

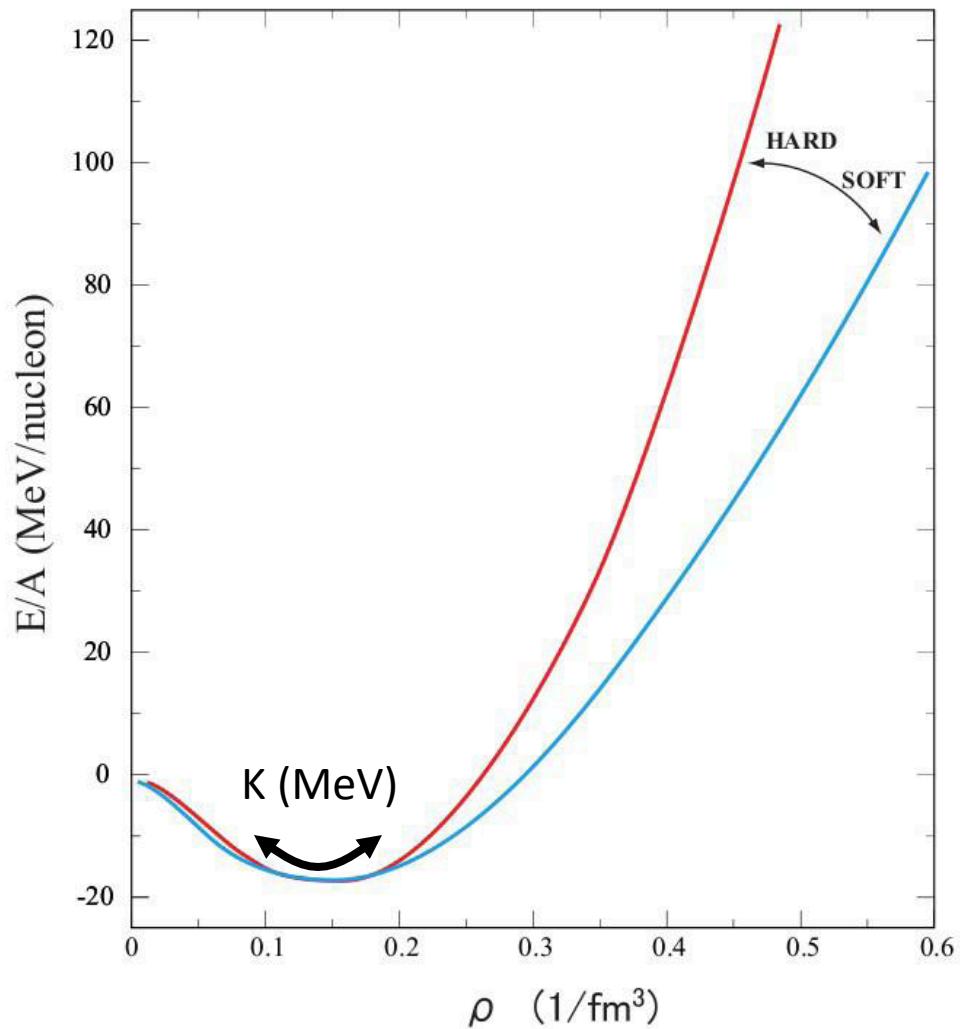
# The determination of the nuclear incompressibility

E. Khan

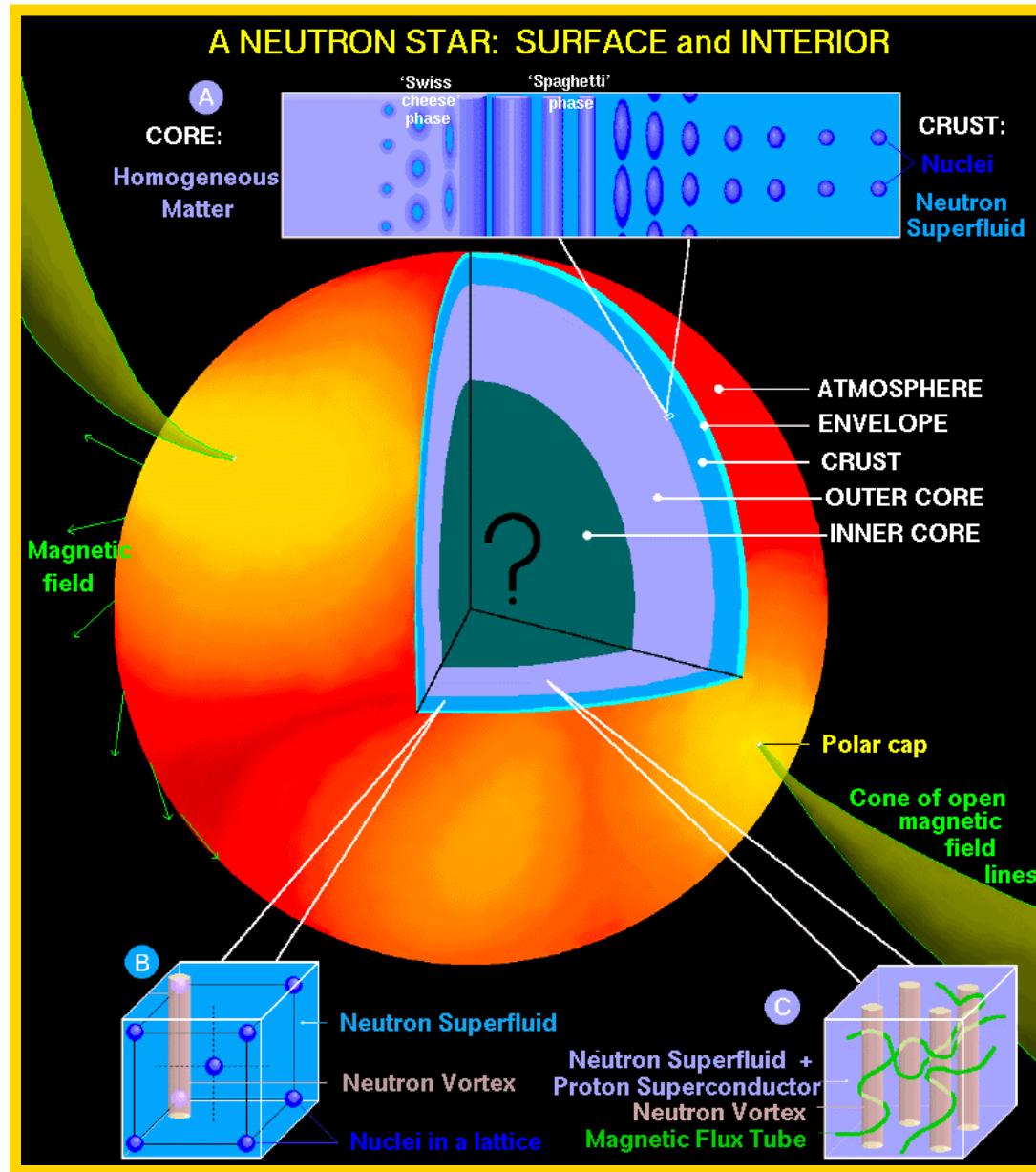


# Nuclear incompressibility

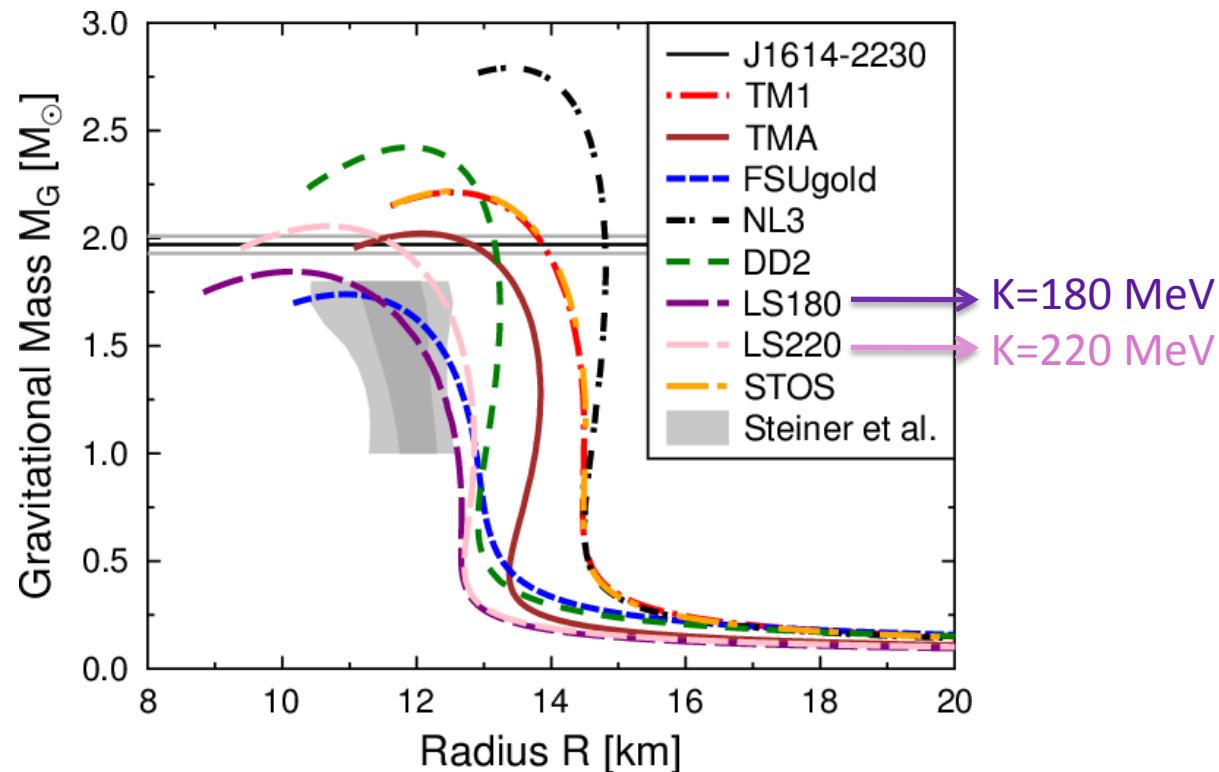
Incompressibility: energy needed to change the density of the nuclear matter around equilibrium



