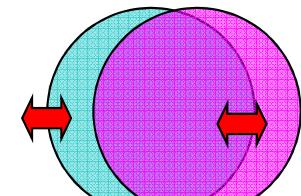


**IV GMR**

**Dipole**

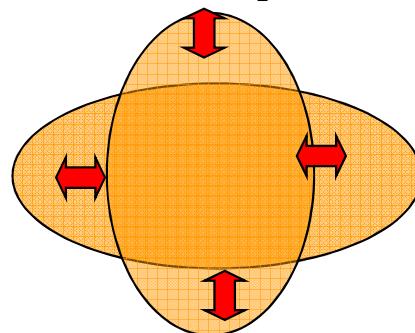


*spurious state*

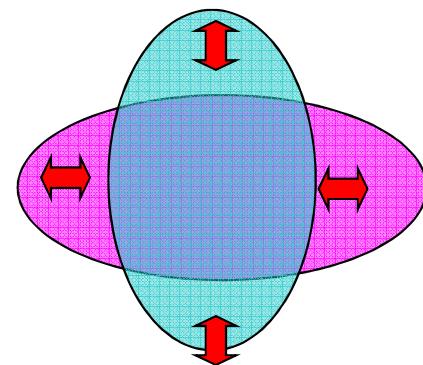


**IV GDR**

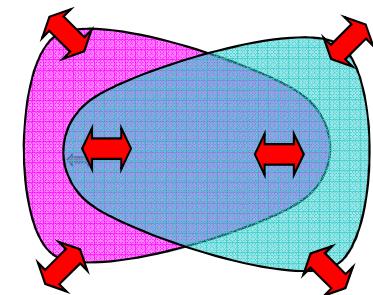
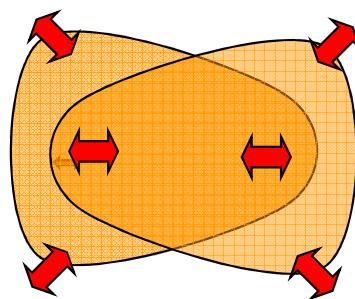
**Quadrupole**



**GQR**



**Octupole**

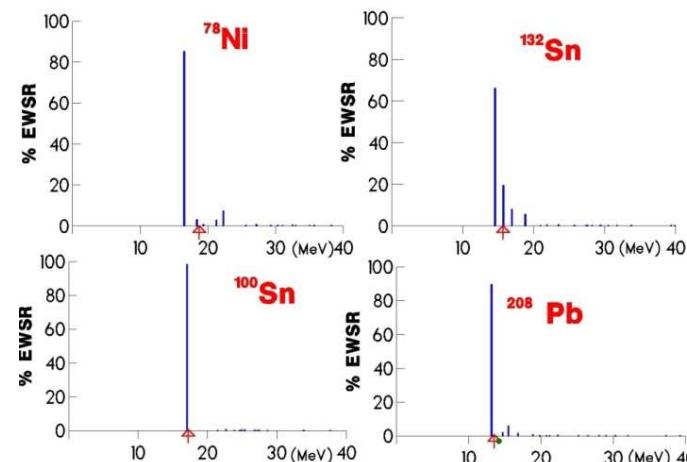


# RPA in spherical symmetry

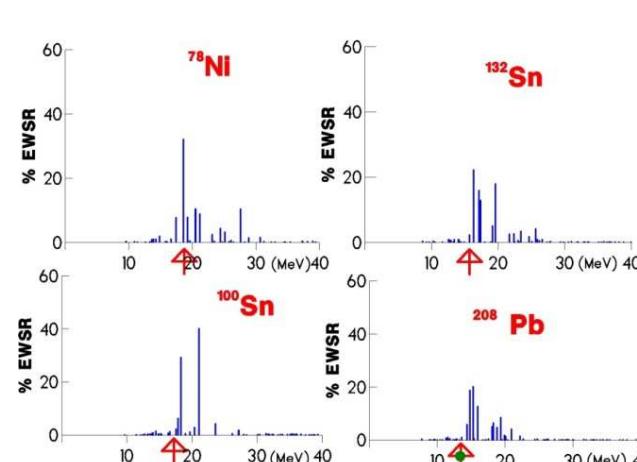
## Giant resonances in exotic nuclei:

$^{100}\text{Sn}$ ,  $^{132}\text{Sn}$ ,  $^{78}\text{Ni}$ ; S. Péru, J.F. Berger, and P.F. Bortignon, Eur. Phys. Jour. A **26**, 25-32 (2005)

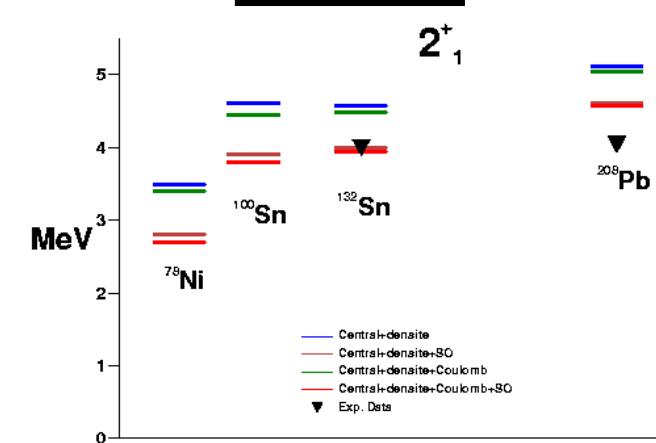
Monopole



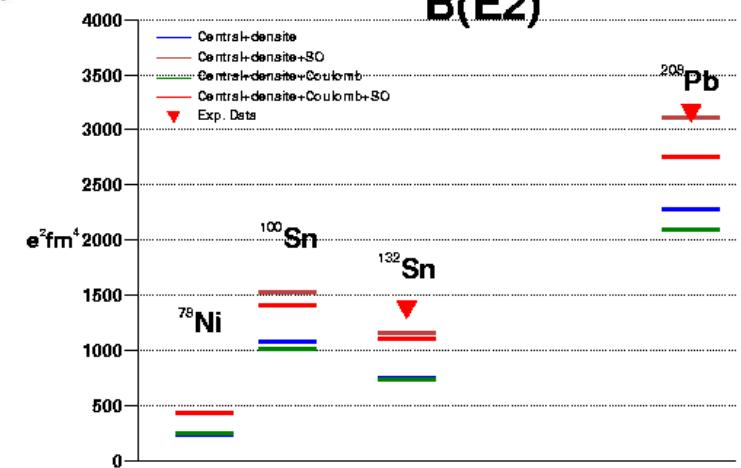
Dipole



Quadrupole



B(E2)



→ Such study have shown  
the role of the consistence  
between mean field and RPA matrix.

