

How transparent is nuclear matter ?

(from an experimental point of view)

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Outlines

- Multiplicities
- Event shapes « central » events
- Isospin equilibria
- Isospin dependence of spectra
- Isotropy ratio (energy) and experimental determinations of λ_{NN} and σ_{NN}
- *Other probes...*

Caution : work in progress...

Motivations

- At low energy ($E \ll E_{\text{Fermi}}$), provide a link to **viscosity** and macroscopic (nuclear) degrees of freedom : **1-body dissipation** by the mean-field, nucleus-nucleus potential
- At high energy ($E \gg E_{\text{Fermi}}$), provide a link to microscopic (nucleonic) d.o.f and **in-medium NN cross section** : **2-body dissipation** by hard (elastic) NN collisions, NN interaction
- At intermediate energy ($E \approx E_{\text{Fermi}}$), exhibit the **crossover** between these 2 phenomena

Motivations (II)

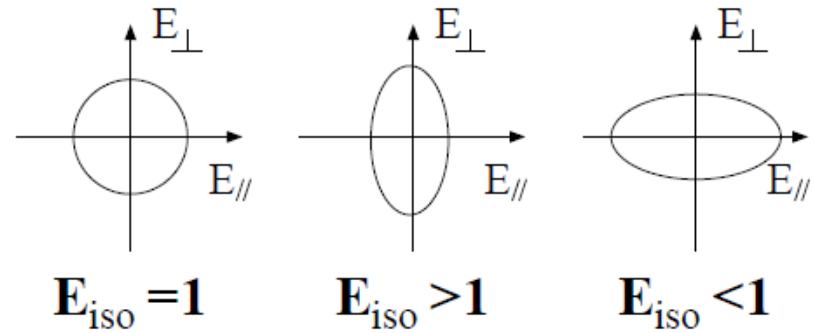
- In a « pure » nuclear physics context :
 - Variety of **reaction mechanisms** in nuclear reactions : fusion, deep inelastic, incomplete fusion
 - Variety of **deexcitation processes** : evaporation, fission, multifragmentation
 - **Transport properties** of nuclear matter : equilibrations (E, N/Z)
- In the astrophysical context :
 - **supernovae collapse** and formation of **neutron stars** (EOS)

Measuring the stopping : strategy

- Do **event selection** by using a minimum-bias observable , the **total multiplicity for light charged particle ($0 < Z < 3$)** : v_{tot}
- Avoid **trivial correlations** with the isotropy variables (R_E , E_{trans} , θ_{flow} , velocities, ...)
- Very **basic (simple) criterion** : applicable to all systems
- **Caution : selection of the most central events is not guaranteed (not an impact parameter selector...)**

Isotropy ratio

$$R_E = \frac{1}{2} \frac{\sum E_{\perp}}{\sum E_{\parallel}}$$



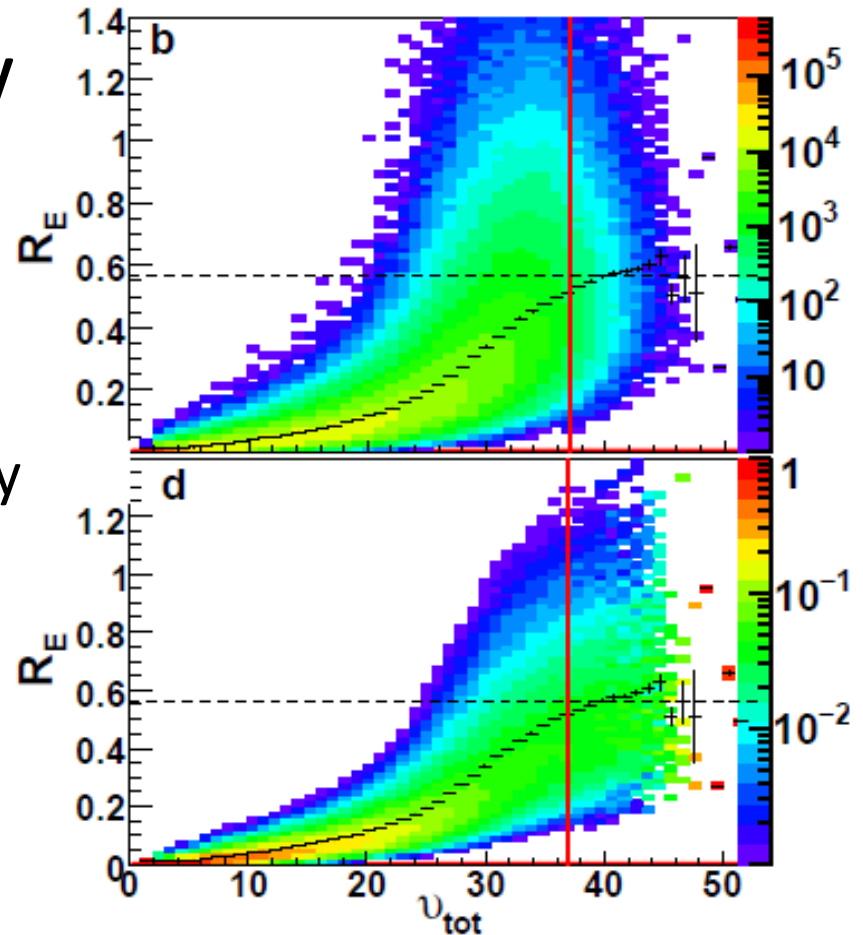
- Saturation of R_E at high multiplicity

- Define the maximal average R_E value

- Large fluctuations in R_E are partially due to statistics

- « Normalized » correlation to the same number of entries by bin of

V_{tot}



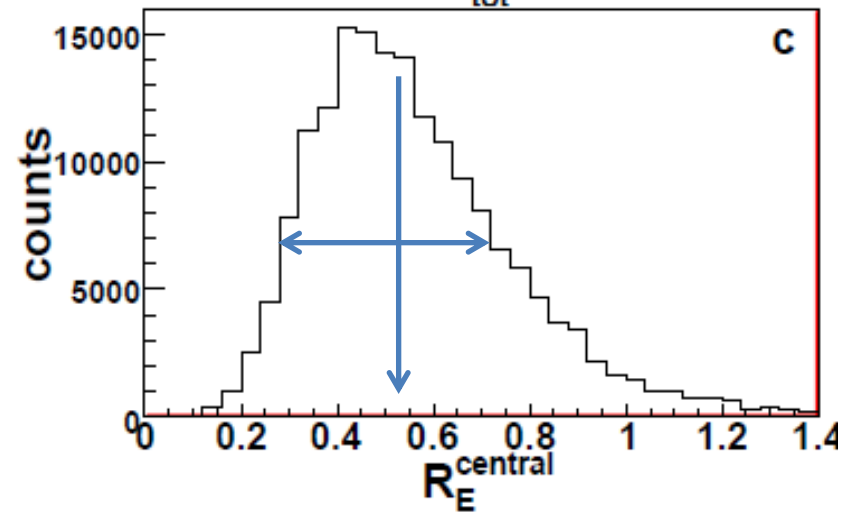
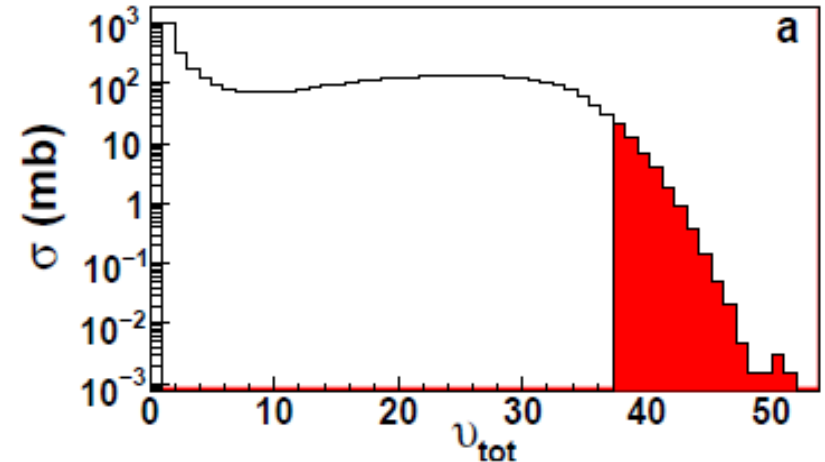
Event selection : most violent collisions selected by v_{tot}

- v_{tot} cut-off is defined by the observed saturation in $R_E \times v_{tot}$ correlation

- Applied to all INDRA symmetric systems

- Corresponds roughly to **50-100 mb** (detected) hence to $b/b_{max} \approx 0.1$

- R_E values are taken by reporting the **mean** and **FWHM** values of the selected distribution



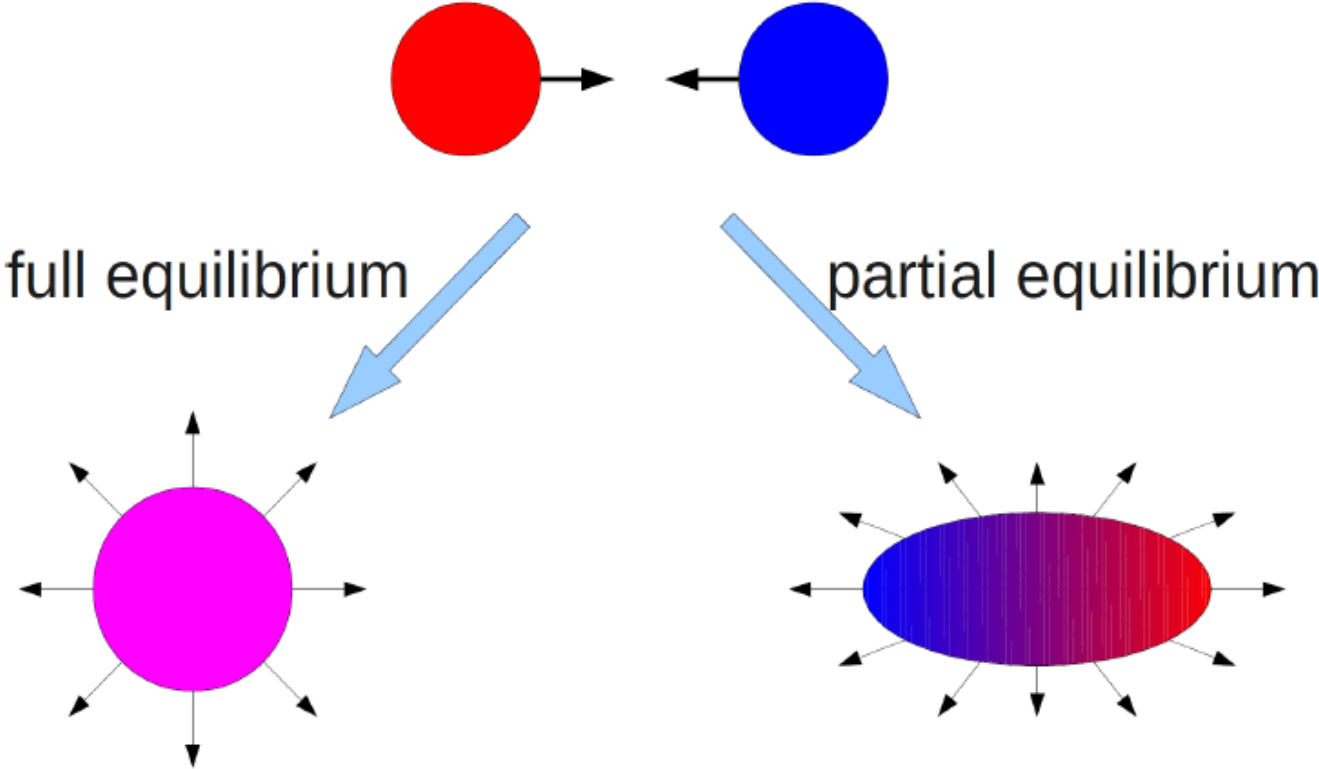
INDRA dataset

| System | Incident energy (A.MeV) | A_{tot} | $(N/Z)_{\text{tot}}$ | Dataset |
|-----------------|-------------------------|------------------|----------------------|---------|
| Ar+KCl | 32 - 74 | 72 | 1.00 | 4 |
| Ni+Ni | 32 - 90 | 116 | 1.11 | 7 |
| Xe+Sn | 12 (8) - 100 | 248 | 1.39 | 15 |
| Xe+Sn (isospin) | 32 - 45 | 220 - 250 | 1.27 - 1.50 | 4 |
| Au+Au | 40-100 | 394 | 1.49 | 5 |
| U+U | 24,36 | 476 | 1.59 | 2 |

- 5 systems spanning a **large total mass and isospin** domain
- Cover the **whole Fermi energy domain** from $12A$ to $100A$ MeV
- Offer the **most extensive, comprehensive and exclusive** database for nuclear reactions in the Fermi energy domain

Isospin diffusion and equilibration ?