# Neutron stars

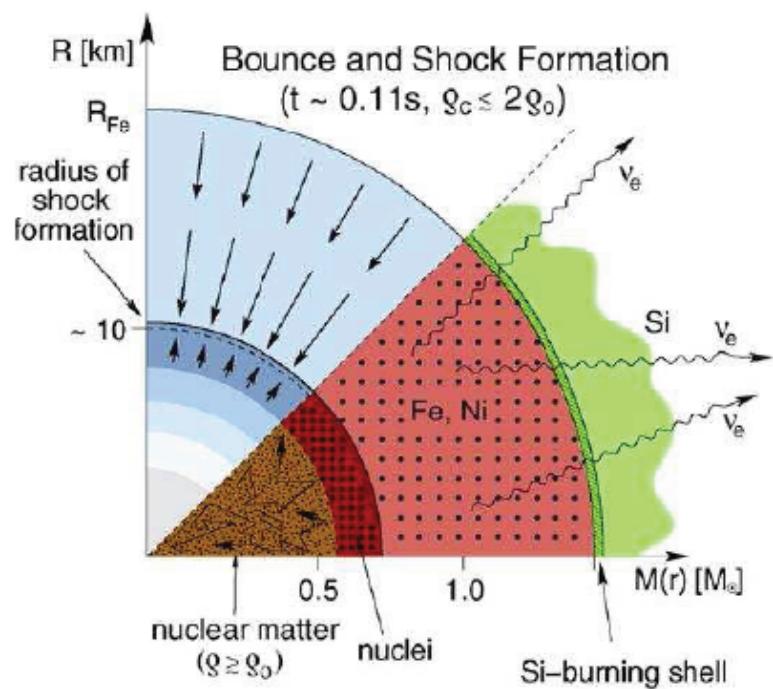


# Neutron stars

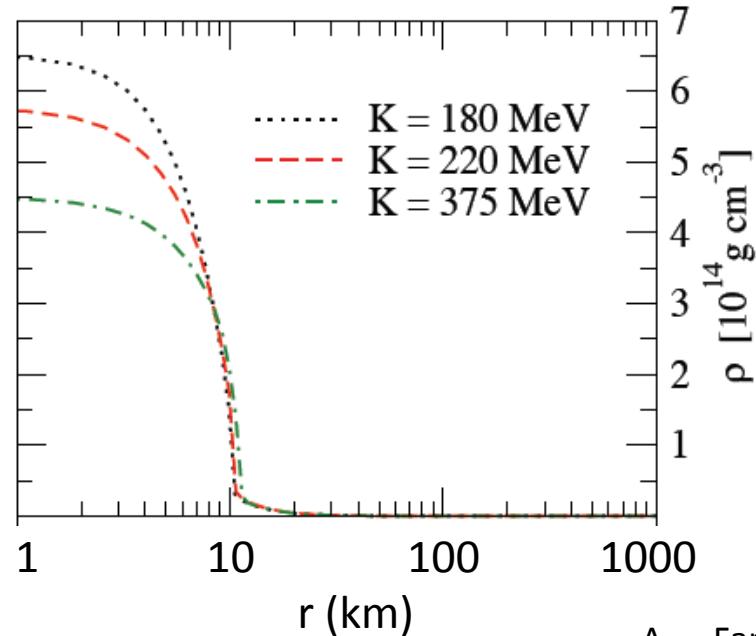


Matthias Hempel  
ITP Frankfurt

# SuperNovae bounce



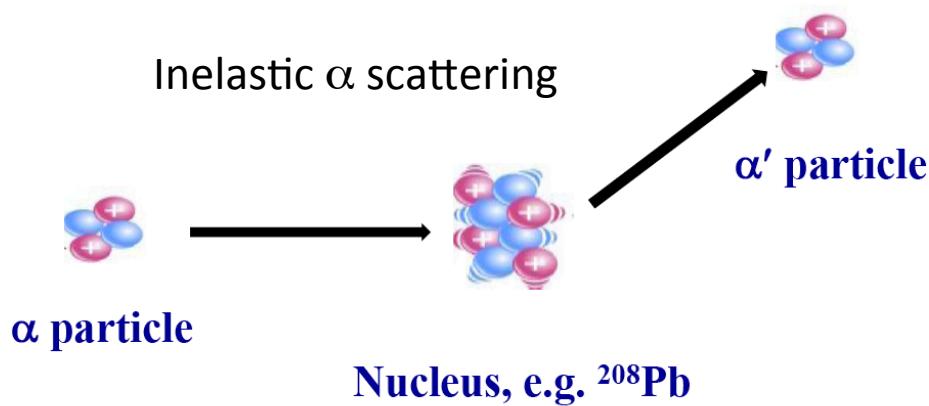
Density profile at bounce



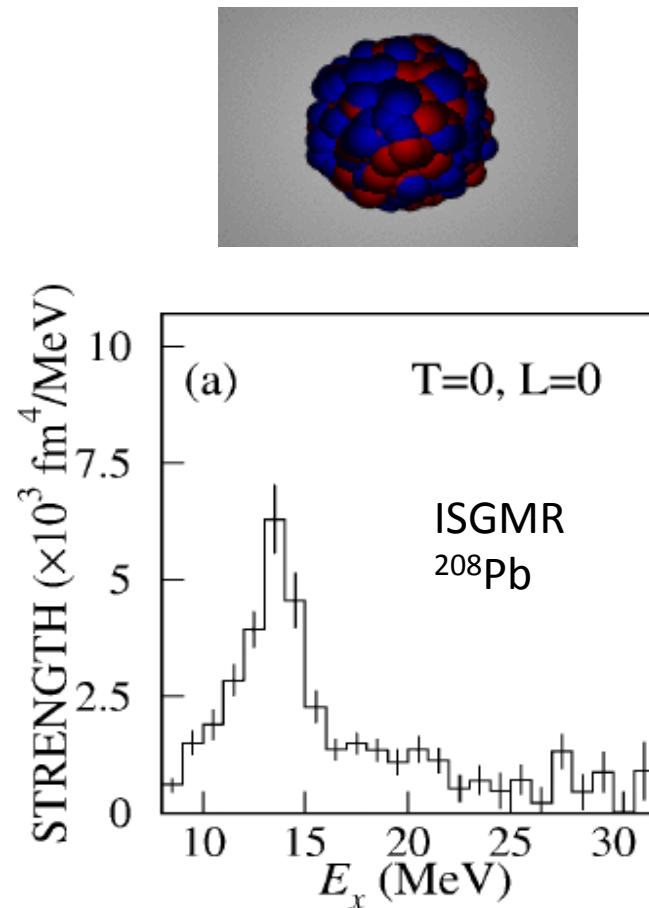
A. Fantina  
PhD (2010)  
IPNO-IAA

# Method to determine $K_\infty$

- The nucleus exhibits a compression mode (how lucky !):  
the Giant Monopole Resonance



- How to link  $E_{\text{GMR}}$  to  $K_\infty$  ?