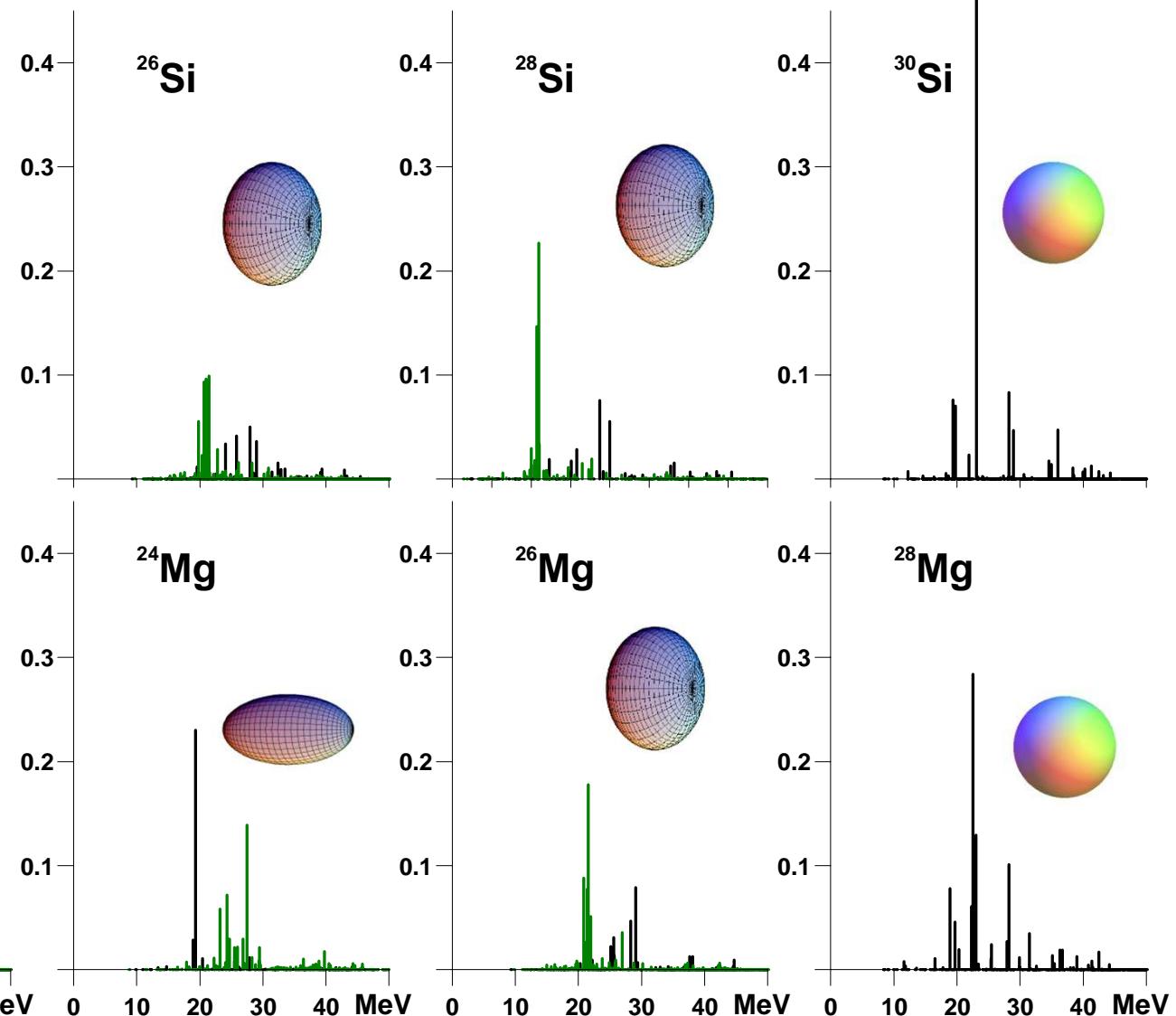
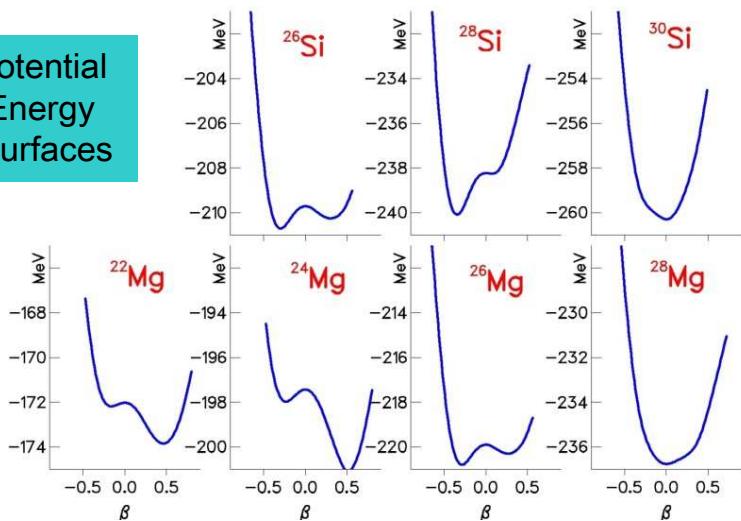
Approach limited to Spherical nuclei with no pairing

# QRPA in axial symmetry :

IV Dipole

$K^\pi=0^-$      $K^\pi=1^-$

Potential Energy Surfaces

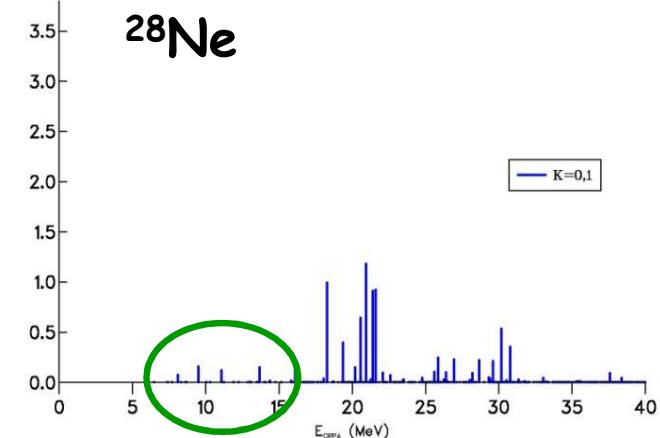
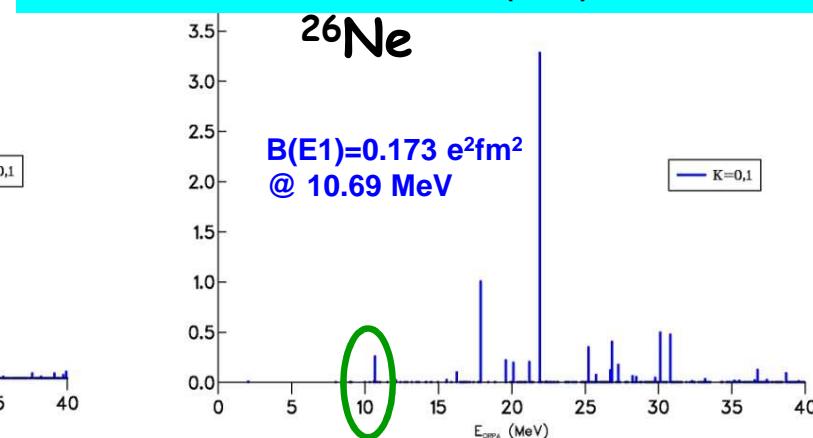
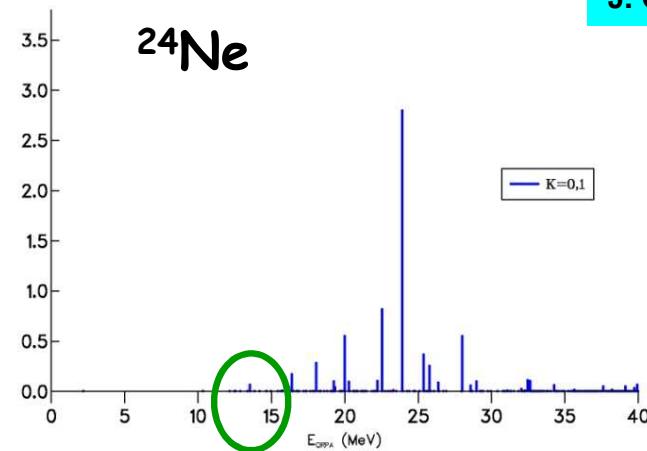
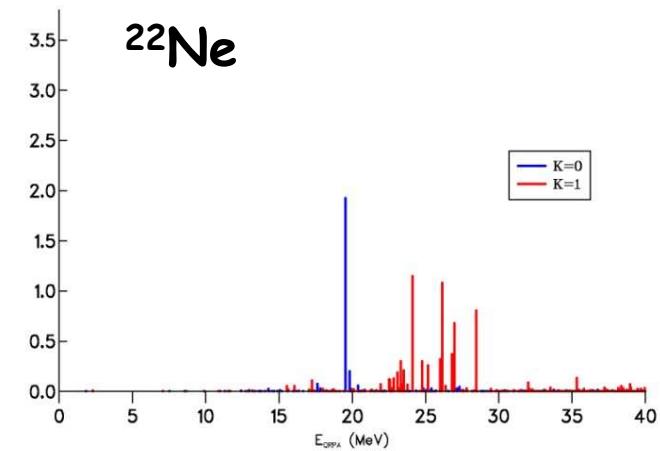
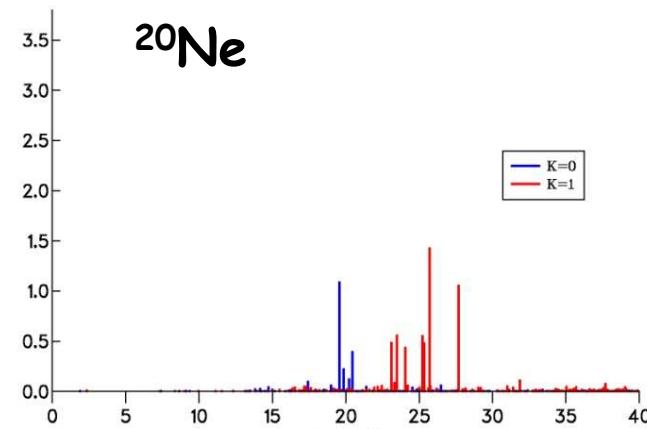
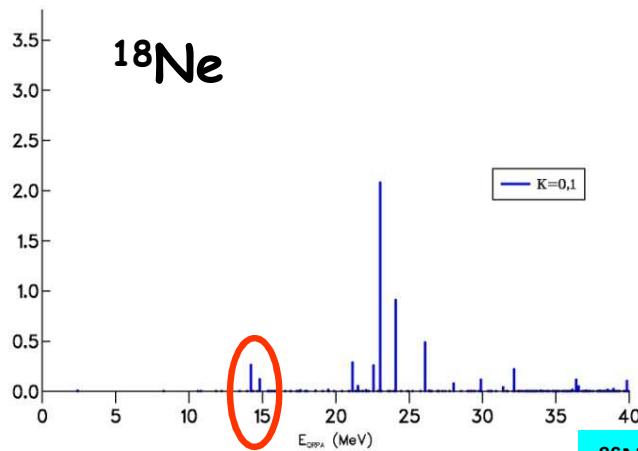


*Role of deformation on giant resonances within the quasiparticle random-phase approximation and the Gogny force,  
S. Péru and H. Goutte, Phys. Rev. C 77, 044313 (2008).*

