

GCM and QRPA

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Collaborators and other people I bothered

P.-H. Heenen, J.-M. Yao, V. Hellemans

M. Bender, B. Avez

A. Pastore

D. Tarpanov

J. Toivanen

P.-G. Reinhard

The main codes I used

GCM side:

HFBCS: ev8

projection + kernel calculation: promesse

(P. Bonche, H. Flocard, P.-H. Heenen, M. Bender)

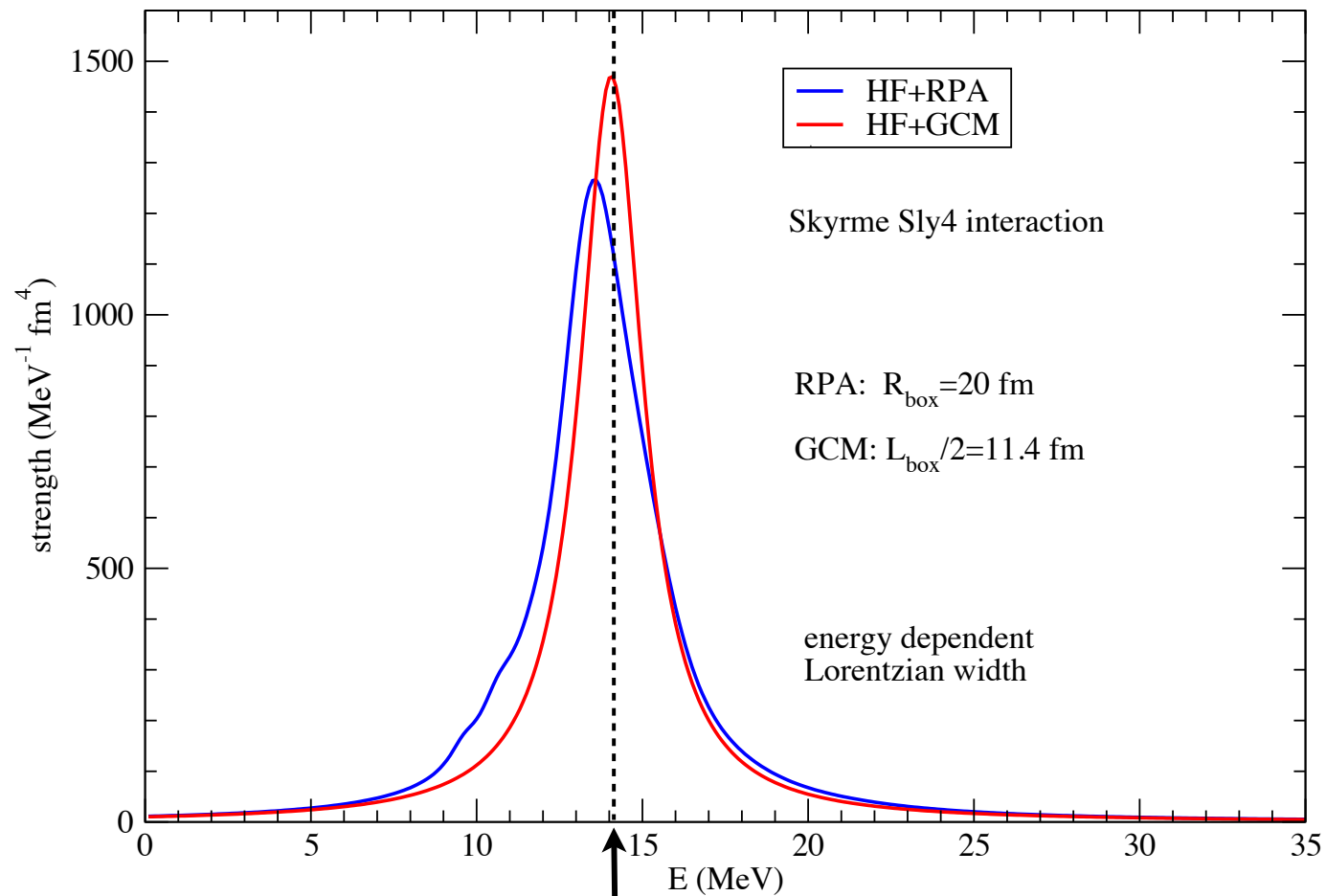
QRPA side:

sphHFB

QRPA (J. Terasaki)

Monopole response

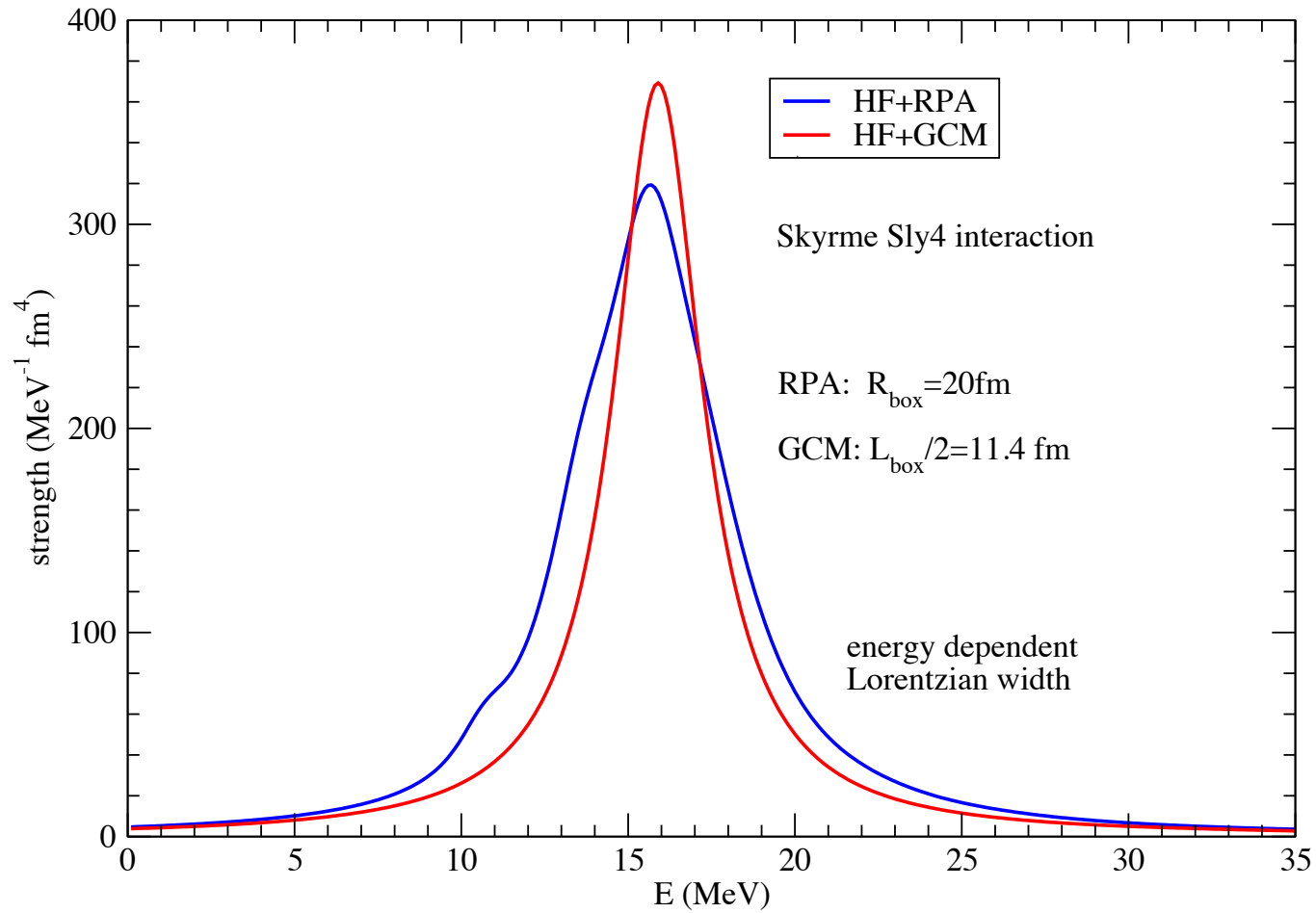
$^{208}\text{Pb}, J^\pi=0^+$ response



↑
experimental $m_1/m_0 = 14.18 \pm 0.11$ MeV
(Youngblood et al, PRL82 (1999))