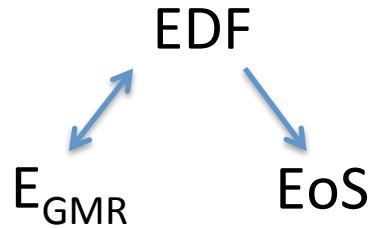
# 1) Macroscopic method

$$E_{ISGMR} = \sqrt{\frac{\hbar^2 K_A}{m \langle r^2 \rangle_m}},$$

$$K_A = K_\infty + K_{surf} A^{-1/3} + K_\tau \delta^2 + K_{Coul} \frac{Z^2}{A^{4/3}},$$

- Limitations : shell effects, data accuracy
- Necessity for a more accurate method

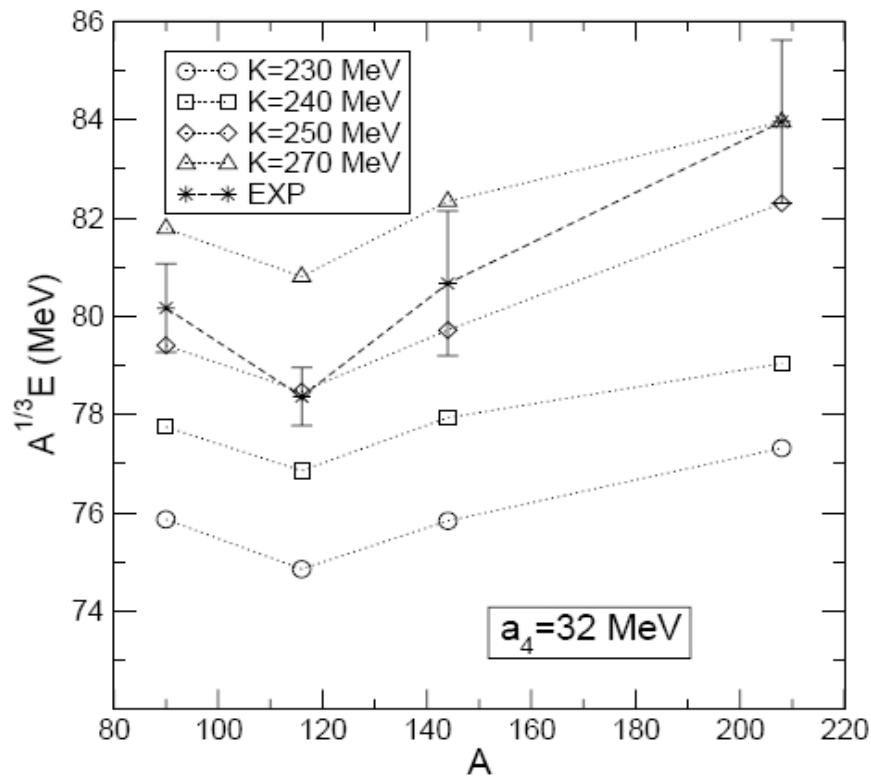
## 2) Microscopic method



- Nuclear structure models: from EDF to  $E_{GMR}$
- Limitations : all the terms (EoS) have to be correctly predicted at once