# dipole response for Neon isotopes

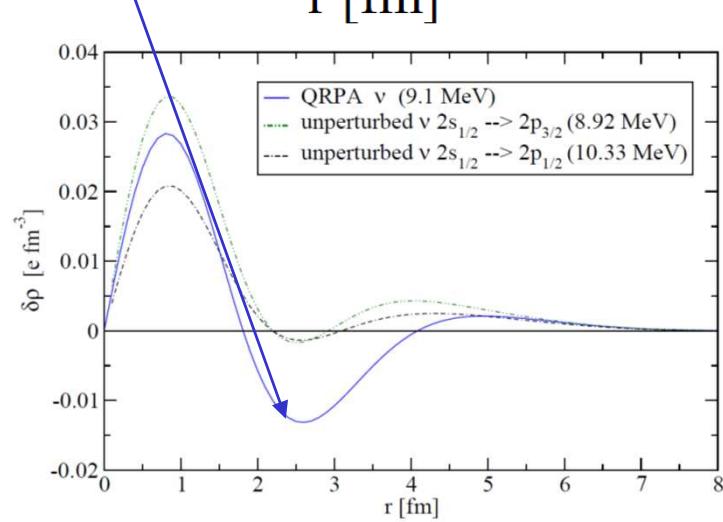
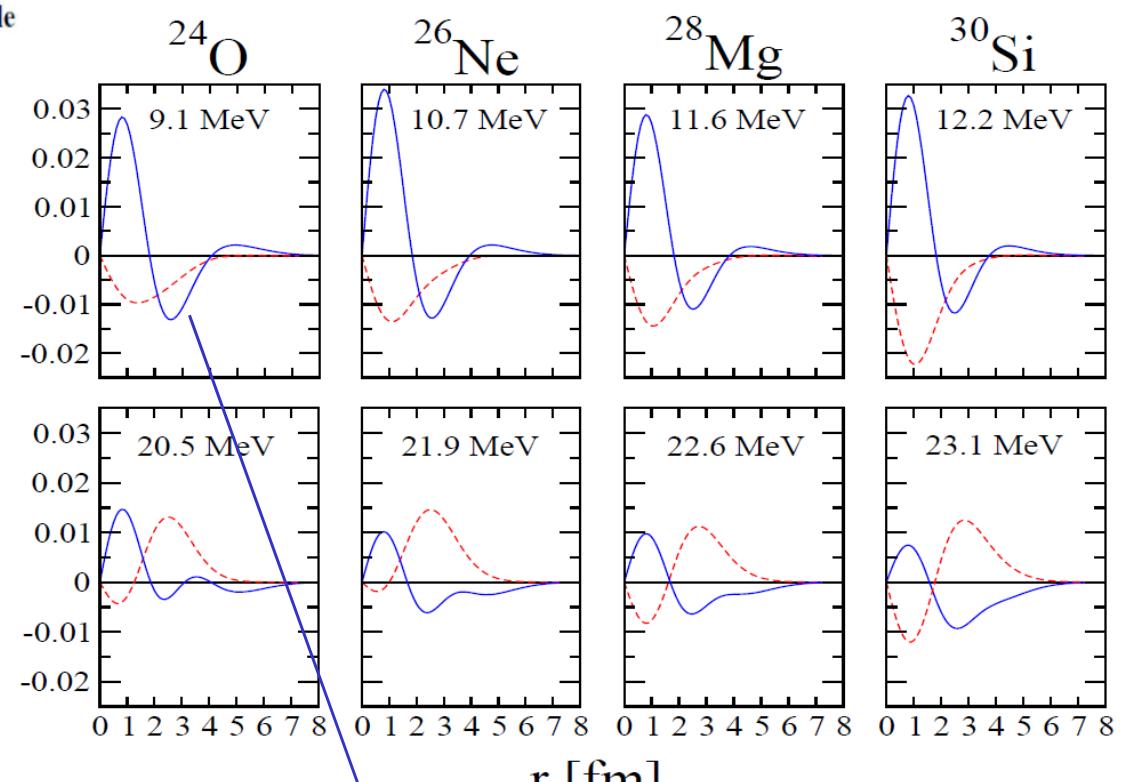
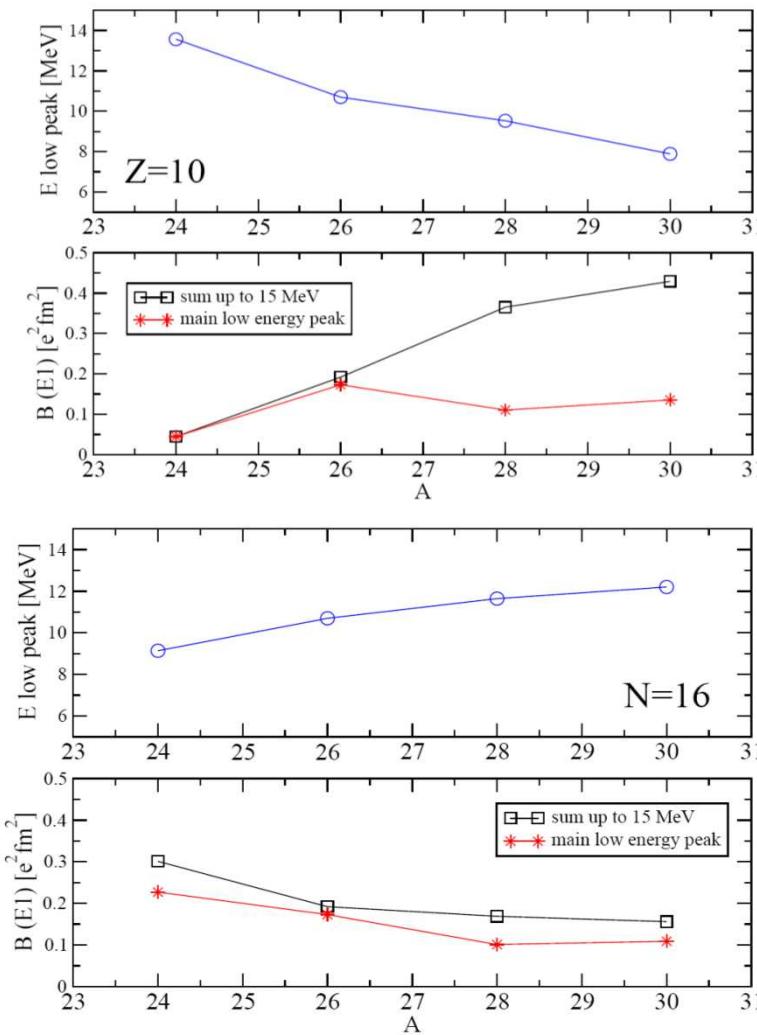
## Increasing neutron number

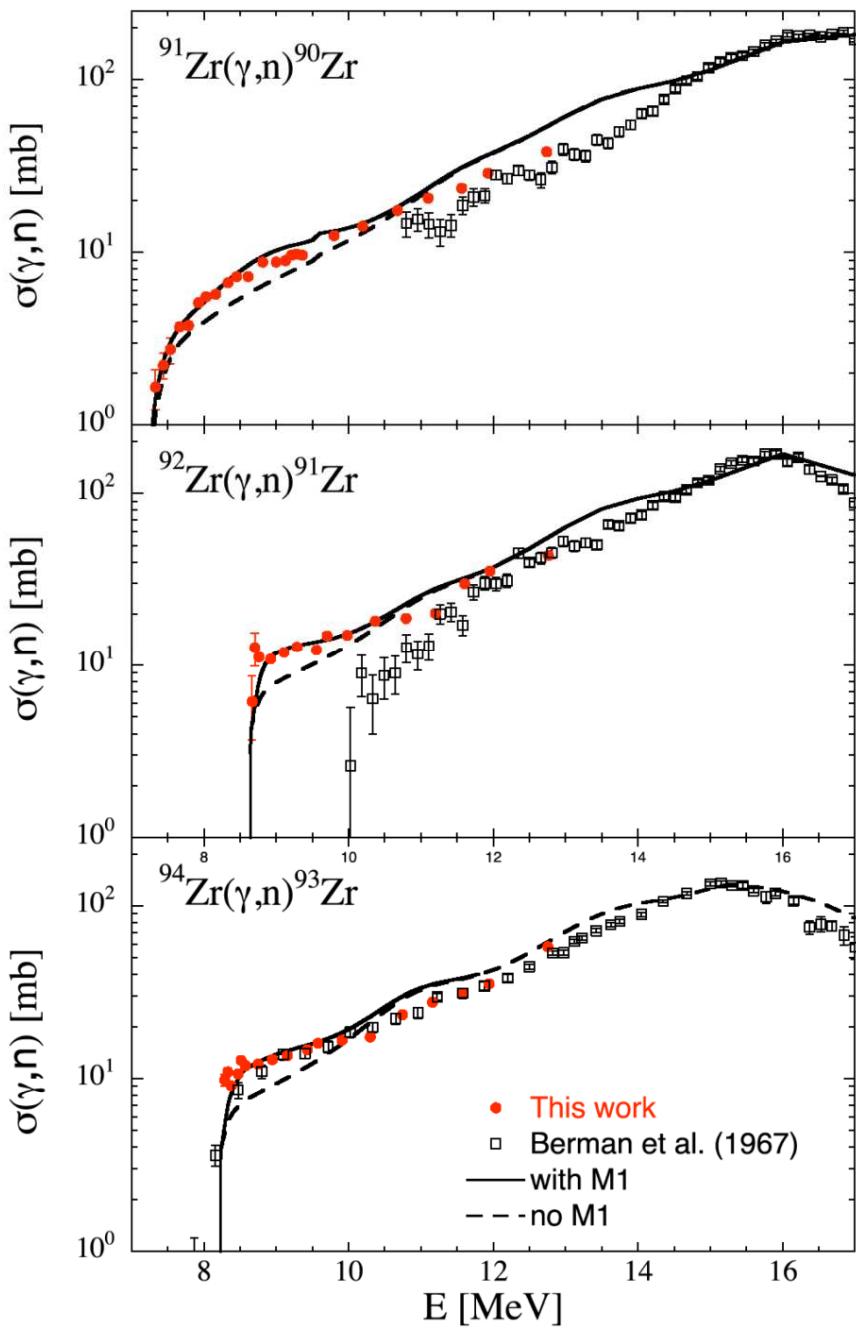
- Low energy dipole resonances and shift to low energies
- Increasing of fragmentation