Isospin equilibration



- ▶ memory of entrance channel is lost
- ▶ same isospin everywhere

- ▶ memory of the entrance channel is partially conserved
- ▶ dependence of the isospin along the beam axis

Isospin ratio

Imbalance ratio

$$\tilde{R}_{p/t} = \frac{2R_{p/t} - R_{p/t}^{NN} - R_{p/t}^{PP}}{R_{p/t}^{NN} - R_{p/t}^{PP}}$$

where $R_{p/t}$ is the normalized yield of different particles in isospin with the same atomic number Z .

$$\tilde{R}_{proton/triton} = \begin{cases} +1 & \text{if } R_{p/t} = R_{p/t}^{NN} \\ -1 & \text{if } R_{p/t} = R_{p/t}^{PP} \end{cases}$$

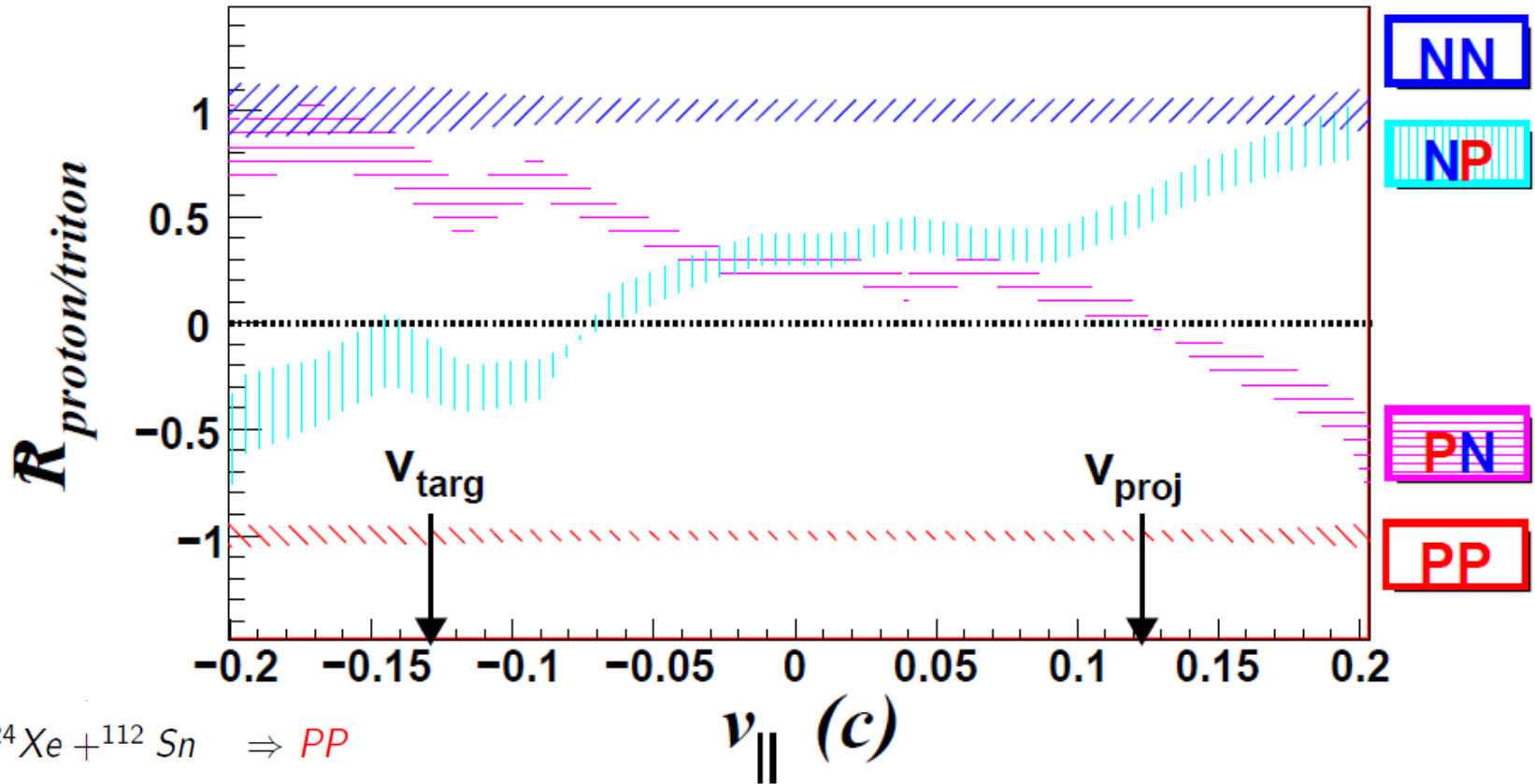
F. Rami, PRL **84**, 1120 (2000)

V. Baran, PRC **72**, 064620 (2005)

- ▶ $^{124}\text{Xe} + ^{112}\text{Sn} \Rightarrow PP$
- ▶ $^{124}\text{Xe} + ^{124}\text{Sn} \Rightarrow PN$
- ▶ $^{136}\text{Xe} + ^{112}\text{Sn} \Rightarrow NP$
- ▶ $^{136}\text{Xe} + ^{124}\text{Sn} \Rightarrow NN$

Isospin diffusion from p/t ratio for central collisions (v_{tot} selection)

Xe+Sn @ 32 MeV/A

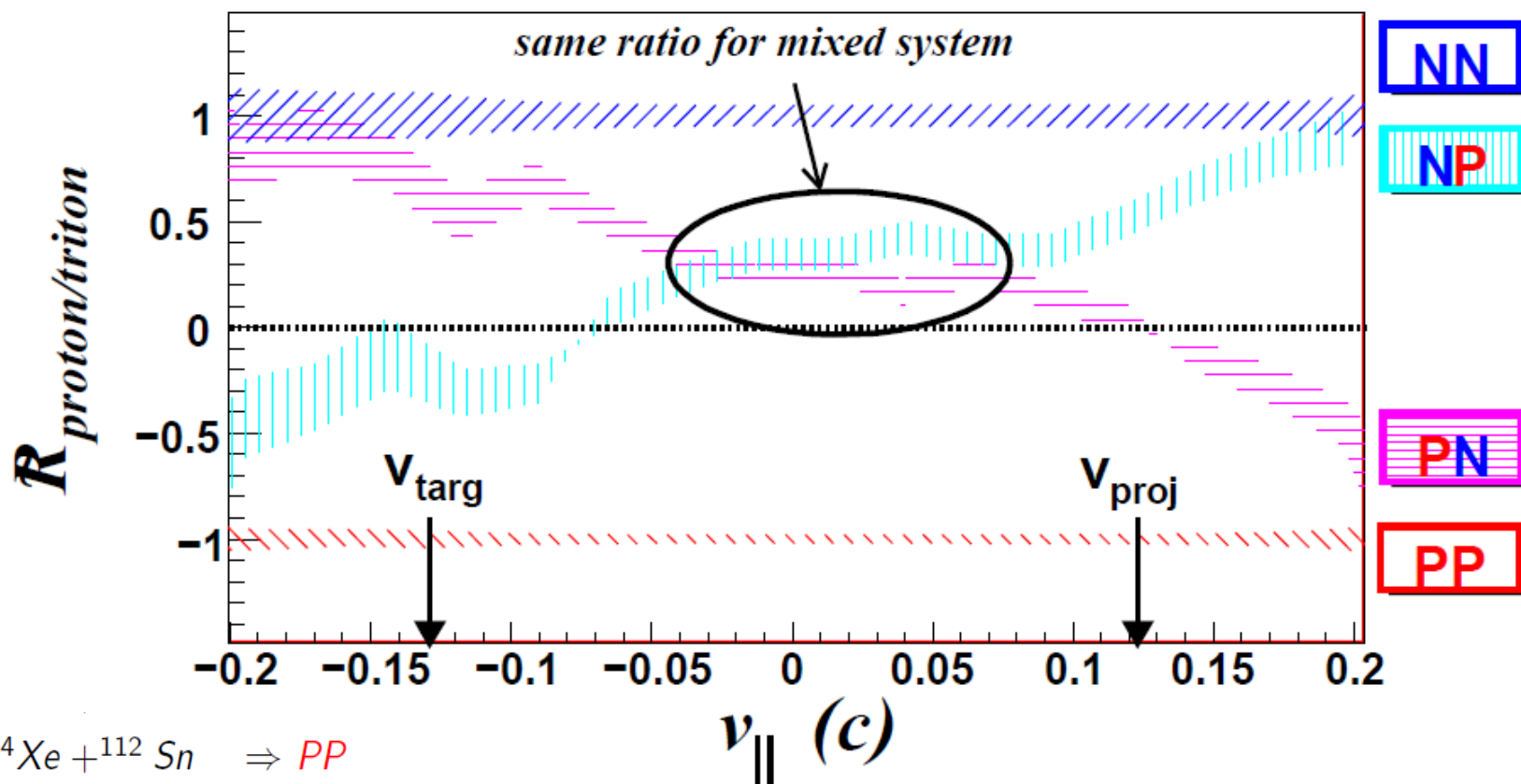


- ▶ $^{124}\text{Xe} + ^{112}\text{Sn} \Rightarrow \text{PP}$
- ▶ $^{124}\text{Xe} + ^{124}\text{Sn} \Rightarrow \text{PN}$
- ▶ $^{136}\text{Xe} + ^{112}\text{Sn} \Rightarrow \text{NP}$
- ▶ $^{136}\text{Xe} + ^{124}\text{Sn} \Rightarrow \text{NN}$

Velocity along the beam axis

Isospin diffusion from p/t ratio for central collisions (v_{tot} selection)

Xe+Sn @ 32 MeV/A

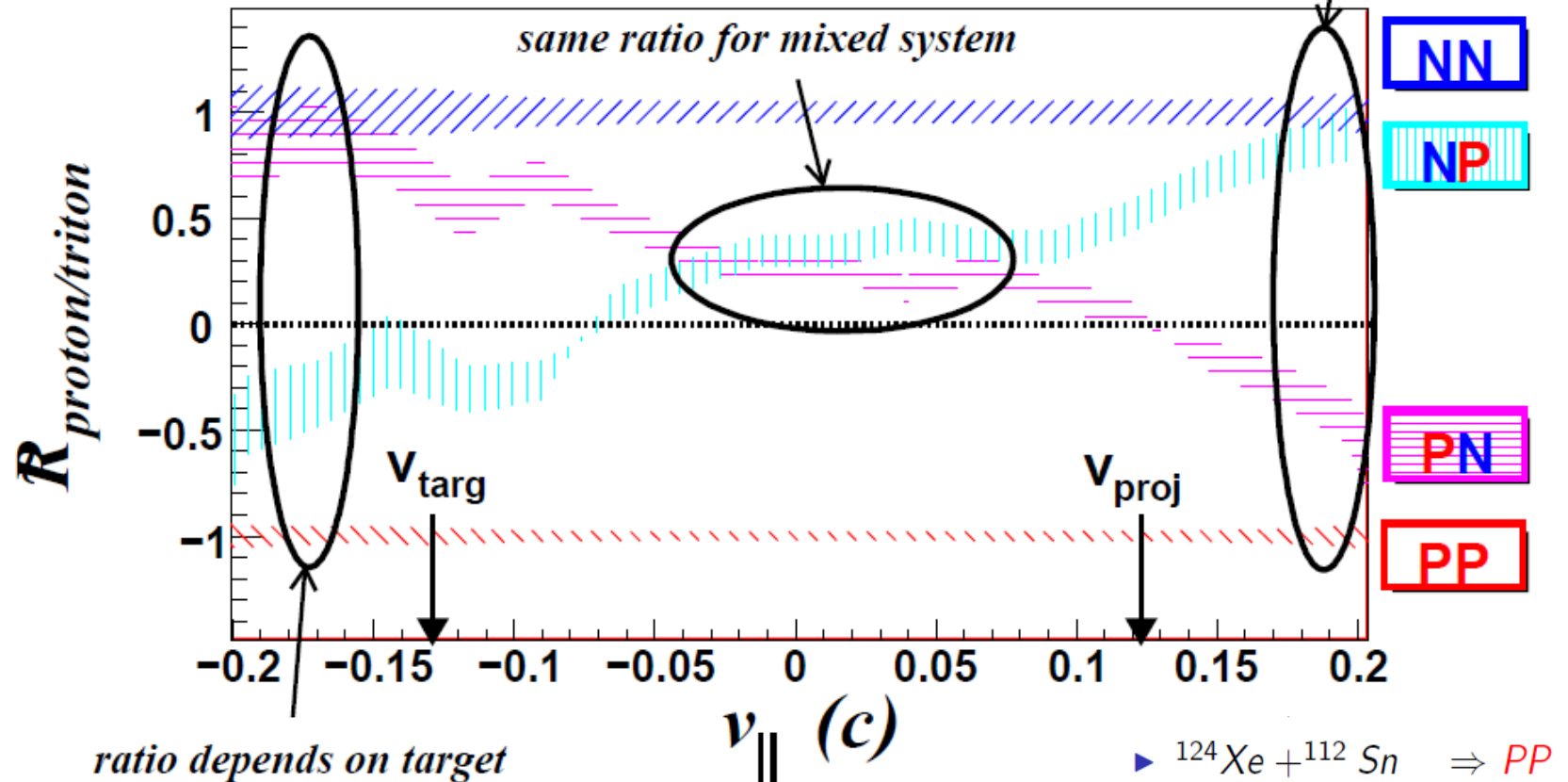


- ▶ $^{124}\text{Xe} + ^{112}\text{Sn} \Rightarrow \text{PP}$
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Isospin diffusion from p/t ratio for central collisions (v_{tot} selection)