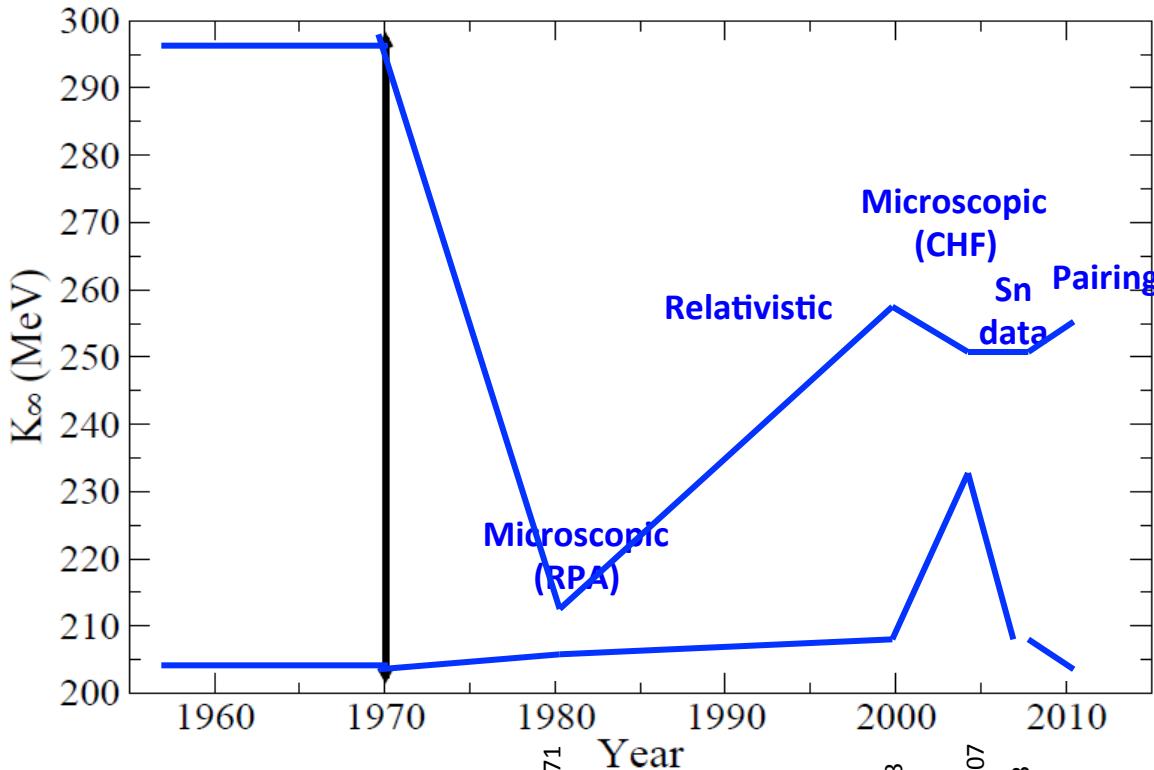
# From EDF to $E_{GMR}$

- HF, RMF, RPA, CHF : the only parameter is the EDF



D. Vretenar et al, PRC**68**(2003)024310

# Uncertainties on $K_\infty$



J.P. Blaizot, Phys. Rep. **64**(1980)171

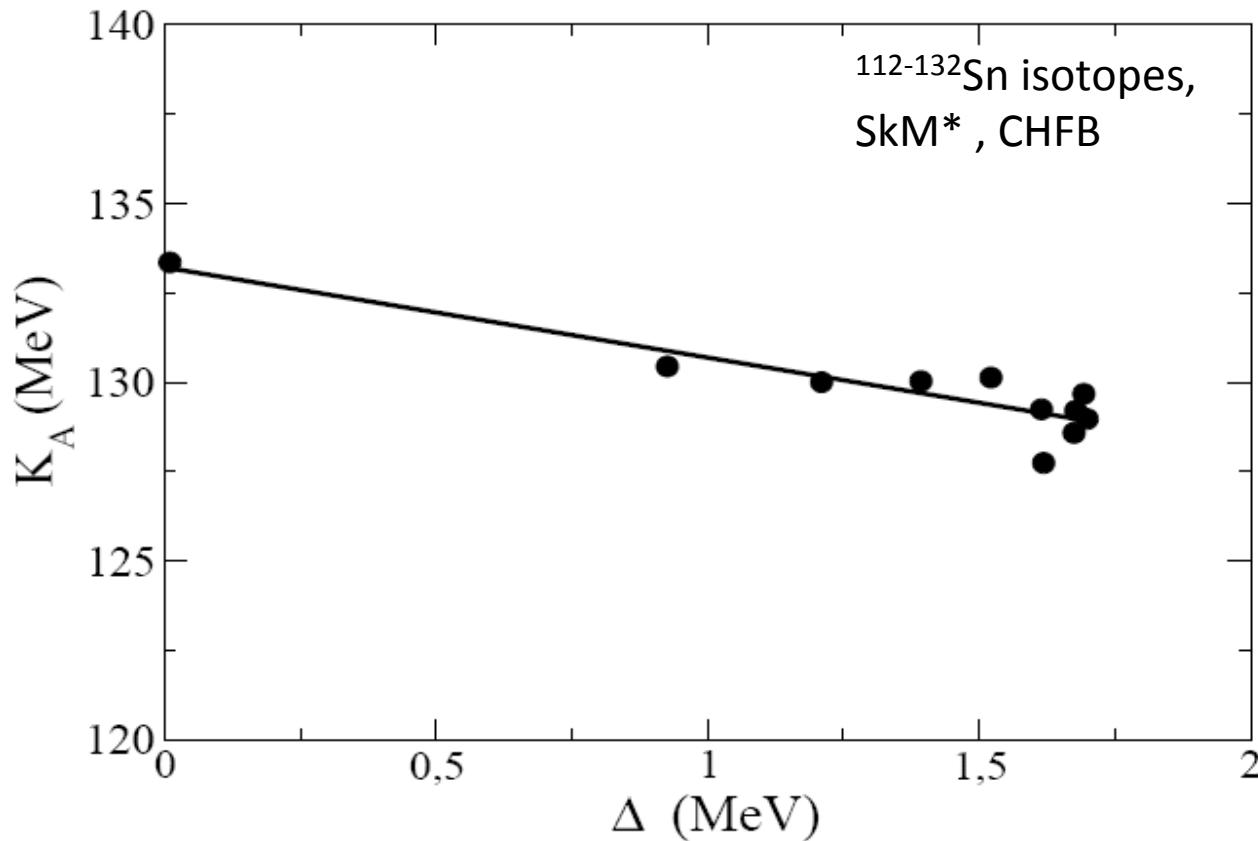
Z.Y. Ma et al, NPA**686**(2001)173

G. Colo et al, PRC**70**(2004)024307

J.Li et al, PRC**78**(2008)064303

E. Khan PRC**80**(2009)011307(R)

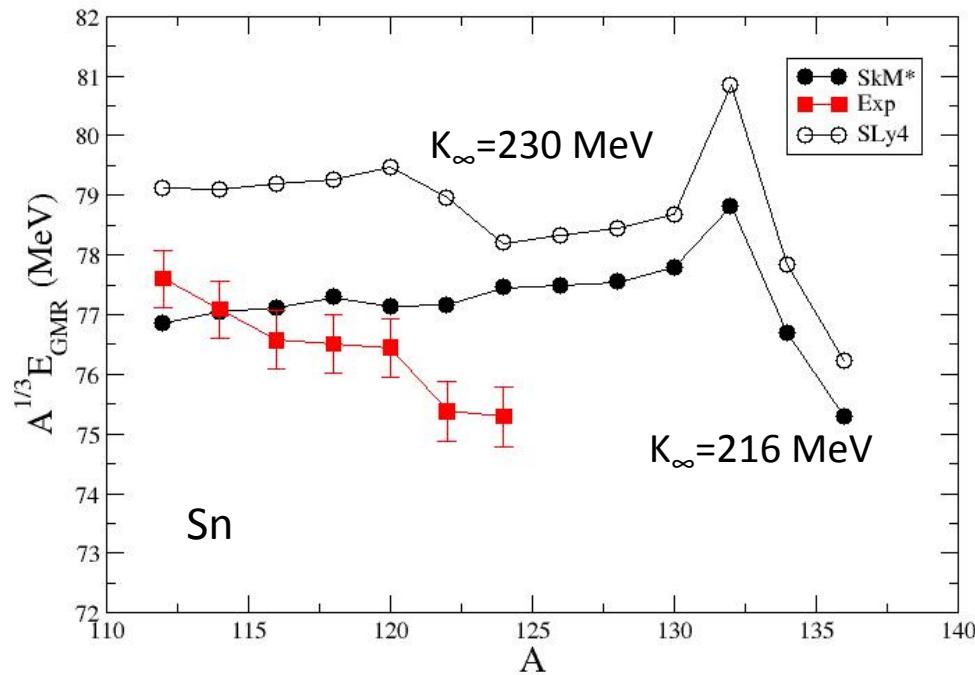
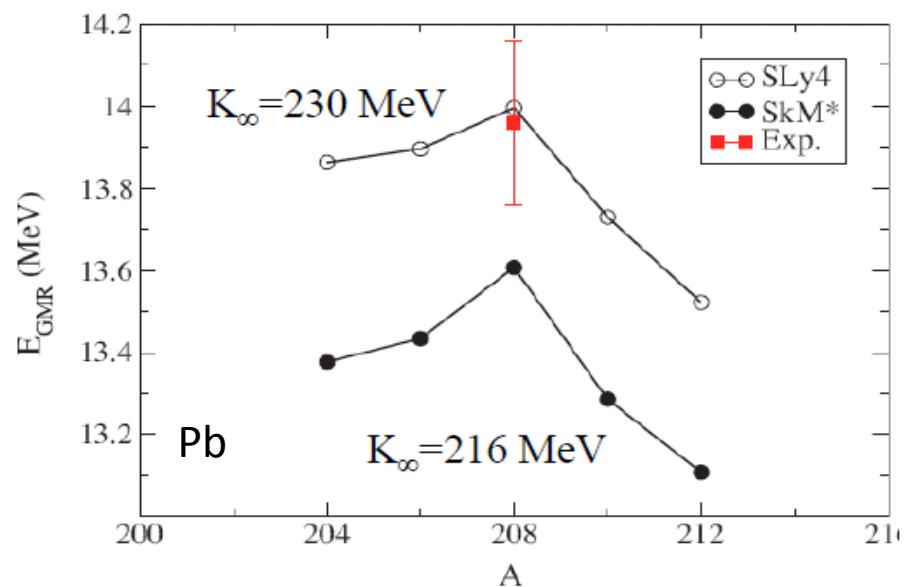
# Nuclear incompressibility vs. pairing



- Cooper pairs favor compressibility
- Incompressibility of **superfluid** nuclear matter:  $K_\infty(\Delta)$

# Pairing and shell effects on the GMR

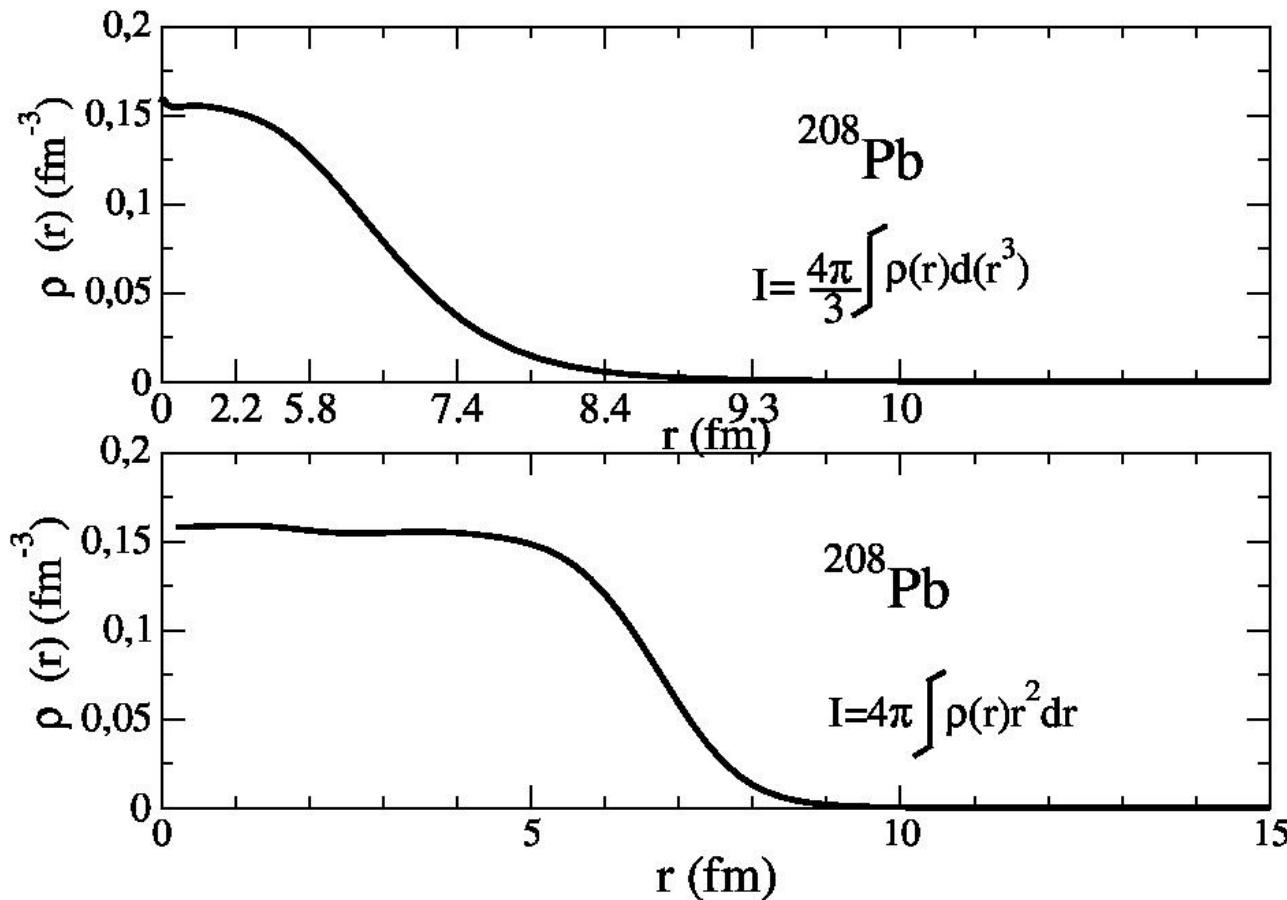
- Pairing  $\Rightarrow$  shell effects on the GMR value



E. Khan, PRC**80**(2009)011307(R)

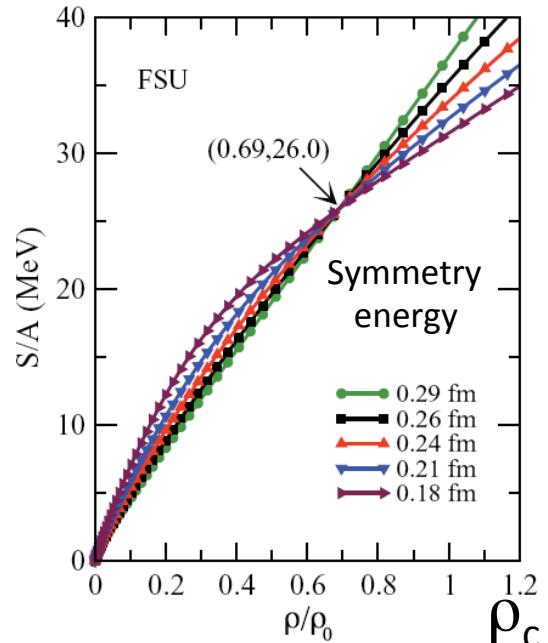
- Softness of Sn
- Necessity to measure isotopic chains, including unstable neutron-rich nuclei