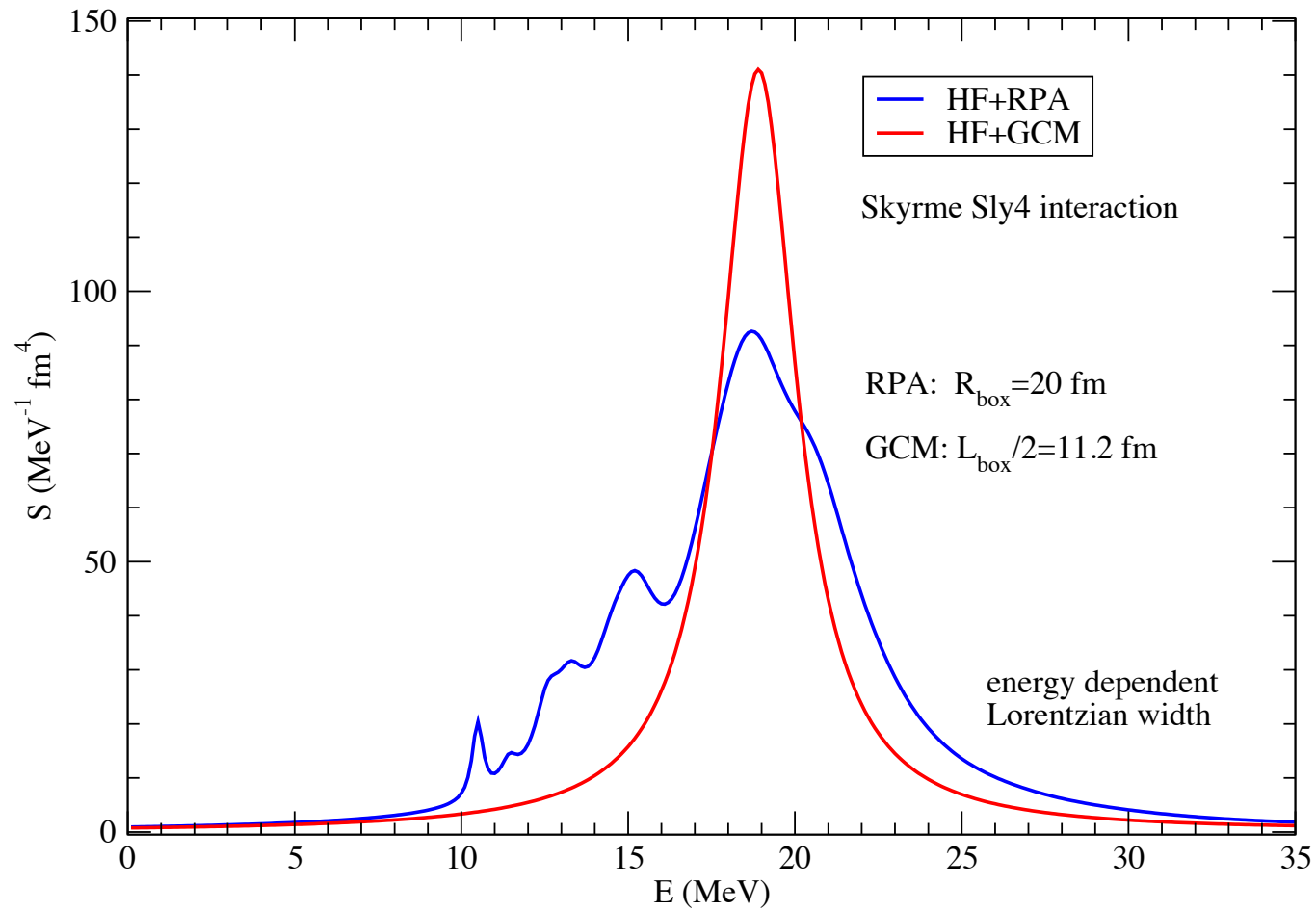
Monopole response

$^{132}\text{Sn}, J^\pi=0^+$ response

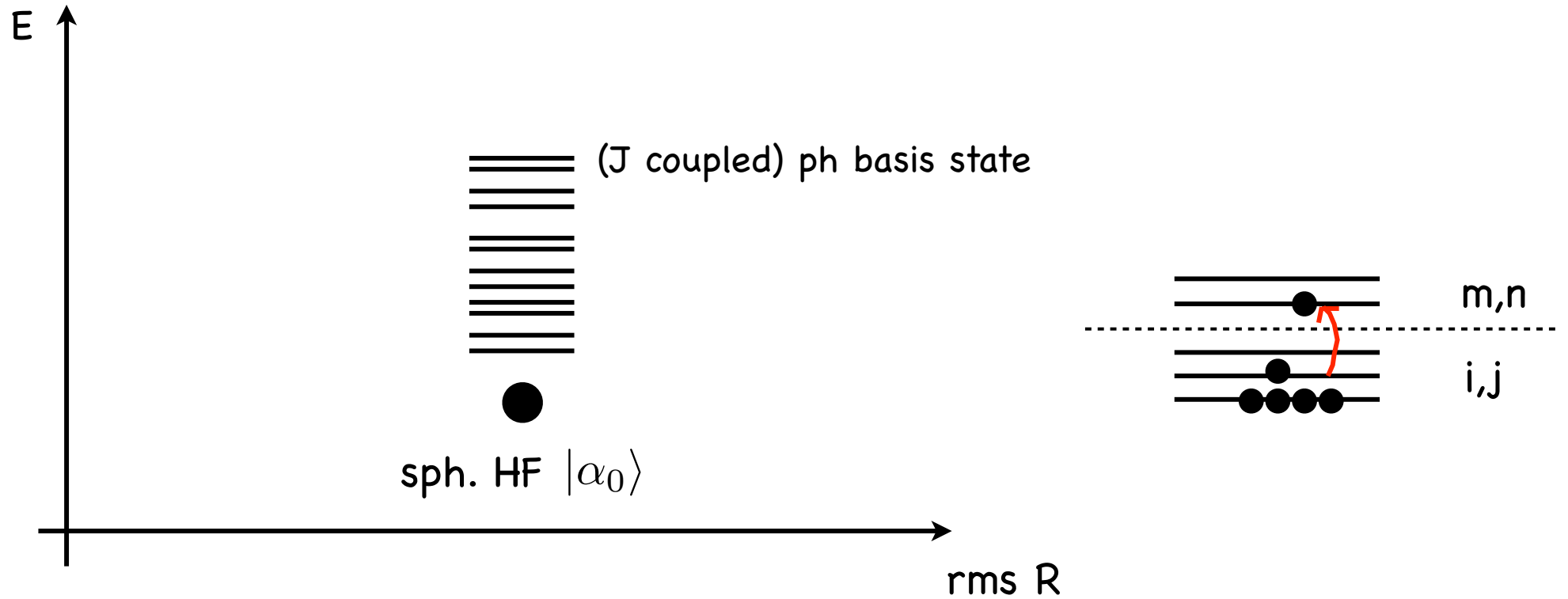


Monopole response

$^{68}\text{Ni}, J^\pi=0^+$ response



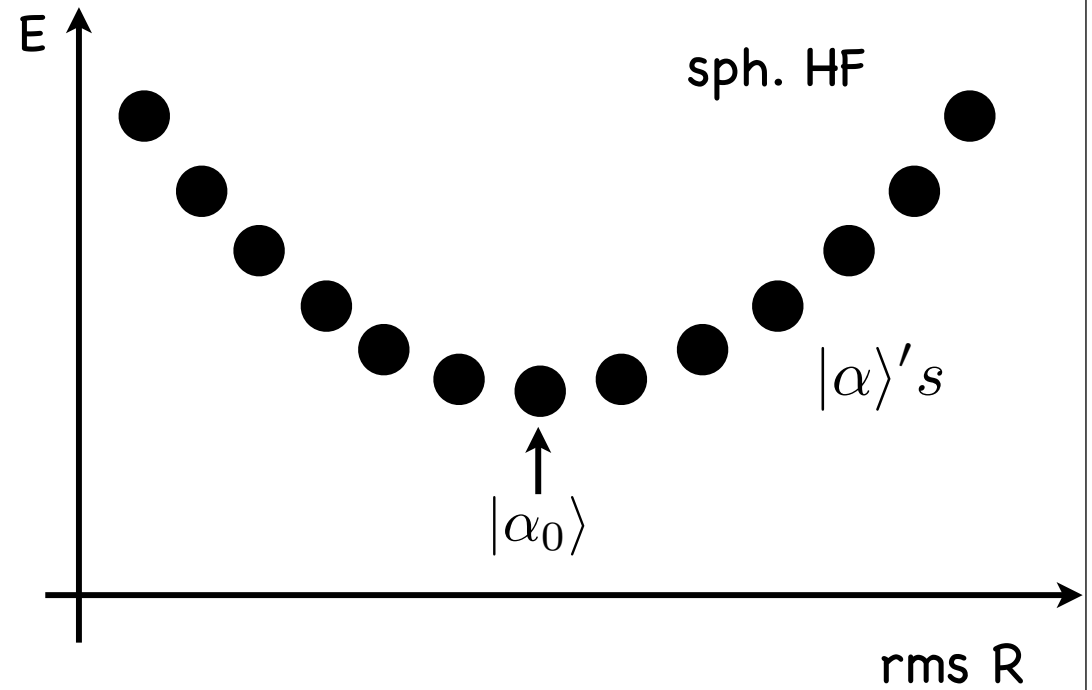
Single reference (RPA) vs. Multi reference (GCM)



$$|RPA(k)\rangle = \sum_{mi} \left(X_{mi}^k (a_m^\dagger a_i)^{J^\pi} - Y_{mi}^k (a_i^\dagger a_m)^{J^\pi} \right) |RPA_{gs}\rangle$$

Single reference (RPA) vs. Multi reference (GCM)

$$|GCM(k)\rangle = \sum_{\alpha} f_{k\alpha} |\alpha\rangle$$



Single reference (RPA) vs. Multi reference (GCM)

$$|GCM(k)\rangle = \sum_{\alpha} f_{k\alpha} |\alpha\rangle$$

$$|\alpha_0\rangle = \prod_{i=1}^A a_i^{\dagger} |0\rangle$$

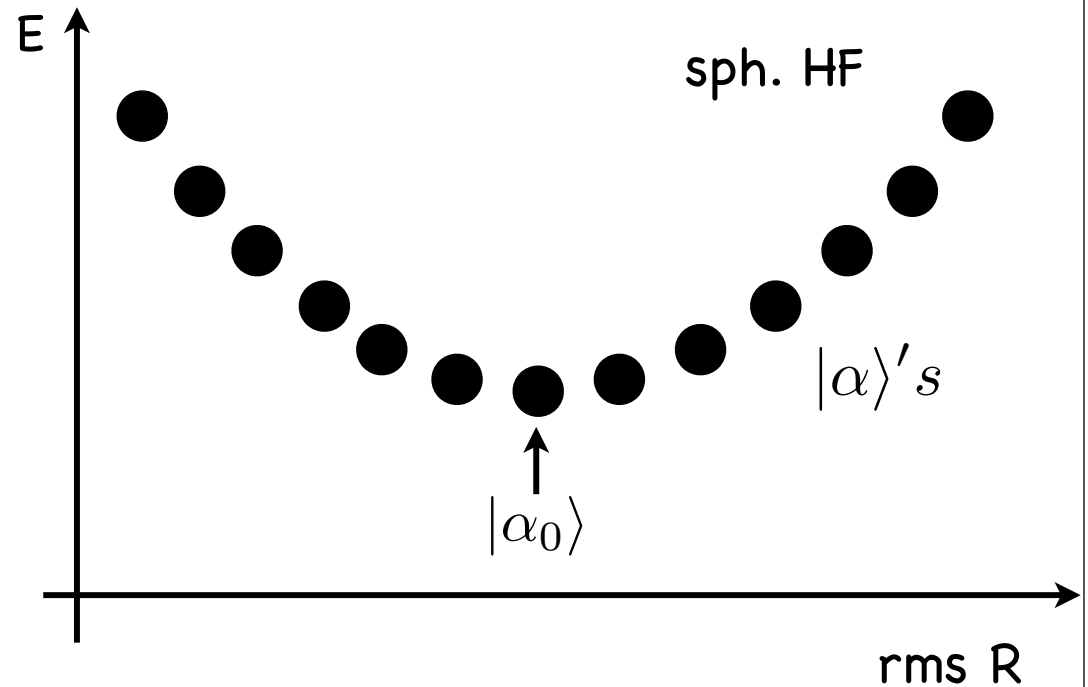
$$|\alpha\rangle = \prod_{i=1}^A \prod_{m=A+1}^{\infty} (1 + C_{mi}^{\alpha} a_m^{\dagger} a_i) |\alpha_0\rangle$$

$$= |\alpha_0\rangle + \sum_{mi} C_{mi}^{\alpha} a_m^{\dagger} a_i |\alpha_0\rangle + \sum_{mi} \sum_{m'i'} C_{mi}^{\alpha} C_{m'i'}^{\alpha} a_m^{\dagger} a_i a_{m'}^{\dagger} a_{i'} |\alpha_0\rangle + \dots$$

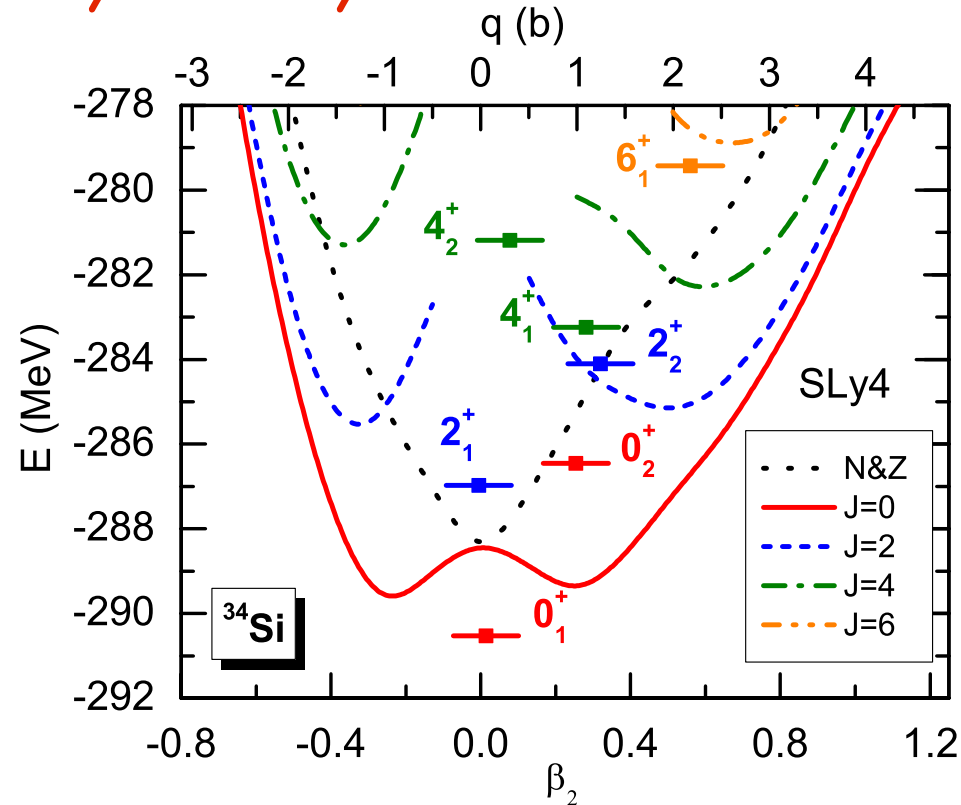
(Thouless, NP21 (1960) 225)

$$|GCM(k)\rangle = \sum_{\alpha} f_{k\alpha} |\alpha_0\rangle + \sum_{mi} \left(\sum_{\alpha} f_{k\alpha} C_{mi}^{\alpha} \right) a_m^{\dagger} a_i |\alpha_0\rangle + \sum_{mi} \sum_{m'i'} \left(\sum_{\alpha} f_{k\alpha} C_{mi}^{\alpha} C_{m'i'}^{\alpha} \right) a_m^{\dagger} a_i a_{m'}^{\dagger} a_{i'} |\alpha_0\rangle + \dots$$