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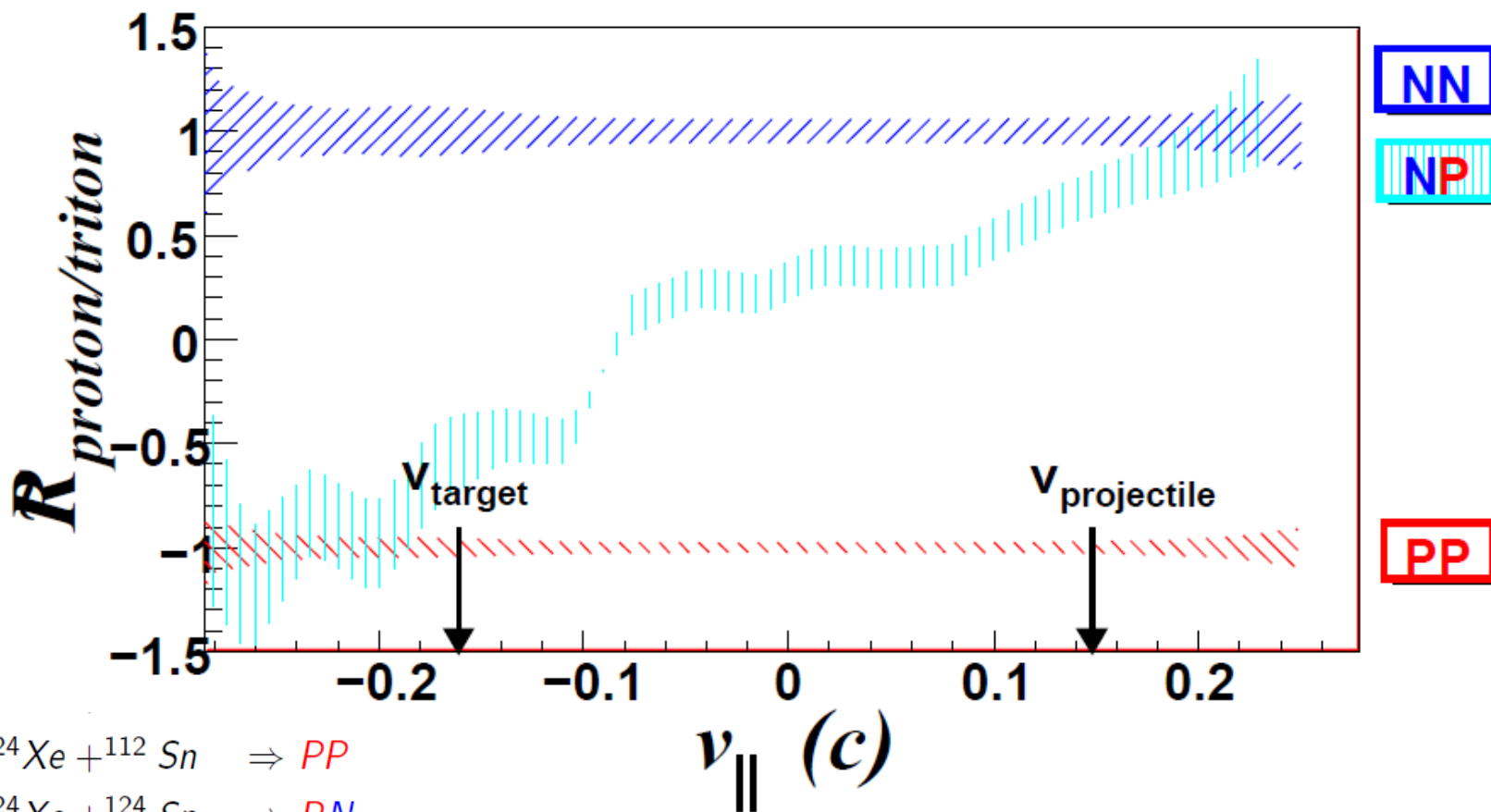
ratio depends on projectile



- ▶ $^{124}\text{Xe} + ^{112}\text{Sn} \Rightarrow \text{PP}$
- ▶ $^{124}\text{Xe} + ^{124}\text{Sn} \Rightarrow \text{PN}$
- ▶ $^{136}\text{Xe} + ^{112}\text{Sn} \Rightarrow \text{NP}$
- ▶ $^{136}\text{Xe} + ^{124}\text{Sn} \Rightarrow \text{NN}$

Isospin diffusion from p/t ratio for central collisions (v_{tot} selection)

Xe+Sn at 45 MeV/A central collisions



- ▶ $^{124}\text{Xe} + ^{112}\text{Sn} \Rightarrow PP$
- ▶ $^{124}\text{Xe} + ^{124}\text{Sn} \Rightarrow PN$
- ▶ $^{136}\text{Xe} + ^{112}\text{Sn} \Rightarrow NP$
- ▶ $^{136}\text{Xe} + ^{124}\text{Sn} \Rightarrow NN$

From isospin probe : nuclear matter is semi-transparent : no full isospin equilibration

Isospin dependence for stopping ?

From IQMD calculations...

Isospin Quantum Molecular Dynamics

In-medium nucleon-nucleon
cross-section :

$$\sigma_{NN}^{med} = \left(1 + \alpha \frac{\rho}{\rho_0} \right) \sigma_{NN}^{free}$$

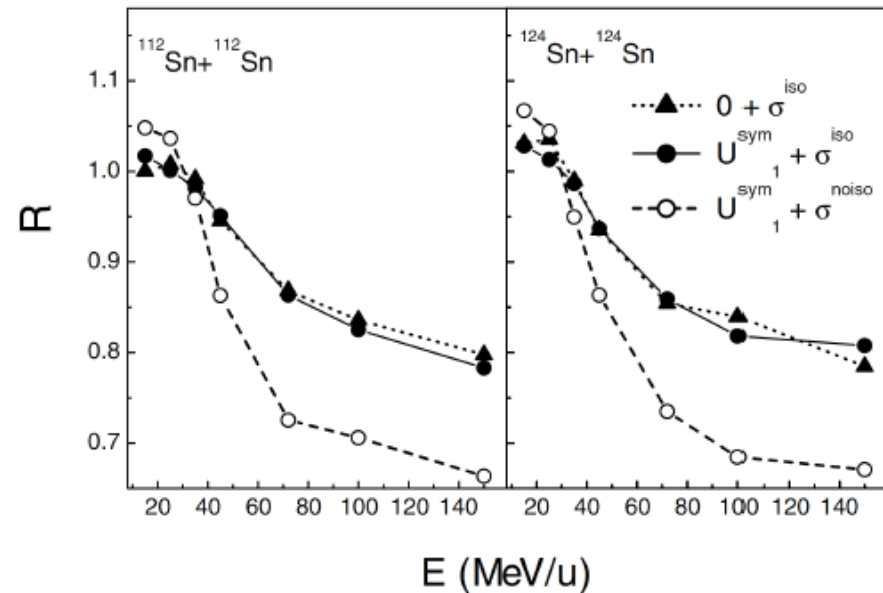
Interaction potential :

$$U = U^{Sky} + U^{Yuk} + U^{coul} + U^{Pauli} + U^{MDI} \\ + U^{sym}$$

Observation on momentum isotropy R :

- ▶ No effect of U^{sym}
- ▶ the isospin of entrance channel has no effect
- ▶ dependence of the nucleon-nucleon cross-section

J.-Y. Liu, *et al.*, PRL **86** 975 (2001)

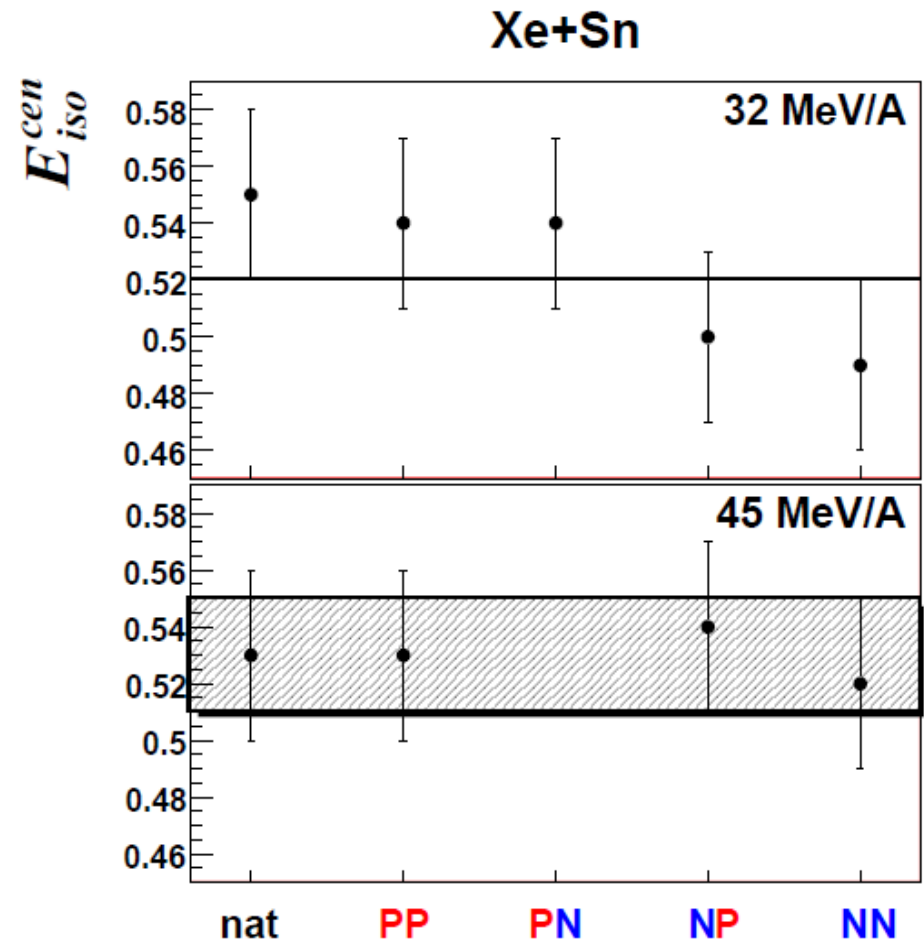


From experimental Data...