# Saturation ?

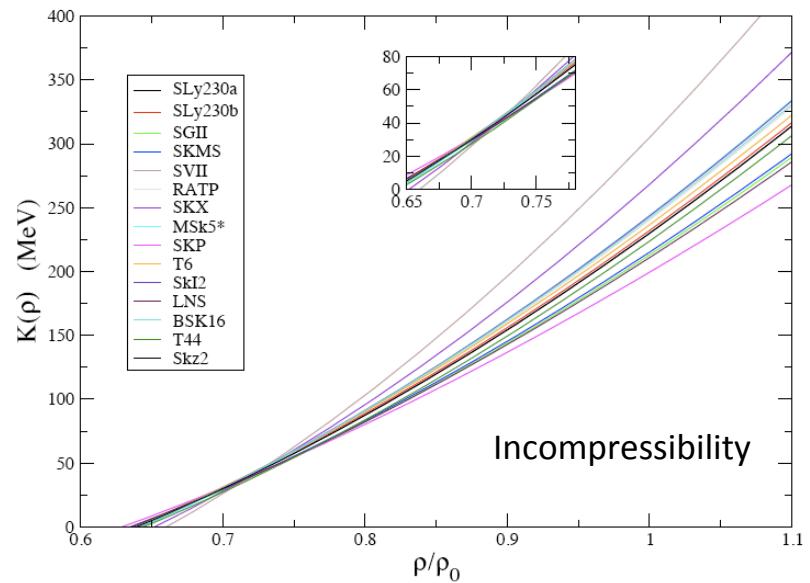
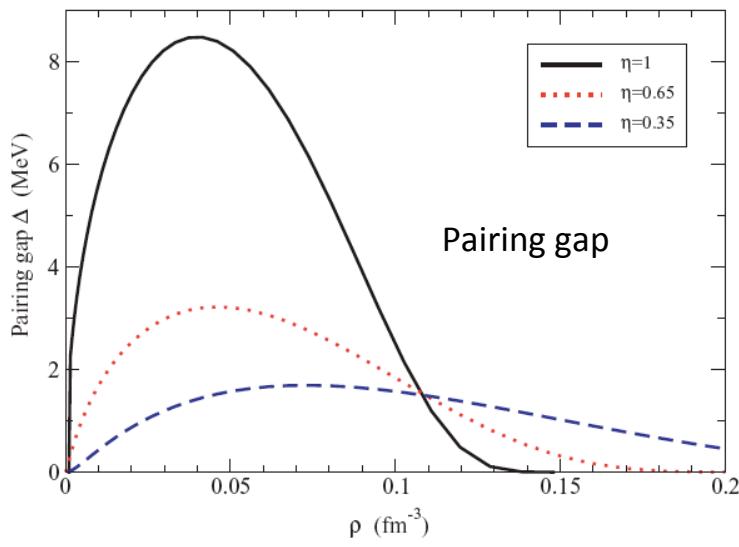
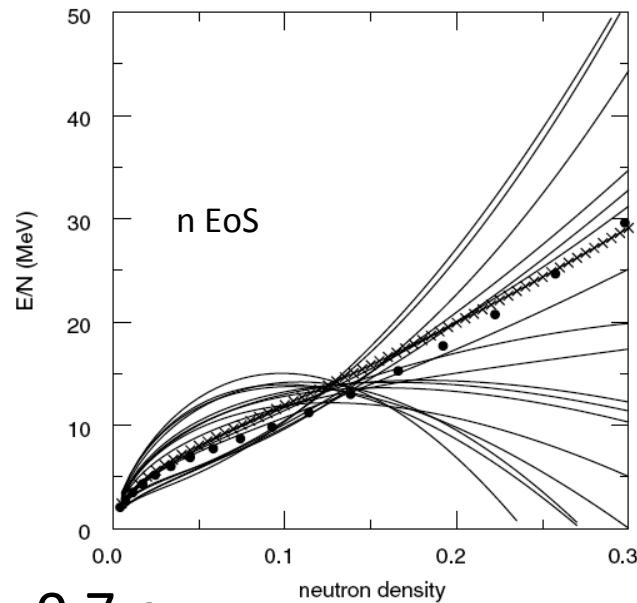


- Surface: 2/3 of nucleons in  $^{208}\text{Pb}$
- Saturation density area may not be the most probed

# The crossing density

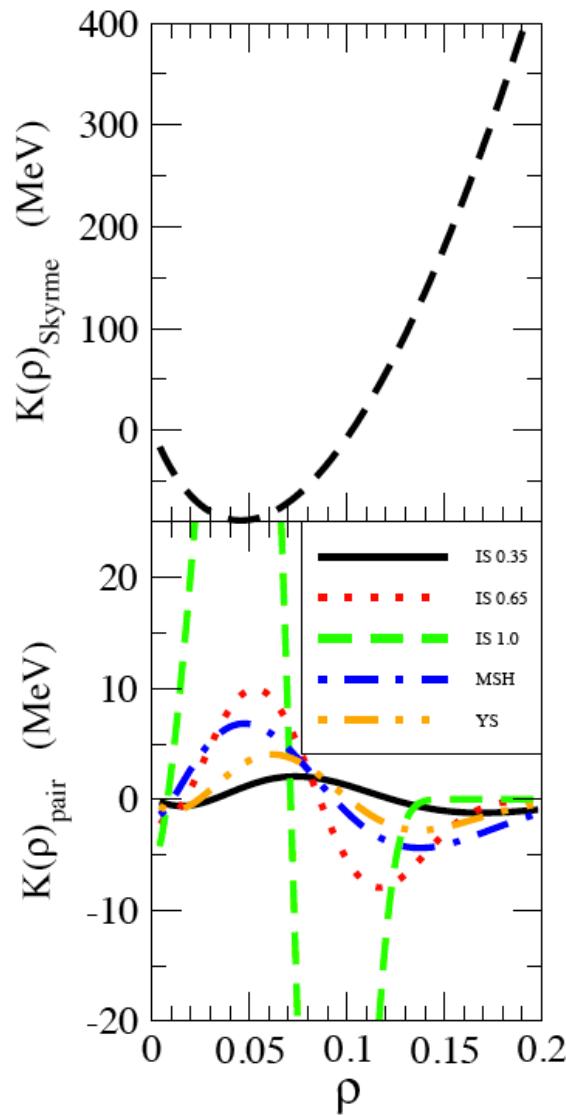


$$\rho_c \sim 0.11 \text{ fm}^{-3} = 0.7 \rho_0$$



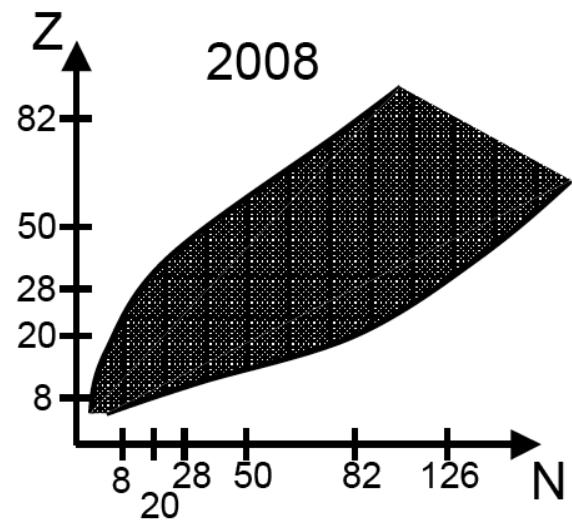
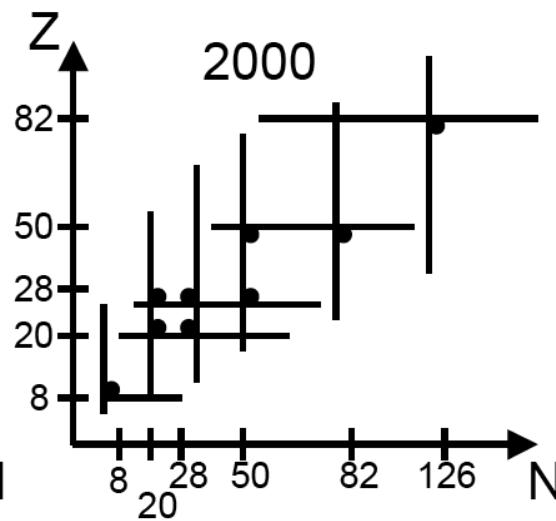
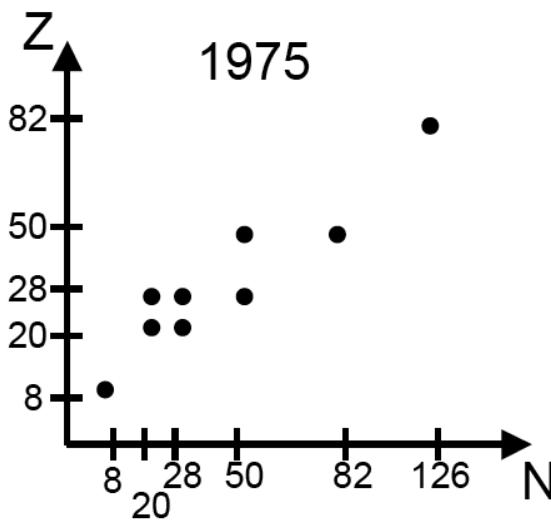
# Superfluidity acting on incompressibility