# Low-energy dipole excitations in neon isotopes and $N = 16$ isotones within the quasiparticle random-phase approximation and the Gogny force

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CEA/DAM/DIF, F-91297 Arpajon, France





PRL 100, 162502 (2008)

PHYSICAL REVIEW LETTERS

week ending  
25 APRIL 2008**M1  $\gamma$  Strength for Zirconium Nuclei in the Photoneutron Channel**

H. Utsunomiya,<sup>1</sup> S. Goriely,<sup>2</sup> T. Kondo,<sup>1</sup> T. Kaihori,<sup>1</sup> A. Makinaga,<sup>1</sup> S. Goko,<sup>3</sup> H. Akimune,<sup>1</sup> T. Yamagata,<sup>1</sup> H. Toyokawa,<sup>4</sup> T. Matsumoto,<sup>4</sup> H. Harano,<sup>4</sup> S. Hohara,<sup>5</sup> Y.-W. Lui,<sup>6</sup> S. Hilaire,<sup>7</sup> S. Péru,<sup>7</sup> and A. J. Koning<sup>8</sup>

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<sup>2</sup>Institut d'Astronomie et d'Astrophysique, Université Libre de Bruxelles, Campus de la Plaine, CP-226, 1050 Brussels, Belgium

<sup>3</sup>Japan Atomic Energy Agency, Tokai-mura, Naka, Ibaraki 319-1195, Japan

<sup>4</sup>National Institute of Advanced Industrial Science and Technology, Tsukuba 305-8568, Japan

<sup>5</sup>Atomic Energy Research Institute, Kinki University, Kowakae 3-4-1, Osaka 577-8502, Japan

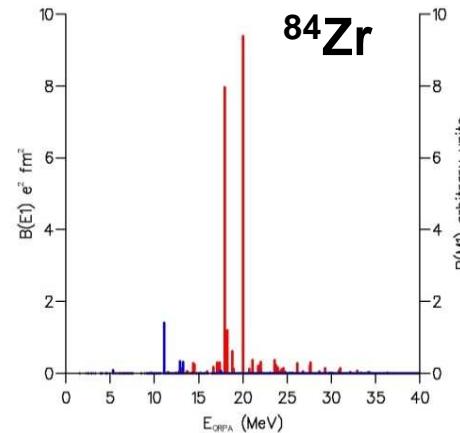
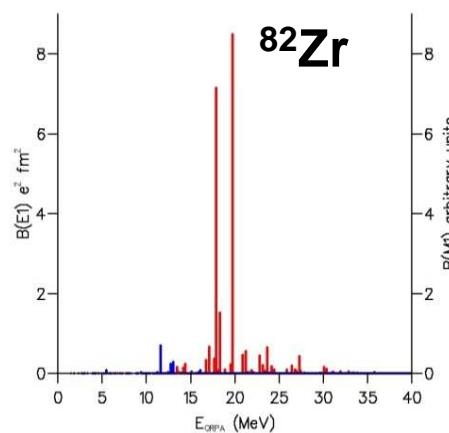
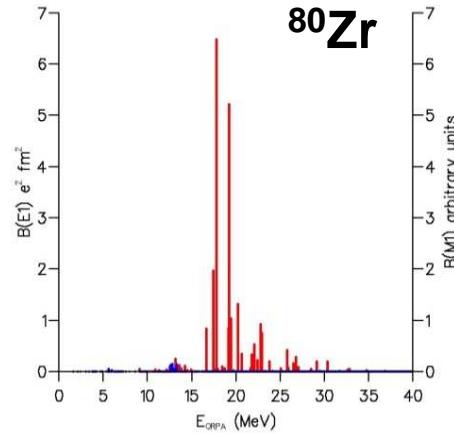
<sup>6</sup>Cyclotron Institute, Texas A&M University, College Station, Texas 77843, USA

<sup>7</sup>Département de Physique Théorique et Appliquée, Service de Physique Nucléaire, B.P. 12 - F-91680 Bruyères-le-Châtel, France

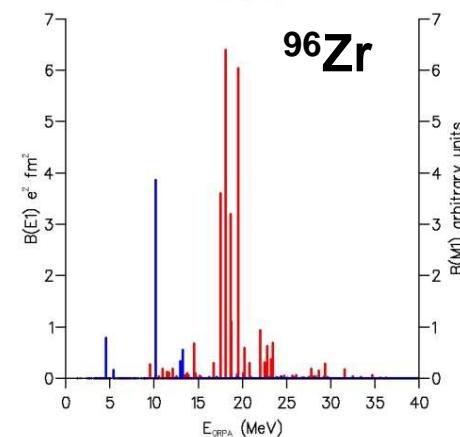
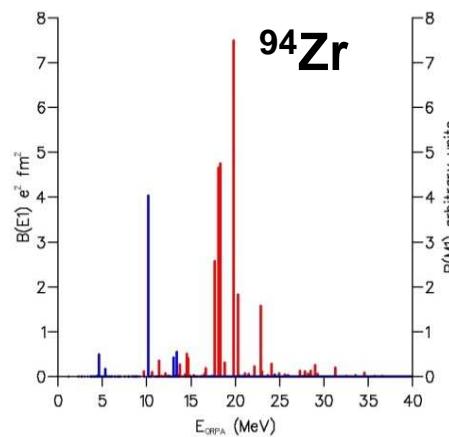
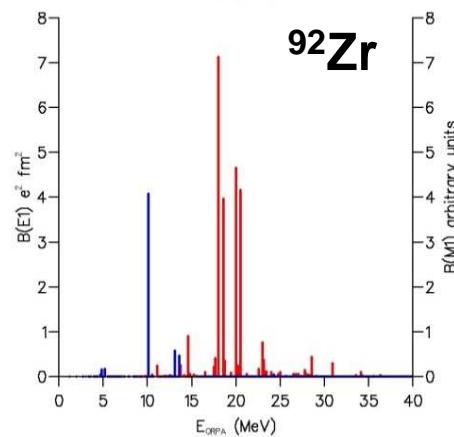
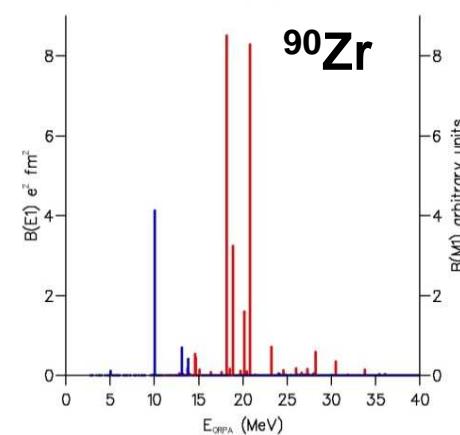
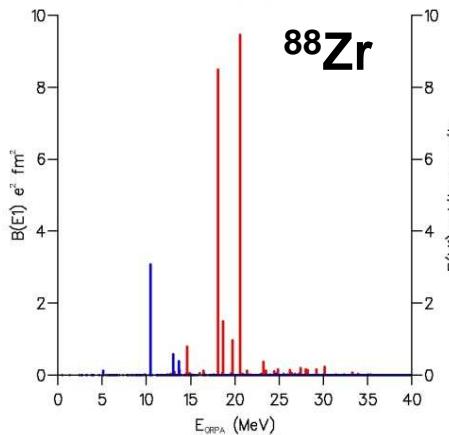
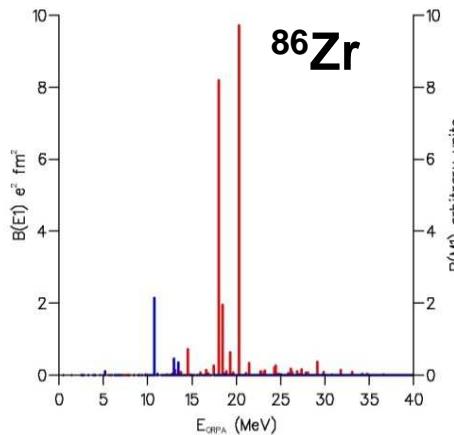
<sup>8</sup>Nuclear Research and Consultancy Group, P.O. Box 25, NL-1755 ZG Petten, The Netherlands