Isospin effect

- ▶ $^{129}\text{Xe} + ^{119}\text{Sn} \Rightarrow \text{nat}$
- ▶ $^{124}\text{Xe} + ^{112}\text{Sn} \Rightarrow \text{PP}$
- ▶ $^{124}\text{Xe} + ^{124}\text{Sn} \Rightarrow \text{PN}$
- ▶ $^{136}\text{Xe} + ^{112}\text{Sn} \Rightarrow \text{NP}$
- ▶ $^{136}\text{Xe} + ^{124}\text{Sn} \Rightarrow \text{NN}$

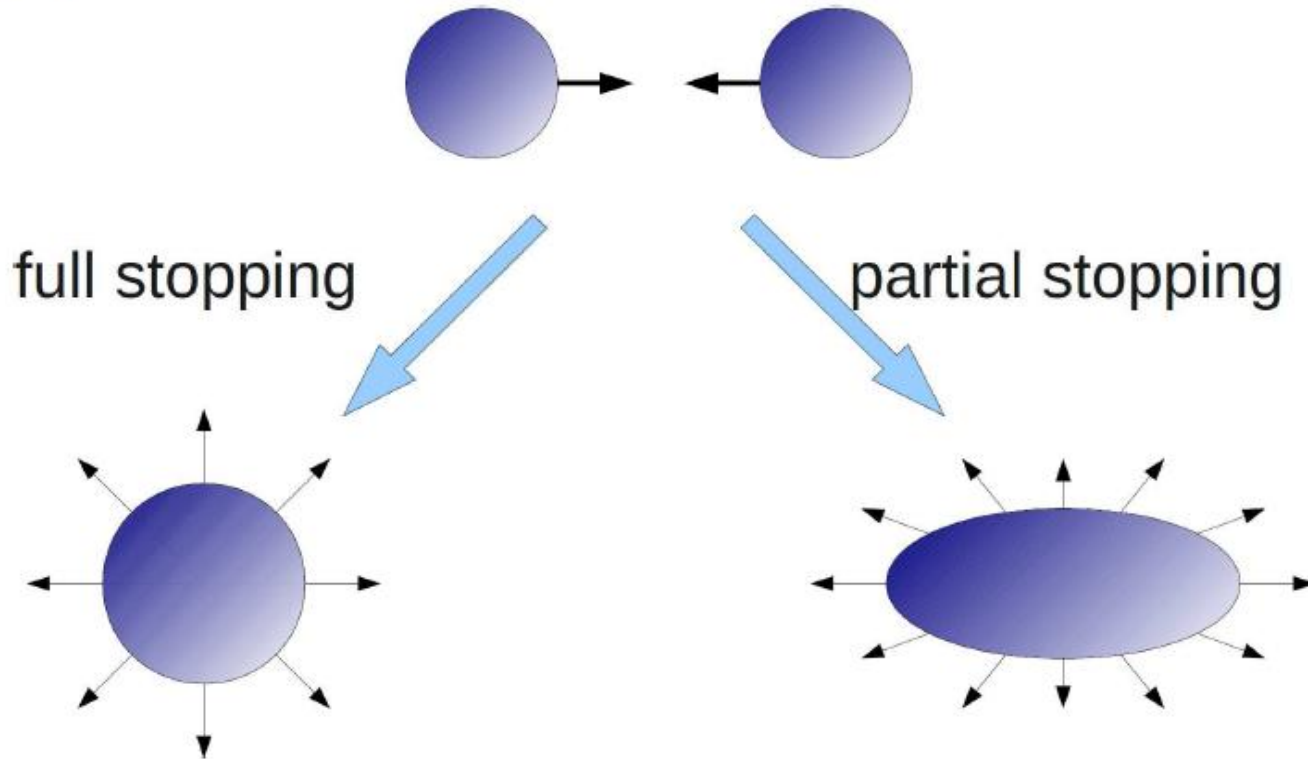
- Error bars are here systematics



No clear dependence is observed in this incident energy range
but isospin excursion $\Delta(N/Z)$ is only $\sim 15\%$

Energy dissipation and thermalization ?

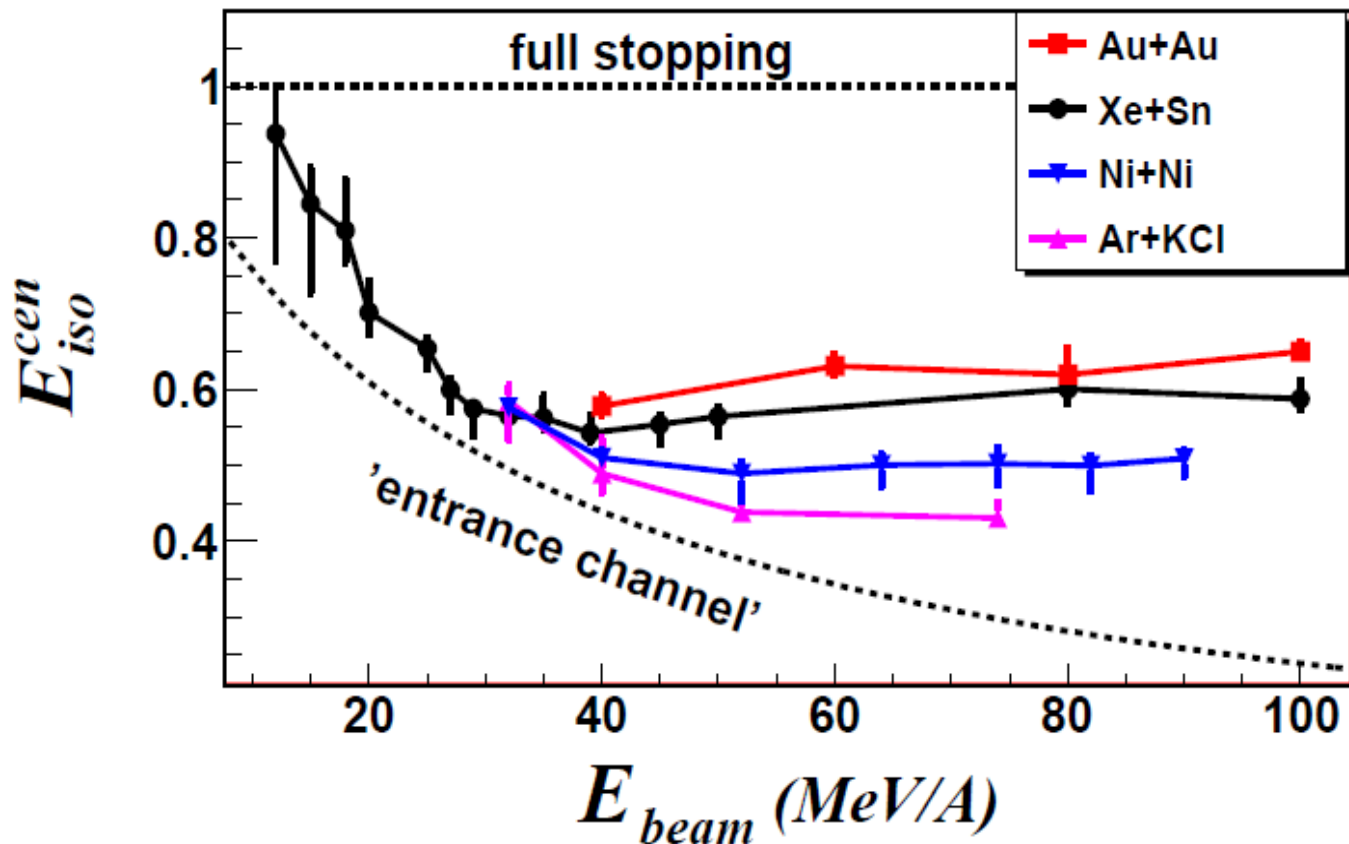
Stopping power measurement



- ▶ memory of entrance channel is lost
- ▶ no preferential axis

- ▶ memory of the entrance channel is partially conserved
- ▶ preferential direction along the beam axis

Systematics

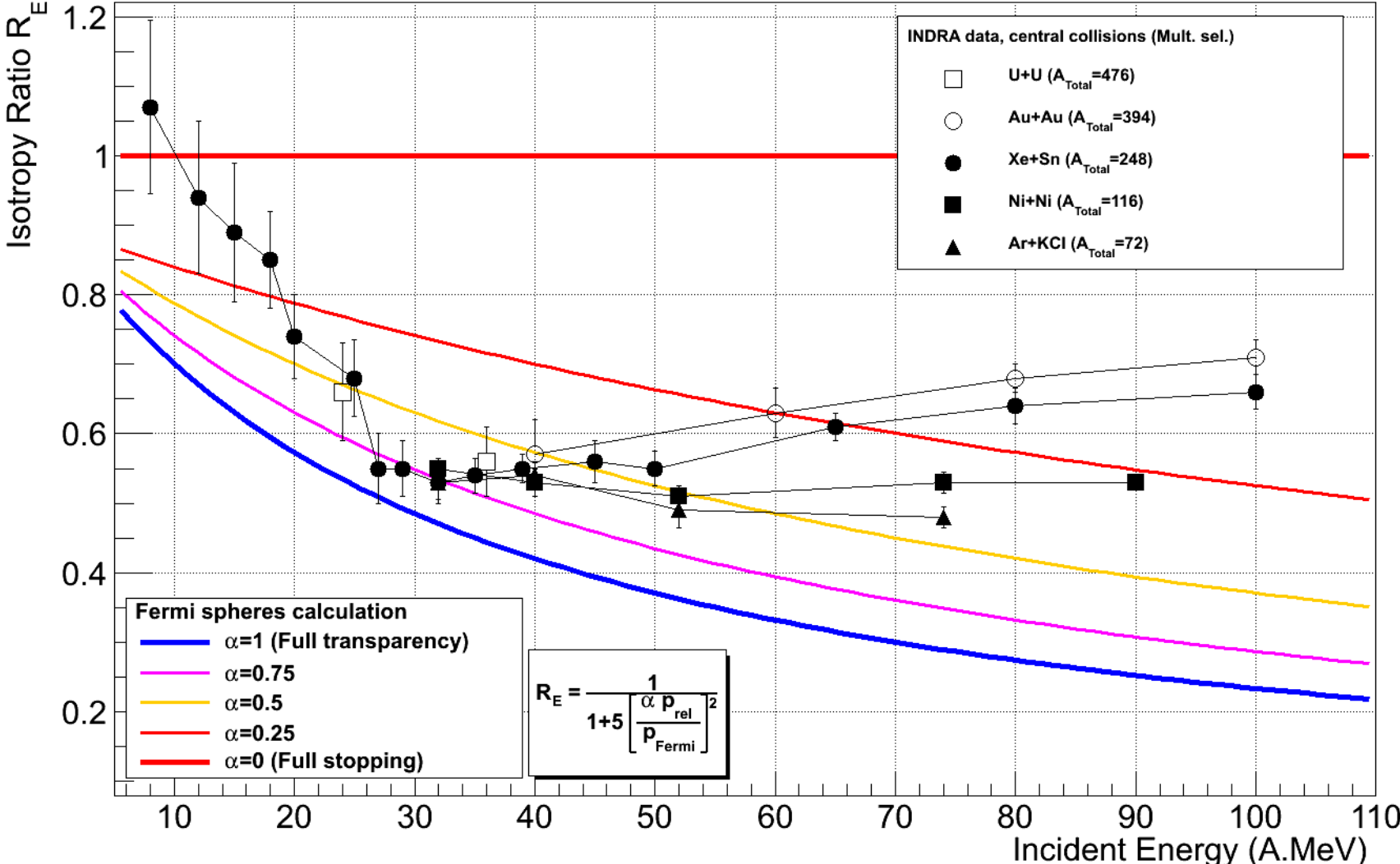


2 regimes :

- Below $30-35A$ MeV, Mean-Field picture and **1-dissipation** : **viscosity**
- Above $35A$ MeV, elastic NN collisions and **2-dissipation** : λ_{NN} and σ_{NN}

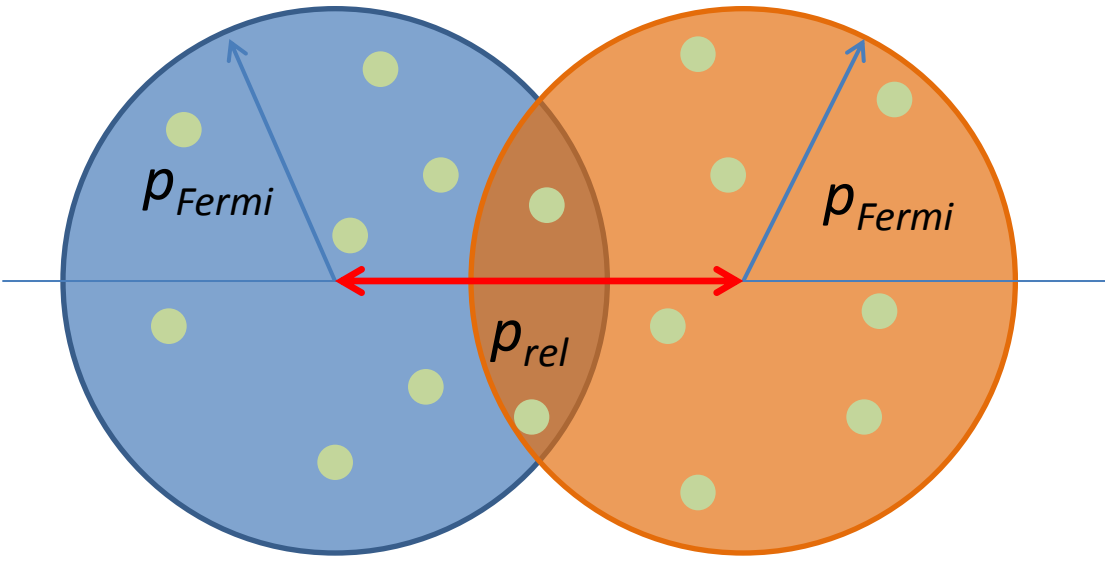
Situation in 2012 : one system added (U/Gd+U) + extension to low E_{inc}

Nuclear Stopping systematics (INDRA data)



Entrance channel estimate for R_E

Fermi spheres with radius p_{Fermi} , separated by the relative momentum $p_{rel} = \mu V_{rel}$