- Explains why superfluidity acts on incompressibility
- The microscopic method is necessary



Compressing nuclei  
from all over the nuclear chart

# Nuclear excitations

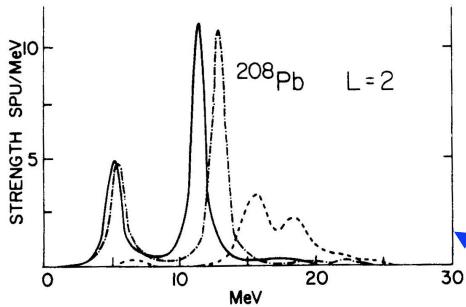
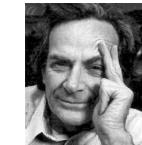


# Theory

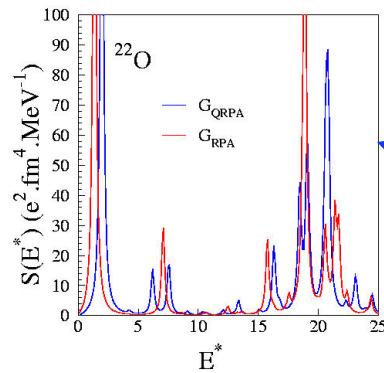
EDF

$E[\rho]$

HK theorem  
Skyrme  
Gogny



G.F. Bertsch and S.F. Tsai,  
Phys. Rev. C18 (1975) 125



E. Khan, Nguyen Van Giai,  
Phys. Lett. B472 (2000) 253

$$S = \int_{t_1}^{t_2} dt \int d\vec{r} (i\hbar \Psi^*(\vec{r}, t) \partial_t \Psi(\vec{r}, t) - E[\rho])$$

Action

Many-body  
problem

Magic  
nuclei

$$S = i\hbar \sum_{i=1}^A \int_{t_1}^{t_2} dt \int d\vec{r} (\varphi_i^*(\vec{r}, t) \partial_t \varphi_i(\vec{r}, t) - E[\rho])$$

Ind. Particles

Least action principle

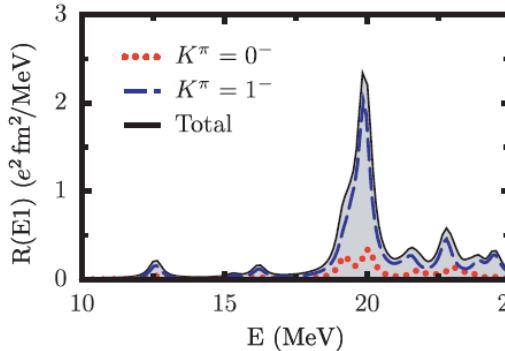
$$\delta S=0$$

TDHF

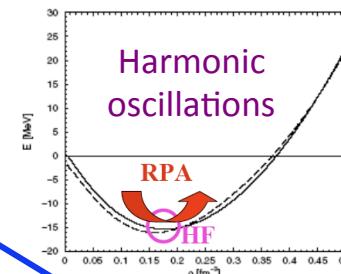
Linear  
response  
theory

$$i\hbar \partial_t \varphi_i = \frac{\delta E[\rho]}{\delta \rho} \varphi_i \hat{=} h \varphi_i$$

$$\Pi = \Pi_0 + \Pi_0 \frac{\delta h}{\delta \rho} \Pi$$



D. Pena Arteaga, P. Ring Phys.  
Rev. C77(2008) 034317

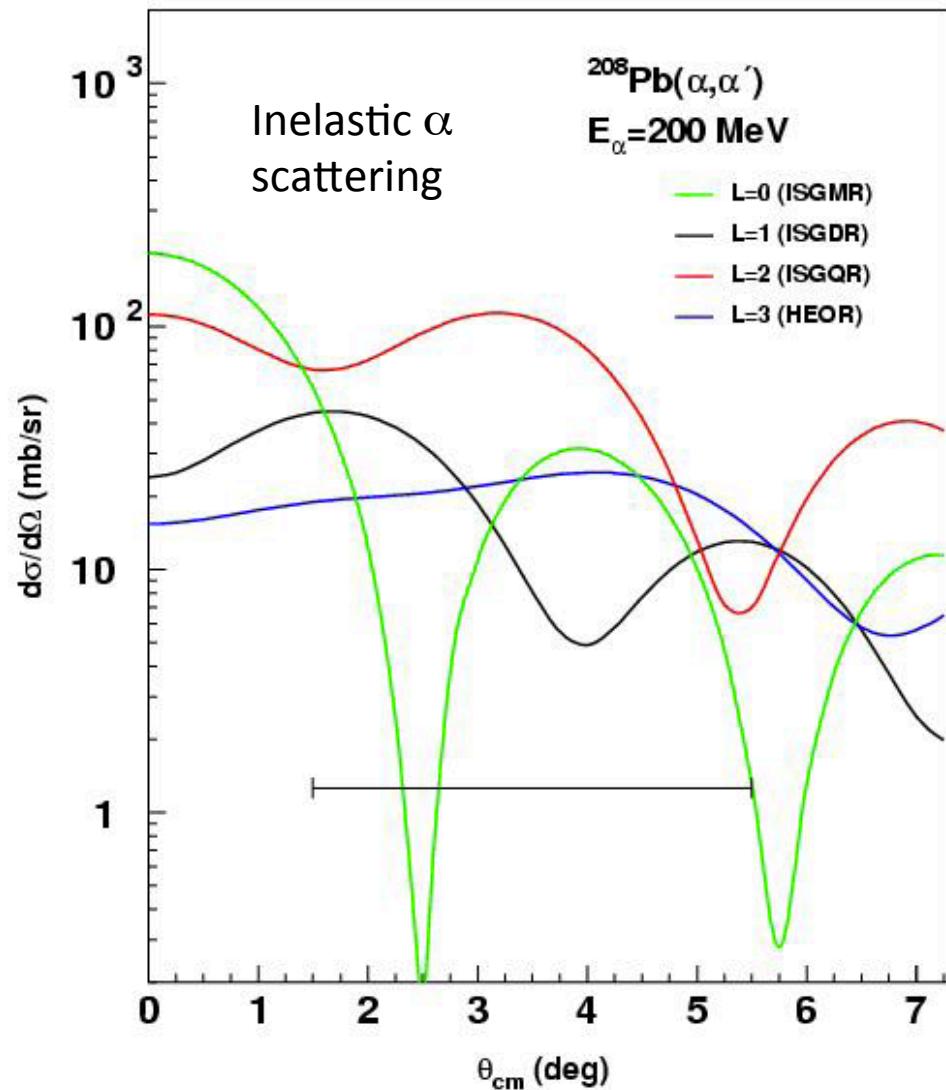


Deformed  
nuclei

Response  
function  $S(E^*)$

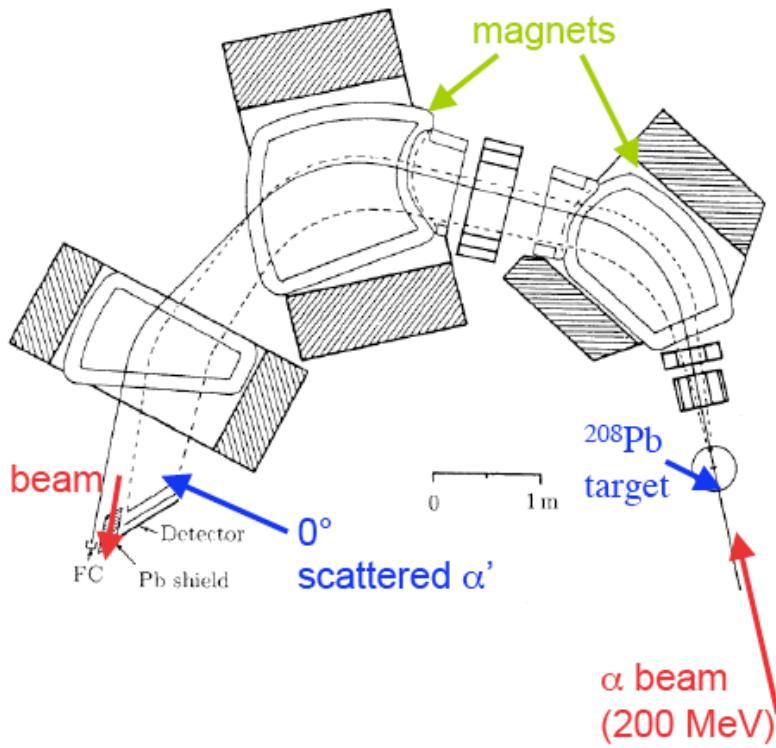
# Measurement of $E_{GMR}$

- Necessity for isotopic chains
- Measurement close to 0 deg. CM
- L separation using the angular distributions