(Received 30 November 2007; published 24 April 2008)

# Dipole response for Zr isotopes :

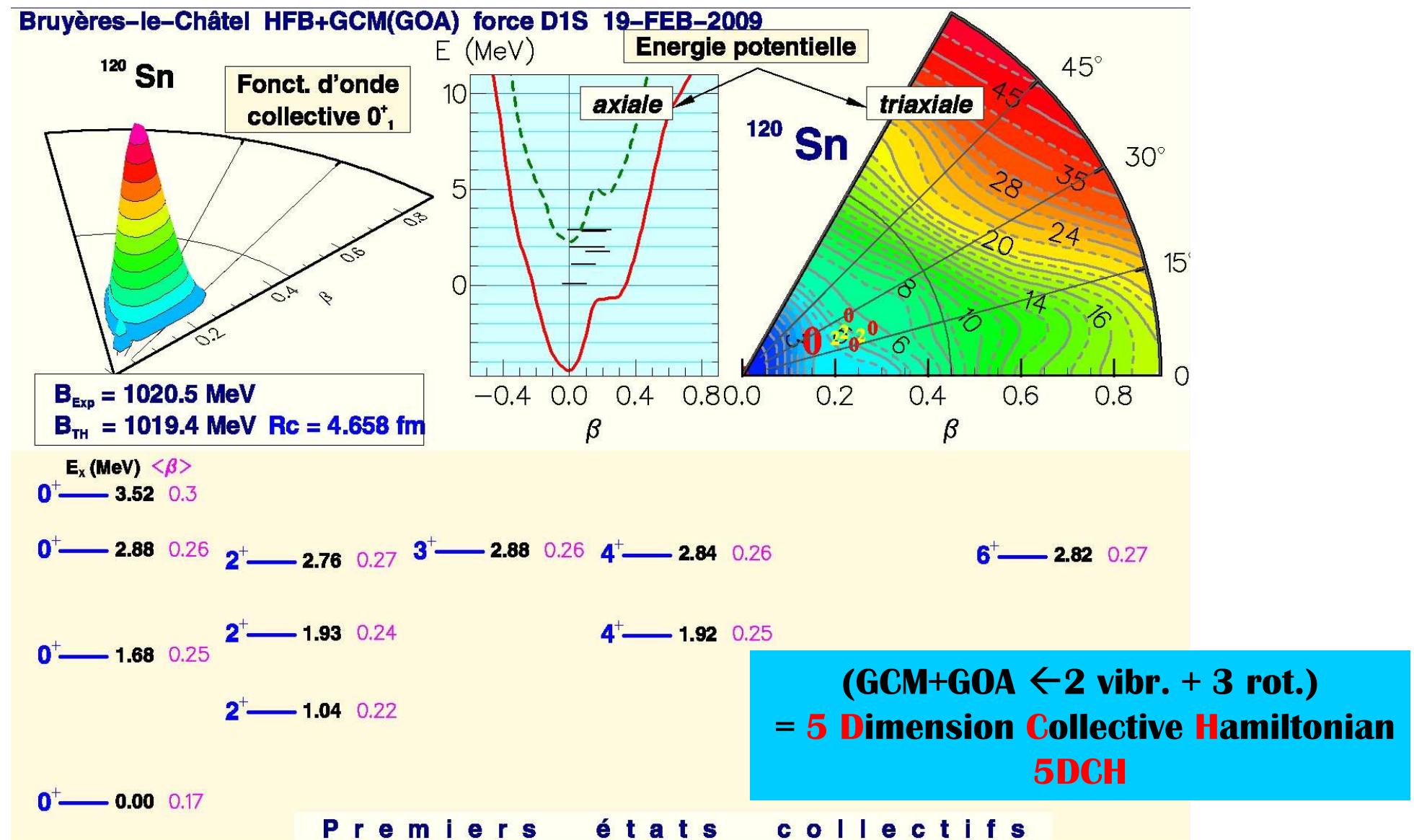


**B(E1)  
B(M1)**

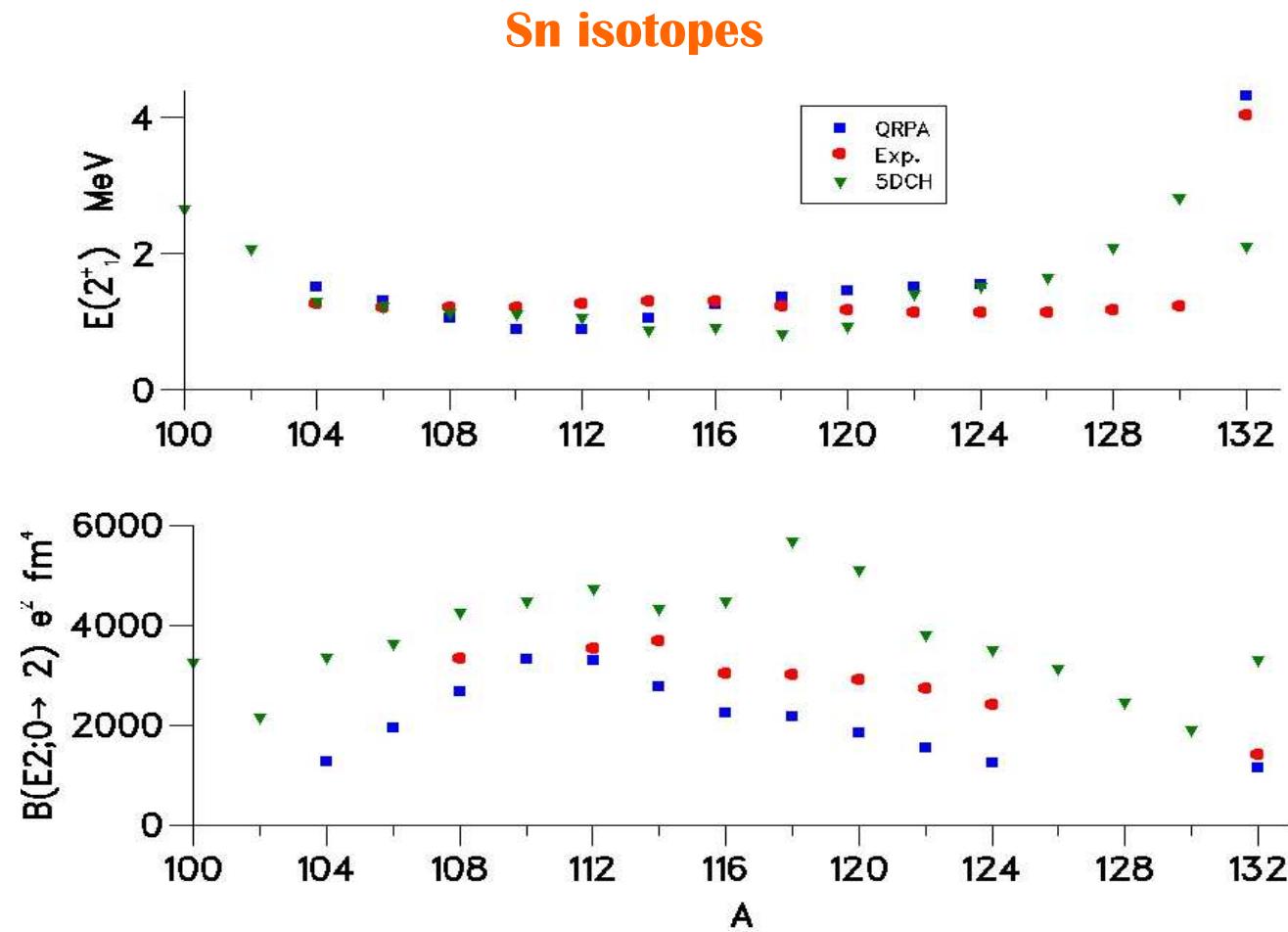
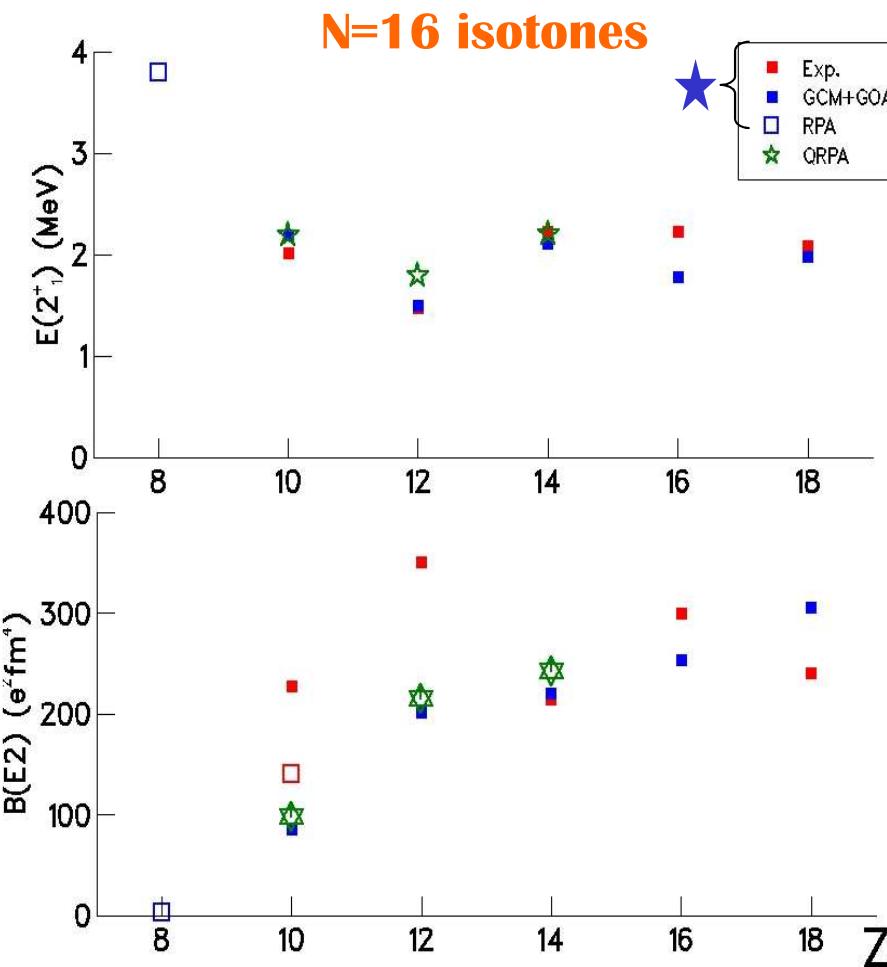