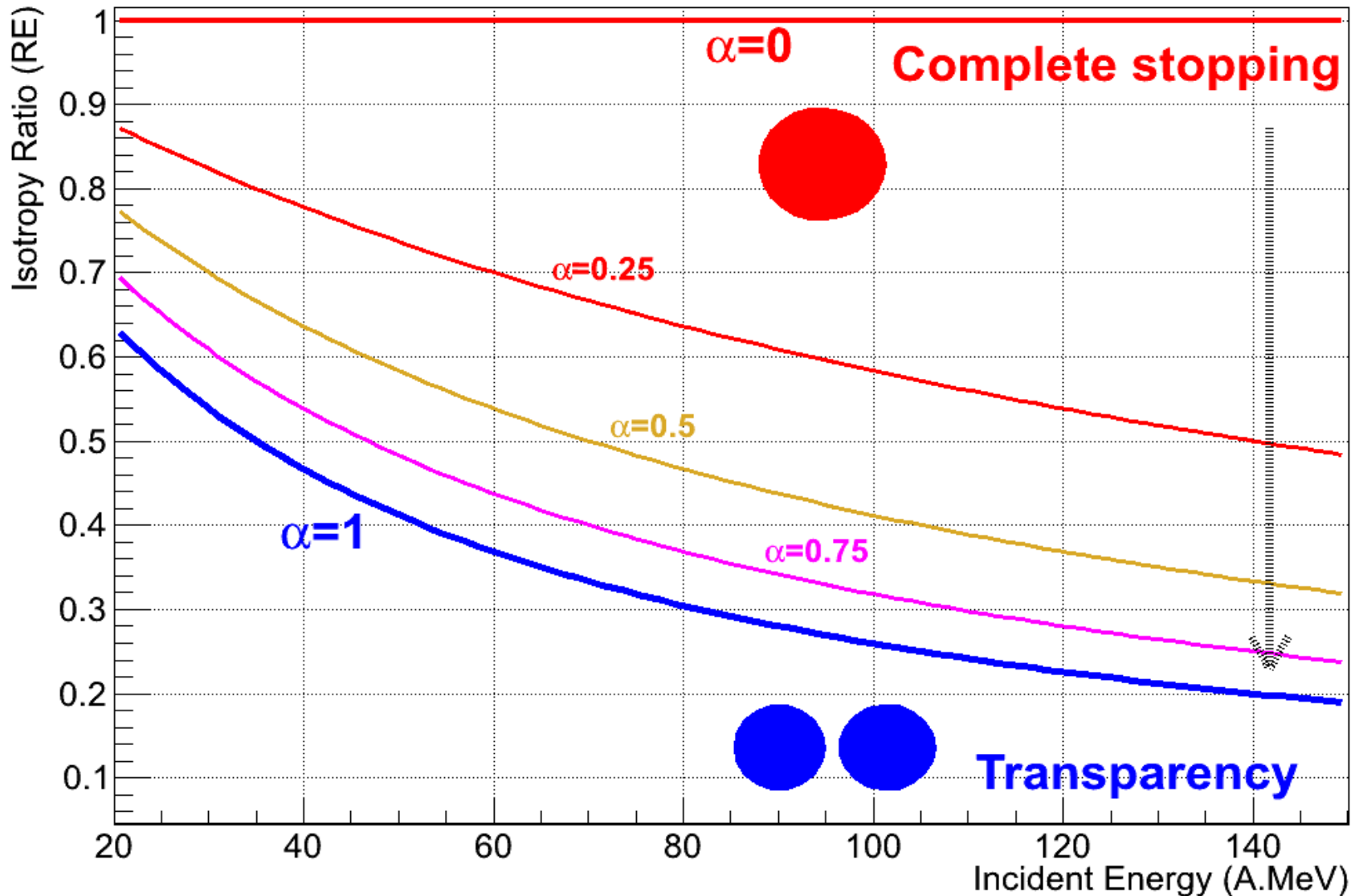
For an **infinite number** of particles sampled in these 2 distributions, we obtain :

$$R_E = \frac{1}{1+5 \left[\frac{\alpha p_{rel}}{p_{Fermi}} \right]^2}$$

where α between 0 and 1 measures the dissipation

In practice, $N > 10-15$ is enough to get $\langle R_E \rangle$

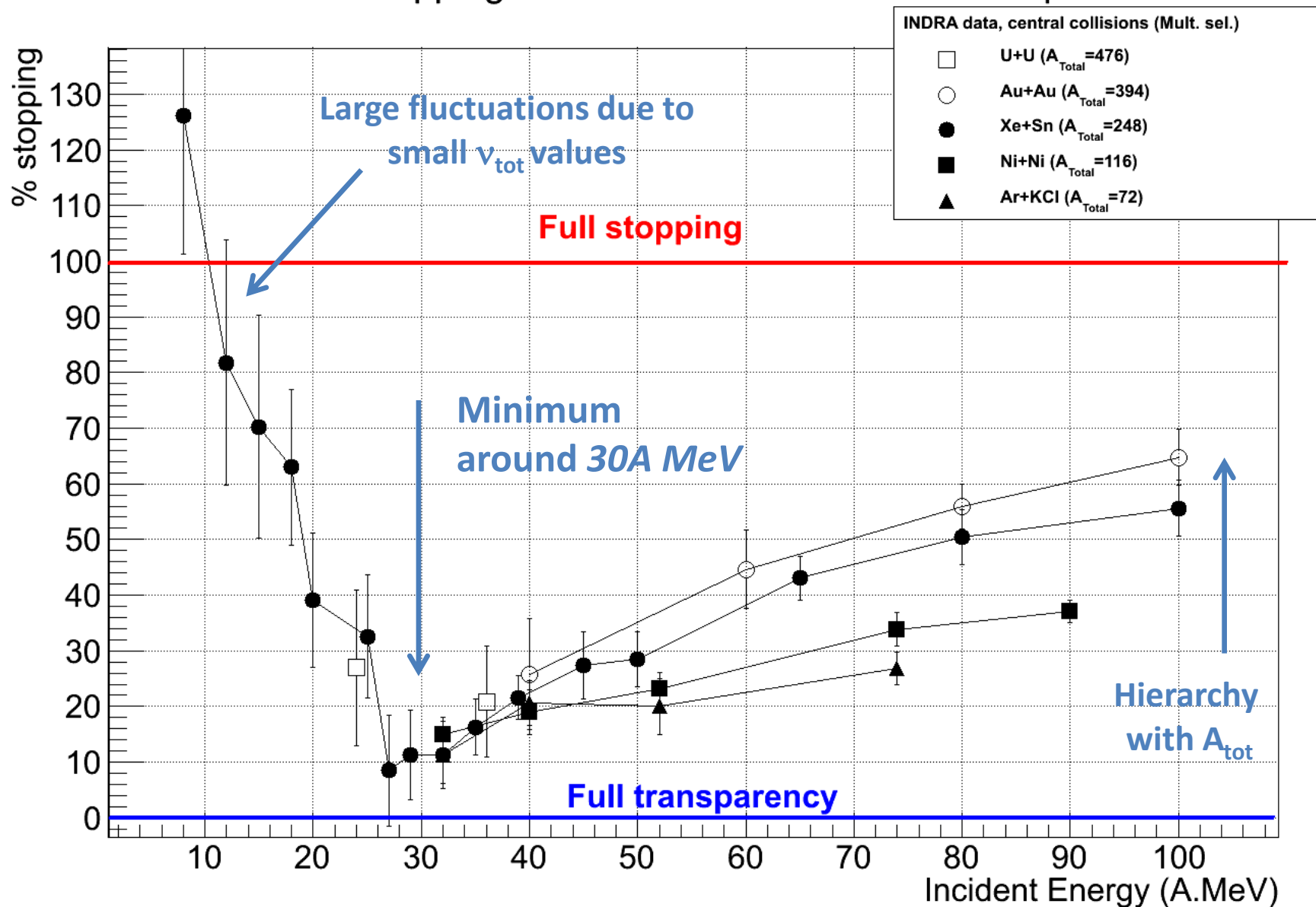
Fermi Spheres Hypothesis with relaxation factor α



Clusterization effects ? see Zhang et al., Phys. Rev. C 84, 034612 (2011)

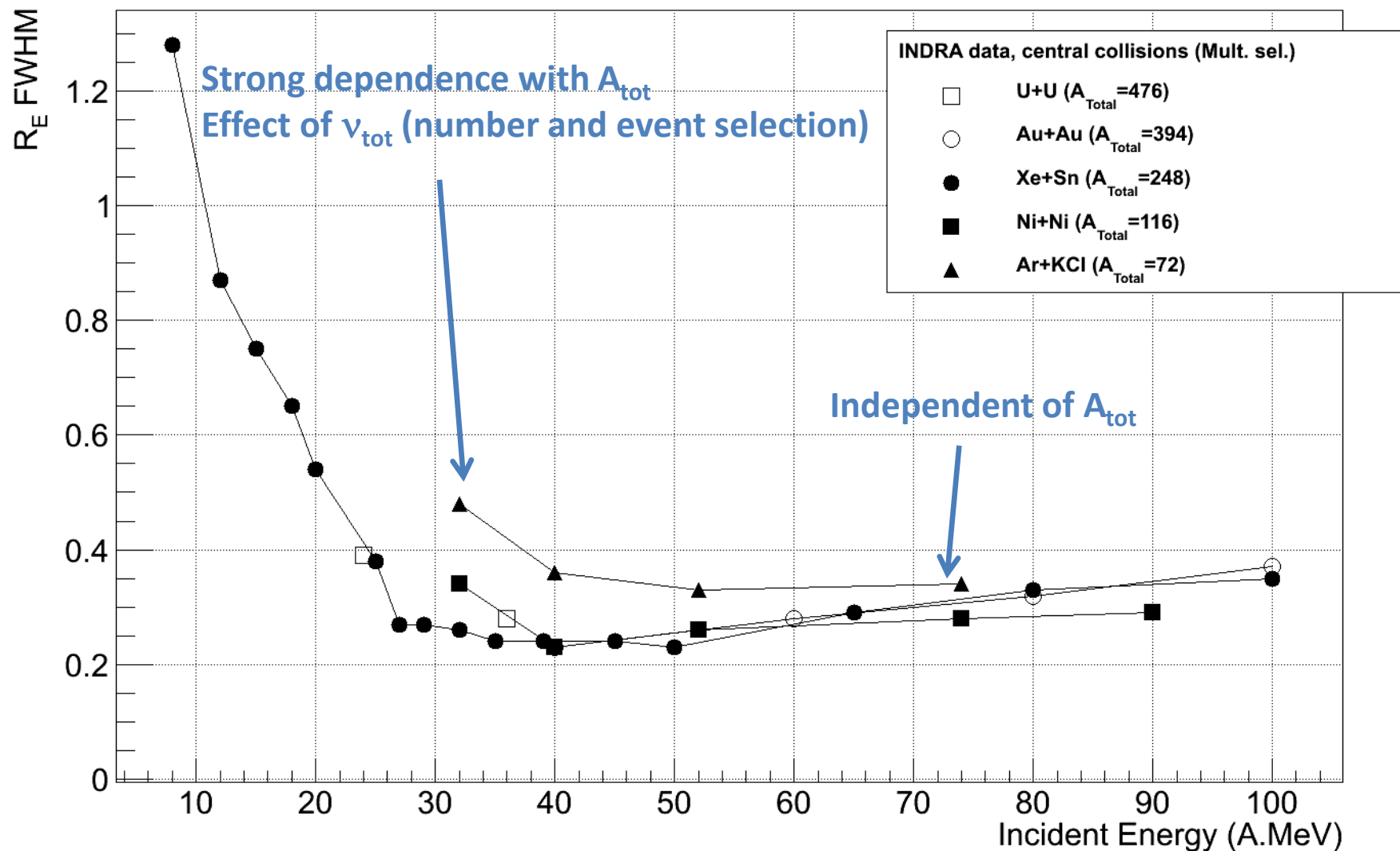
Percentage of stopping/transparency

Nuclear stopping distance to non-relaxed Fermi spheres



Widths / fluctuations* ...