- both g.s. and excited states
- richer than RPA



Symmetry restoration in GCM



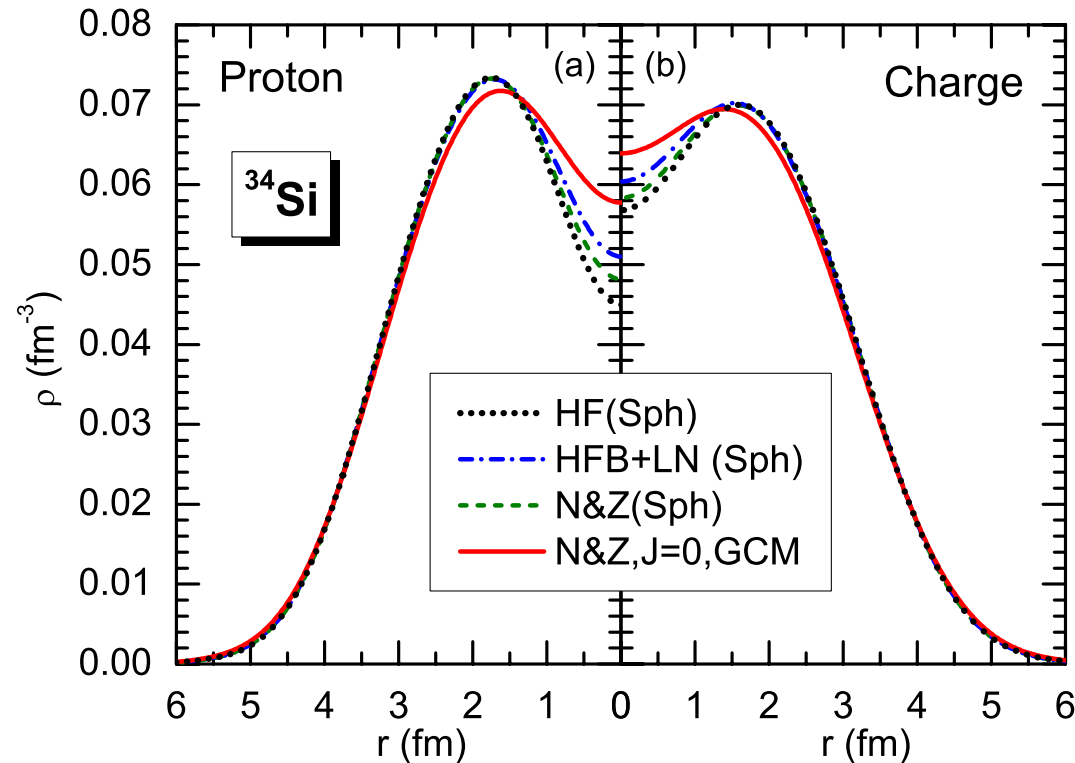
(J.-M. Yao, S. Baroni, M. Bender, P.-H. Heenen, arXiv:1205.2262)

q-constrained HFB : $|\alpha\rangle \equiv |q\rangle$

symmetry restoration : $|NZJMq\rangle = \frac{\hat{P}_{M0}^J \hat{P}_N \hat{P}_Z |q\rangle}{\sqrt{\langle q | \hat{P}_{00}^J \hat{P}_N \hat{P}_Z | q \rangle}}$

configuration mixing : $|GCM^{NZJM}(k)\rangle = \sum_q f_{kq}^J |NZJMq\rangle$

Ground-state properties in GCM

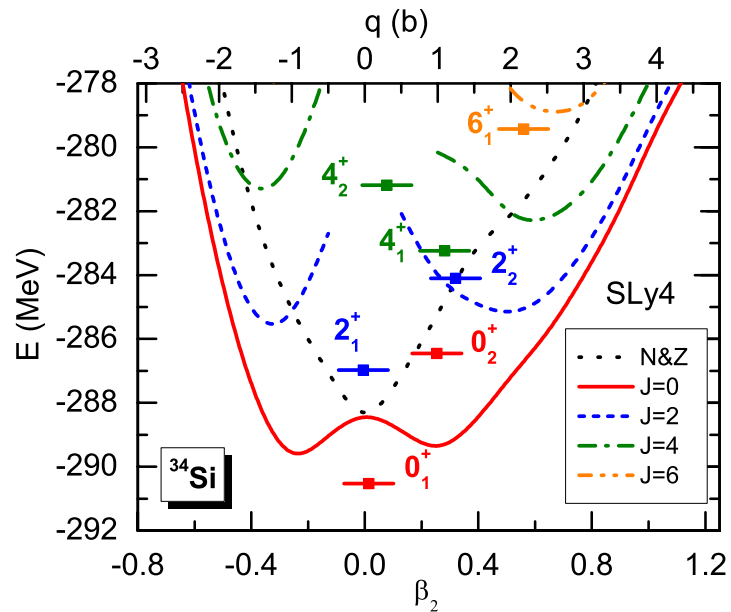


Bubble nuclei?
There's no such
a thing!

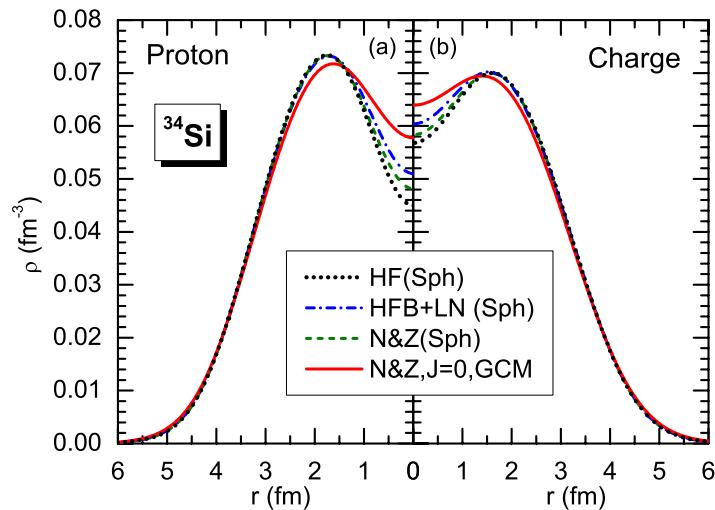
(J.-M. Yao, S. Baroni, M. Bender, P.-H. Heenen, arXiv:1205.2262)

- ground-state correlations accessible
- effect of pairing, deformation, symmetry restoration on gs properties

GCM and RPA

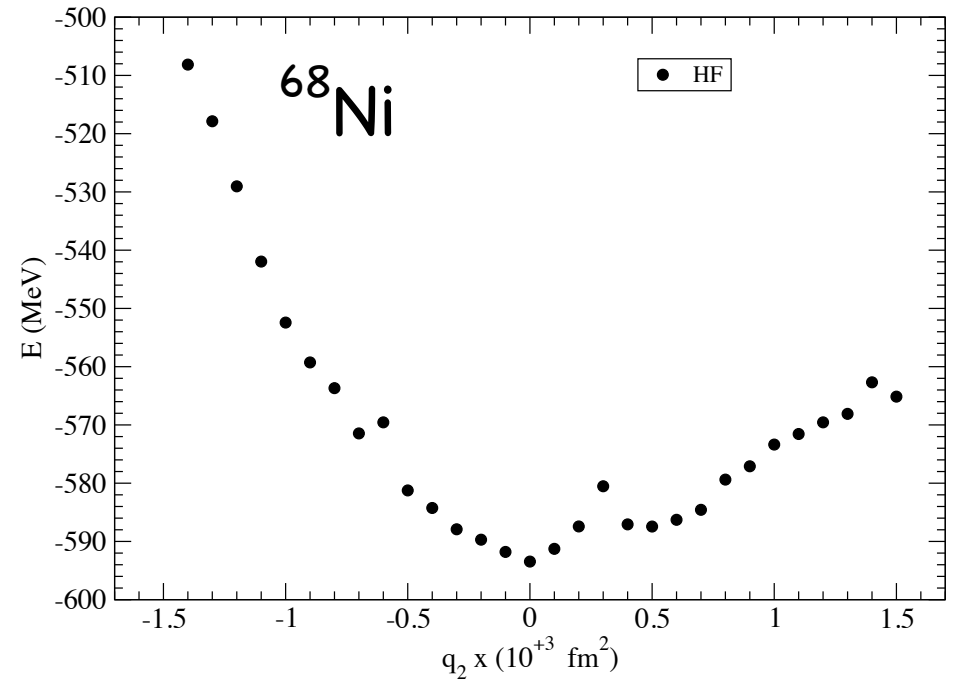
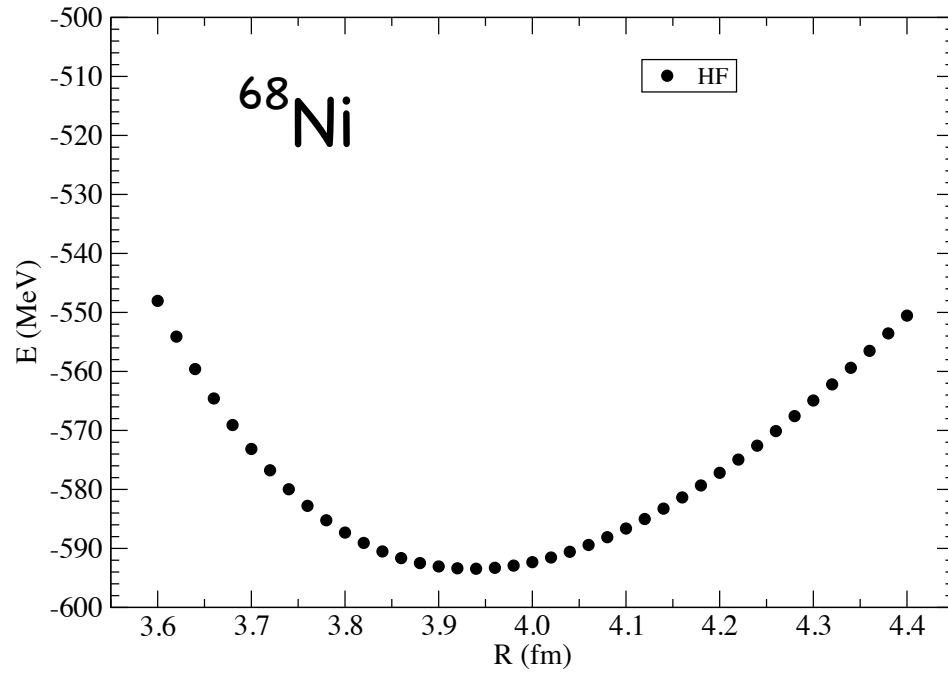


- Symmetry-restored GCM states
- RPA gives g.s. correlation energies separately for each mode, w/o coupling them