**S. Goriely,  
H. Goutte,  
S. Hilaire,  
M. Martini,  
S. Péru, ...**

# Beyond mean field ... with “GCM”

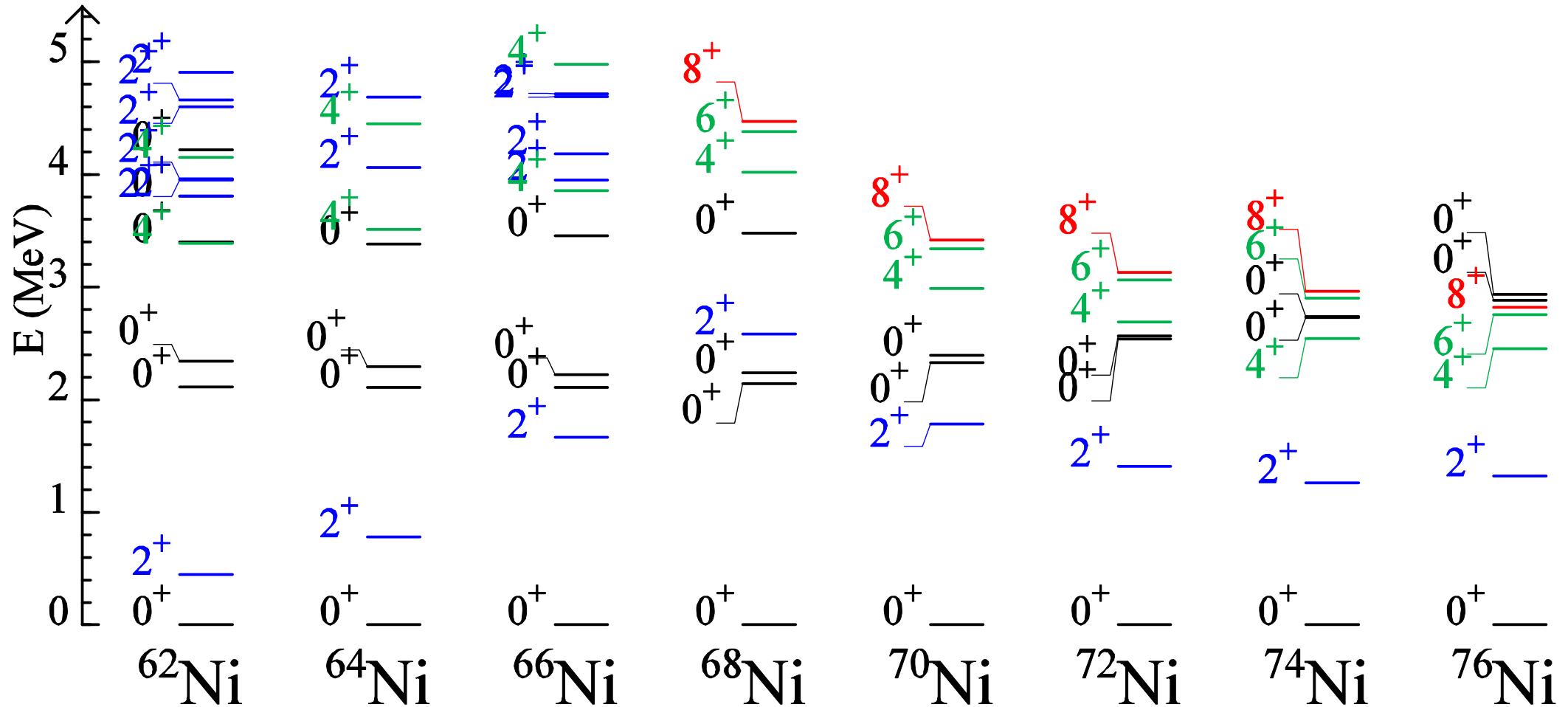


# HFB+QRPA / HFB+5DCH with the same interaction:



★ A. Obertelli, et al, Phys. Rev. C 71, 024304 (2005)

# Spectroscopy in Ni isotopes within QRPA



L. Gaudefroy & S. Péru

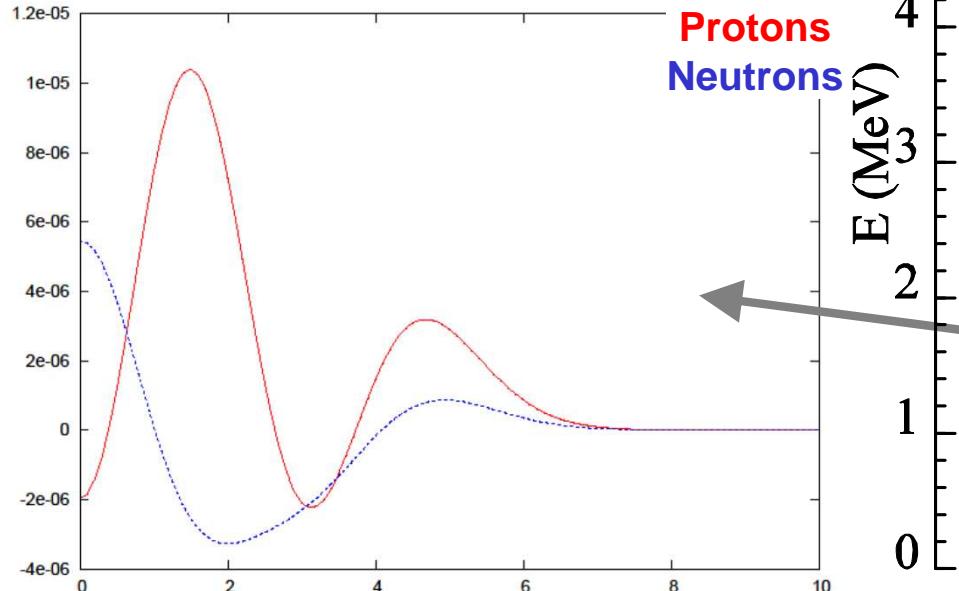
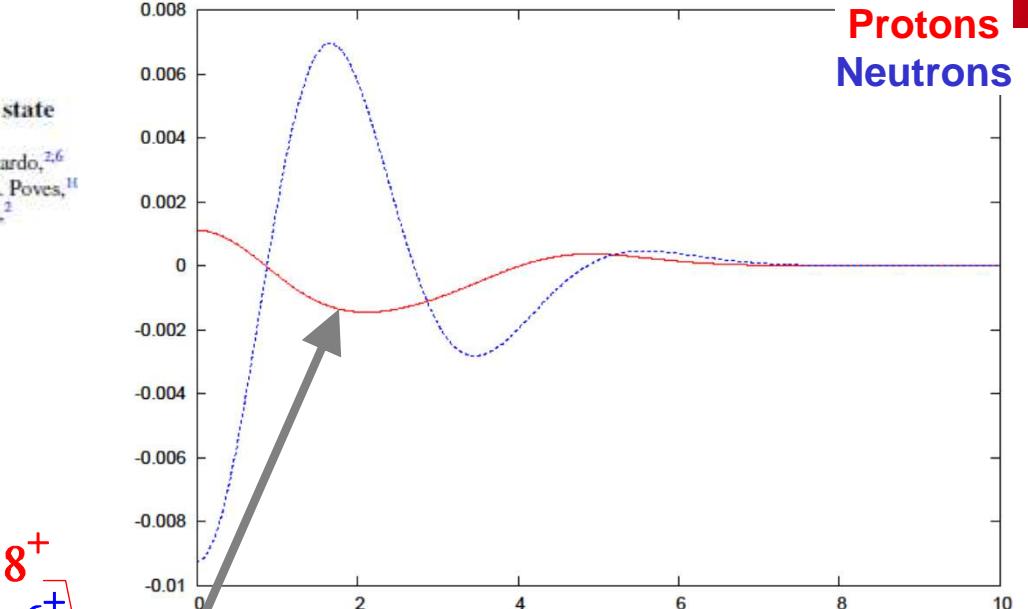
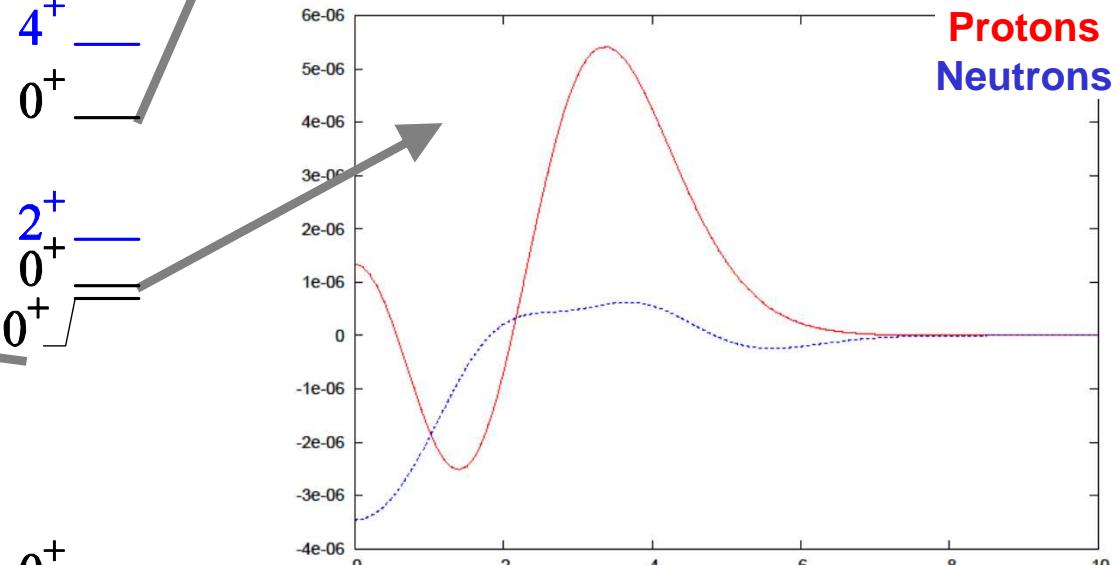
PHYSICAL REVIEW C 85, 031301(R) (2012)