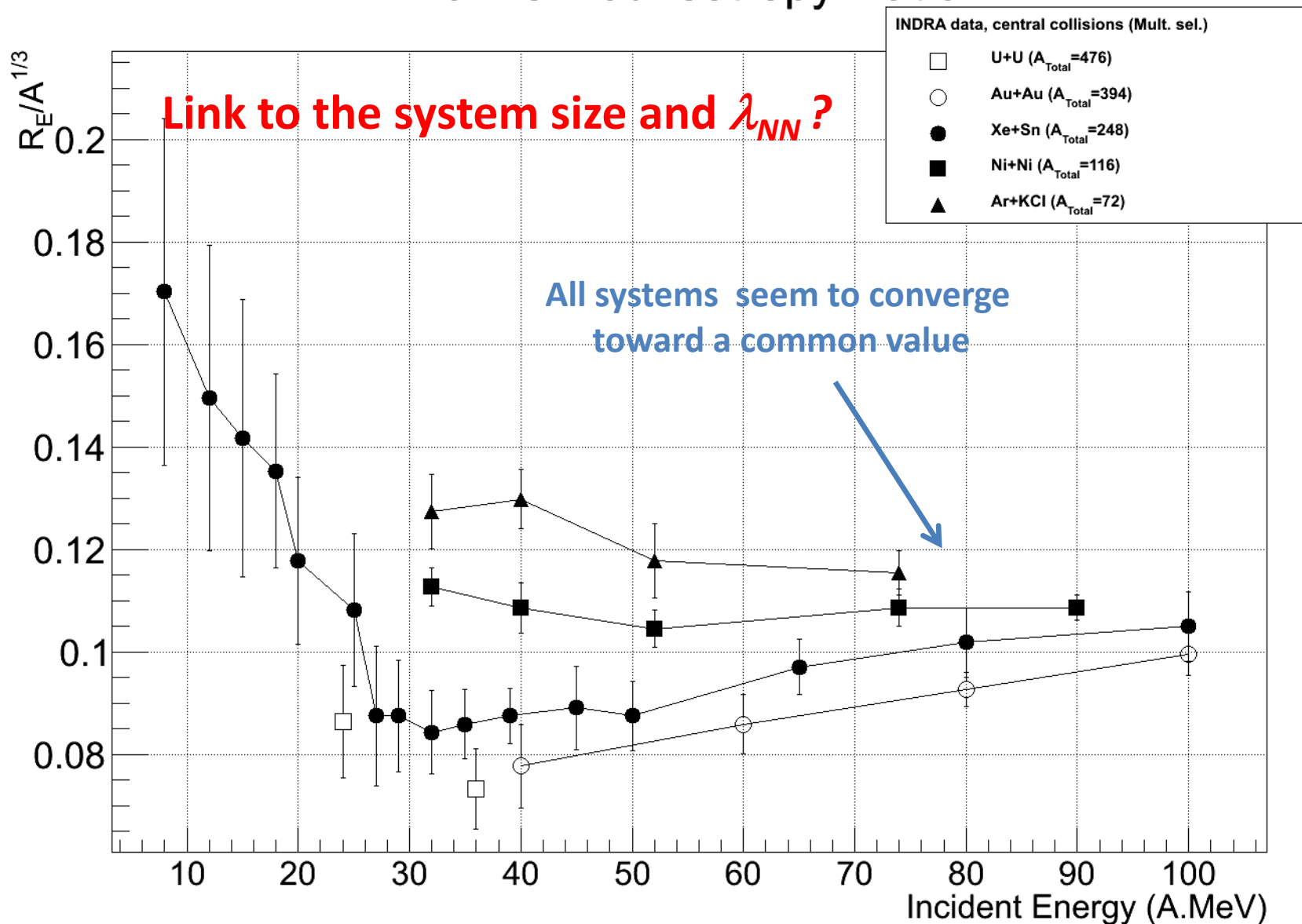
Isotropy Ratio FWHM



* Very sensitive to the event selection (impact parameter range)

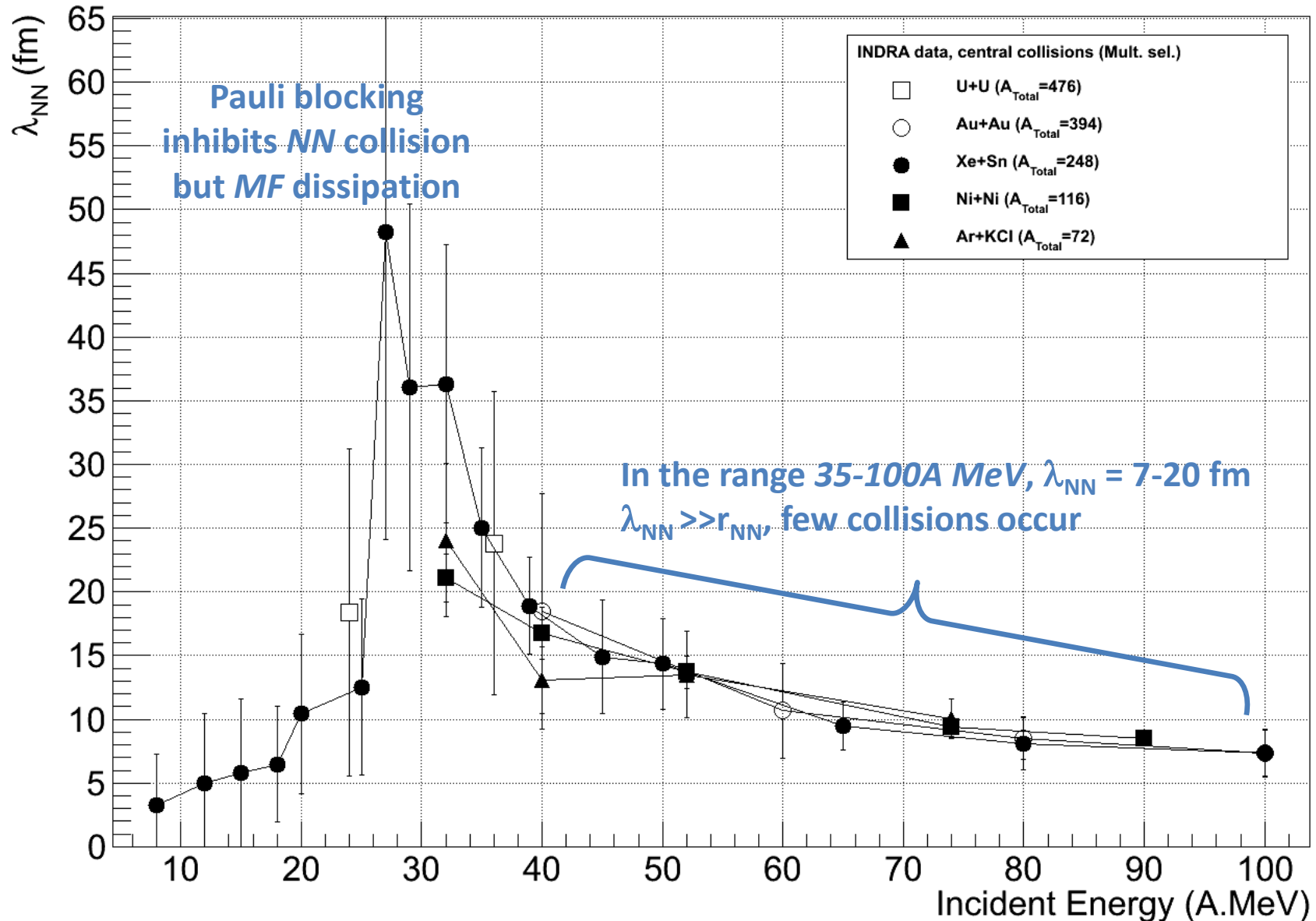
Scaling with the system size A_{tot}

Normalized Isotropy Ratio



Estimation of the mean free path for nucleons in NMA

In-medium NN Mean Free Path, $\lambda_{NN} = r_0 \cdot A^{1/3} / \text{stopping}$

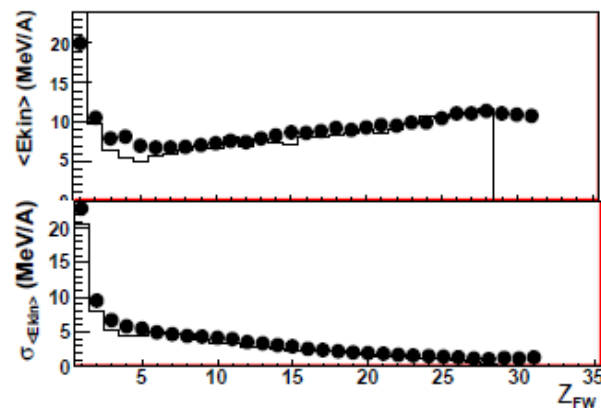
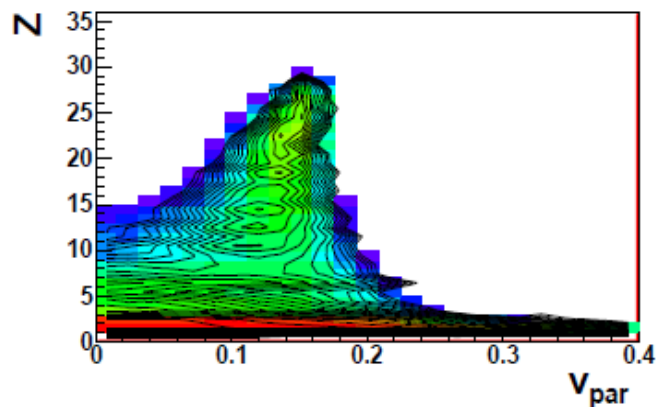
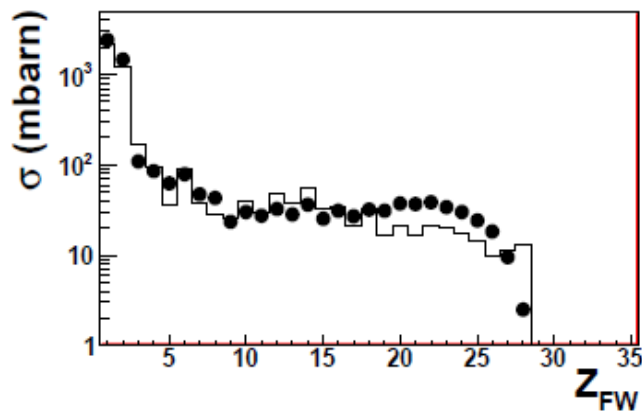
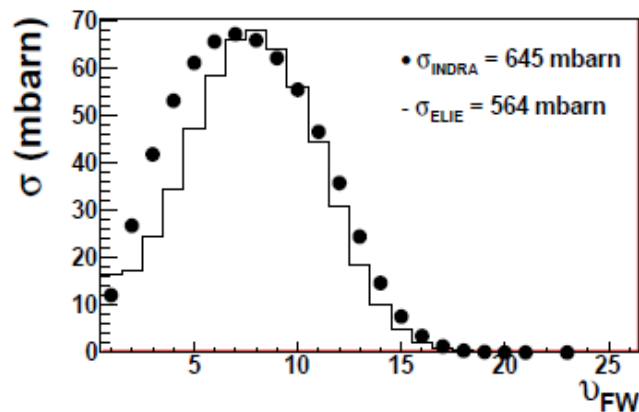


Partitions and kinematics

Ni + Ni@52A.MeV

INDRA : selection $Z_{tot}^{FW} \in [0.8; 1.2]$

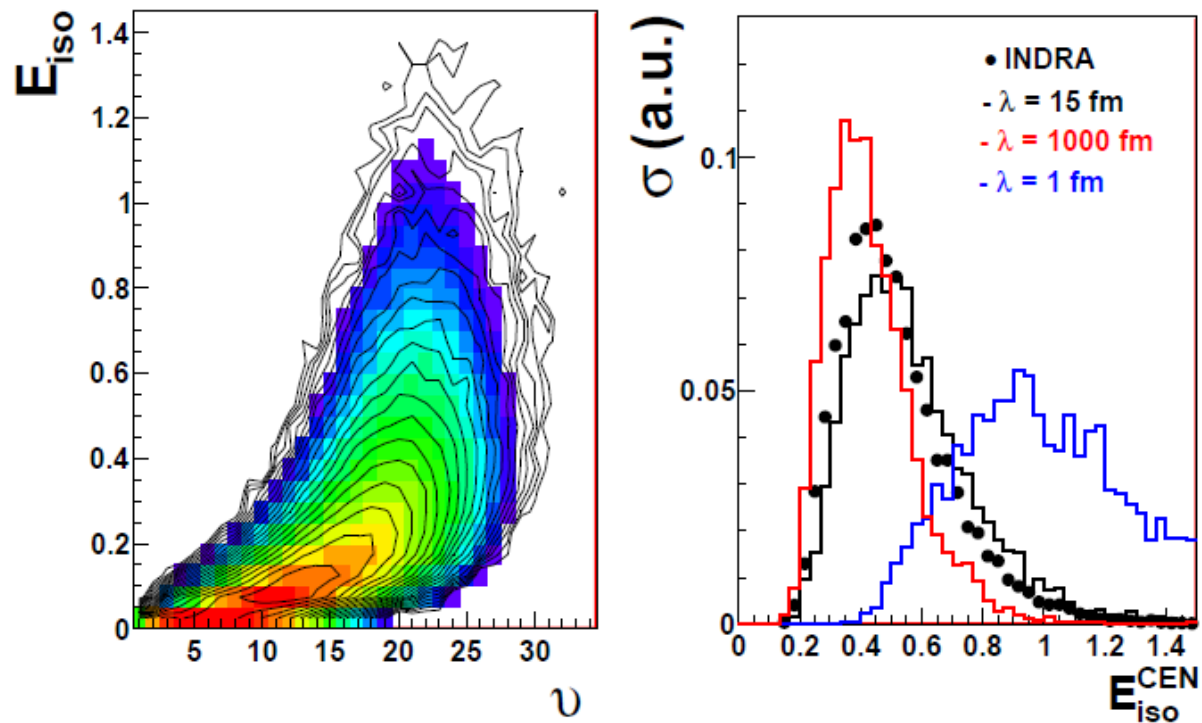
ELIE filtered : selection $Z_{tot}^{FW} \in [0.8; 1.2]$