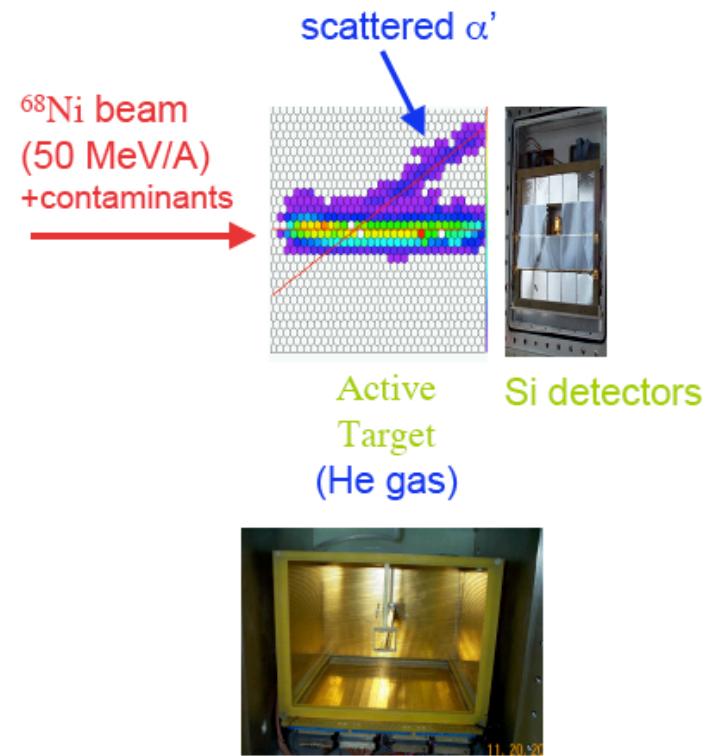


# Measurement of $E_{GMR}$

With stable nuclei

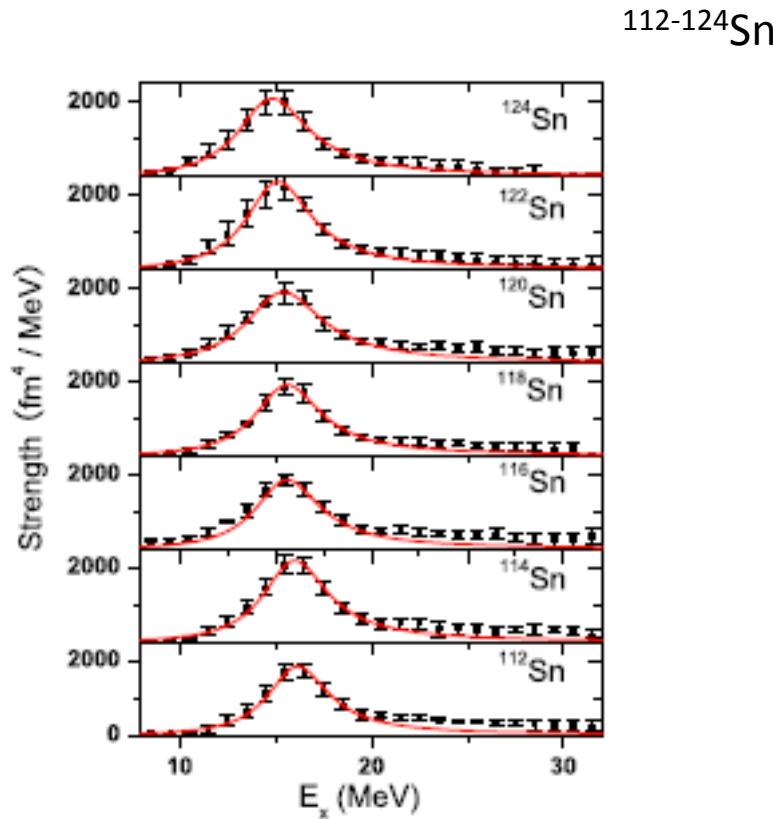


With exotic nuclei



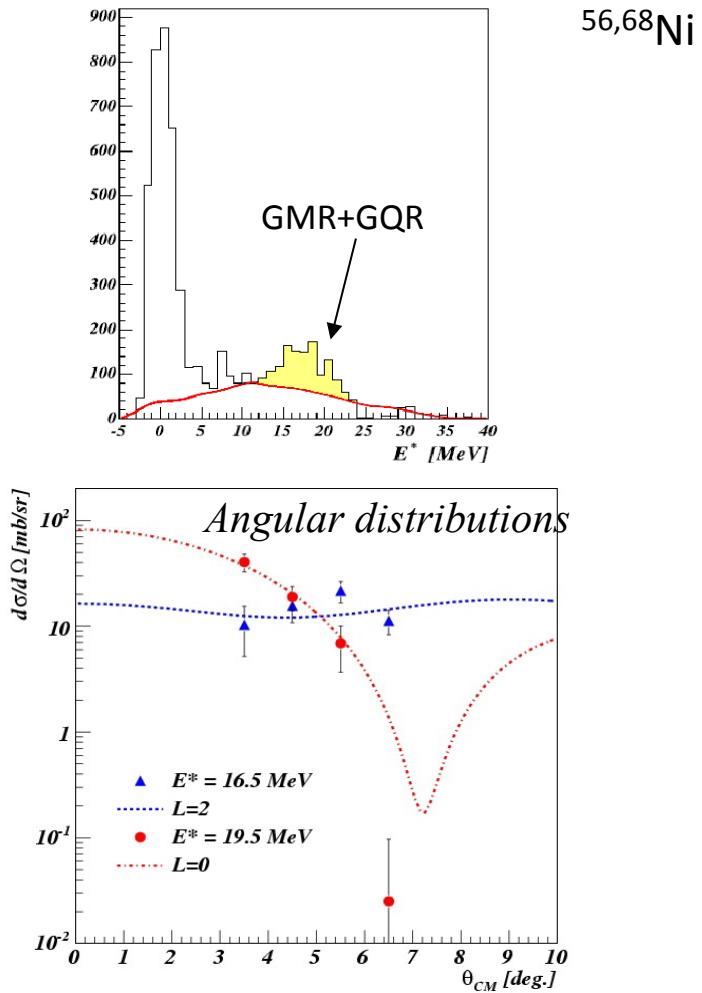
# Measurement of $E_{GMR}$

With stable nuclei



T. Li *et al.*, PRL99(2007)162503

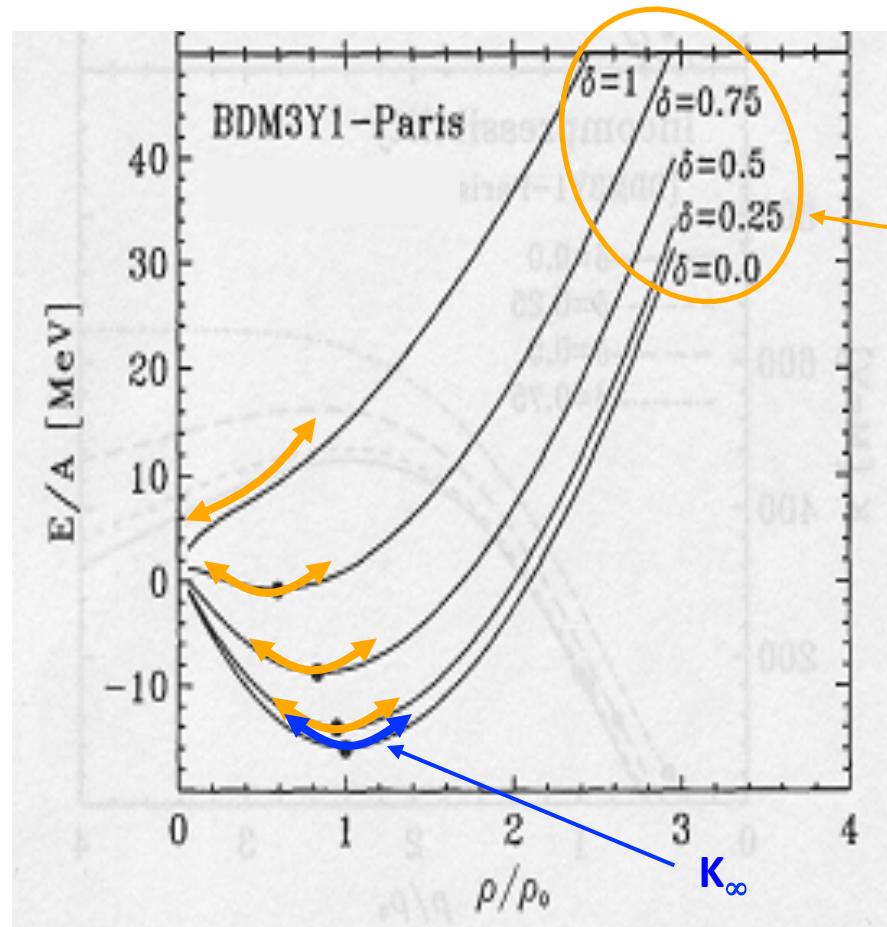
With exotic nuclei



C. Monrozeau *et al.*,  
PRL100(2008)042501

# Incompressibility and neutron excess

$$E(\rho, \delta) = E(\rho, 0) + a_{sym}(\rho)\delta^2$$
 : density and neutron excess  $\delta = (N-Z)/A$