Discovery of a new isomeric state in  $^{68}\text{Ni}$ : Evidence for a highly deformed proton intruder state

A. Dijon,<sup>1</sup> E. Clément,<sup>1</sup> G. de France,<sup>1</sup> G. de Angelis,<sup>2</sup> G. Duchêne,<sup>3</sup> J. Dudouet,<sup>1</sup> S. Franschoo,<sup>4</sup> A. Gadea,<sup>5</sup> A. Gottardo,<sup>2,6</sup> T. Hüyük,<sup>5</sup> B. Jacquot,<sup>1</sup> A. Kusoglu,<sup>7</sup> D. Lebhertz,<sup>1</sup> G. Lehaut,<sup>8</sup> M. Martini,<sup>9</sup> D. R. Napoli,<sup>3</sup> F. Nowacki,<sup>3</sup> S. Péru,<sup>9</sup> A. Poves,<sup>11</sup> F. Recchia,<sup>6</sup> N. Redon,<sup>8</sup> E. Sahin,<sup>2</sup> C. Schmitt,<sup>1</sup> M. Sferrazza,<sup>11</sup> K. Sieja,<sup>3</sup> O. Stezowski,<sup>8</sup> J. J. Valiente-Dobón,<sup>2</sup> A. Vancraeyenest,<sup>8</sup> and Y. Zheng<sup>1,12</sup>

# 0<sup>+</sup> states in $^{68}\text{Ni}$ within QRPA

## Transition densities


**Protons**  
**Neutrons**
 $^{68}\text{Ni}$ 

**Protons**  
**Neutrons**

**M. Martini, S. Péru ...**

# Multipolar response for $^{238}\text{U}$

PHYSICAL REVIEW C 83, 014314 (2011)

## Giant resonances in $^{238}\text{U}$ within the quasiparticle random-phase approximation with the Gogny force

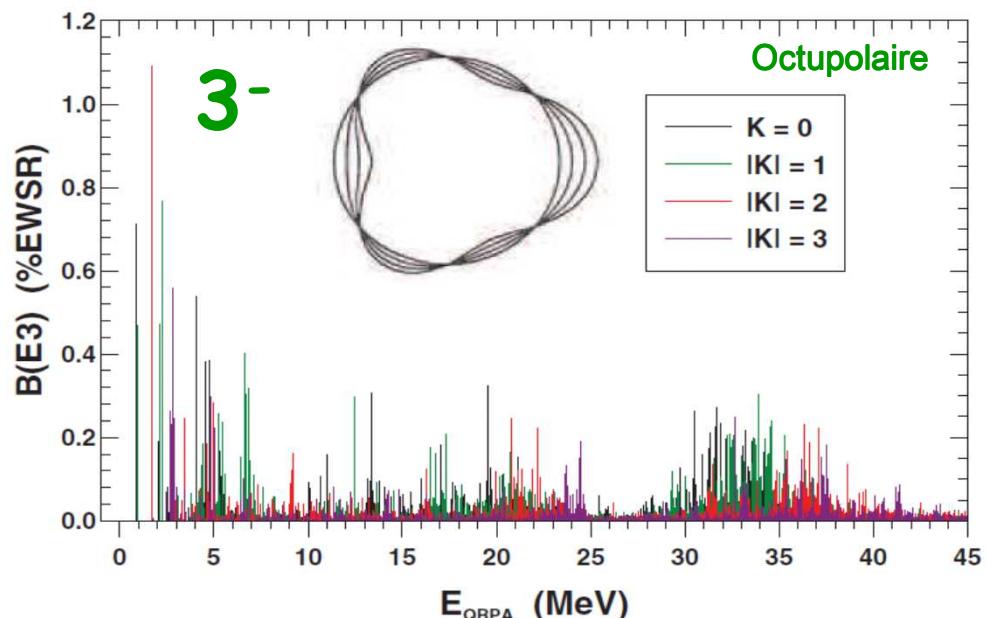
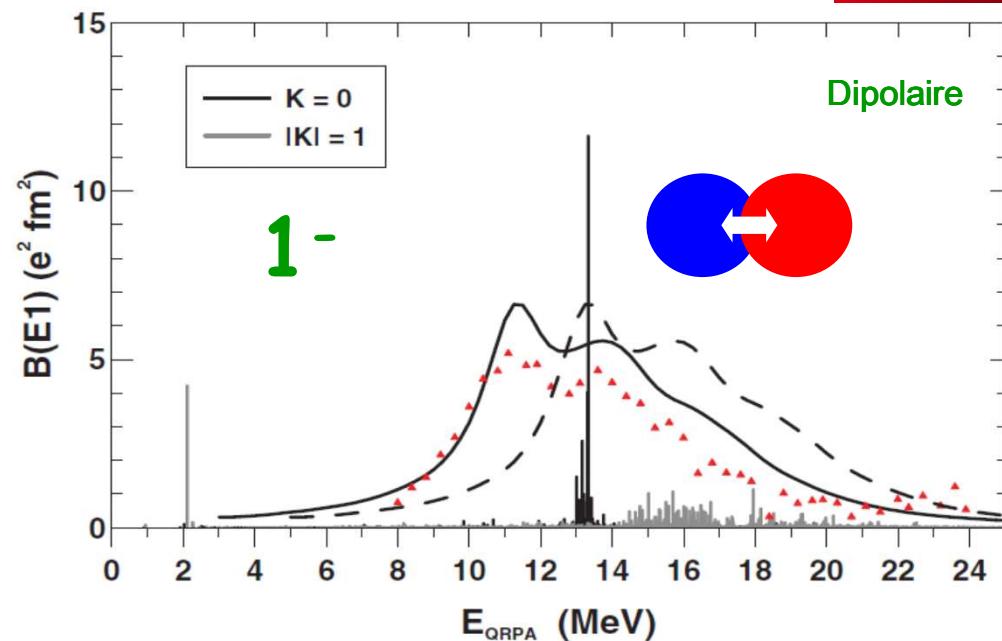
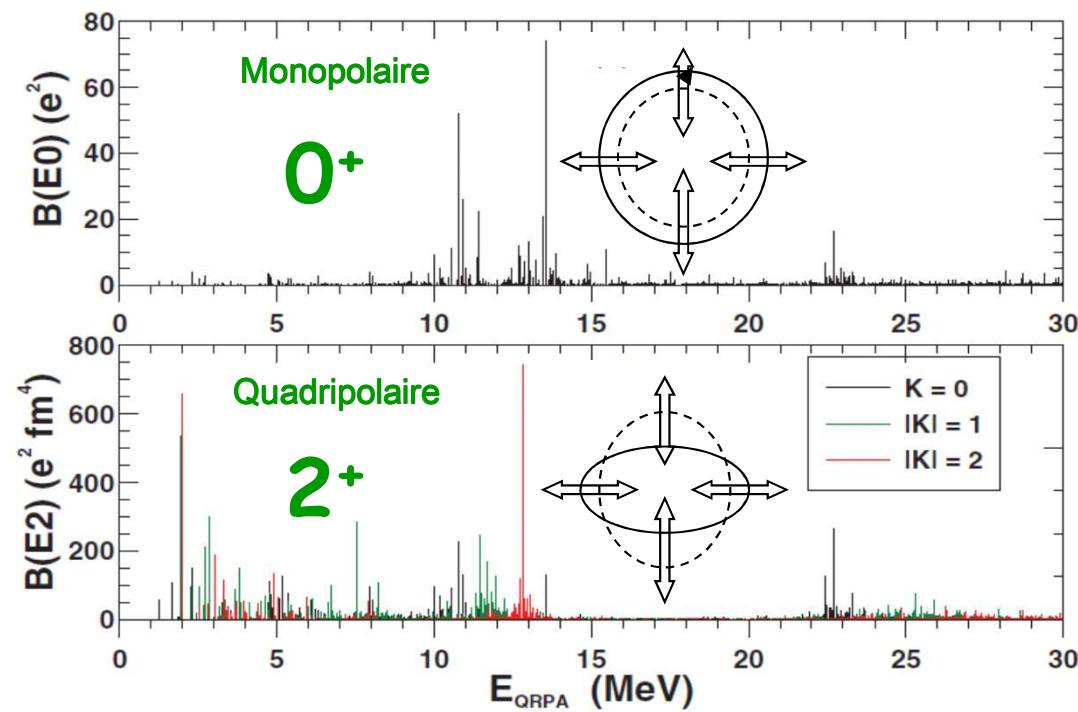
S. Péru,<sup>1,\*</sup> G. Gosselin,<sup>1</sup> M. Martini,<sup>1</sup> M. Dupuis,<sup>1</sup> S. Hilaire,<sup>1</sup> and J.-C. Devaux<sup>2</sup>