► An excellent agreement between ELIE and the INDRA data is found

Comparison on stopping:

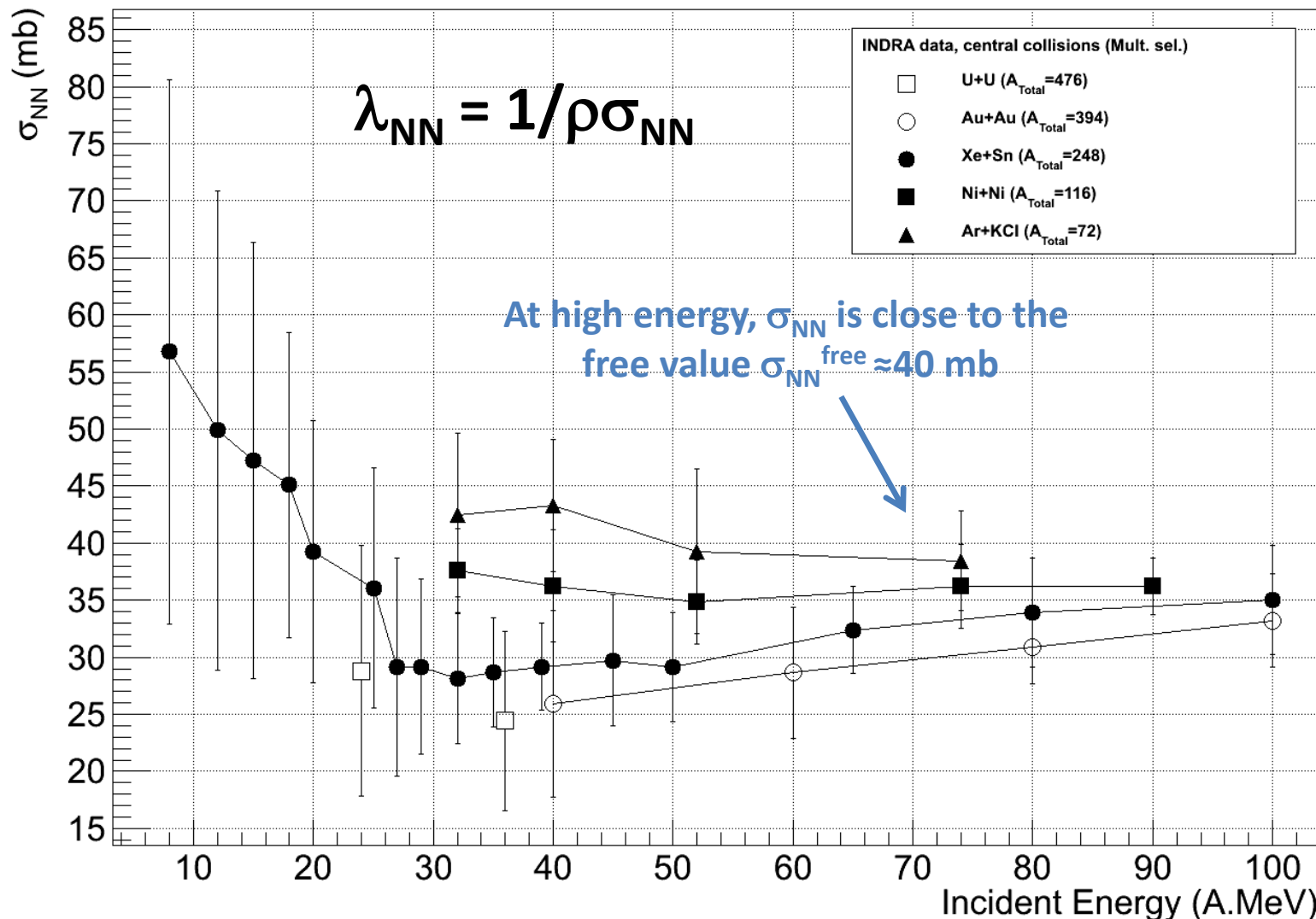
$Ni + Ni@52A.MeV$, central collisions $\nu > 26$



- ▶ sensitivity to λ is found for E_{iso}^{cen} , especially for $\lambda < (R_{proj} + R_{targ})$
- ▶ data is closer to $\lambda = 15$ fm ($> R_{proj} + R_{targ}$), suggesting no complete thermalization since the number of collisions per participant is less than 1.

Experimental NN cross-section estimate from λ_{NN}

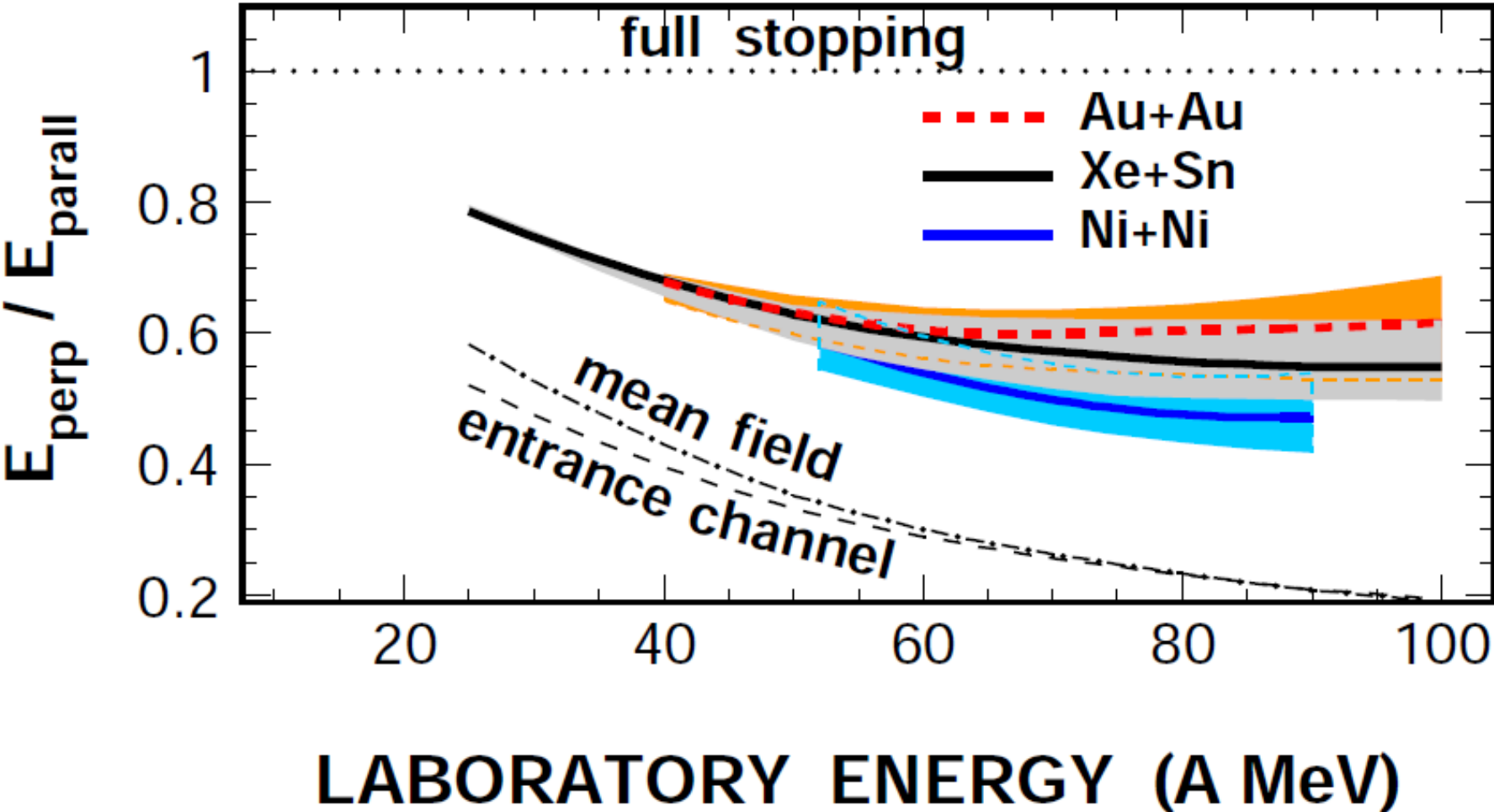
In-medium NN cross section , $\sigma_{NN} = \text{stopping} / (r_0 \cdot A^{1/3} \rho_0)$



Comparison with a transport model

Landau-Vlasov* : Gogny + variable σ_{NN}

$\sigma_{NN} \pm 20\%$ of free σ_{NN}



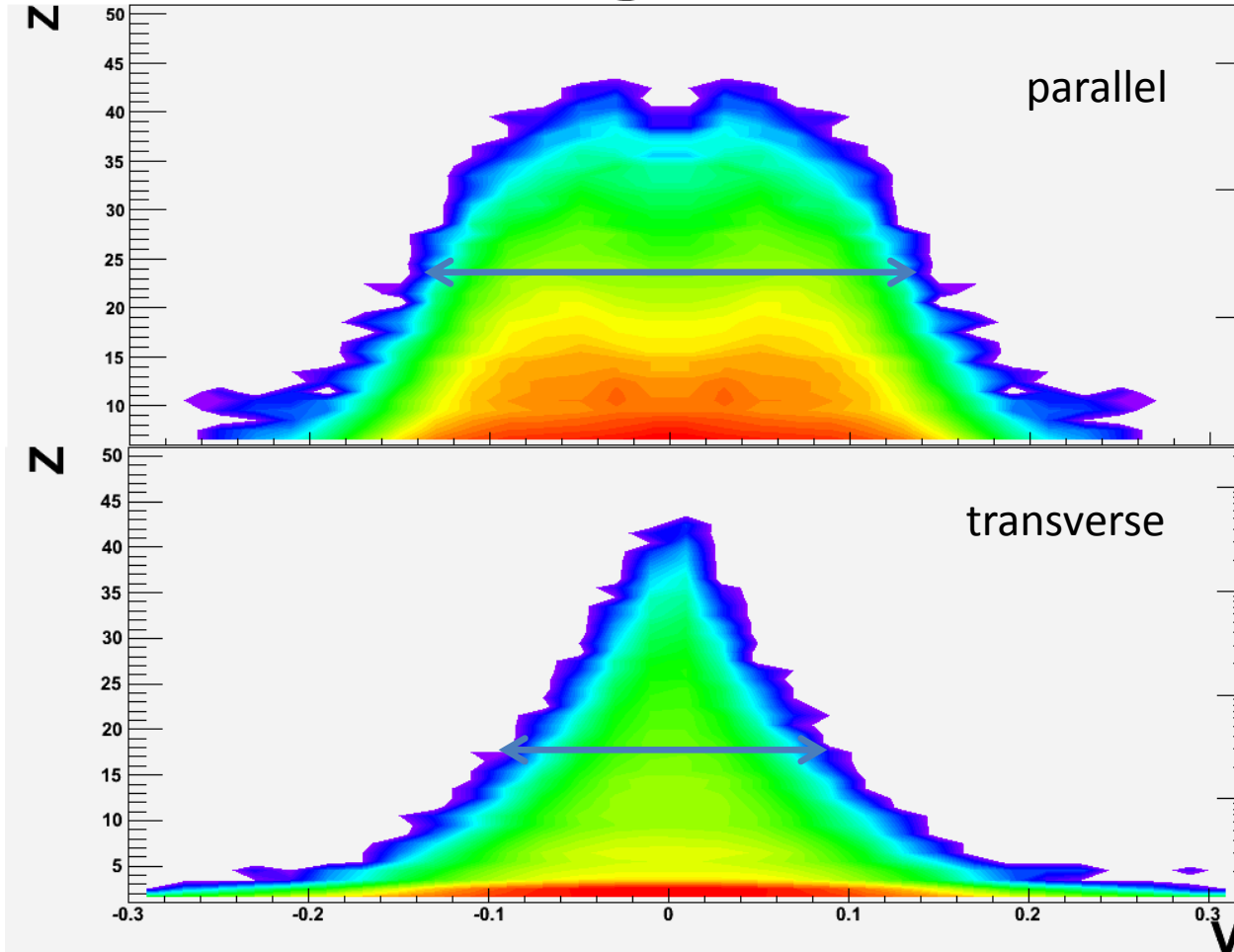
* Courtesy of Ph. Eudes and Z. Basrak

New probes ...