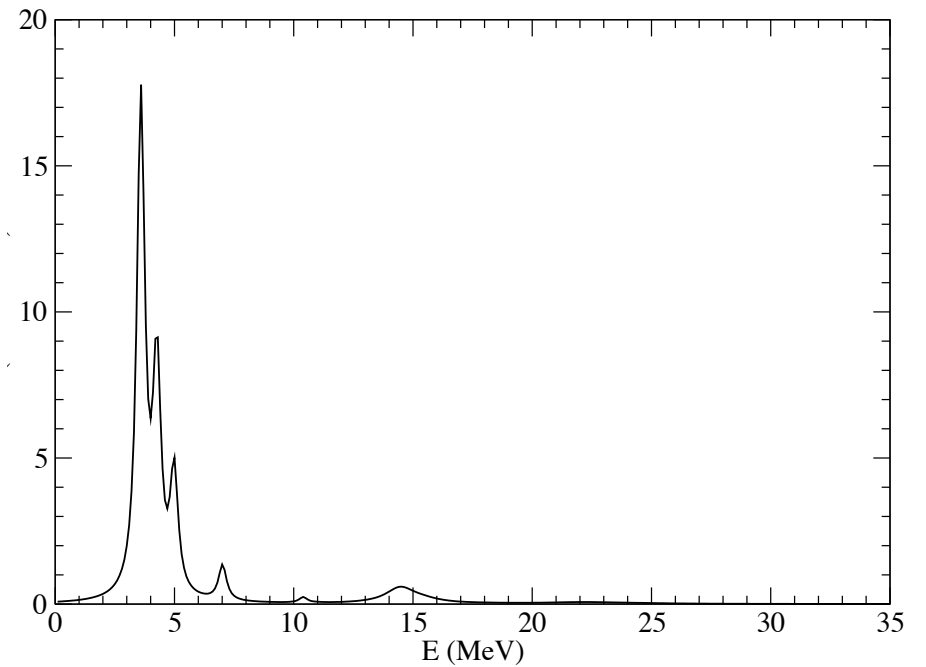
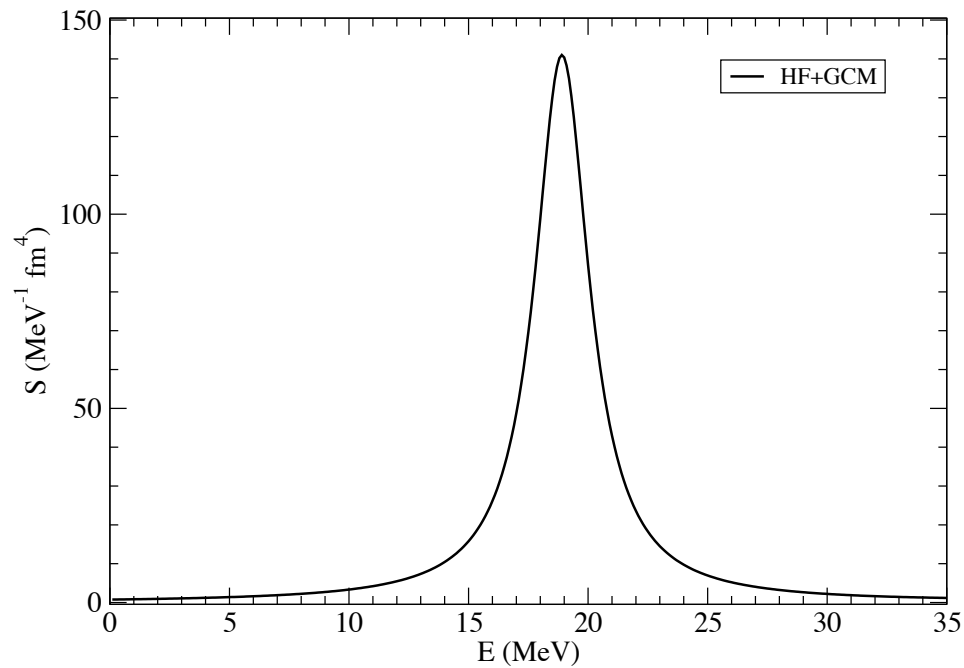
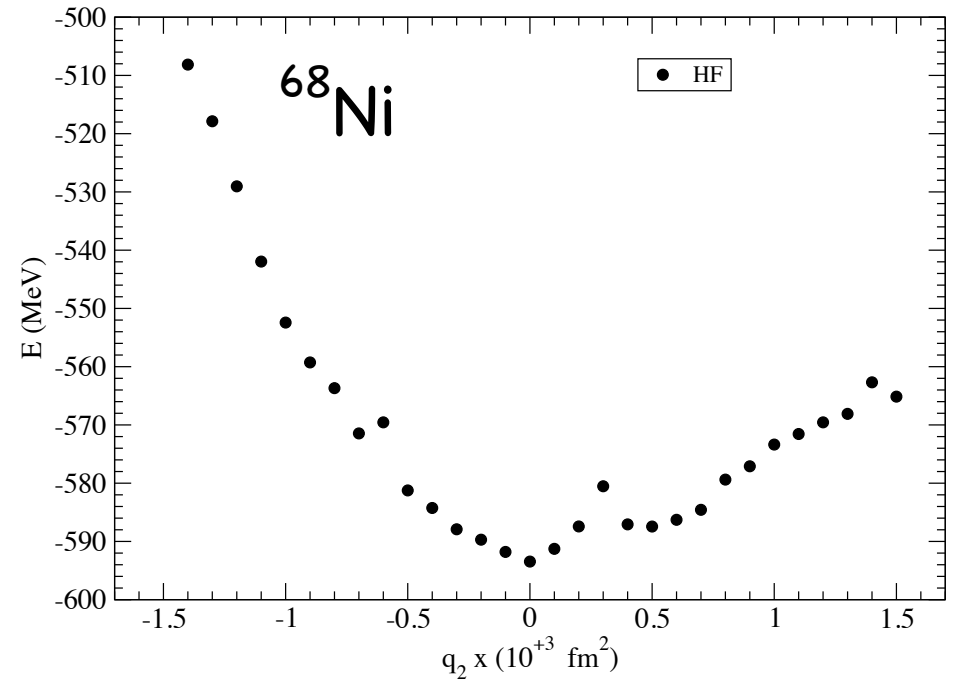
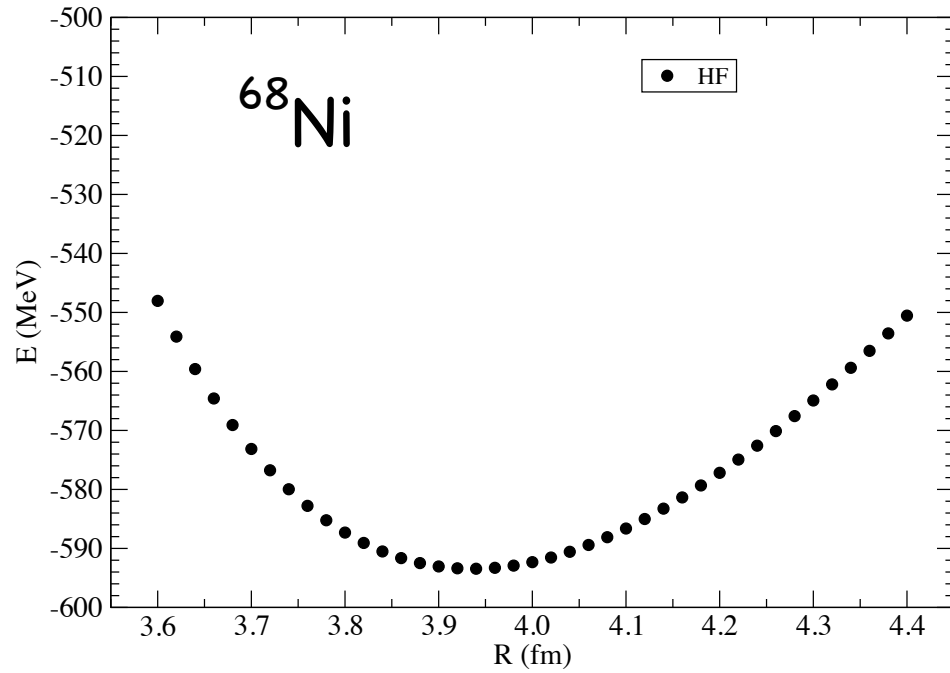


- g.s. correlations accessible in GCM
- GCM can handle shape mixing
- proper pairing treatment beyond mean field

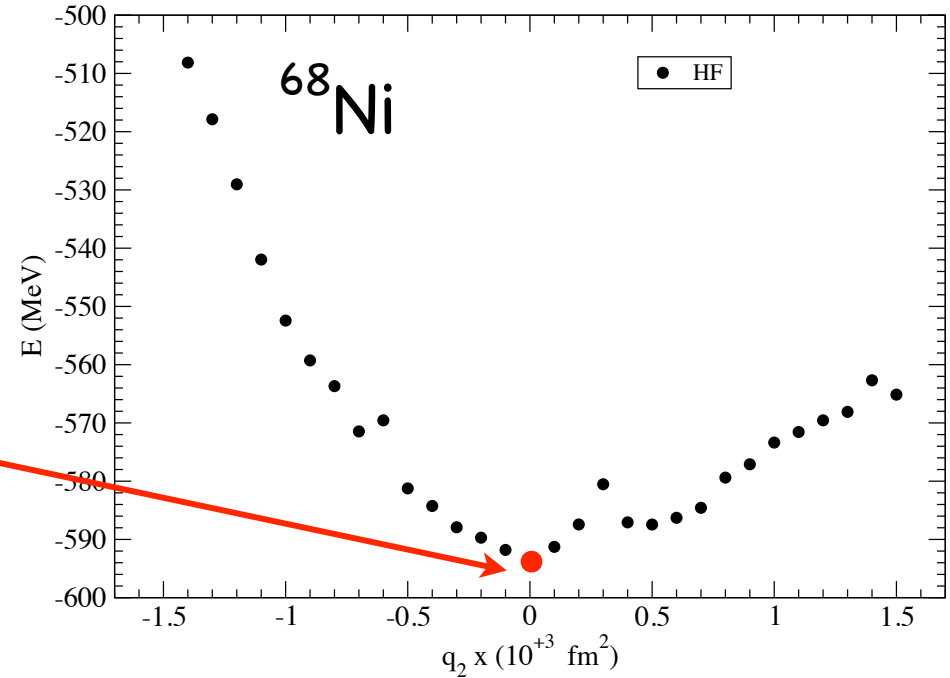
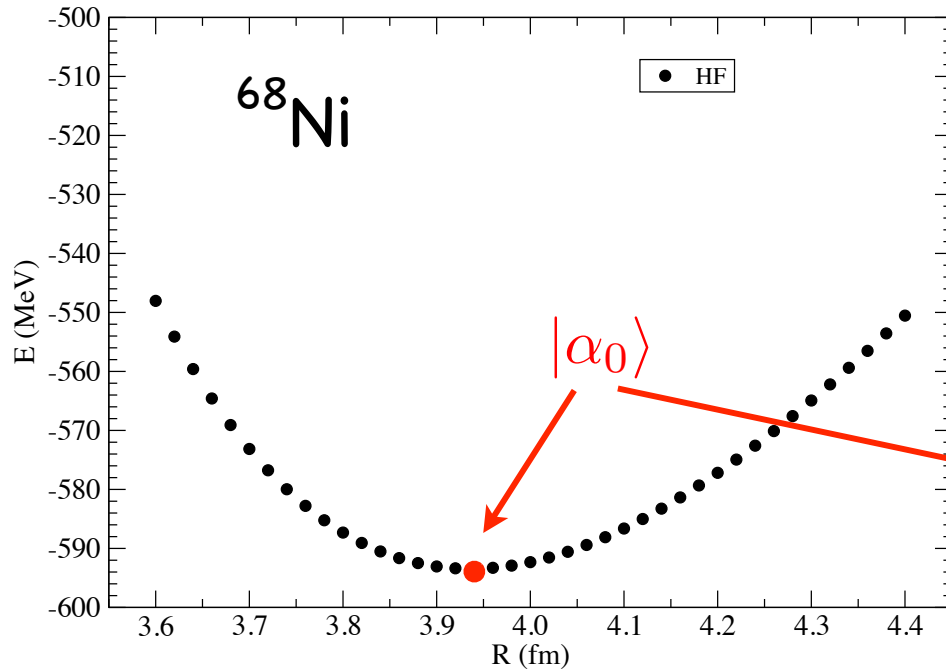
The choice of the generator coordinate



