

# Derivation of effective interactions

Angelo Signoracci

CEA/Saclay

Lecture 7, 15 May 2013

# Outline

- 1 Generalities
- 2 Empirical interactions
- 3 Non-empirical interactions

# Outline

- 1 Generalities
- 2 Empirical interactions
- 3 Non-empirical interactions

## Brief Review

- Microscopic bare interactions ( $NN$  and  $NNN$ ) have been derived and fit to data
- Separation into components depends on renormalization scheme
- Bare interactions reproduce  $NN$  scattering data up to 300-350 MeV
- Not constrained by theory or experiment for higher energies
- For purpose of these tutorials, assume accurate bare interactions
- In reduced model space, require an effective interaction
  - Must incorporate effects from outside the model space
  - Components: one-body (SPE) and two-body (TBME)
  - Explicit three-body excluded due to computational difficulties
  - Inclusion of effects at one- and two-body level?
- For historical effective interactions
  - Calculations deteriorate with increasing number of valence particles
  - Claimed that microscopic effective interactions are not practical
- Today, effective two-body component of three-body forces improves results
- Empirical correction to monopole terms provides satisfactory results
- Phenomenologically adusted effective interactions typically used for calculations
- Does not make general CI theory phenomenological!
- RG methods and MBPT provide prescriptions to construct effective interactions

## Brief Review

- Microscopic bare interactions ( $NN$  and  $NNN$ ) have been derived and fit to data
- Separation into components depends on renormalization scheme
- Bare interactions reproduce  $NN$  scattering data up to 300-350 MeV
- Not constrained by theory or experiment for higher energies
- For purpose of these tutorials, assume accurate bare interactions
- **In reduced model space, require an effective interaction**
  - Must incorporate effects from outside the model space
  - Components: one-body (SPE) and two-body (TBME)
  - Explicit three-body excluded due to computational difficulties
  - Inclusion of effects at one- and two-body level?
- For historical effective interactions
  - Calculations deteriorate with increasing number of valence particles
  - Claimed that microscopic effective interactions are not practical
- Today, effective two-body component of three-body forces improves results
- Empirical correction to monopole terms provides satisfactory results
- Phenomenologically adusted effective interactions typically used for calculations
- Does not make general CI theory phenomenological!
- RG methods and MBPT provide prescriptions to construct effective interactions

## Brief Review

- Microscopic bare interactions ( $NN$  and  $NNN$ ) have been derived and fit to data
- Separation into components depends on renormalization scheme
- Bare interactions reproduce  $NN$  scattering data up to 300-350 MeV
- Not constrained by theory or experiment for higher energies
- For purpose of these tutorials, assume accurate bare interactions
- **In reduced model space, require an effective interaction**
  - Must incorporate effects from outside the model space
  - Components: one-body (SPE) and two-body (TBME)
  - Explicit three-body excluded due to computational difficulties
  - Inclusion of effects at one- and two-body level?
- **For historical effective interactions**
  - Calculations deteriorate with increasing number of valence particles
  - Claimed that microscopic effective interactions are not practical
- Today, effective two-body component of three-body forces improves results
- Empirical correction to monopole terms provides satisfactory results
- Phenomenologically adusted effective interactions typically used for calculations
- Does not make general CI theory phenomenological!
- RG methods and MBPT provide prescriptions to construct effective interactions

## Brief Review

- Microscopic bare interactions ( $NN$  and  $NNN$ ) have been derived and fit to data
- Separation into components depends on renormalization scheme
- Bare interactions reproduce  $NN$  scattering data up to 300-350 MeV
- Not constrained by theory or experiment for higher energies
- For purpose of these tutorials, assume accurate bare interactions
- **In reduced model space, require an effective interaction**
  - Must incorporate effects from outside the model space
  - Components: one-body (SPE) and two-body (TBME)
  - Explicit three-body excluded due to computational difficulties
  - Inclusion of effects at one- and two-body level?
- For historical effective interactions
  - Calculations deteriorate with increasing number of valence particles
  - Claimed that microscopic effective interactions are not practical
- Today, effective two-body component of three-body forces improves results
- Empirical correction to monopole terms provides satisfactory results
- Phenomenologically adusted effective interactions typically used for calculations
- Does not make general CI theory phenomenological!
- RG methods and MBPT provide prescriptions to construct effective interactions