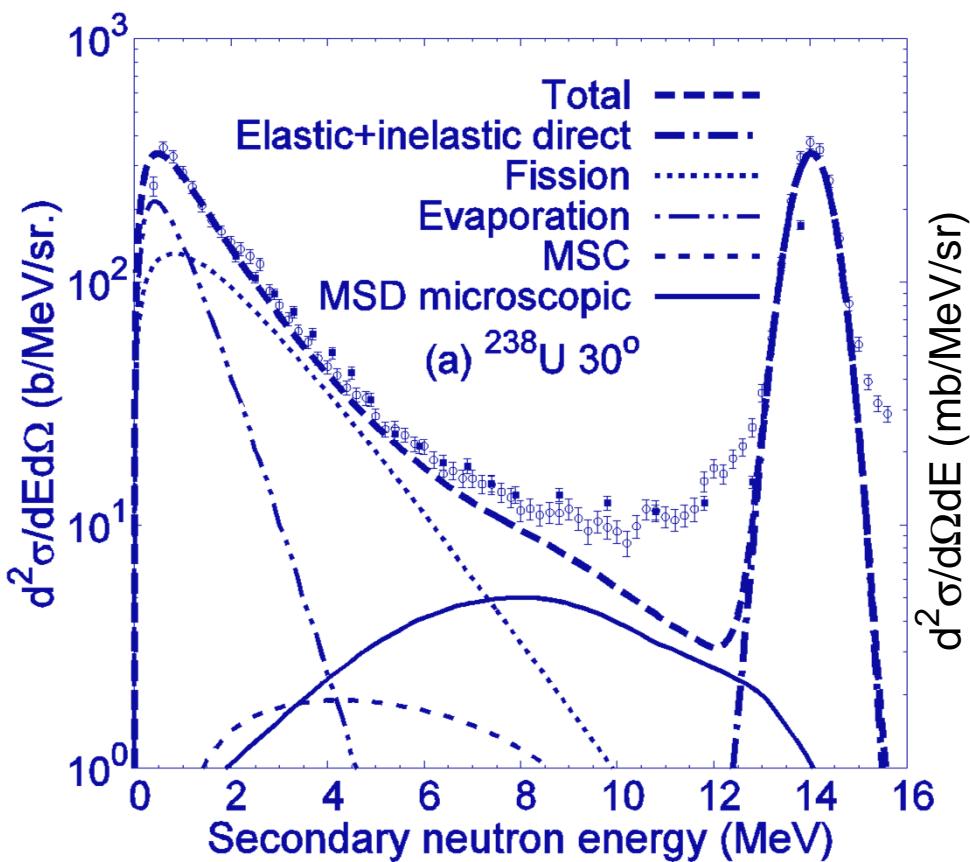
<sup>1</sup>CEA/DAM/DIF, F-91297 Arpajon, France

<sup>2</sup>ENSIIE, 1 square de la résistance, F-91025 Evry Cedex, France

(Received 29 October 2010; published 27 January 2011)

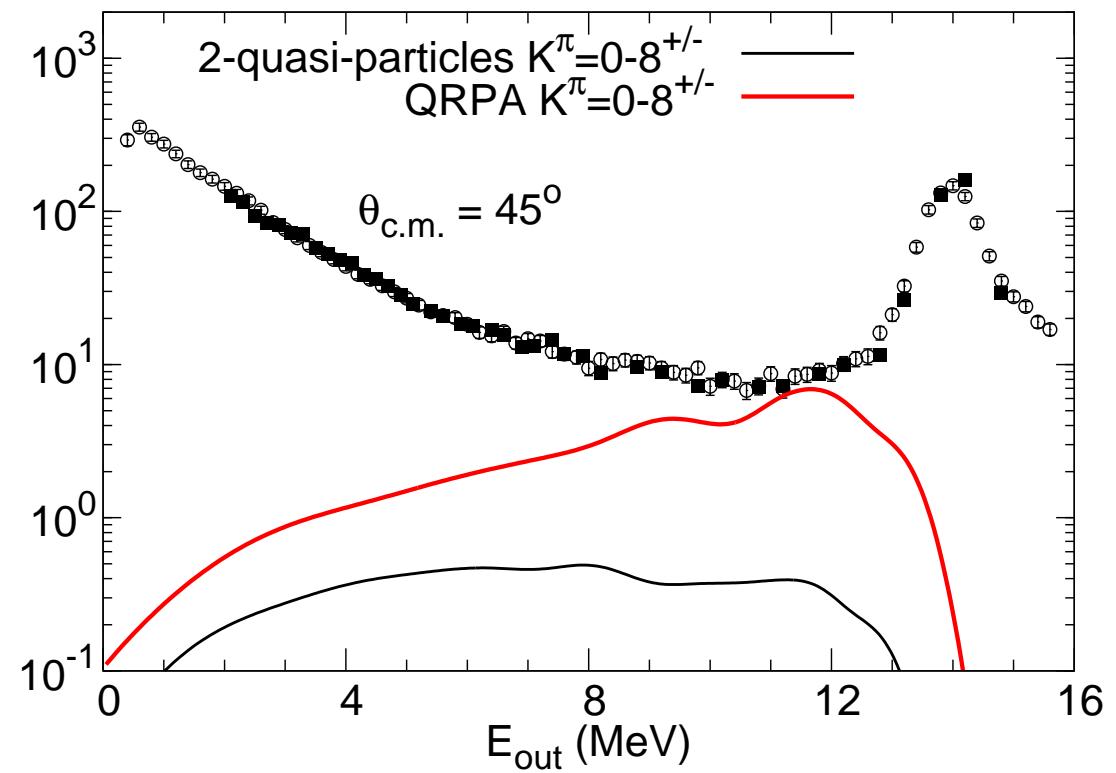
More than 716800 hours (~82 years)  
of computing time  
spread over 256 and 512 proc.





Comparison between experimental data (circles) and one-step contributions (full curves) to the double-differential cross sections for 14.1 MeV neutron on  $^{238}\text{U}$  (a,c).

M. Dupuis et al,  
Proceedings of the Second International Workshop  
on Nuclear Compound Reactions and Related Topics, (2010).



M. Dupuis et al,  
13<sup>th</sup> International Conference on Nuclear Reaction Mechanisms,  
Varenna, june 11-15, 2012.

# ... beyond the nuclear structure :

Test of QRPA and 5DCH (GCM) wave functions  
in proton inelastic scattering...

$^{36}\text{S}$

HFB+5DCH

$E(2^+_1) = 2.34 \text{ MeV}$

$B(E2) = 375 \text{ e}^2\text{fm}^4$

HFB+QRPA

$E(2^+_1) = 3.29 \text{ MeV}$

$B(E2) = 139.7 \text{ e}^2\text{fm}^4$

Exp

$E(2^+_1) = 3.29 \text{ MeV}$

$B(E2) = 100 \text{ e}^2\text{fm}^4$