The choice of the generator coordinate

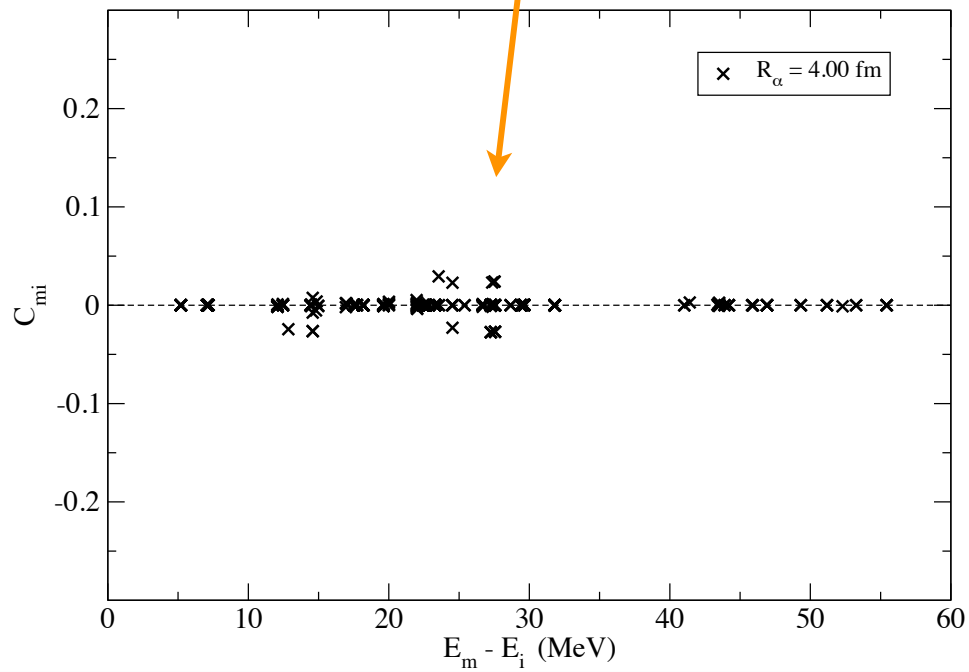
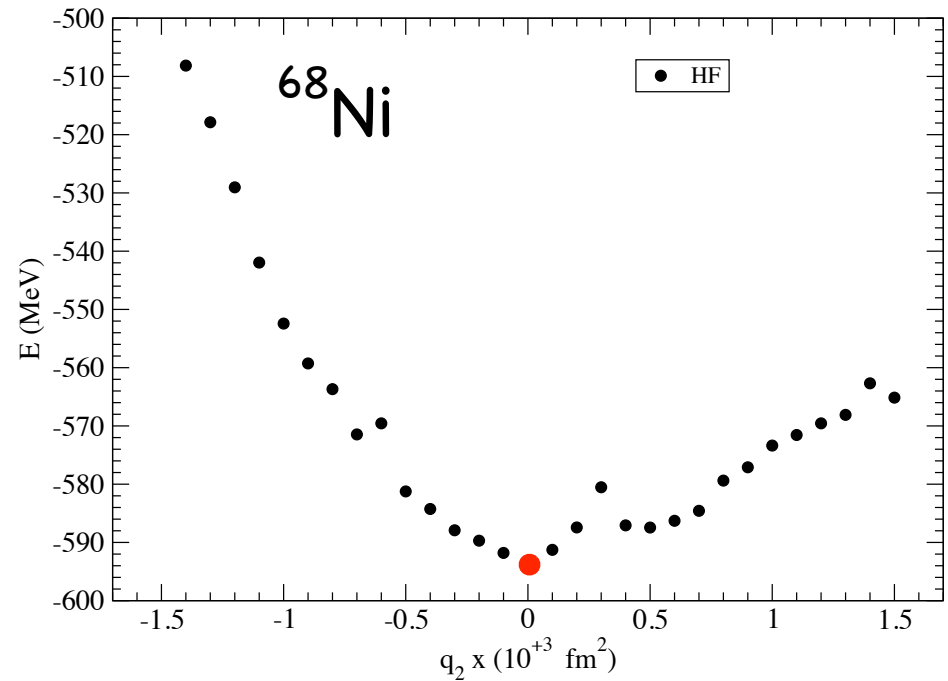
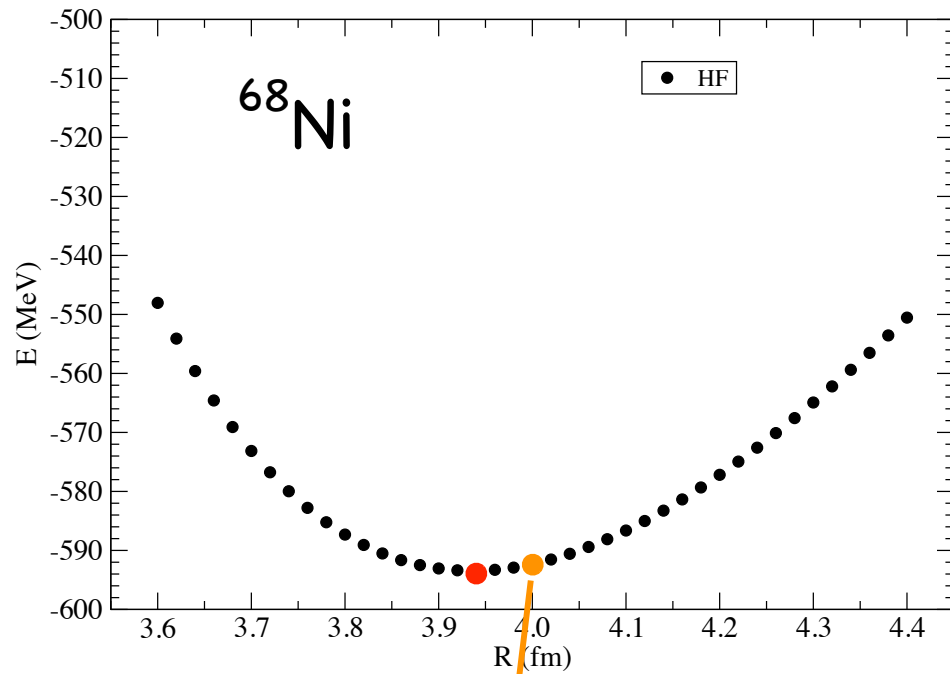


The choice of the generator coordinate

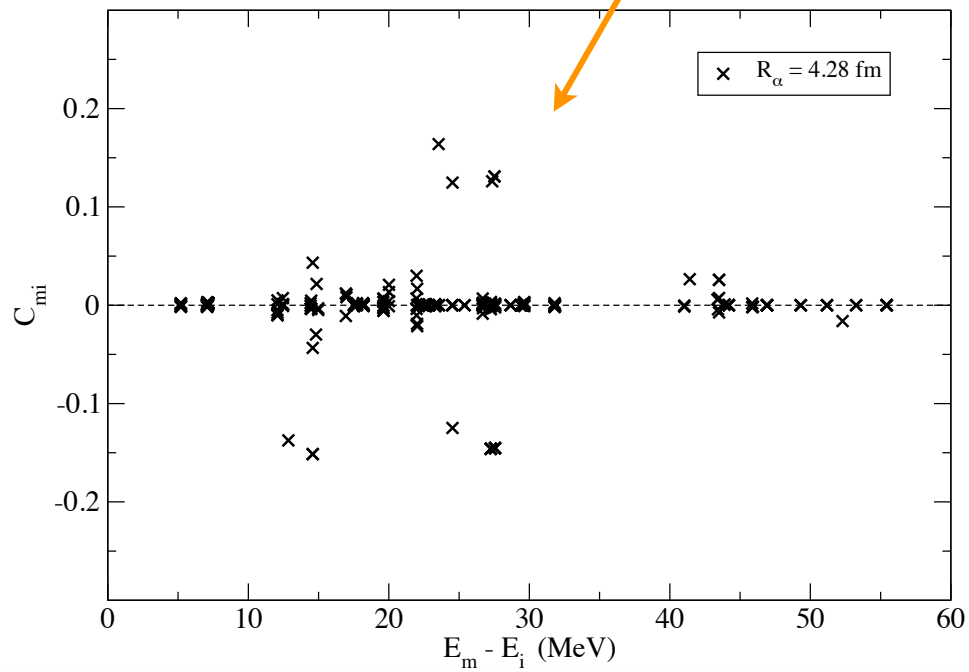
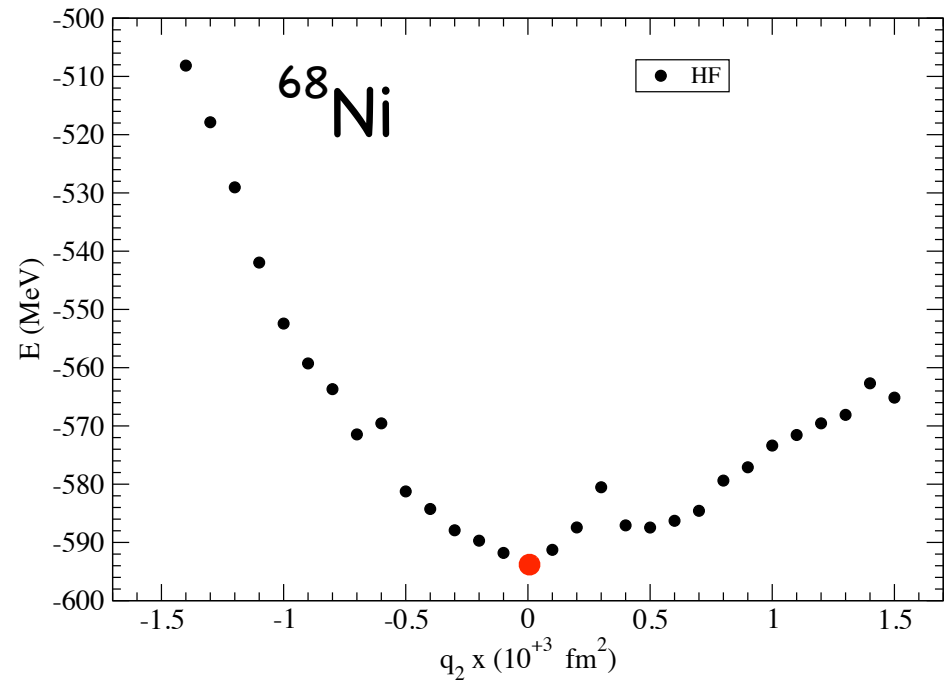
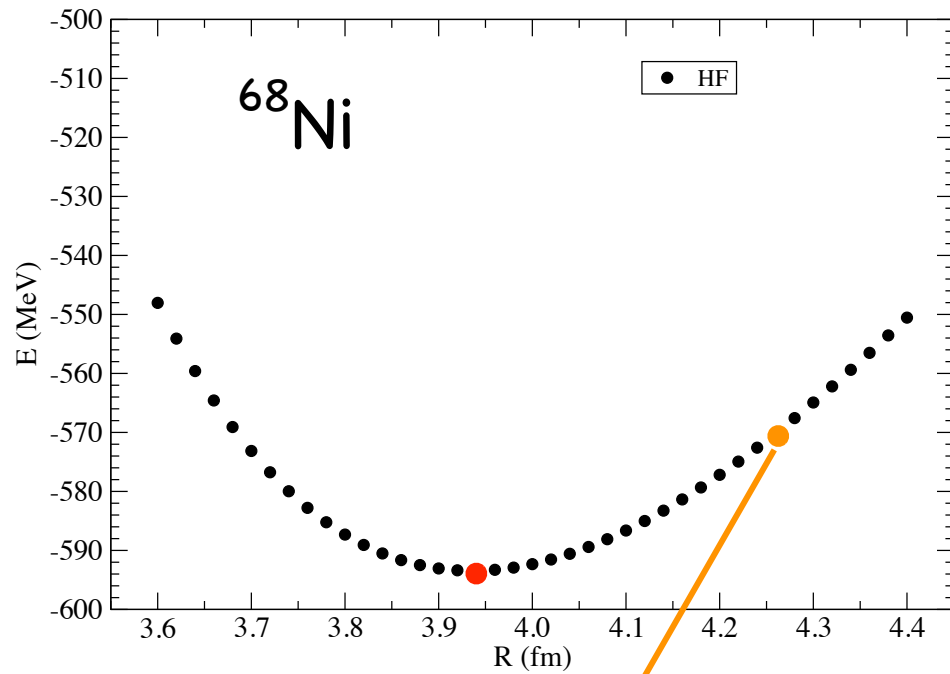


$$\begin{aligned}
 |\alpha\rangle &= \prod_{i=1}^A \prod_{m=A+1}^{\infty} (1 + C_{mi}^{\alpha} a_m^{\dagger} a_i) |\alpha_0\rangle \\
 &= |\alpha_0\rangle + \sum_{mi} C_{mi}^{\alpha} a_m^{\dagger} a_i |\alpha_0\rangle + \sum_{mi} \sum_{m'i'} C_{mi}^{\alpha} C_{m'i'}^{\alpha} a_m^{\dagger} a_i a_{m'}^{\dagger} a_{i'} |\alpha_0\rangle + \dots
 \end{aligned}$$