## Brief Review

- Microscopic bare interactions ( $NN$  and  $NNN$ ) have been derived and fit to data
- Separation into components depends on renormalization scheme
- Bare interactions reproduce  $NN$  scattering data up to 300-350 MeV
- Not constrained by theory or experiment for higher energies
- For purpose of these tutorials, assume accurate bare interactions
- **In reduced model space, require an effective interaction**
  - Must incorporate effects from outside the model space
  - Components: one-body (SPE) and two-body (TBME)
  - Explicit three-body excluded due to computational difficulties
  - Inclusion of effects at one- and two-body level?
- For historical effective interactions
  - Calculations deteriorate with increasing number of valence particles
  - Claimed that microscopic effective interactions are not practical
- Today, effective two-body component of three-body forces improves results
- Empirical correction to monopole terms provides satisfactory results
- Phenomenologically adusted effective interactions typically used for calculations
- **Does not make general CI theory phenomenological!**
- RG methods and MBPT provide prescriptions to construct effective interactions



## Brief Review

- Microscopic bare interactions ( $NN$  and  $NNN$ ) have been derived and fit to data
- Separation into components depends on renormalization scheme
- Bare interactions reproduce  $NN$  scattering data up to 300-350 MeV
- Not constrained by theory or experiment for higher energies
- For purpose of these tutorials, assume accurate bare interactions
- **In reduced model space, require an effective interaction**
  - Must incorporate effects from outside the model space
  - Components: one-body (SPE) and two-body (TBME)
  - Explicit three-body excluded due to computational difficulties
  - Inclusion of effects at one- and two-body level?
- For historical effective interactions
  - Calculations deteriorate with increasing number of valence particles
  - Claimed that microscopic effective interactions are not practical
- Today, effective two-body component of three-body forces improves results
- Empirical correction to monopole terms provides satisfactory results
- Phenomenologically adusted effective interactions typically used for calculations
- Does not make general CI theory phenomenological!
- **RG methods and MBPT provide prescriptions to construct effective interactions**

# Outline

- 1 Generalities
- 2 Empirical interactions**
- 3 Non-empirical interactions

# Parameterization of interaction: Two main schemes

- 1 Unconstrained parameterization
  - Interaction completely unknown
  - Treat all SPE and TBME as parameters
  - 66 (199) parameters in  $sd$  ( $pf$ ) shell
  - Parameters become correlated through fit to data
  - Complicated fitting procedure required (singular value decomposition)
- 2 Constrained parameterization
  - Select fewer parameters to vary
  - For instance, only treat monopoles as free parameters
    - 6 (10) parameters in  $sd$  ( $pf$ ) shell
    - Standard fitting procedures sufficient
  - Another popular procedure: fix (not fit) to experimental data
    - Fix one-body terms (SPE) to core + one nucleon
    - Fix two-body terms (TBME) to core + two nucleons

## Example: $^{17}\text{O}$ and $^{18}\text{O}$ data

- For the  $sd$  shell, outside of the doubly magic  $^{16}\text{O}$  core
  - Use data from  $^{17}\text{O}$  and  $^{18}\text{O}$  to determine effective interaction for neutrons

$$E(^{17}\text{O}; 5/2^+) - E(^{16}\text{O}; g.s.) = -4.14\text{MeV} \equiv \epsilon(0d_{5/2})(\text{SPE})$$

$$E(^{17}\text{O}; 1/2^+) - E(^{16}\text{O}; g.s.) = -3.27\text{MeV} \equiv \epsilon(1s_{1/2})(\text{SPE})$$