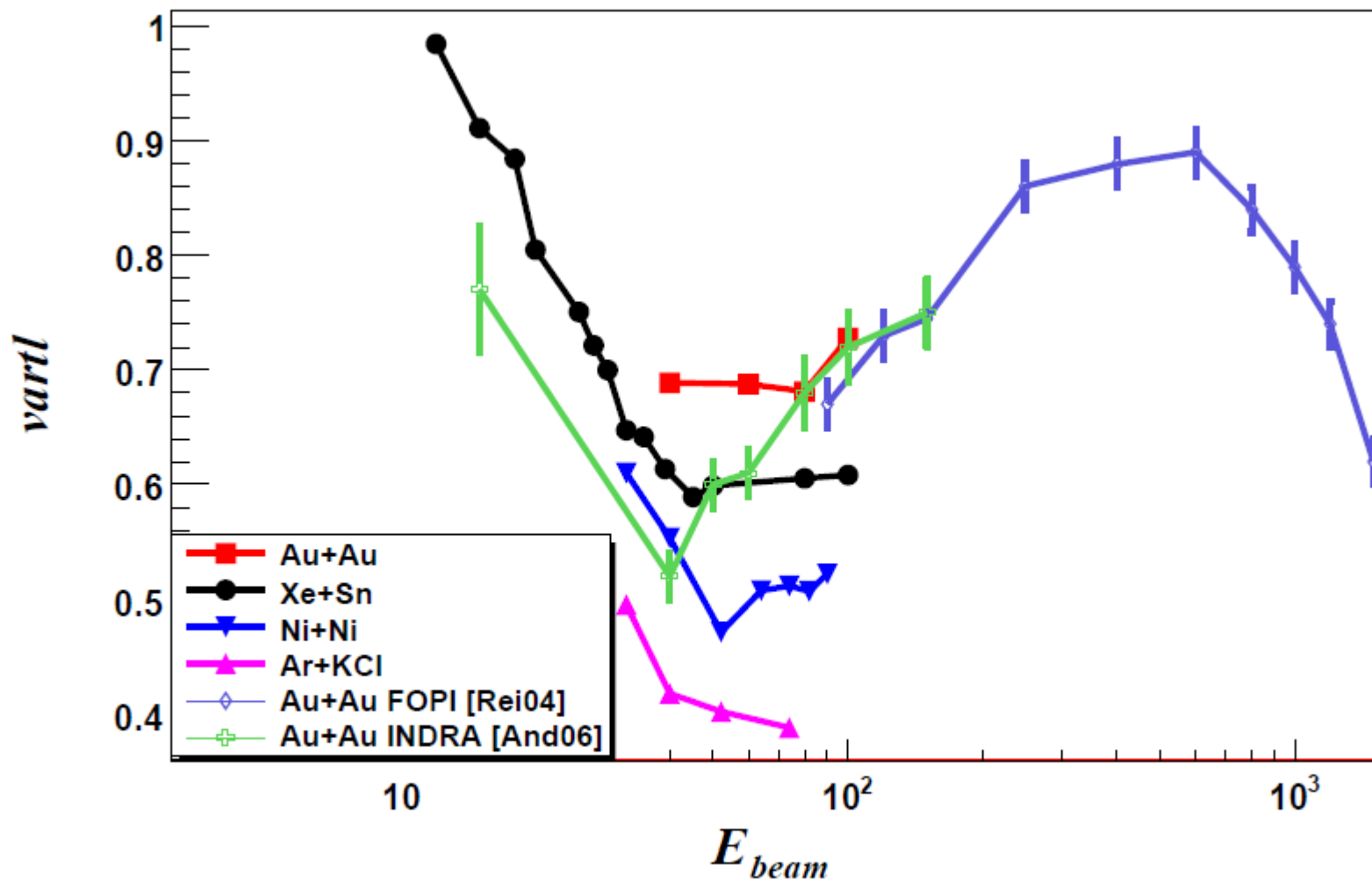
Ratio of velocity variances : v_{artl}

$$v_{artl} = \frac{\text{variance}(y_{\perp})}{\text{variance}(y_{\parallel})}$$

Xe+Sn @ 39 MeV indra



*V*_{artl} systematics from FOPI/INDRA data



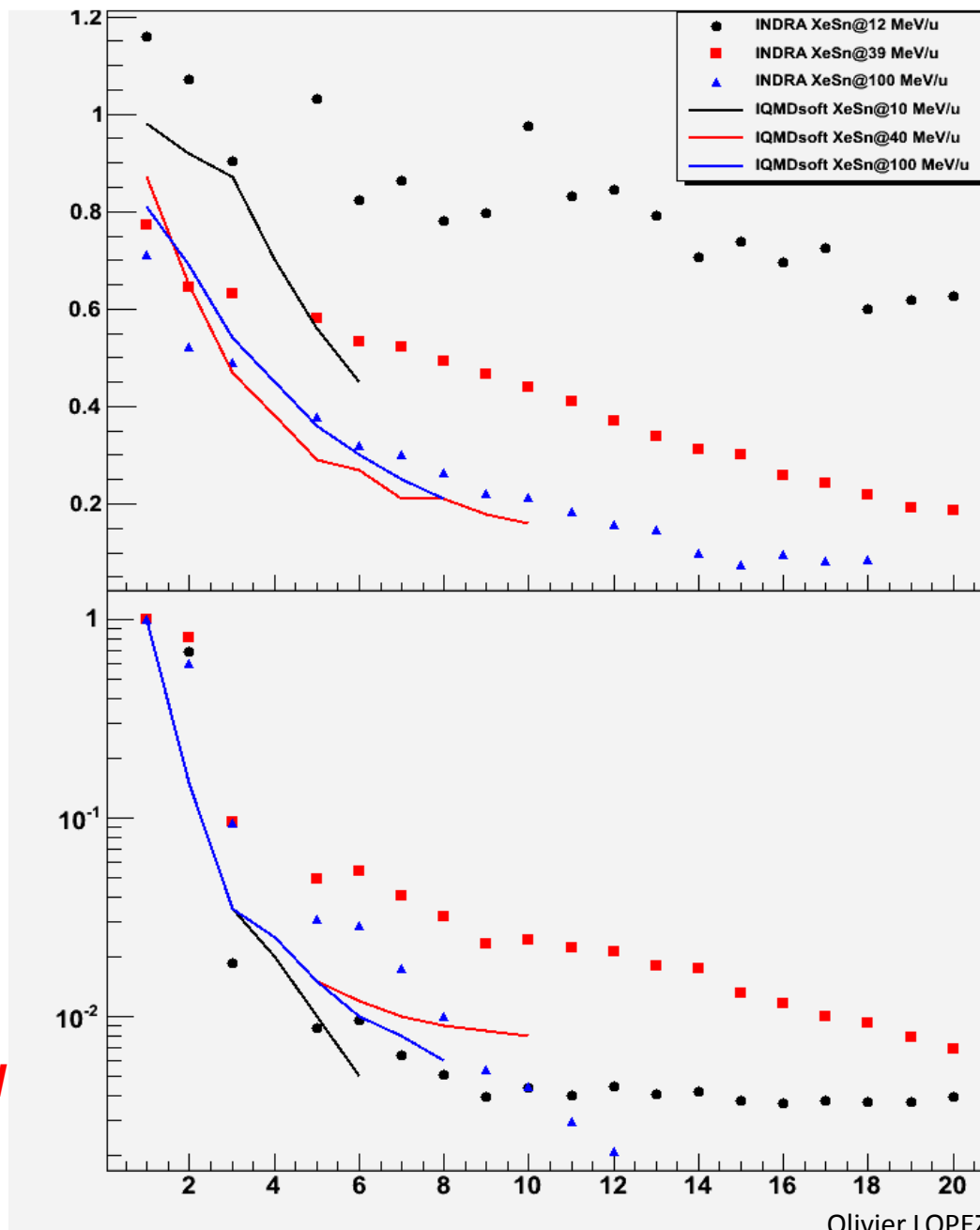
[And06] A. Andronic, J. Lukasik, W. Reisdorf, W. Trautmann. *Systematics of stopping and flow in Au+Au collisions*, Eur. Phys. J. A **30**, 31-46 (2006).

Vartl and production yield

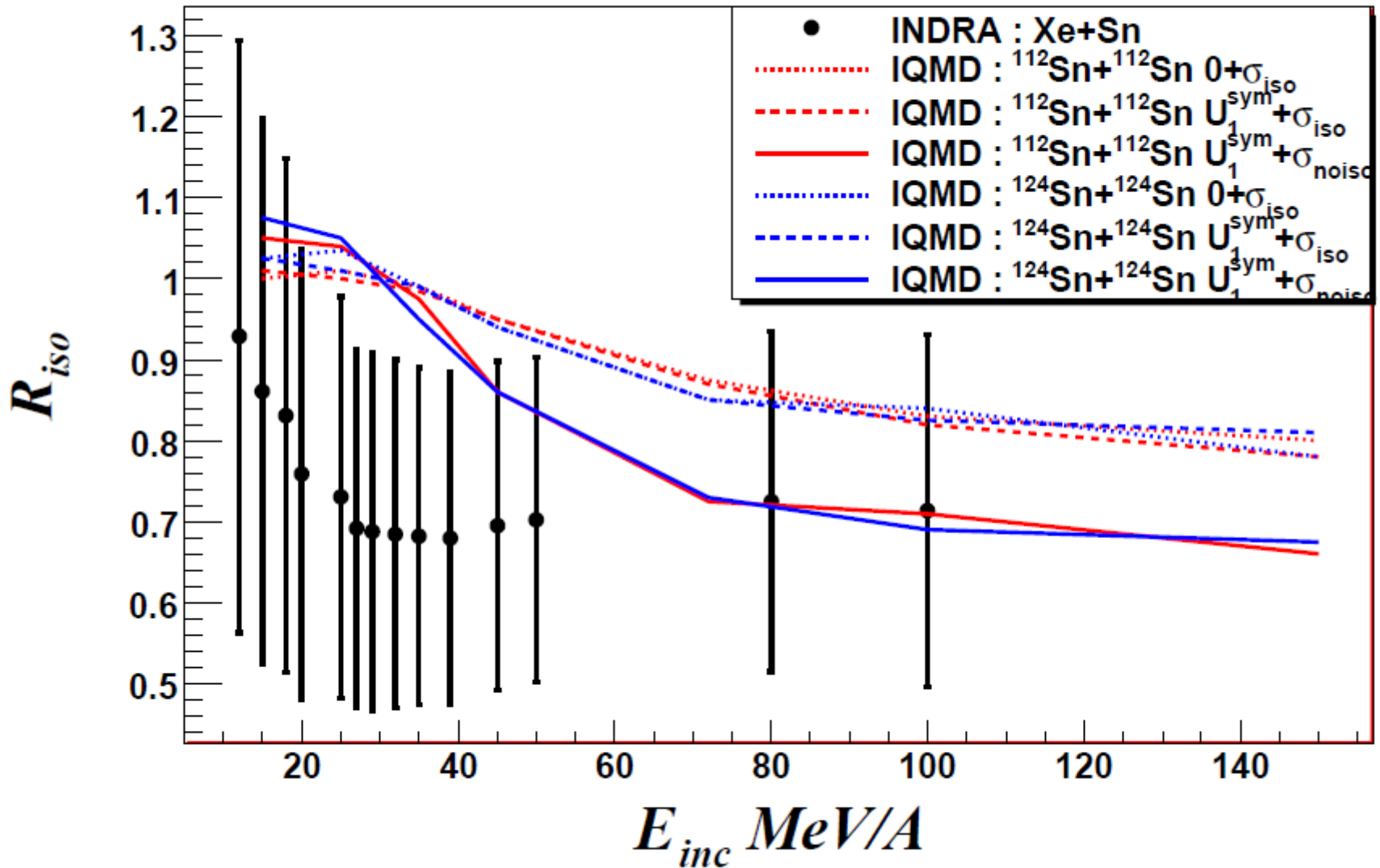
vartl

Yield (Z=1)

IQMD fails to reproduce vartl and yield for $E/A < 100$ MeV



Stringent test for transport model...



But here R_{iso} is determined after $t=200 \text{ fm/c}$, no fragment formation ...

Conclusions

- **Transparency** of nuclear matter is reported around Fermi Energy and above by looking at **isospin** and **energy ratios**
- **2 distinct mechanisms** for dissipation (Mean-Field/NN collisions) with a **sharp transition** around **30A MeV**
- no **isospin dependence** for the stopping : **isovector channels** for NN collision (nn/pp, np) ?
- at low energy : (bulk) **viscosity** can be accessed by studying stopping
- At high energy : λ_{NN} and σ_{NN} can be experimentally estimated :
 λ_{NN} is rather large ($\lambda_{NN} \approx 10-15 \text{ fm}$) and $\sigma_{NN}^{\text{in-medium}}$ close to $\sigma_{NN}^{\text{free}}$

Provide a **stringent benchmark** for any kind of transport model

-Request for comparison with microscopic transport models