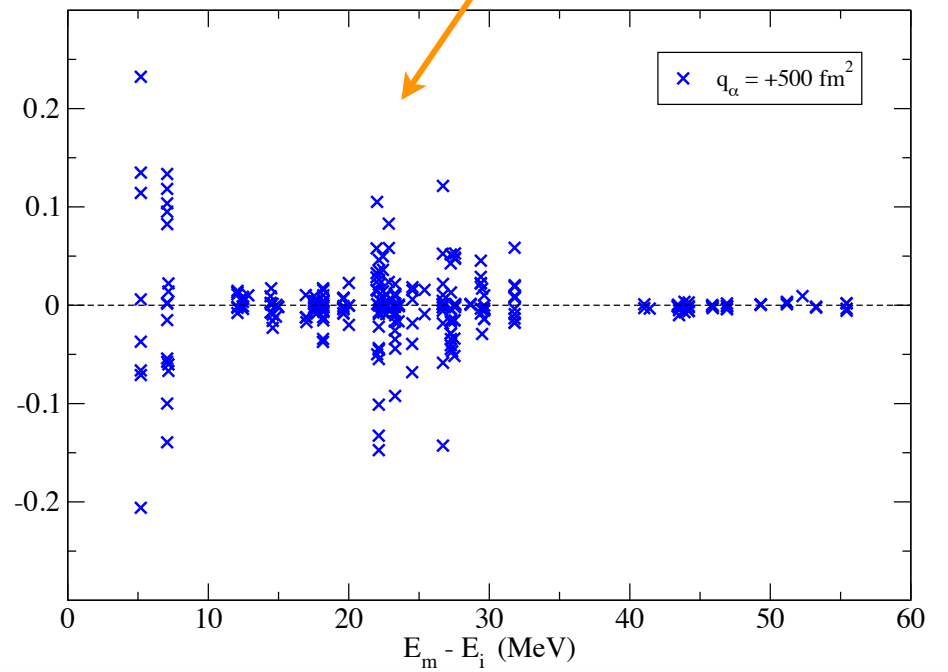
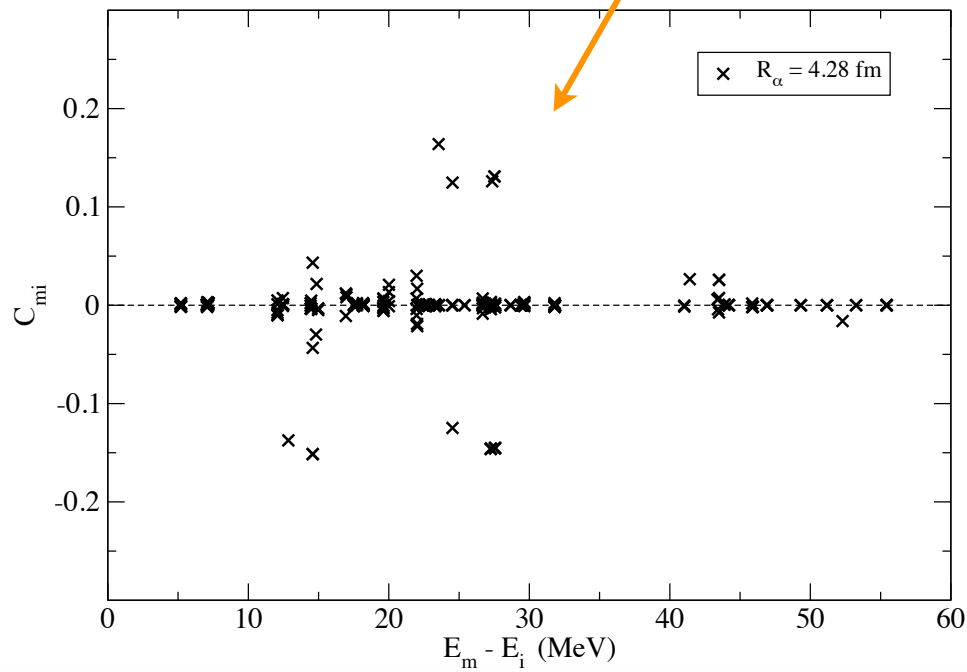
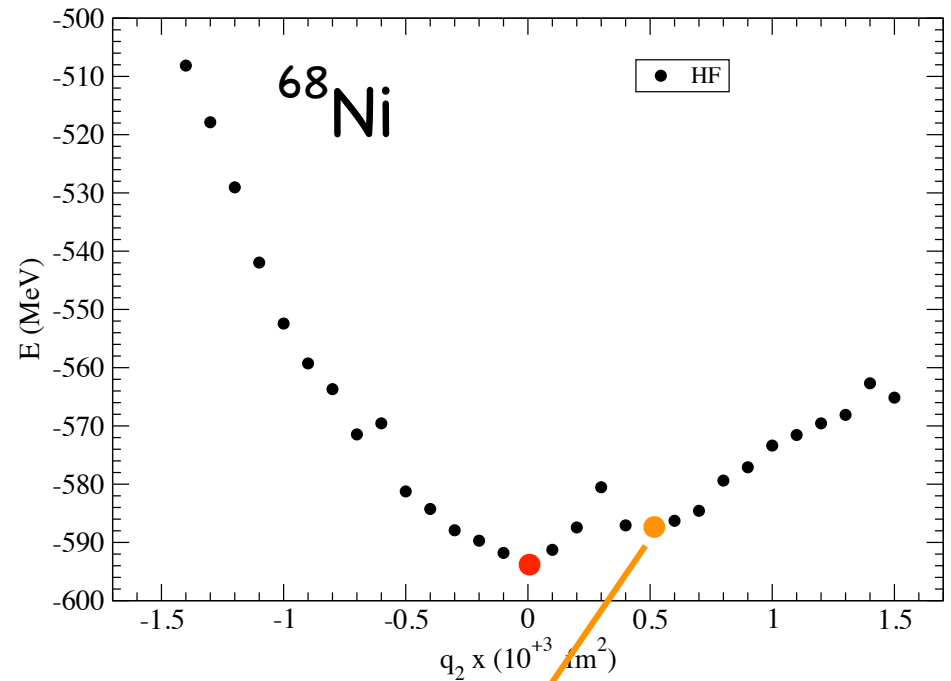
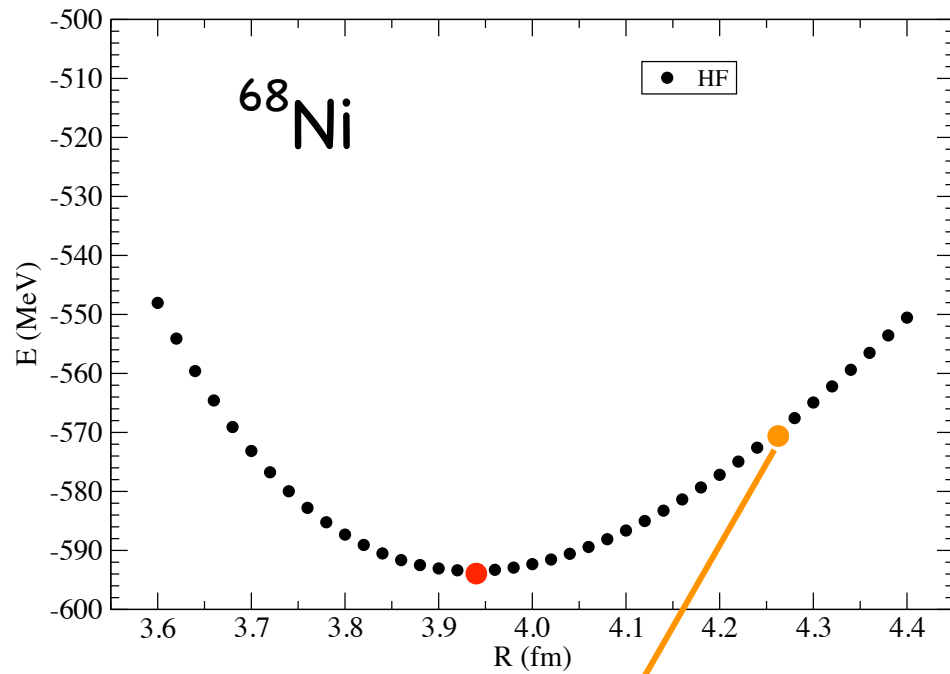
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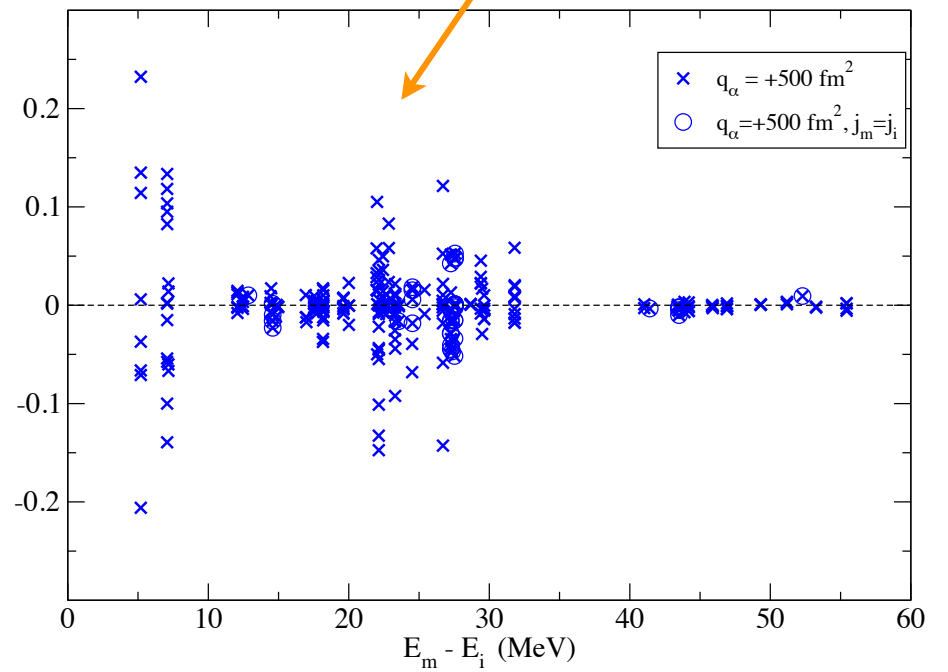
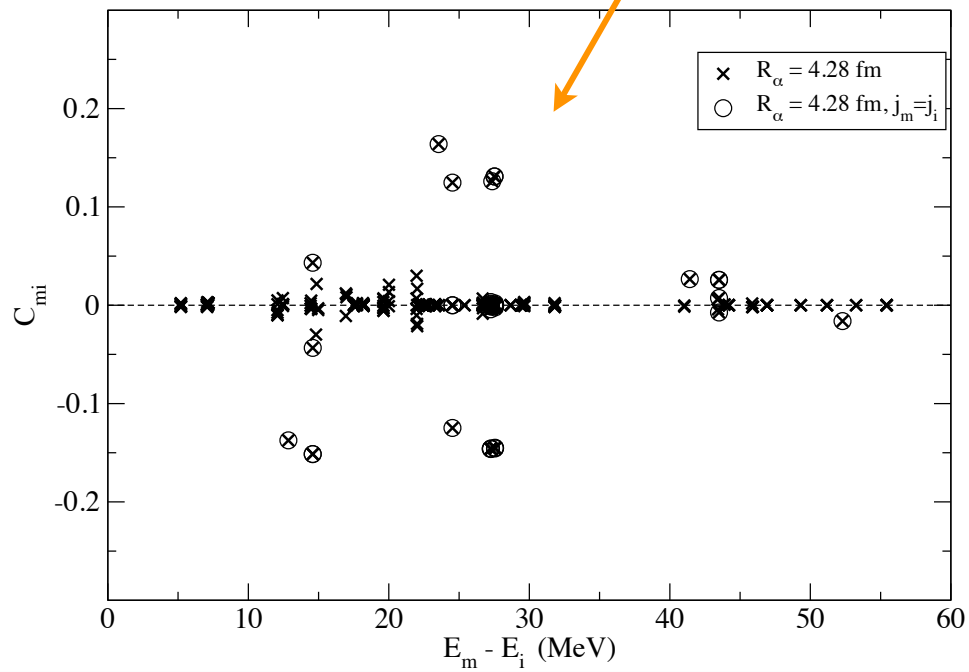
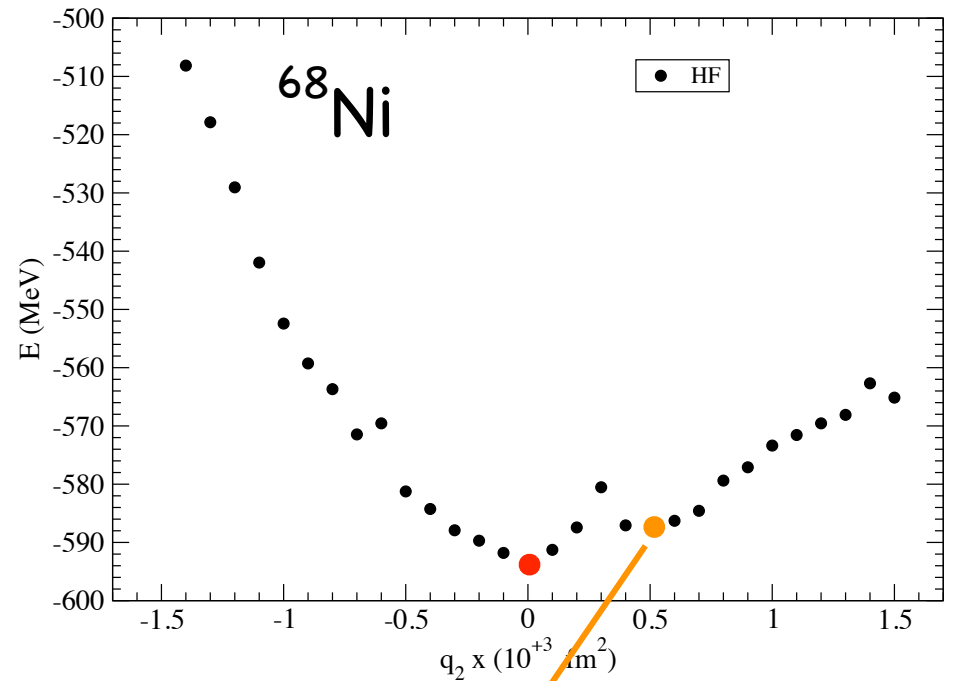
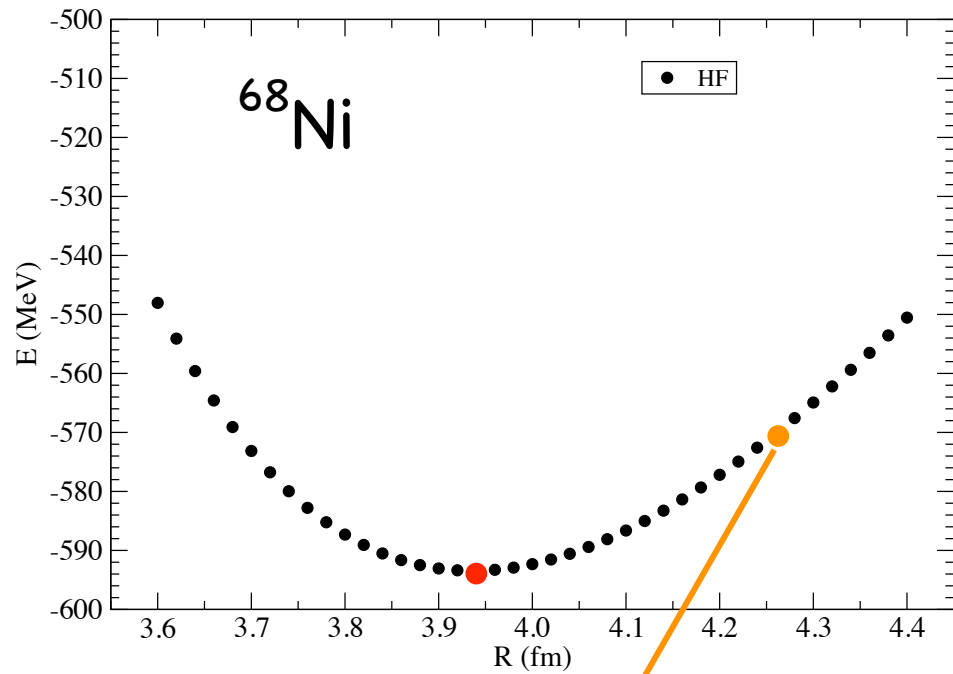