$$E(^{17}\text{O}; 3/2^+) - E(^{16}\text{O}; g.s.) = 0.94\text{MeV} \equiv \epsilon(0d_{3/2})(\text{SPE})$$

$$\begin{aligned} E(^{18}\text{O}; g.s.) - E(^{16}\text{O}; g.s.) &= -12.19\text{MeV} \\ &\equiv 2\epsilon(0d_{5/2}) + \langle (0d_{5/2}0d_{5/2})_{J=0} | V_{ms} | (0d_{5/2}0d_{5/2})_{J=0} \rangle \end{aligned}$$

$$\vdots$$

- Can obtain most important TBME in this way

$$\langle (0d_{5/2}0d_{5/2})_{J=0} | V_{ms} | (0d_{5/2}0d_{5/2})_{J=0} \rangle = -3.91\text{MeV} \text{ (TBME)}$$

- For the remainder, G-matrix result typically used

# Fitting procedure

- 1 Select model space of interest
- 2 Select free parameters to fit (constrained vs. unconstrained)
- 3 Select experimental data within model space for fit (typically, energy levels)
- 4 Initialize parameters with “microscopic” input, i.e. from RG + MBPT methods
- 5 Iterate by minimizing deviation with respect to data

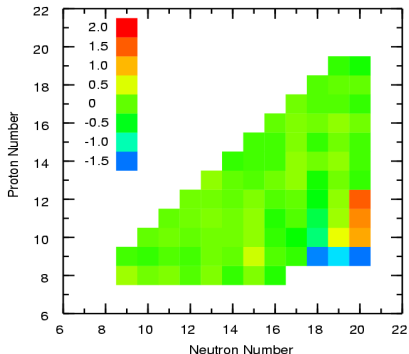
## Example: USDA and USDB interactions

- Empirical universal  $sd$  (USD) interaction created around 1980
- As experimental capabilities extended further from stability
  - Reached nuclei beyond those included in the fit
  - Large disagreements for exotic nuclei
  - Predictive power lost in fitting procedure

## Example: USDA and USDB interactions

- Empirical universal  $sd$  (USD) interaction created around 1980
- As experimental capabilities extended further from stability

$$BE_{exp}(Z, N) - BE_{th}(Z, N)$$



New interactions needed within  $sd$  shell!

## Example: USDA and USDB interactions

- Brown and Richter undertook this task<sup>a</sup>
- 608 energy levels in *sd* shell with uncertainty  $\sigma \leq 200$  keV compiled
- Procedure:

$$\begin{aligned}
 H(n=0) &= \text{SPE}(\text{exp}) + \text{TBME}(\text{G-matrix}) \\
 &\equiv P_i(n=0) \\
 i = 1 - 3 \quad P_i(n) &= \text{SPE}(n) \\
 i = 4 - 66 \quad P_i(n) &= \frac{18^{0.3}}{A} \text{TBME}(n) \\
 \{E_k(n)\} &= \langle \Psi_k | H(n) | \Psi_k \rangle \xrightarrow{\text{SVD}} P_i(n+1)
 \end{aligned}$$

- Iteration number  $n$  increased until convergence
- Mass-dependence due to G-matrix formalism, but phenomenological

<sup>a</sup>B.A. Brown and W. Richter, Phys. Rev. C **74**, 034315 (2006)



## Example: USDA and USDB interactions

- Brown and Richter undertook this task<sup>a</sup>
- 608 energy levels in *sd* shell with uncertainty  $\sigma \leq 200$  keV compiled
- USDA (USDB) found from 30 (56) linear combinations of correlated parameters
- Two interactions provide a way to estimate theoretical errors
- USDA
  - More conservative
  - Smaller rms deviation from input G-matrix values
  - 170 keV rms deviation to experimental data (global rms)
- USDB
  - More accurate
  - Also determined by plateau in deviation as function of linear parameters varied
  - 126 keV global rms deviation