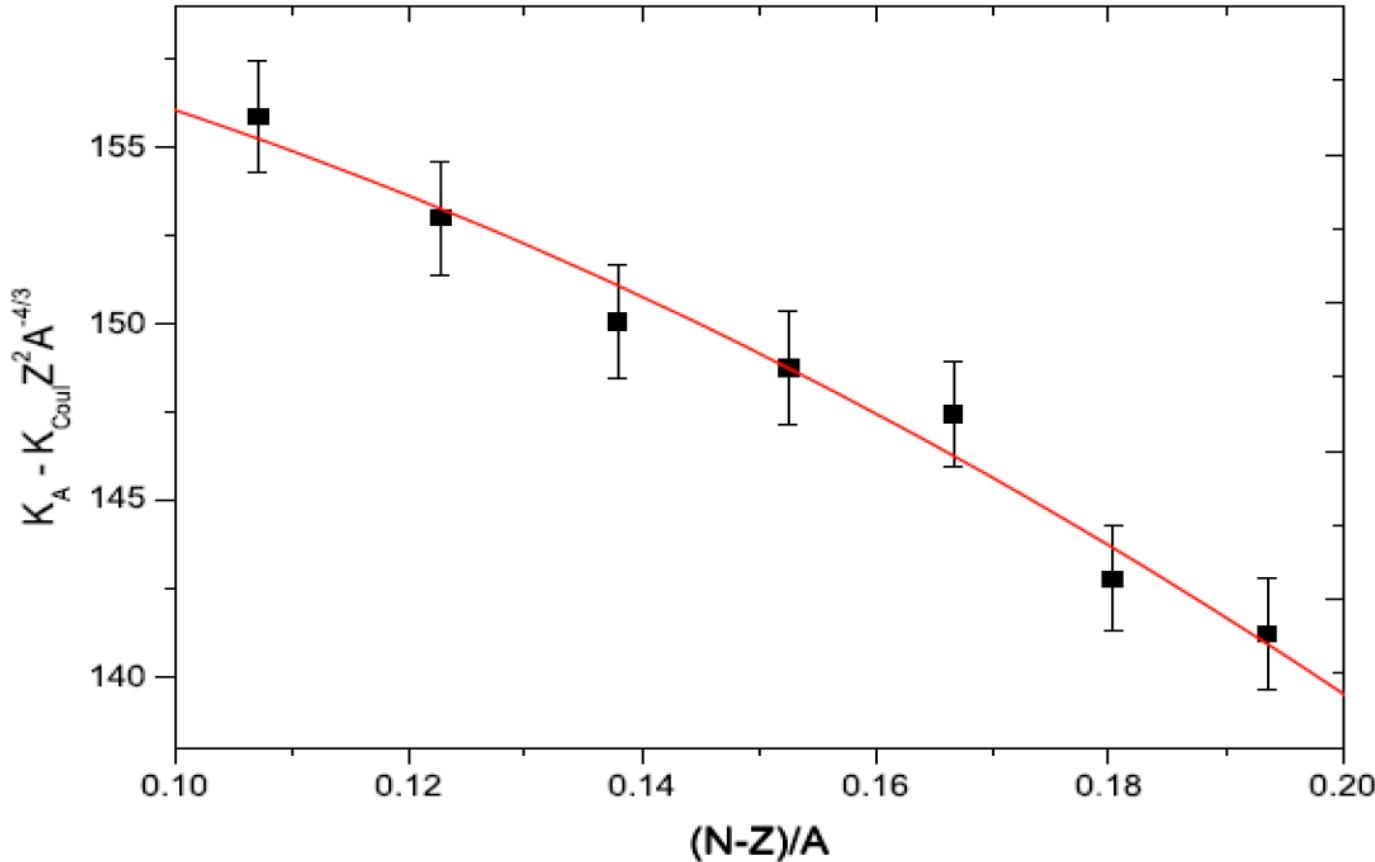


evolution of  
incompressibility  
with asymmetry:

$$K(\rho, \delta) \sim \frac{1}{2} \frac{\partial^2 E(\rho, \delta)}{\partial \rho^2} = K(\rho) + K_{sym}(\rho)\delta^2$$

$$K_{sym} = \left. \frac{1}{4} \frac{\partial^4 E(\rho, \delta)}{\partial \rho^2 \partial \delta^2} \right|_{\rho=\rho_0, \delta=0}$$

# Determining the isospin dependence of the incompressibility



- $K_\tau = -550 \pm 100$  MeV

- However the method is macroscopic

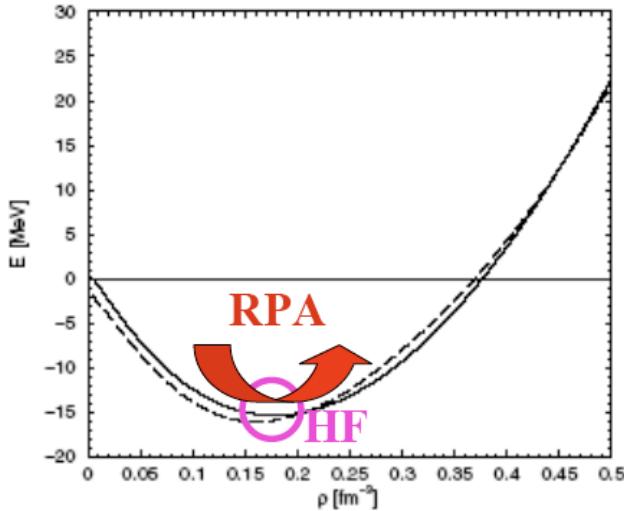
T. Li *et al.*, PRL 99(2007)162503

$$K_A = K_\infty + K_{surf} A^{-1/3} + K_\tau \delta^2 + K_{Coul} \frac{Z^2}{A^{4/3}},$$

# Conclusion

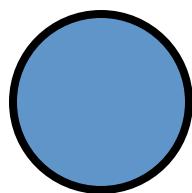
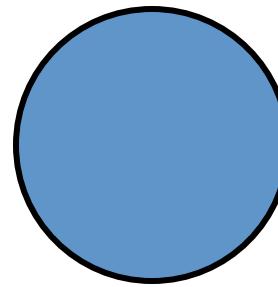
- Nuclear incompressibility has an impact on some astro quantities: neutron stars and SN bounce
- Nuclei have a compression mode : GMR !
- Macro: easy but not very reliable
- Micro:  $K_\infty = 240 \pm 30$  MeV
- Status: superfluidity effect, crossing density, Pb vs Sn softness
- Need to measure the GMR in isotopic chains including neutron-rich nuclei
- Isospin dep. of incompressibility : only macro:  $K_\tau = -550 \pm 100$  MeV  
micro needs more data to constrain the EDF

# Picture of a GMR



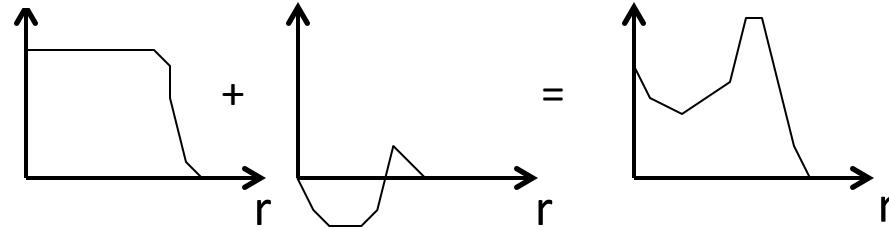
$$\rho(r, t) = \rho(r) + \delta\rho(r)\cos(\omega t)$$

GMR



transition density

$$\rho(r) + \delta\rho(r) = \rho(r, 0)$$



- GR are collective (many ph pairs involved)
- Small amplitude vibration:  $\delta\rho \ll \rho$

$$\delta\rho(r) = \sum_{mi} (X_{mi} - Y_{mi}) \phi_i^*(r) \phi_m(r)$$