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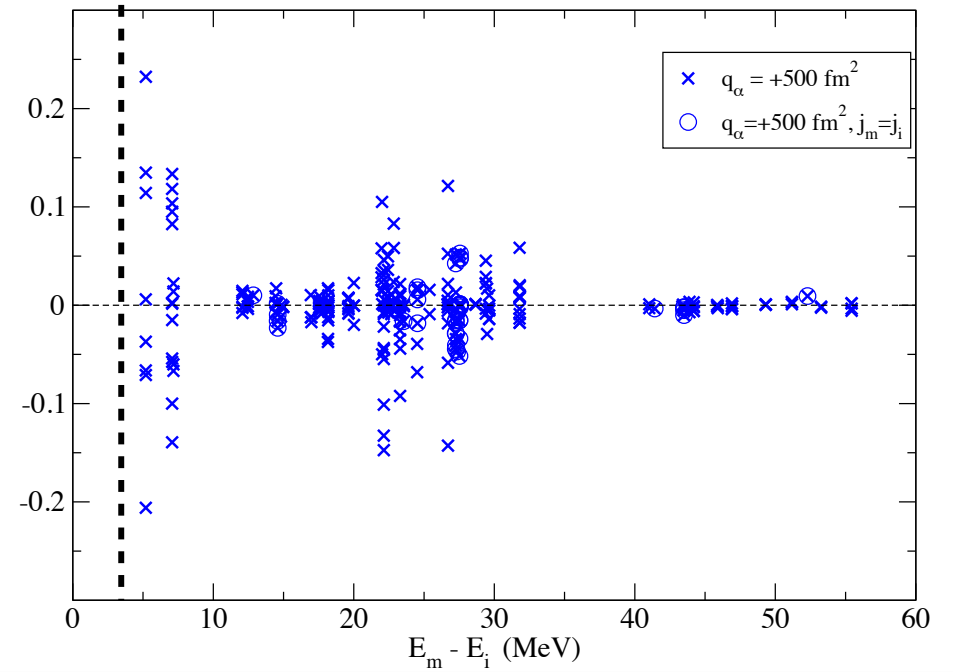
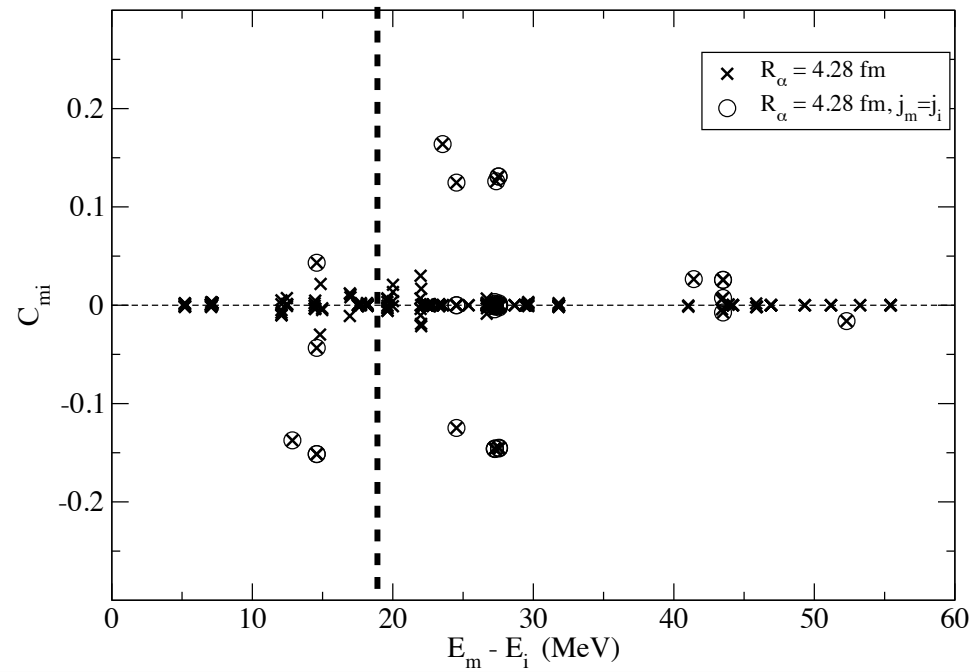
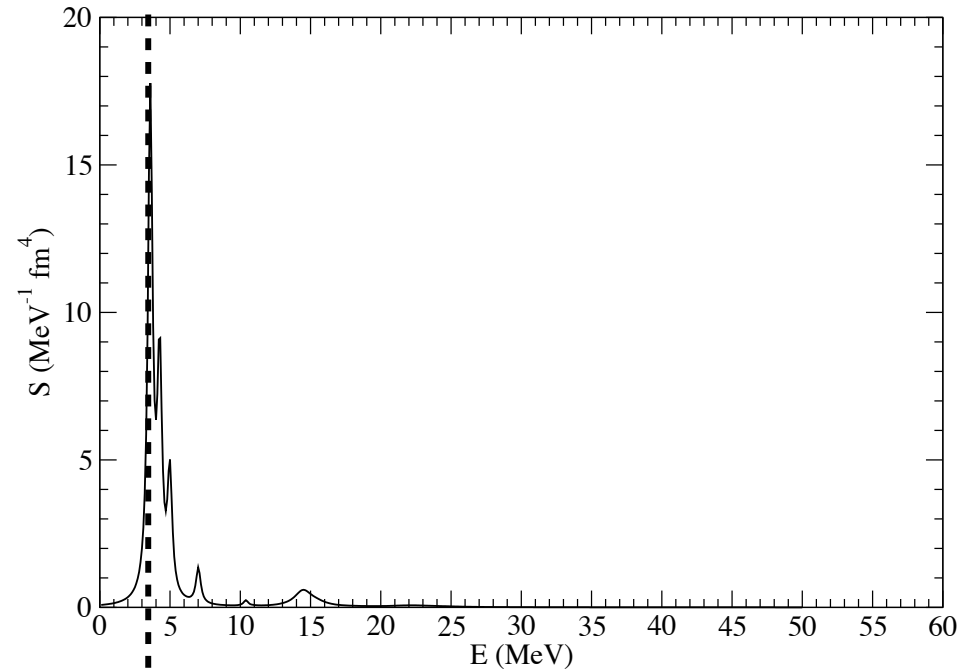
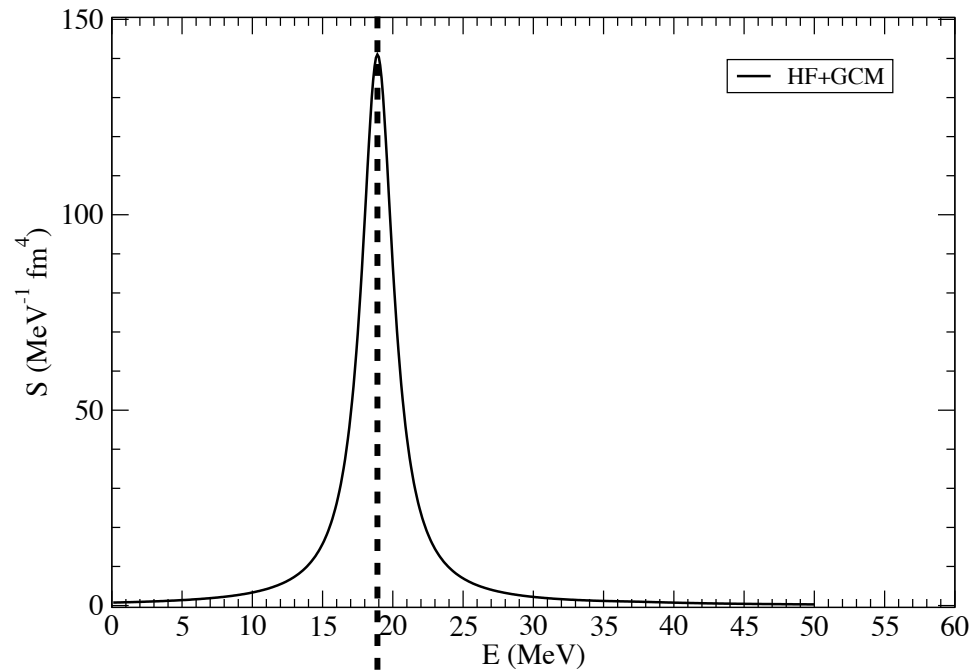
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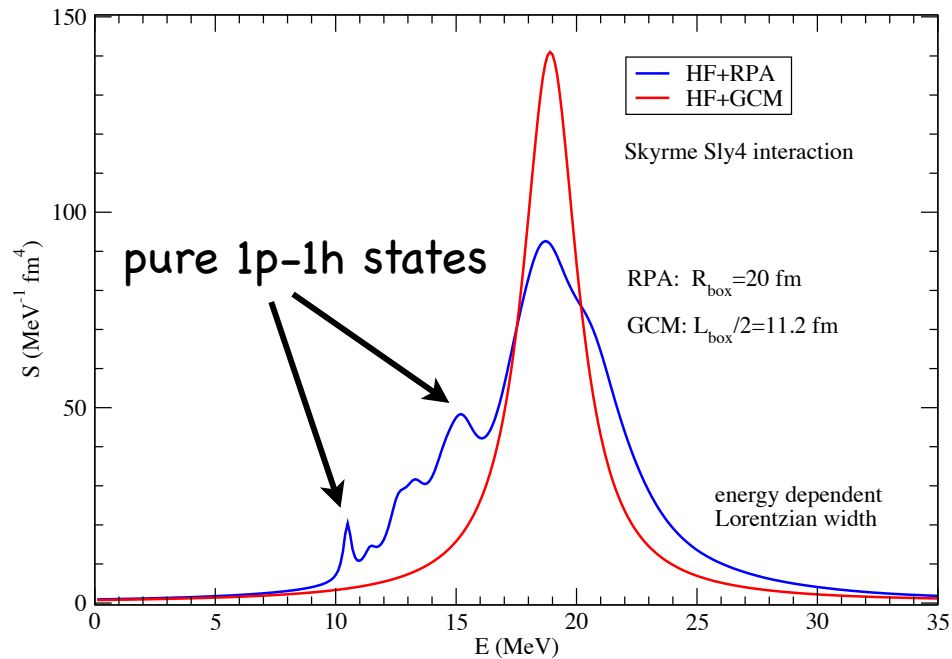
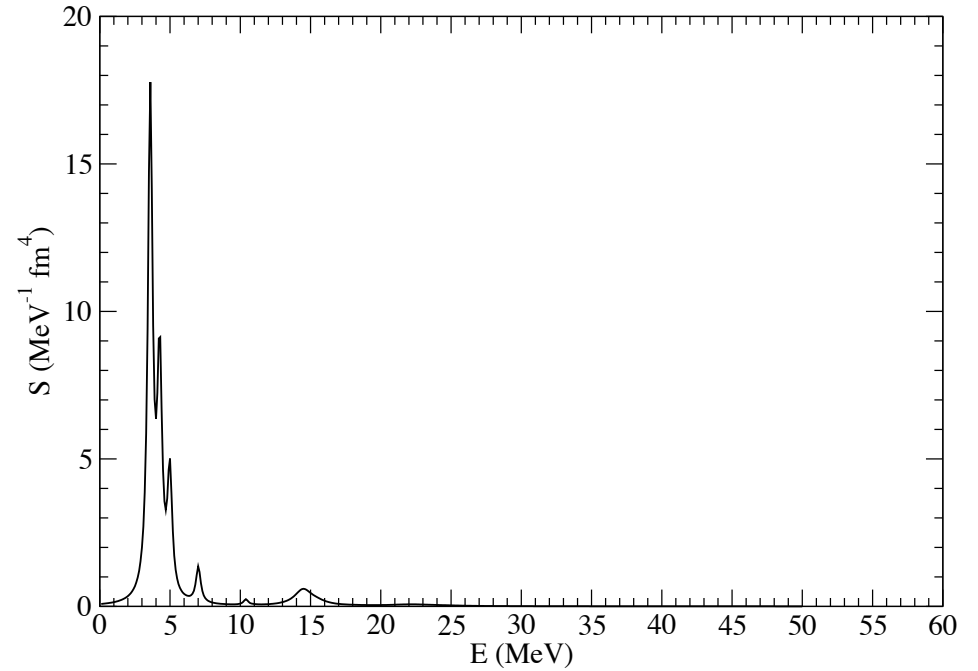
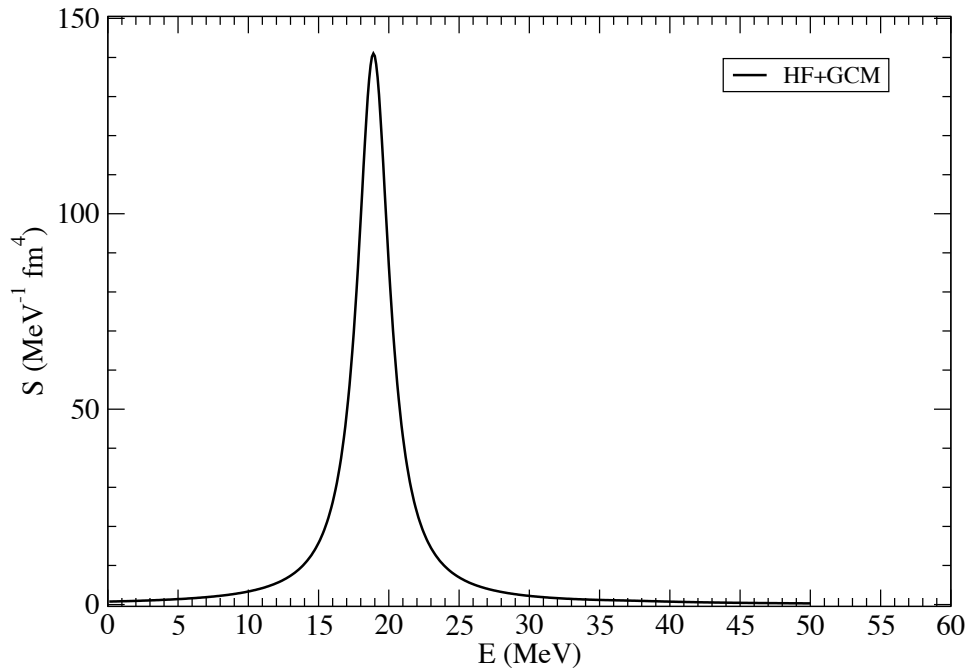
The choice of the generator coordinate