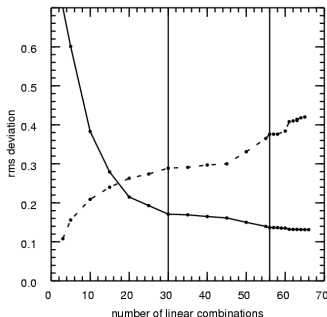
---

<sup>a</sup>B.A. Brown and W. Richter, Phys. Rev. C **74**, 034315 (2006)

## Example: USDA and USDB interactions

- Brown and Richter undertook this task<sup>a</sup>
- 608 energy levels in  $sd$  shell with uncertainty  $\sigma \leq 200$  keV compiled

$$BE_{exp}(Z, N) - BE_{th}(Z, N)$$



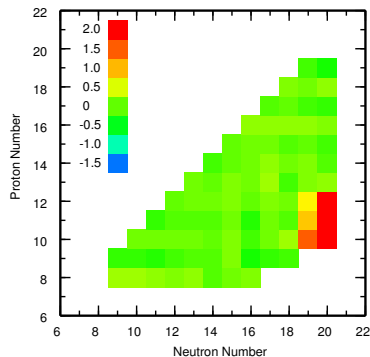
- Two interactions created based on plateau in rms deviations
- USDA more conservative (closer to G-matrix)
- USDB more accurate (smaller deviation to experimental data)

<sup>a</sup>B.A. Brown and W. Richter, Phys. Rev. C **74**, 034315 (2006)

## Example: USDA and USDB interactions

- Brown and Richter undertook this task<sup>a</sup>
- 608 energy levels in *sd* shell with uncertainty  $\sigma \leq 200$  keV compiled

$$BE_{exp}(Z, N) - BE_{th}(Z, N)$$



- Improvement relative to USD interaction
- Still underbound for some exotic nuclei  $\rightarrow$  island of inversion region (see lecture 1)

<sup>a</sup>B.A. Brown and W. Richter, Phys. Rev. C **74**, 034315 (2006)

# Outline

- 1 Generalities
- 2 Empirical interactions
- 3 Non-empirical interactions**

# Motivation

- Empirical interactions are only predictive within fitting data
- Continually improve by refitting as new energy levels are observed
- Lengthy, difficult procedure to determine effective interactions
  - Requires compilation of hundreds of data
  - Iterative procedure is prohibitive for larger model spaces
  - Each model space requires this procedure
- **Microscopic procedures not tuned**
- Assuming sufficient data, cannot improve upon empirical parameterization
- Improvements
  - ① Less time-consuming procedure to determine effective interactions
  - ② No limitations on model space (number of parameters vs. data points)
  - ③ Theoretical error given by aspects excluded from RG+MBPT
  - ④ Method for explicitly determining three-body contribution

# Motivation

- Empirical interactions are only predictive within fitting data
- Continually improve by refitting as new energy levels are observed
- Lengthy, difficult procedure to determine effective interactions
  - Requires compilation of hundreds of data
  - Iterative procedure is prohibitive for larger model spaces
  - Each model space requires this procedure
- **Microscopic procedures not tuned**
- Assuming sufficient data, cannot improve upon empirical parameterization
- **Improvements**
  - 1 Less time-consuming procedure to determine effective interactions
  - 2 No limitations on model space (number of parameters vs. data points)
  - 3 Theoretical error given by aspects excluded from RG+MBPT
  - 4 Method for explicitly determining three-body contribution

# Review

- Main topics already presented in prior two lectures (J. Holt)
  - ① Select microscopic bare interactions which reproduce scattering data
  - ② Soften using renormalization group methods (G-matrix,  $v_{lowk}$ , SRG, etc.)
  - ③ Define  $P$  and  $Q$  operators (select reduced model space and basis truncation)
  - ④ Employ many-body perturbation theory to determine two-body matrix elements
  - ⑤ Determine single particle energies (HF, Dyson's equation, empirically, etc.)
- NUSHELLX executable "ham" produces effective interactions
- Practical aspects of calculations must be discussed
  - Selection of basis for MBPT
  - Convergence (order of perturbation theory,  $\hbar\omega$  excitations, etc.)
  - Divergences due to small energy denominators and large model spaces

# Review

- Main topics already presented in prior two lectures (J. Holt)
  - ① Select microscopic bare interactions which reproduce scattering data
  - ② Soften using renormalization group methods (G-matrix,  $v_{lowk}$ , SRG, etc.)
  - ③ Define  $P$  and  $Q$  operators (select reduced model space and basis truncation)
  - ④ Employ many-body perturbation theory to determine two-body matrix elements
  - ⑤ Determine single particle energies (HF, Dyson's equation, empirically, etc.)
- NUSHELLX executable "ham" produces effective interactions
- **Practical aspects of calculations must be discussed**
  - Selection of basis for MBPT
  - Convergence (order of perturbation theory,  $\hbar\omega$  excitations, etc.)
  - Divergences due to small energy denominators and large model spaces



# Behavior of exotic nuclei

- Renormalization is basis-dependent (HO typical for nuclear structure applications)
- **Magic numbers evolve away from stability**
  - Suggests evolution of single particle shell structure
  - Not reproduced by standard HO potential in nuclear physics
- For exotic nuclei, valence orbits are often loosely bound
- Well-known problem
  - Loosely bound orbits extend farther in space
  - Huge basis required to reproduce behavior with HO wavefunctions
  - Realistic basis preferred for reasonable truncation needed computationally
- **Typical realistic bases**
  - 1 Woods-Saxon basis
  - 2 **Skyrme Hartree-Fock (SHF) basis**
  - 3 Gamow basis

# Behavior of exotic nuclei

- Renormalization is basis-dependent (HO typical for nuclear structure applications)
- Magic numbers evolve away from stability
  - Suggests evolution of single particle shell structure
  - Not reproduced by standard HO potential in nuclear physics
- **For exotic nuclei, valence orbits are often loosely bound**
- Well-known problem
  - Loosely bound orbits extend farther in space
  - Huge basis required to reproduce behavior with HO wavefunctions
  - Realistic basis preferred for reasonable truncation needed computationally
- **Typical realistic bases**
  - 1 Woods-Saxon basis
  - 2 **Skyrme Hartree-Fock (SHF) basis**
  - 3 Gamow basis

# Behavior of exotic nuclei

- Renormalization is basis-dependent (HO typical for nuclear structure applications)
- Magic numbers evolve away from stability
  - Suggests evolution of single particle shell structure
  - Not reproduced by standard HO potential in nuclear physics
- For exotic nuclei, valence orbits are often loosely bound
- Well-known problem
  - Loosely bound orbits extend farther in space
  - Huge basis required to reproduce behavior with HO wavefunctions
  - Realistic basis preferred for reasonable truncation needed computationally
- **Typical realistic bases**
  - 1 Woods-Saxon basis
  - 2 **Skyrme Hartree-Fock (SHF) basis**
  - 3 Gamow basis

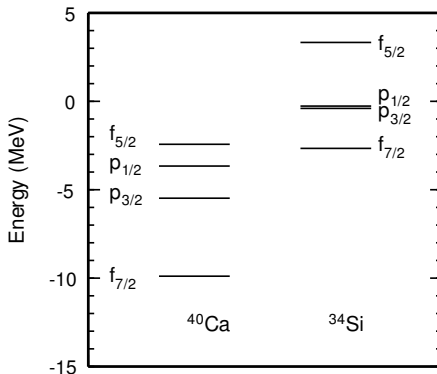
## Example: $pf$ neutron orbits

- Compare bases for  $pf$  valence space for stable  $^{40}\text{Ca}$  and exotic  $^{34}\text{Si}$  isotopes
- Both nuclei have  $N = 20$  (same neutron occupation, same neutron valence orbits)
- **HO basis energies fixed to reproduce SHF value for valence orbits (bold)**