The choice of the generator coordinate



The choice of the generator coordinate



- RPA does not need to couple different $J=0$ responses
- one generator coordinate seems to capture almost all physics in GCM
- RPA can handle non-collective states

A link between GCM and RPA

$$|RPA(k)\rangle = \sum_{mi} \left(X_{mi}^k (a_m^\dagger a_i)^{J^\pi} - Y_{mi}^k (a_i^\dagger a_m)^{J^\pi} \right) |RPA_{gs}\rangle$$

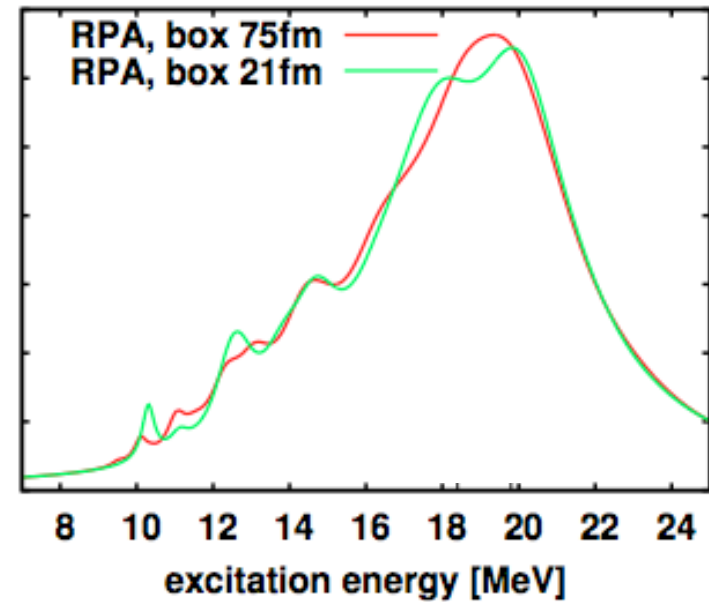
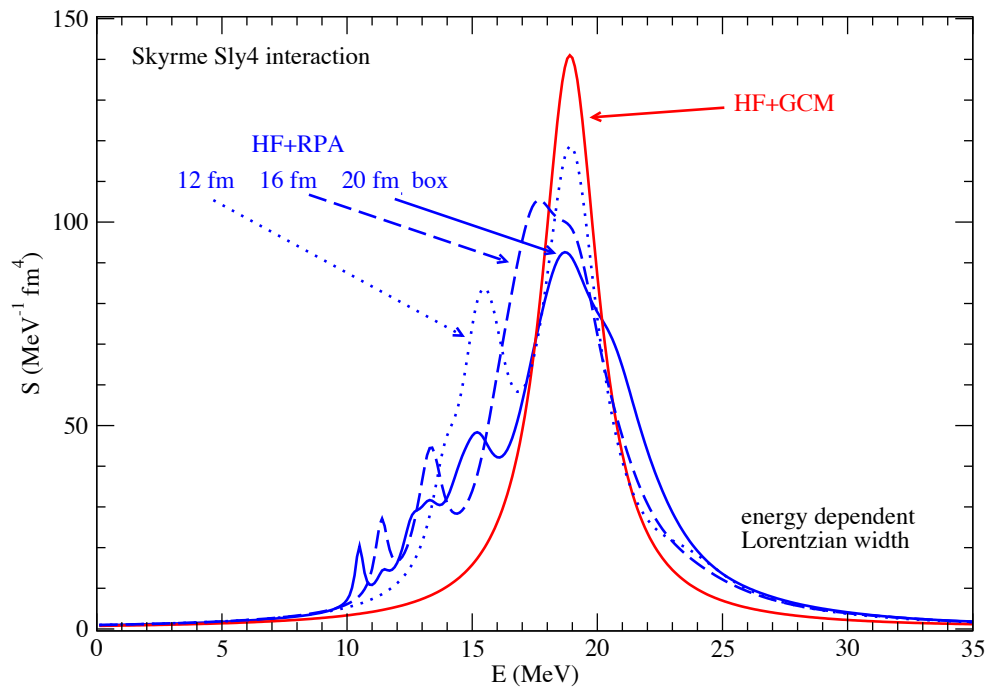
$$\begin{aligned} |GCM(k)\rangle &= \sum_{\alpha} f_{k\alpha} |\alpha_0\rangle + \sum_{mi} \left(\sum_{\alpha} f_{k\alpha} C_{mi}^{\alpha} \right) a_m^\dagger a_i |\alpha_0\rangle \\ &+ \sum_{mi} \sum_{m'i'} \left(\sum_{\alpha} f_{k\alpha} C_{mi}^{\alpha} C_{m'i'}^{\alpha} \right) a_m^\dagger a_i a_{m'}^\dagger a_{i'} |\alpha_0\rangle + \dots \end{aligned}$$

$$|GCM(k)\rangle \approx \sum_{mi} \left(X_{mi}^k (a_m^\dagger a_i)^{J^\pi} - Y_{mi}^k (a_i^\dagger a_m)^{J^\pi} \right) |GCM_{gs}\rangle$$

- how big are correlations beyond 1p-1h in GCM?

The continuum

$^{68}\text{Ni}, J^\pi=0^+$ response



P.-G. Reinhard, private comm.

- GCM does not need an explicit treatment of the continuum
- RPA needs states at $E>0 \implies$ box dependence

Other pros and cons of GCM

- GCM can study large- A deformed systems with no extra effort

- GCM has problems with light nuclei ($A < 60$?)
requires regularizable functionals
requires forces
- GCM calculations take longer than RPA (spherical case)
- pp and hh excitations?
pairing vibrations?
ex: ^{208}Pb 0^+ state at about 4MeV
 ^{68}Ni 0^+ state at 1.8 MeV