$n\ell_j$	$^{34}\text{Si}$ HO	$^{34}\text{Si}$ SHF	$^{40}\text{Ca}$ HO	$^{40}\text{Ca}$ SHF
$0s_{1/2}$	-34.59	-32.79	-39.21	-38.18
$0p_{3/2}$	-23.09	-23.10	-28.19	-29.70
$0p_{1/2}$	-23.09	-21.74	-28.19	-26.67
$0d_{5/2}$	-11.58	-13.07	-17.17	-20.20
$0d_{3/2}$	-11.58	-9.03	-17.17	-14.65
$1s_{1/2}$	-11.58	-10.04	-17.17	-15.75
$0f_{7/2}$	<b>-0.07</b>	<b>-2.62</b>	<b>-6.15</b>	<b>-9.89</b>
$0f_{5/2}$	<b>-0.07</b>	<b>3.33</b>	<b>-6.15</b>	<b>-2.43</b>
$1p_{3/2}$	<b>-0.07</b>	<b>-0.40</b>	<b>-6.15</b>	<b>-5.48</b>
$1p_{1/2}$	<b>-0.07</b>	<b>-0.27</b>	<b>-6.15</b>	<b>-3.66</b>
$0g_{9/2}$	11.44	9.22	4.87	1.15
$0g_{7/2}$	11.44	18.23	4.87	10.28

## Example: $pf$ neutron orbits

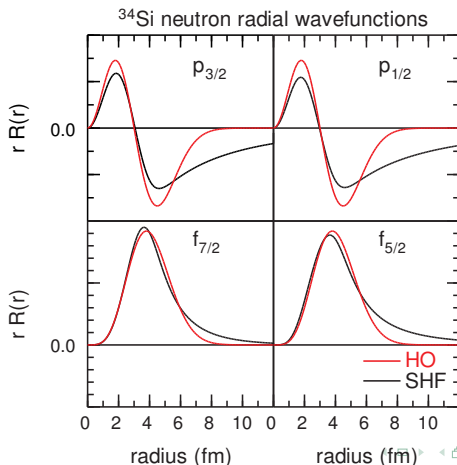
- Compare bases for  $pf$  valence space for stable  $^{40}\text{Ca}$  and exotic  $^{34}\text{Si}$  isotopes
- Both nuclei have  $N = 20$
- Focus on model space orbits



Model Space Neutron Orbits in SHF Basis

## Example: $pf$ neutron orbits

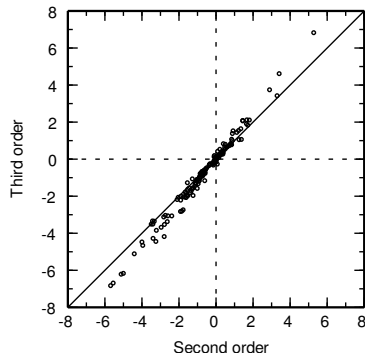
- Compare bases for  $pf$  valence space for stable  $^{40}\text{Ca}$  and exotic  $^{34}\text{Si}$  isotopes
- Both nuclei have  $N = 20$
- **Focus on model space orbits**



# Convergence

- Many-body perturbation theory derived up to third order

TBME in  $sd$  shell including  $6\hbar\omega$  excitations in SHF basis



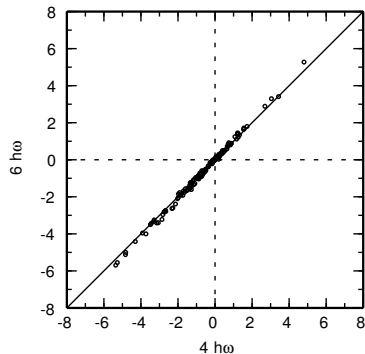
- Results with HO basis do not converge at third order<sup>a</sup>
- Better convergence expected with realistic basis, but not achieved at third order

<sup>a</sup>M. Hjorth-Jensen et al., Phys. Lett. B **248**, 243 (1990)

# Convergence

- Computational limit (typical laptop/desktop):  $10\hbar\omega$  in  $sd$  shell

TBME in  $sd$  shell renormalized to second order in SHF basis

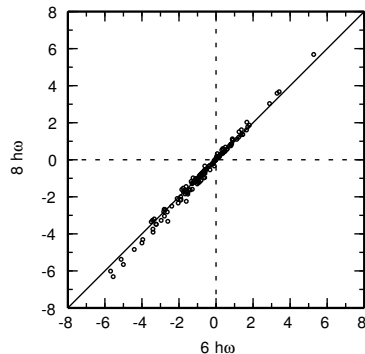




# Convergence

- Computational limit (typical laptop/desktop):  $10\hbar\omega$  in  $sd$  shell

TBME in  $sd$  shell renormalized to second order in SHF basis



# Convergence

- Lack of convergence as a function of excitations and order of perturbation theory
- More attractive interaction for higher excitations and order of perturbation theory
- Must be aware of possible dependence
  - Few percent from  $4\hbar\omega$  to  $6\hbar\omega$  excitations
  - $\sim 20\%$  for third order in *sd* shell example
- Evaluate error bars by various renormalization procedures?
- **Less dependence for low-energy states in even-even nuclei**
  - Statement not proven in these lectures
  - Effect on pairing matrix elements ( $J = 0$ ) reduced relative to effect of basis
- **Be consistent and honest in procedure**
  - NUSHELLX 'ham' executable uses second order and  $6\hbar\omega$  by default
  - Best to evaluate dependence if possible
  - At least, state explicitly parameters used
  - Realize calculations are dependent on RG+MBPT scheme

# Divergences

- Small or null energy denominators result in infinite matrix elements in MBPT
- Very common (almost automatic) with any basis
- **Primary way to avoid**
  - Introduce constant valence energy for all model space orbits
  - Provide starting energy (typically twice the valence energy)
  - In energy denominators of two-body diagrams
    - Use starting energy  $\pm\delta\epsilon$  in place of valence orbit energy
- In model spaces comprised of orbits from multiple oscillator shells
  - Intruder states enter MBPT renormalization
  - Requires calculation of Q-box to higher order to resolve divergences
  - In practice: artificially place all model space orbits in same oscillator shell
  - Current area of research in nuclear structure theory
- Divergences
  - More common with third order of MBPT
  - More common with realistic SHF basis
  - Primarily occur when evaluating Q-box (derivative contributions)
- Can avoid divergences by selection of options in ham

# Divergences

- Small or null energy denominators result in infinite matrix elements in MBPT
- Very common (almost automatic) with any basis
- Primary way to avoid
  - Introduce constant valence energy for all model space orbits
  - Provide starting energy (typically twice the valence energy)
  - In energy denominators of two-body diagrams
    - Use starting energy  $\pm\delta\epsilon$  in place of valence orbit energy
- **In model spaces comprised of orbits from multiple oscillator shells**
  - Intruder states enter MBPT renormalization
  - Requires calculation of Q-box to higher order to resolve divergences
  - In practice: artificially place all model space orbits in same oscillator shell
  - Current area of research in nuclear structure theory
- Divergences
  - More common with third order of MBPT
  - More common with realistic SHF basis
  - Primarily occur when evaluating Q-box (derivative contributions)
- Can avoid divergences by selection of options in ham

# Divergences

- Small or null energy denominators result in infinite matrix elements in MBPT
- Very common (almost automatic) with any basis
- Primary way to avoid
  - Introduce constant valence energy for all model space orbits
  - Provide starting energy (typically twice the valence energy)
  - In energy denominators of two-body diagrams
    - Use starting energy  $\pm\delta\epsilon$  in place of valence orbit energy
- In model spaces comprised of orbits from multiple oscillator shells
  - Intruder states enter MBPT renormalization
  - Requires calculation of Q-box to higher order to resolve divergences
  - In practice: artificially place all model space orbits in same oscillator shell
  - Current area of research in nuclear structure theory
- **Divergences**
  - More common with third order of MBPT
  - More common with realistic SHF basis
  - Primarily occur when evaluating Q-box (derivative contributions)
- Can avoid divergences by selection of options in ham

# Divergences

- Small or null energy denominators result in infinite matrix elements in MBPT
- Very common (almost automatic) with any basis
- Primary way to avoid
  - Introduce constant valence energy for all model space orbits
  - Provide starting energy (typically twice the valence energy)
  - In energy denominators of two-body diagrams
    - Use starting energy  $\pm\delta\epsilon$  in place of valence orbit energy
- In model spaces comprised of orbits from multiple oscillator shells
  - Intruder states enter MBPT renormalization
  - Requires calculation of Q-box to higher order to resolve divergences
  - In practice: artificially place all model space orbits in same oscillator shell
  - Current area of research in nuclear structure theory
- Divergences
  - More common with third order of MBPT
  - More common with realistic SHF basis
  - Primarily occur when evaluating Q-box (derivative contributions)
- **Can avoid divergences by selection of options in ham**

# Implementation

- Simplest procedure to create interactions
  - ① In NUSHELLX, run executable 'ham'
  - ② Select model space in proton-neutron formalism (i.e., *sdpn* in *sps* folder, not *sd*)
  - ③ Select target nucleus with closed subshell single particle structure
- Remaining parameters have default values printed out in \*.inf file
  - Modify as desired
  - Copy \*.inf file to ham.ini
  - Rerun ham to include updated parameters
- RG calculation performed by ham only if output file \*.reint is nonexistent
- If parameters of RG procedure are modified (e.g. change in cutoff  $\Lambda$ )
  - Must enforce new RG calculation
  - Create new directory and copy ham.ini to the new directory
- More advanced options can be modified by hand
- See comment lines in bhf.ini and renorm.ini

# Implementation

- Simplest procedure to create interactions
  - ① In NUSHELLX, run executable 'ham'
  - ② Select model space in proton-neutron formalism (i.e., *sdpn* in *sps* folder, not *sd*)
  - ③ Select target nucleus with closed subshell single particle structure
- Remaining parameters have default values printed out in \*.inf file
  - Modify as desired
  - Copy \*.inf file to ham.ini
  - Rerun ham to include updated parameters
- RG calculation performed by ham only if output file \*.reint is nonexistent
- If parameters of RG procedure are modified (e.g. change in cutoff  $\Lambda$ )
  - Must enforce new RG calculation
  - Create new directory and copy ham.ini to the new directory
- More advanced options can be modified by hand
- See comment lines in bhf.ini and renorm.ini



# Implementation

- Simplest procedure to create interactions
  - ① In NUSHELLX, run executable 'ham'
  - ② Select model space in proton-neutron formalism (i.e., *sdpn* in *sps* folder, not *sd*)
  - ③ Select target nucleus with closed subshell single particle structure
- Remaining parameters have default values printed out in \*.inf file
  - Modify as desired
  - Copy \*.inf file to ham.ini
  - Rerun ham to include updated parameters
- RG calculation performed by ham only if output file \*.reint is nonexistent
- If parameters of RG procedure are modified (e.g. change in cutoff  $\Lambda$ )
  - Must enforce new RG calculation
  - Create new directory and copy ham.ini to the new directory
- More advanced options can be modified by hand
- See comment lines in bhf.ini and renorm.ini

# Implementation

- Simplest procedure to create interactions
  - ① In NUSHELLX, run executable 'ham'
  - ② Select model space in proton-neutron formalism (i.e., *sdpn* in *sps* folder, not *sd*)
  - ③ Select target nucleus with closed subshell single particle structure
- Remaining parameters have default values printed out in \*.inf file
  - Modify as desired
  - Copy \*.inf file to ham.ini
  - Rerun ham to include updated parameters
- RG calculation performed by ham only if output file \*.reint is nonexistent
- If parameters of RG procedure are modified (e.g. change in cutoff  $\Lambda$ )
  - Must enforce new RG calculation
  - Create new directory and copy ham.ini to the new directory
- More advanced options can be modified by hand
- See comment lines in bhf.ini and renorm.ini